QGJQRC(3) QGJQRC(3)

#### **NAME**

```
qgiqrc - Gauss-Jacobi logarithmic Quadrature Recursion Coefficients
```

# **SYNOPSIS**

```
Fortran (77, 90, 95, HPF):
        f77 [ flags ] file(s) \dots -L/usr/local/lib -lgil
                 SUBROUTINE qgjqrc (a, b, s, t, alpha, beta, nquad, ierr)
                 INTEGER
                                   ierr,
                                            nguad
                 REAL*16
                                  a(0:MAXPTS), alpha,
                                                            b(0:MAXPTS), beta
                                  s(0:MAXPTS), t(0:MAXPTS)
                 REAL*16
C (K&R, 89, 99), C++ (98):
        cc [ flags ] -I/usr/local/include file(s) . . . -L/usr/local/lib -lgjl
        Use
                 #include <gjl.h>
        to get this prototype:
                 void qgjqrc(fortran_quadruple_precision a_[],
                        fortran_quadruple_precision b_[],
                        fortran_quadruple_precision s_[],
                        fortran_quadruple_precision t_[],
                        const fortran_quadruple_precision * alpha_,
                        const fortran_quadruple_precision * beta_,
                        const fortran_integer * nquad_,
                        fortran integer * ierr );
```

NB: The definition of C/C++ data types **fortran**\_xxx, and the mapping of Fortran external names to C/C++ external names, is handled by the C/C++ header file. That way, the same function or subroutine name can be used in C, C++, and Fortran code, independent of compiler conventions for mangling of external names in these programming languages.

### DESCRIPTION

Compute the recursion coefficients and zeroth and first moments of the monic polynomials corresponding to the positive weight function

```
w(x,\lambda heta) = (1-x)^\alpha (1+x)^\beta (-\ln((1+x)/2)) with recursion relation (n = 0, 1, 2, ...) P_{n+1}^{\alpha}(x) = (x - B_n^{\alpha}(x)) * P_n^{\alpha}(x) + P_n^{\alpha}(x) = (x - A_n^{\alpha}(x)) * P_n^{\alpha}(x) + P_n^{\alpha}(x) = 0 and initial conditions P_{n-1}^{\alpha}(x) = 0 P_{n-1}^{\alpha}(x) = 0 P_{n-1}^{\alpha}(x) = 0 P_{n-1}^{\alpha}(x) = 0
```

Except in the weight function, the superscripts indicate dependence on \alpha, NOT exponentiation.

The required moments are:

From these moments, the recursion coefficients are computed as:

```
 A_n^{\alpha} = T_n^{\alpha} \ / T_{n-1}^{\alpha} \ B_n^{\alpha} = S_n^{\alpha} \ / T_n^{\alpha} \
```

On entry:

```
alpha Power of (1-x) in the integrand (alpha > -1).
```

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**beta** Power of (1+x) in the integrand (**beta** > -1).

**nquad** Number of quadrature points to compute. It must be less than the limit MAXPTS defined in the header file, *maxpts.inc*. The default value chosen there should be large enough for any realistic application.

## On return:

### **SEE ALSO**

qgjqf(3), qgjqfd(3).

### **AUTHORS**

The algorithms and code are described in detail in the paper

Fast Gaussian Quadrature for Two Classes of Logarithmic Weight Functions in ACM Transactions on Mathematical Software, Volume ??, Number ??, Pages ????--???? and ????--????, 20xx, by

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