Data driven analysis of Global Warming Causes

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In this project, we investigate the evidence for human-made global warming using historical climate datasets. We analyze global surface temperature trends from both land and ocean records, compare them with atmospheric COD levels, and evaluate alternative drivers such as solar activity and volcanic eruptions. Through statistical analysis and visualizations, we aim to understand the relationships between these factors and assess the primary causes of observed warming.

Importing the required libraries

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
import scipy.stats as stats
from scipy.stats import linregress, pearsonr
import xarray as xr
import seaborn as sns
import statsmodels.api as sm
from statsmodels.stats.anova import anova_lm
from statsmodels.stats.diagnostic import het_breuschpagan
from statsmodels.stats.stattools import durbin_watson
from statsmodels.stats.outliers_influence import OLSInfluence, variance_infl
```

Loading CO_2 Data

Here we are using annual mean atmospheric COD measurements from the Mauna Loa Observatory, which provides one of the longest and most reliable continuous COD records in the world.

```
In [5]: co2 = pd.read_csv("co2_annmean_mlo.csv", comment="#")
    co2 = co2.rename(columns={"year": "Year", "mean": "C02_ppm", "unc": "Uncerta
    co2["Year"] = co2["Year"].astype(int)
```

```
print(co2.head())
 print("\nMissing values per column:\n", co2.isna().sum())
  Year CO2_ppm Uncertainty
0 1959 315.98
                    0.12
1 1960 316.91
                    0.12
2 1961 317.64
                    0.12
3 1962 318.45
                     0.12
4 1963 318.99
                    0.12
Missing values per column:
Year
            0
CO2_ppm
             0
Uncertainty
dtype: int64
```

- The ${\rm CO}_2$ dataset from Mauna Loa covers annual mean atmospheric ${\rm CO}_2$ concentrations starting from 1959.
- The first few rows show values increasing from 315.98 ppm in 1959 to 318.99 ppm in 1963, with a reported measurement uncertainty of ±0.12 ppm.
- \bullet We have performed a missing values check to confirm that there are no gaps in the dataset for Year, CO_2 concentration, or Uncertainty.

Loading Land Temperature Data

We are using the annual land surface temperature anomaly data from the Berkeley Earth dataset, which offers long-term, high-quality records with global coverage and uncertainty estimates.

```
In [6]: berkeley = pd.read_csv(
    "Complete_TAVG_summary.txt",
    sep=r"\s+",
    comment="%",
    header=None,
    names=[
        "Year", "Ann_Anom_air", "Ann_Unc_air", "FiveYr_Anom_air", "FiveYr_Unc_ann_anom_water", "Ann_Unc_water", "FiveYr_Anom_water", "FiveYr_Unc_ander", "FiveYr_Unc_ander", "Ann_Unc_air"]].rename(
    columns={"Ann_Anom_air": "Land_Anom_C", "Ann_Unc_air": "Land_Uncertainty)
    print(land_df.head())
    print("\nMissing values per column:\n", land_df.isna().sum())
```

```
Year Land_Anom_C Land_Uncertainty
0 1750 -0.816
                          1.078
1 1751
          -0.951
                           1.278
2 1753
          -0.384
                           1.130
3 1754
           0.081
                           1.662
4 1755
          -0.250
                           1.246
Missing values per column:
Year
Land_Anom_C
                0
Land_Uncertainty
                0
dtype: int64
```

- The Berkeley Earth land temperature dataset starts in 1750, with values reported as annual anomalies relative to a baseline climate average.
- There are no missing values detected for Year, anomaly, or uncertainty.

Loading Ocean Temperature Data

We are using annual sea surface temperature anomaly data from the HadSST dataset, which provides globally gridded ocean temperature records along with uncertainty estimates.

```
Year Ocean_Anom_C Ocean_Uncertainty
0 1850 -0.291801
                              0.111393
1 1851 -0.176054
2 1852 -0.167859
                               0.112537
                               0.107004
3 1853 -0.195570
4 1854 -0.254887
                              0.094381
                               0.087261
Missing values per column:
Year
Ocean_Anom_C
                    0
Ocean_Uncertainty
                    0
dtype: int64
```

- The HadSST4 ocean temperature dataset begins in 1850, reporting sea surface temperature anomalies relative to a baseline.
- The early values such as -0.292 °C in 1850 and -0.176 °C in 1851 indicate cooler than average conditions for the 19th century.
- Uncertainty estimates for these early measurements are relatively small (± 0.09 to ± 0.11 °C).
- No missing values are found for Year, anomaly, or uncertainty.

Merge Land & Ocean into Global Temperature Series

We are combining the land and ocean temperature anomalies into a single global series using area-weighted averaging (29% land, 71% ocean) and propagate uncertainties to reflect the combined measurement error.

```
Year Land_Anom_C Land_Uncertainty Ocean_Anom_C Ocean_Uncertainty \
0 1850 -0.774
                   0.438 -0.291801 0.111393
                         0.711 -0.176054
0.679 -0.167859
1 1851
          -0.490
                                                  0.112537
                                                  0.107004
2 1852
          -0.593
3 1853
                         0.529
          -0.583
                                  -0.195570
                                                  0.094381
                                  -0.254887
4 1854
                          0.319
          -0.396
                                                   0.087261
  Global_Anom_C Global_Uncertainty
0
     -0.431639 0.149630
1
     -0.267098
                     0.221130
     -0.291150
2
                     0.211058
    -0.307925
                     0.167407
     -0.295810
                     0.111340
Missing values per column:
                  0
Year
Land_Anom_C
                  0
Land_Uncertainty
Ocean_Anom_C
Ocean_Uncertainty
Global_Anom_C
                  0
Global_Uncertainty 0
dtype: int64
```

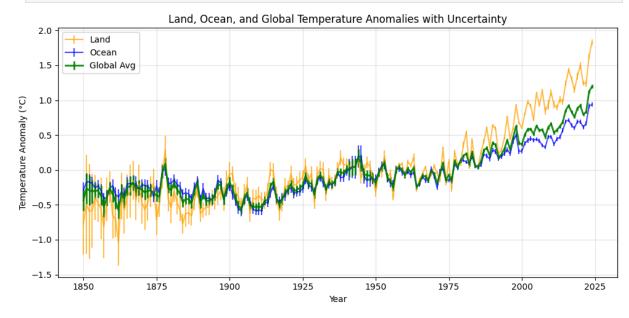
- We merged the land (Berkeley Earth) and ocean (HadSST4) temperature series on common years and combined them into a global temperature anomaly using area weights (29% land, 71% ocean).
- Early examples match our calculations: for 1850, Land -0.774 °C and Ocean -0.292 °C yield Global -0.432 °C.
- We propagated uncertainties using a root-sum-of-squares with the same weights. Our checks show no missing values in any column (Year, Land/Ocean anomalies & uncertainties, Global anomaly & uncertainty).

Plot Land, Ocean, and Global Temperature Trends with Error Bars

We will visualize the annual temperature anomalies for land, ocean, and the combined global series, adding error bars to reflect the uncertainty in each measurement

```
In [9]: plt.figure(figsize=(10, 5))
    plt.errorbar(
        merged_temp["Year"], merged_temp["Land_Anom_C"],
        yerr=merged_temp["Land_Uncertainty"], label="Land", color="orange", alph
)
    plt.errorbar(
        merged_temp["Year"], merged_temp["Ocean_Anom_C"],
```

```
yerr=merged_temp["Ocean_Uncertainty"], label="Ocean", color="blue", alph
)
plt.errorbar(
    merged_temp["Year"], merged_temp["Global_Anom_C"],
    yerr=merged_temp["Global_Uncertainty"], label="Global Avg", color="green
)
plt.title("Land, Ocean, and Global Temperature Anomalies with Uncertainty")
plt.xlabel("Year")
plt.ylabel("Temperature Anomaly (°C)")
plt.legend()
plt.grid(alpha=0.3)
plt.tight_layout()
plt.show()
```



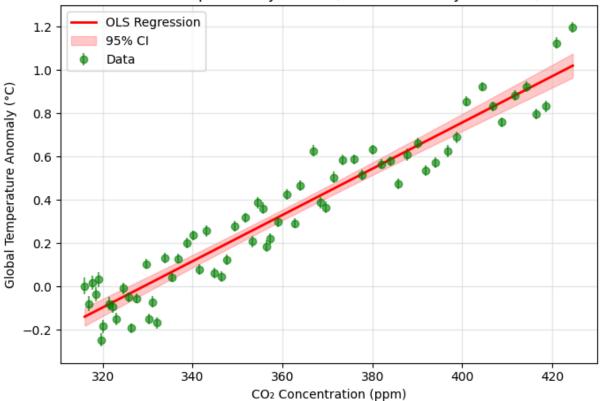
- We plotted the land, ocean, and global temperature anomalies from 1850 to the present, each with their respective uncertainty ranges as error bars.
- The land record shows the greatest warming, especially in recent decades, while the ocean record has warmed more gradually.
- The global average, computed using our area-weighted method, lies between the two and tracks them closely through time.
- Land areas warm faster than oceans due to lower heat capacity and different feedback processes whereas the Oceans exhibit smaller variability and a slower warming trend, reflecting their role as a large heat reservoir.
- The global average smooths these differences but still captures the strong post-1970 warming trend

CO_2 vs Global Temperature Correlation

We are examining the relationship between atmospheric ${\rm CO}_2$ concentrations and global temperature anomalies, calculating statistical correlations and visualizing the trend with a fitted regression line

```
In [10]: # Merging COD with global temperature anomalies
         climate = pd.merge(merged_temp, co2, on="Year", how="inner")
         # Fitting regression
         slope, intercept, r_value, p_value, std_err = linregress(climate["CO2_ppm"],
         line = slope * climate["CO2_ppm"] + intercept
         # Plotting scatter with error bars and regression line
         plt.figure(figsize=(7, 5))
         plt.errorbar(
             climate["CO2_ppm"], climate["Global_Anom_C"],
             yerr=climate["Global_Uncertainty"], fmt='o', alpha=0.6, color="green", 1
         plt.plot(climate["CO2_ppm"], line, color='red', linewidth=2, label="OLS Regr
         # Confidence interval calculation
         X_const = sm.add_constant(climate["C02_ppm"])
         model = sm.OLS(climate["Global_Anom_C"], X_const).fit()
         preds = model.get_prediction(X_const).summary_frame(alpha=0.05)
         plt.fill_between(
             climate["CO2_ppm"],
             preds["mean_ci_lower"], preds["mean_ci_upper"],
             color='red', alpha=0.2, label="95% CI"
         )
         plt.title("Global Temp Anomaly vs COD (with Uncertainty & 95% CI)")
         plt.xlabel("COD Concentration (ppm)")
         plt.ylabel("Global Temperature Anomaly (°C)")
         plt.grid(alpha=0.3)
         plt.legend()
         plt.tight_layout()
         plt.show()
         # Output of regression
         print(f"OLS Regression: Temp = {slope:.4f} \times CO$_2$ + {intercept:.2f}")
         print(f"Pearson correlation (r) = {r_value:.4f}")
         print(f"P-value = {p_value:.3e}")
         print(f"R<sup>2</sup> = {r_value**2:.4f}")
```

Global Temp Anomaly vs CO₂ (with Uncertainty & 95% CI)



OLS Regression: Temp = $0.0107 \times C0\$_2\$ + -3.51$ Pearson correlation (r) = 0.9607P-value = 2.419e-37 $R^2 = 0.9230$

• We merged the global temperature anomaly dataset with atmospheric CO₂ concentration records and performed an ordinary least squares (OLS) regression. The fitted regression line (red) shows a strong positive linear relationship, with a 95% confidence interval. The equation from our model is:

Temp anomaly (°C)= $0.0107 \times CO_2$ (ppm)-3.51

- Our analysis shows an exceptionally strong and statistically significant link between atmospheric CO_2 concentration and global temperature anomalies. With an R^2 of 92.3%, we find that CO_2 alone accounts for nearly all the year-to-year variation in long-term global temperature trends. -The Pearson r of 0.9607 indicates a near-perfect positive correlation, meaning the two variables move together very closely.
- The extremely low p-value (2.42×10 $^-37$) confirms that this relationship is not due to random chance.

Loading TSI, AOD and VEI

We are using the datasets for Total Solar Irradiance (TSI), Aerosol Optical Depth (AOD), and Volcanic Explosivity Index (VEI) to investigate the potential influence of solar activity and volcanic events on global temperature trends

```
In [11]: # Suppress specific deprecation warnings from xarray and pandas to keep the
         # These warnings are related to long-term changes in library APIs ('use_cfti
         # They do not affect results in our current environment,
         # and fixing them would require version changes outside the scope of this pr
         import warnings
         warnings.filterwarnings(
             "ignore",
             category=DeprecationWarning,
             message=".*use_cftime.*CFDatetimeCoder.*"
         # Solar Irradiance (TSI)
         print("\nLoading Total Solar Irradiance (TSI)...")
         tsi_ds = xr.open_dataset('tsi_v03r00_yearly_s1610_e2024_c20250221.nc', decod
         years_tsi = [t.year for t in tsi_ds['time'].values]
         tsi_vals = tsi_ds['TSI'].values
         tsi_df = pd.DataFrame({"Year": years_tsi, "TSI": tsi_vals})
         print(f"TSI Data: {tsi_df['Year'].min()}-{tsi_df['Year'].max()}, "
               f"mean={tsi_df['TSI'].mean():.2f} W/m2, missing={tsi_df.isna().sum().s
         # Volcanic Aerosol Optical Depth (AOD)
         print("\nLoading Volcanic Aerosol Optical Depth (AOD)...")
         aod_ds = xr.open_dataset('tau_map_2012-12.nc')
         aod_monthly_da = aod_ds['tau'].mean(dim='lat')
         times_pandas = pd.to_datetime(aod_monthly_da['month'].values)
         aod_ann = pd.Series(aod_monthly_da.values, index=times_pandas).resample('YE'
         aod_ann.index = aod_ann.index.year # convert to year index
         print(f"AOD Data: {aod_ann.index.min()}-{aod_ann.index.max()}, "
               f"mean={aod_ann.mean():.4f}, missing={aod_ann.isna().sum()}")
         # Volcanic Eruption Index (VEI)
         print("\nLoading Volcanic Eruption Index (VEI)...")
         vei_df = pd.read_excel("GVP_Eruption_Search_Result.xlsx", sheet_name="Erupti
         year_vei = pd.to_numeric(vei_df.filter(regex=r'(?i)^start\s*year$').iloc[;,
         vei_vals = pd.to_numeric(vei_df.filter(regex=r'(?i)^vei$').iloc[:, 0], error
         # Aggregating annual VEI sum
         annual_vei = pd.DataFrame({"Year": year_vei, "VEI": vei_vals}).dropna()
         annual_vei = annual_vei.groupby("Year")["VEI"].sum().reset_index()
         print(f"VEI Data: {annual_vei['Year'].min()}-{annual_vei['Year'].max()}, "
               f"mean={annual_vei['VEI'].mean():.2f}, missing={annual_vei.isna().sum(
```

```
Loading Total Solar Irradiance (TSI)...
TSI Data: 1610-2024, mean=1361.47 W/m², missing=0

Loading Volcanic Aerosol Optical Depth (AOD)...
AOD Data: 1850-2012, mean=0.0130, missing=0

Loading Volcanic Eruption Index (VEI)...
VEI Data: -55500-2025, mean=12.52, missing=0
```

We successfully loaded three important climate drivers:

- Total Solar Irradiance (TSI): Data spans from 1610 to 2024, with an average of 1361.47 W/m² and no missing values.TSI will help us examine the role of solar energy changes in driving climate trends.
- Volcanic Aerosol Optical Depth (AOD): Data covers 1850 to 2012, with an average value of 0.0130 and no missing entries. AOD captures volcanic aerosol loading, which can cause short-term cooling by blocking incoming sunlight.
- Volcanic Eruption Index (VEI): Dataset spans -55,500 to 2025, with an average annual VEI of 12.52 and no missing entries.VEI quantifies volcanic activity severity, useful for identifying strong eruption years.
- These datasets will allow us to explore multi-factor regression models later, helping determine how much of the observed temperature variability is explained by natural drivers (solar and volcanic) compared to anthropogenic ${\rm CO}_2$.

Merging everything Into One Table

We combine the temperature, CO_2 , solar irradiance, volcanic activity, and aerosol datasets into a single, aligned table to enable direct comparisons and multivariate statistical analysis

```
# Keeping only years with no missing Global Anomaly, CO2, TSI, and VEI
 combined = combined.dropna(subset=["Global_Anom_C", "CO2_ppm", "TSI", "VEI"]
 # Sorting by year for plotting
 combined = combined.sort_values("Year").reset_index(drop=True)
 print("\nMerged Dataset Overview:")
 print(combined.head())
 print(f"\nData coverage: {combined['Year'].min()}-{combined['Year'].max()} "
      f"({len(combined)} years)")
 print("Missing values per column:\n", combined.isna().sum())
Merged Dataset Overview:
  Year Global_Anom_C Global_Uncertainty CO2_ppm Uncertainty
                                                                      TSI
\
0 1959
           0.002543
                                0.037197 315.98
                                                         0.12 1362.096069
1 1960
           -0.079486
                                0.035243 316.91
                                                         0.12 1361.942871
2 1961
           0.018816
                               0.032769 317.64
                                                         0.12 1361.557007
3 1962
          -0.035783
                               0.031229 318.45
                                                         0.12 1361.375488
4 1963
           0.032786
                              0.034265 318.99
                                                         0.12 1361.316406
   VEI
            AOD
0 60.0 0.000179
1 66.0 0.004713
2 59.0 0.009013
3 51.0 0.010394
4 73.0 0.040130
Data coverage: 1959-2024 (66 years)
Missing values per column:
Year
Global_Anom_C
                     0
Global_Uncertainty
                     0
                     0
CO2_ppm
Uncertainty
                     0
TSI
                     0
VEI
                     0
                     12
AOD
dtype: int64
```

Correlation Heatmap & Pairwise Scatterplots.

We are creating a correlation heatmap and pairwise scatterplots to visually explore the relationships between temperature, CO_2 , solar activity, volcanic indicators, and aerosols, helping identify potential patterns and strengths of association.

```
In [13]: sns.set_theme(context="notebook", style="whitegrid") # Use a clean style wi
# Calculating solar irradiance anomaly
tsi_df["TSI_anom"] = tsi_df["TSI"] - tsi_df["TSI"].mean()
```

```
# Counting and smooth large volcanic eruptions
VEI_MIN = 4 # Only including eruptions with VEI of 4 or higher
_vei = vei_df.copy()
# Extracting numeric year and VEI values from the dataframe
_vei["Year"] = pd.to_numeric(_vei.filter(regex=r"(?i)^start\s*year$").iloc[:
_vei["VEI_val"] = pd.to_numeric(_vei.filter(regex=r"(?i)^vei$").iloc[:, 0],
_vei = _vei.dropna(subset=["Year", "VEI_val"])
# Counting how many large eruptions occurred each year
vei_counts = (
    _vei[_vei["VEI_val"] >= VEI_MIN]
   .groupby("Year")["VEI_val"].count()
   .rename("VEI_count")
   .to_frame()
   .reset_index()
# Filling in missing years with zeros and applying a 3-year rolling average
yrs_full = pd.DataFrame({"Year": np.arange(merged_temp["Year"].min(), merged
vei_counts = yrs_full.merge(vei_counts, on="Year", how="left").fillna({"VEI_
vei_counts["VEI_count_rm3"] = (
   vei_counts.set_index("Year")["VEI_count"].rolling(window=3, center=True,
# Merging all variables into a single dataframe for correlation analysis
combined_corr = (
    merged_temp[["Year", "Global_Anom_C"]]
    .merge(co2[["Year", "CO2_ppm"]], on="Year", how="inner")
    .merge(tsi_df[["Year", "TSI_anom"]], on="Year", how="left")
    .merge(vei_counts[["Year", "VEI_count_rm3"]], on="Year", how="left")
    .dropna(subset=["Global_Anom_C", "CO2_ppm", "TSI_anom", "VEI_count_rm3"]
   .sort_values("Year")
   .reset_index(drop=True)
)
# Creating a correlation heatmap
corr_vars = ["Global_Anom_C", "CO2_ppm", "TSI_anom", "VEI_count_rm3"]
corr_matrix = combined_corr[corr_vars].corr()
plt.figure(figsize=(5, 4)) # Keeping the plot compact for reports
sns.heatmap(
    corr_matrix, annot=True, cmap="coolwarm", fmt=".2f", square=True,
    cbar_kws={"shrink": 0.75, "aspect": 30} # Make the colorbar smaller to
plt.title("Correlation Matrix\n(Temp, CO$_2$, Solar anom, Volcanic 3-yr mean
plt.xticks(rotation=45, ha="right")
plt.yticks(rotation=0)
plt.tight_layout()
plt.show()
# Pairwise scatterplots
g = sns.pairplot(
   combined_corr[corr_vars],
    kind="reg", diag_kind="kde", corner=True,
```

```
height=2.0, # Make each subplot smaller for a more compact layout
    plot_kws={"scatter_kws": {"alpha": 0.7, "s": 20}, "line_kws": {"linewidt})

g.fig.suptitle(
    "Pairwise Relationships with Regression Lines\n(Temp, CO$_2$, Solar anom
    y=1.02, fontsize=10
)

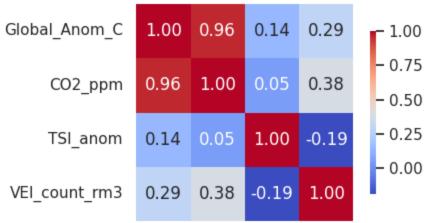
plt.show()

# Correlation values

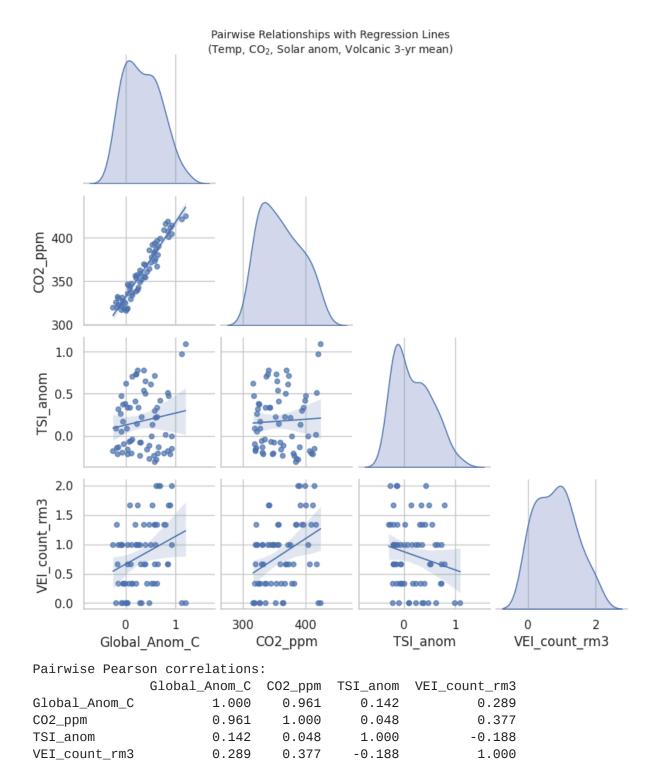
print("\nPairwise Pearson correlations:")

print(corr_matrix.round(3))
```

Correlation Matrix (Temp, CO₂, Solar anom, Volcanic 3-yr mean)



Global Anom CO2 ppm St anom WEI Count Im3



The correlation analysis reveals that global temperature anomalies are overwhelmingly linked to atmospheric ${\rm CO}_2$ levels.

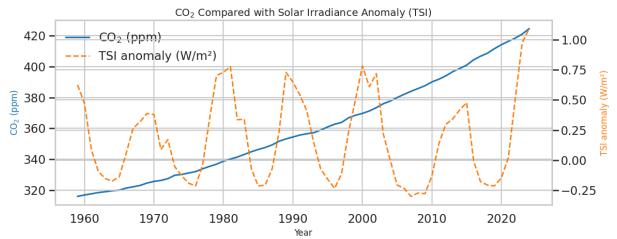
• The Pearson correlation of 0.961 between Global_Anom_C and COl_ppm indicates an almost perfectly linear relationship as COl rises, temperatures increase in near synchrony. This strong association is consistent with well established physical principles of greenhouse gas-driven warming and suggests ${\rm CO}_2$ is the dominant driver of recent climate trends.

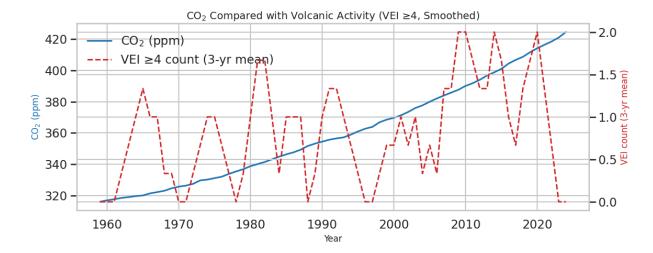
- In contrast, solar irradiance anomalies (TSI_anom) show only a weak positive correlation (r = 0.142) with temperature. This implies that while solar variability may have small influences on interannual or decadal timescales, it does not explain the long-term warming trend.
- Volcanic activity, represented by the 3 year mean VEI count, has a weak correlation with temperature (r = 0.289). Large eruptions are known to cause short-lived cooling by injecting aerosols into the stratosphere, but these effects are temporary and episodic, leaving little imprint on long-term averages.
- Other relationships, such as CO_2 vs TSI (r = 0.048) and TSI vs VEI (r = -0.188), are negligible, reinforcing that the warming signal is not strongly coupled to natural variability from solar or volcanic sources.
- ullet The correlation structure strongly supports the idea that anthropogenic ${\rm CO}_2$ increases are the primary driver of modern global warming, with natural forcings playing secondary, shorter-term roles.

CO₂ Comparison with Solar and Volcanic Activity (Dual-Axis Time Series)

We are comparing atmospheric CO_2 concentrations with two potential climate drivers—solar irradiance anomalies (TSI) and volcanic activity (VEI ≥ 4 , 3-year mean)—by plotting them together as dual-axis time series. This allows us to visually assess whether variations in solar output or volcanic eruptions align with long-term changes in CO_2 levels.

```
ax1.set_xlabel("Year", fontsize=12)
ax1.set_ylabel("CO$_2$ (ppm)", fontsize=12, color="tab:blue")
ax2.set_ylabel("TSI anomaly (W/m²)", fontsize=12, color="tab:orange")
ax1.set_title("CO$_2$ Compared with Solar Irradiance Anomaly (TSI)", fontsiz
lines, labels = ax1.get_legend_handles_labels()
lines2, labels2 = ax2.get_legend_handles_labels()
ax1.legend(lines + lines2, labels + labels2, loc="upper left", frameon=False
plt.tight_layout()
plt.show()
# Plotting COD alongside volcanic activity counts ----
fig, ax1 = plt.subplots(figsize=(12, 5))
ax2 = ax1.twinx() # Second y-axis for VEI counts
ax1.plot(combined_corr["Year"], combined_corr["CO2_ppm"],
         color="tab:blue", linewidth=2.2, label="CO$_2$ (ppm)")
ax2.plot(combined_corr["Year"], combined_corr["VEI_count_rm3"],
         color="tab:red", linewidth=2, linestyle="--",
         label="VEI ≥4 count (3-yr mean)")
ax1.set_xlabel("Year", fontsize=12)
ax1.set_ylabel("CO$_2$ (ppm)", fontsize=12, color="tab:blue")
ax2.set_ylabel("VEI count (3-yr mean)", fontsize=12, color="tab:red")
ax1.set_title("CO$_2$ Compared with Volcanic Activity (VEI ≥4, Smoothed)", f
lines, labels = ax1.get_legend_handles_labels()
lines2, labels2 = ax2.get_legend_handles_labels()
ax1.legend(lines + lines2, labels + labels2, loc="upper left", frameon=False
plt.tight_layout()
plt.show()
```





These time-series plots compare the trajectory of atmospheric CO_2 levels with two major natural climate drivers: solar irradiance variability and volcanic activity.

- 1. CO_2 vs Solar Irradiance (TSI anomaly)
 - \bullet CO $_2$ concentrations have risen steadily and almost monotonically from ~316 ppm in 1960 to over 420 ppm today.
 - In contrast, TSI anomalies oscillate in a cyclical pattern (~11-year solar cycles), with no long-term upward or downward trend.
 - The mismatch in patterns shows that solar variability cannot explain the persistent, multi-decade rise in ${\rm CO_2}$ or the corresponding long-term warming. Solar cycles influence short-term fluctuations but not the overall climate trend.
- 2. CO_2 vs Volcanic Activity (VEI ≥ 4 , 3-year mean)
 - Volcanic activity is episodic, with peaks corresponding to major eruptions (e.g., Agung 1963, Pinatubo 1991).
 - These peaks have no consistent relationship with the steady increase in ${\rm CO}_2$; instead, large eruptions cause short-lived cooling from aerosol injection, but this effect quickly dissipates.
 - The absence of a trend in volcanic activity over the period confirms that volcanoes have not been a driving factor in the sustained rise of global temperatures.

Regression analysis with confidence intervals and robust errors

We perform regression analysis to quantify the relationship between global temperature anomalies and potential drivers such as CO_2 , solar irradiance, and volcanic activity. Using robust standard errors to account for autocorrelation, we estimate model coefficients, compute confidence intervals, and assess the statistical significance of each predictor. This approach ensures more reliable inference when working with time-series climate data.

```
In [15]: # Ensuring that data is sorted by year
         df_reg = combined_corr.copy().dropna(subset=["Global_Anom_C", "CO2_ppm", "TS
         df_reg = df_reg.sort_values("Year").reset_index(drop=True)
         # Simple regression: Temp ~ COD
         X1 = sm.add_constant(df_reg["C02_ppm"])
         y = df_reg["Global_Anom_C"]
         model1 = sm.OLS(y, X1).fit(cov_type="HAC", cov_kwds={"maxlags": 1}) # HAC r
         print("\nSimple regression: Temp ~ COD (HAC robust SEs)")
         print(model1.summary())
         # Multiple regression: Temp ~ COO + TSI anomaly + VEI count
         X2 = sm.add_constant(df_reg[["CO2_ppm", "TSI_anom", "VEI_count_rm3"]])
         model2 = sm.OLS(y, X2).fit(cov_type="HAC", cov_kwds={"maxlags": 1}) # HAC r
         print("\nMultiple regression: Temp ~ COD + TSI anomaly + VEI count (HAC robu
         print(model2.summary())
         # Saving predictions
         df_reg["pred_temp"] = model2.predict(X2)
         # Coefficient table with 95% CIs
         def coef_table(model):
             ci = model.conf_int()
             ci.columns = ["2.5%", "97.5%"]
             return pd.concat([model.params, model.bse, model.tvalues, model.pvalues,
                      .rename(columns={0: "coef", 1: "std err", 2: "t", 3: "P>|t|"})
         print("\n--- Coefficient Table: Simple model ---")
         print(coef_table(model1))
         print("\n--- Coefficient Table: Multiple model ---")
         print(coef_table(model2))
         # Visualization of Regression Results
         sns.set_theme(style="whitegrid", context="talk")
         # Observed vs Predicted over Time
         fig, ax = plt.subplots(figsize=(12, 5))
         ax.plot(df_reg["Year"], df_reg["Global_Anom_C"], color="navy", lw=2.2, label
         ax.plot(df_reg["Year"], df_reg["pred_temp"], color="darkorange", lw=2, ls="-
         ax.set_xlabel("Year", fontsize=13)
         ax.set_ylabel("Global Temperature Anomaly (°C)", fontsize=13)
```

```
ax.set_title("Observed vs Predicted Global Temperature", fontsize=15)
ax.legend(frameon=False, fontsize=12)
ax.grid(alpha=0.3)
plt.tight_layout()
plt.show()
# Observed vs Predicted Scatter
fig, ax = plt.subplots(figsize=(6, 6))
sns.scatterplot(
    x=df_reg["Global_Anom_C"],
    y=df_reg["pred_temp"],
    s=70, color="steelblue",
    edgecolor="white", linewidth=0.6, ax=ax
minv = float(min(df_reg["Global_Anom_C"].min(), df_reg["pred_temp"].min()))
maxv = float(max(df_reg["Global_Anom_C"].max(), df_reg["pred_temp"].max()))
pad = 0.05 * (maxv - minv or 1)
lims = (minv - pad, maxv + pad)
ax.plot(lims, lims, 'k--', lw=2)
ax.set_xlim(lims)
ax.set_ylim(lims)
ax.set_xlabel("Observed ΔT (°C)", fontsize=13)
ax.set_ylabel("Predicted ΔT (°C)", fontsize=13)
ax.set_title("Observed vs Predicted", fontsize=15)
ax.grid(alpha=0.3)
plt.tight_layout()
plt.show()
```

Simple regression: Temp \sim CO \Box (HAC robust SEs) OLS Regression Results

=========			:======				======			
=										
		Global_A	Anom_C	R-squared:			0.92			
Model:			0LS	Adj.	R-squared:		0.92			
Method:		Least So	quares	F-sta	tistic:		531.			
2 Date:	S	at, 16 Aug	2025	Prob	(F-statistic)	:	1.07e-3			
2 Time:		11	42:45	Log-L	ikelihood:		59.50			
2 No. Observation	ons:		66	AIC:			-115.			
0 Df Residuals:			64	BIC:			-110.			
6 Df Model:			1							
Covariance Typ	oe:		HAC							
==========		=======		=====	========		======			
=	coef	std eri	-	Z	P> z	[0.025	0.97			
5]						-				
_										
const	-3.5119	0.167	-21	.063	0.000	-3.839	-3.18			
5 CO2_ppm	0.0107	0.000) 22	047	0.000	0.010	0.01			
2	0.0107	0.000) 23	.047	0.000	0.010	0.01			
==========		=======	======	=====		=======	======			
= Omnibus:			6.772	Durhi	n-Watson:		1.52			
9			01772	Darbi	ii wacsoiii		1.02			
Prob(Omnibus): 6	:		0.034	Jarqu	e-Bera (JB):		2.55			
Skew:			0.023	Prob(JB):		0.27			
9 Kurtosis:			2.037	Cond.	No.		4.11e+0			
3										
=======================================	======	=======	======	=====	========	=======	======			
Notes:										
[1] Standard Errors are heteroscedasticity and autocorrelation robust (HAC) u										
sing 1 lags and without small sample correction [2] The condition number is large, 4.11e+03. This might indicate that there a										
re										
strong multicollinearity or other numerical problems.										
Multiple regression: Temp ~ COU + TSI anomaly + VEI count (HAC robust SEs) OLS Regression Results										
==========		=======	======	=====	=========	=======	======			
= Norichle		Clobal	lnom C	D 6 ~::	orodi		0.00			
Dep. Variable	•	Global_A	ATTOIN_C	к-squ	ai eu:		0.93			

Model: 3		0LS	Adj. R-sq	uared:	0.93				
Method:	Le	ast Squares	F-statist	ic:	275.				
2 Date:	Sat,	16 Aug 2025	Prob (F-s	tatistic):	9.11e-3				
6 Time:		11:42:45	Log-Likel	ihood:	65.48				
0 No. Observations:		66	AIC:			-123.			
0 Df Residuals:		62	BIC:			-114.			
2 Df Model:		3							
Covariance Type:		HAC	-======	========	=======	======			
====	coef	std err	7	D> 7	[0 025	Θ.			
975]					-				
const 3.310	-3.5768	0.136	-26.227	0.000	-3.844	-			
CO2_ppm 0.012	0.0109	0.000	28.452	0.000	0.010				
	0.0824	0.028	2.909	0.004	0.027				
VEI_count_rm3 0.003	-0.0397	0.019	-2.133	0.033	-0.076	-			
=======================================				=======		======			
Omnibus: 7		6.395	Durbin-Wa	tson:		1.84			
, Prob(Omnibus): 1		0.041	Jarque-Bera (JB):			2.52			
Skew:		-0.070	Prob(JB):			0.28			
4 Kurtosis: 3		2.053	Cond. No.			4.27e+0			
=======================================		========		=======		======			
Notes:									
Notes: [1] Standard Errors are heteroscedasticity and autocorrelation robust (HAC) u sing 1 lags and without small sample correction [2] The condition number is large, 4.27e+03. This might indicate that there a re									
strong multicollinearity or other numerical problems.									
Coefficient Table: Simple model coef std err t P> t 2.5% 97.5% const -3.511898 0.166737 -21.062522 1.755730e-98 -3.838696 -3.18510 CO2_ppm 0.010673 0.000463 23.046825 1.582790e-117 0.009765 0.01158									

--- Coefficient Table: Multiple model --- coef std err t P>|t| 2.5% \

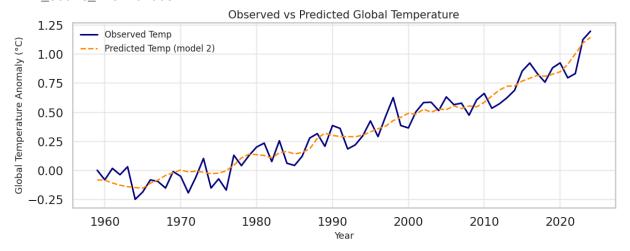
const

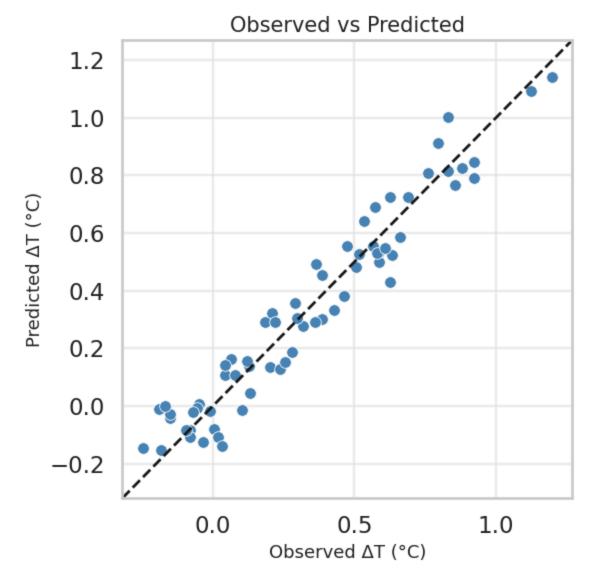
-3.576828 0.136380 -26.226846 1.313359e-151 -3.844128

C02_ppm 0.010903 0.000383 28.451895 4.616964e-178 0.010152 TSI_anom 0.082415 0.028335 2.908587 3.630660e-03 0.026879 VEI_count_rm3 -0.039696 0.018612 -2.132809 3.294039e-02 -0.076176

97.5%

const -3.309527 CO2_ppm 0.011654 TSI_anom 0.137950 VEI_count_rm3 -0.003217





We tested two regression models to explain global temperature anomalies:

- In the simple regression, CO_2 explains 92.3% of the variance in global temperature anomalies ($R^2=0.923$), with a highly significant coefficient of +0.01067 °C per ppm (p < 0.001).
- A 100 ppm increase in CO_2 is linked to about +1.07 °C of warming.
- Adding solar irradiance anomalies (TSI_anom) and volcanic activity (VEI counts) increases explained variance to 93.6% (R² = 0.936).
- CO_2 remains strongest predictor. Even with other factors included, CO_2 retains a coefficient of +0.01090 °C per ppm (p < 0.001), confirming its dominant influence.

- Solar anomalies have a smaller but significant warming effect of +0.0824 °C per W/m² (p = 0.004).
- Large volcanic eruptions (VEI \geq 4) reduce global temperatures by about -0.0397 °C per eruption/year (p = 0.033), reflecting short-term cooling from aerosols.
- Predicted temperatures closely match observations both over time and in scatter plots, with points tightly clustered around the 1:1 line.
- \bullet Recent warming is overwhelmingly driven by rising ${\rm CO}_2$, with solar variability and volcanic activity adding smaller, short-term fluctuations.

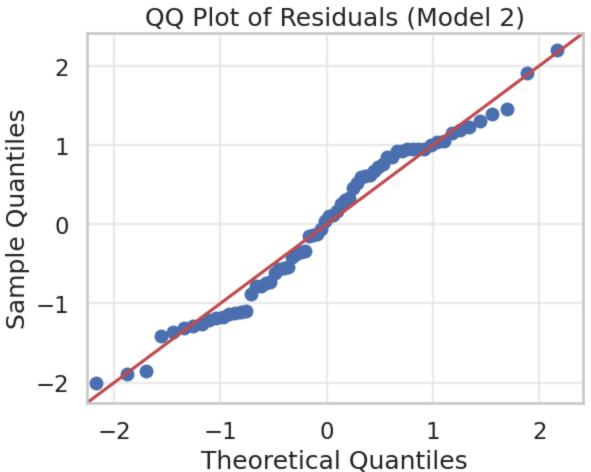
ANOVA model comparison & partial F-test to answer:

We will use ANOVA and a partial F-test to compare two regression models, one that predicts global temperature anomalies using only COO, and another that also includes solar irradiance anomalies (TSI) and volcanic activity as predictors. This statistical comparison allows us to test whether the additional variables provide a significant improvement in explanatory power beyond COO alone.

```
In [16]: # ANOVA comparison
         anova_results = anova_lm(model1, model2)
         print("\n--- ANOVA: Does adding solar + volcanic improve the model? ---")
         print(anova_results)
         # Interpretation
         p_value = anova_results["Pr(>F)"][1]
         if p_value < 0.05:
             print(f"\n Adding TSI anomaly & VEI count significantly improves the mod
             print(f"\n No significant improvement from adding solar & volcanic (p =
         # Model Performance Summary
         print("\nModel 1: Temp ~ CO[")
         print(f" R2: {model1.rsquared:.3f}")
         print(f" Adj R2: {model1.rsquared_adj:.3f}")
         print("\nModel 2: Temp ~ COD + TSI anomaly + VEI count")
         print(f" R2: {model2.rsquared:.3f}")
         print(f" Adj R2: {model2.rsquared_adj:.3f}")
         # Residual diagnostics for Model 2
         residuals = model2.resid
         fitted = model2.fittedvalues
```

```
# Residual plot
 fig, ax = plt.subplots(1, 2, figsize=(12, 5))
 sns.scatterplot(x=fitted, y=residuals, ax=ax[0], color="steelblue", edgecolo
 ax[0].axhline(0, ls="--", color="black")
 ax[0].set_xlabel("Fitted values", fontsize=12)
 ax[0].set_ylabel("Residuals", fontsize=12)
 ax[0].set_title("Residuals vs Fitted", fontsize=14)
 ax[0].grid(alpha=0.3)
 # Histogram and QQ plot for normality
 sns.histplot(residuals, kde=True, ax=ax[1], color="orange", edgecolor="white
 ax[1].set_title("Residuals Distribution", fontsize=14)
 ax[1].set_xlabel("Residual", fontsize=12)
 ax[1].grid(alpha=0.3)
 plt.tight_layout()
 plt.show()
 # QQ plot
 sm.qqplot(residuals, line='45', fit=True)
 plt.title("QQ Plot of Residuals (Model 2)")
 plt.grid(alpha=0.3)
 plt.show()
 # Shapiro-Wilk test for normality
 shapiro_test = stats.shapiro(residuals)
 print(f"\nShapiro-Wilk test for normality: W={shapiro_test[0]:.3f}, p={shapi
--- ANOVA: Does adding solar + volcanic improve the model? ---
                  ssr df_diff
                                                F
                                                      Pr(>F)
   df_resid
                               ss_diff
       64.0 0.636785
0
                           0.0
                                     NaN
                                               NaN
                                                         NaN
       62.0 0.531280
                           2.0 0.105505 6.156196 0.003641
1
 Adding TSI anomaly & VEI count significantly improves the model (p = 0.004)
Model 1: Temp ~ CO
  R2: 0.923
 Adj R2: 0.922
Model 2: Temp ~ COD + TSI anomaly + VEI count
  R2: 0.936
  Adj R2: 0.933
```





Shapiro-Wilk test for normality: W=0.968, p=0.087

• Adding TSI anomaly and VEI (3-yr mean) to CO_2 significantly improves the temperature model (F = 6.16, p = 0.0036).

Explained variance:

- Model 1: Temp ~ $CO_2 \rightarrow R^2 = 0.923$, Adj $R^2 = 0.922$
- Model 2: Temp ~ CO_2 + TSI + VEI \rightarrow R^2 = 0.936, Adj R^2 = 0.933

This is a $\sim 1.3\%$ increase in explained variance — statistically significant but modest in magnitude.

Predictor roles:

- CO₂: Strongest positive driver of warming.
- TSI anomaly: Small positive effect (slight warming influence).
- VEI count: Small negative effect (short-term cooling after major eruptions).

Residual patterns:

No evidence of heteroscedasticity or non-linearity in residuals vs fitted plot.

Normality check:

Histogram and QQ plot closely follow a normal distribution; Shapiro-Wilk W = 0.968, p = $0.087 \rightarrow \text{residuals}$ are consistent with normality.

Autocorrelation:

Durbin-Watson \approx 1.85, indicating mild positive autocorrelation – addressed with HAC robust standard errors.

• Natural variability (solar cycles & volcanic activity) adds a small but measurable contribution to short-term temperature fluctuations. However, ${\rm CO}_2$ overwhelmingly drives the long-term warming trend, and the model is statistically sound.

Final summary table

We will present a final summary table that bring together all key variables temperature anomalies, ${\rm CO}_2$, solar irradiance anomalies, and volcanic activity. These tabular summaries provide a clear overview of the relationships and statistical strengths between the factors examined in our analysis.

```
In [17]: df_corr_final = combined_corr[["Global_Anom_C", "CO2_ppm", "TSI_anom", "VEI_
# Summary statistics table
summary_table = df_corr_final.describe().T

summary_table = summary_table[["mean", "std", "min", "max"]]

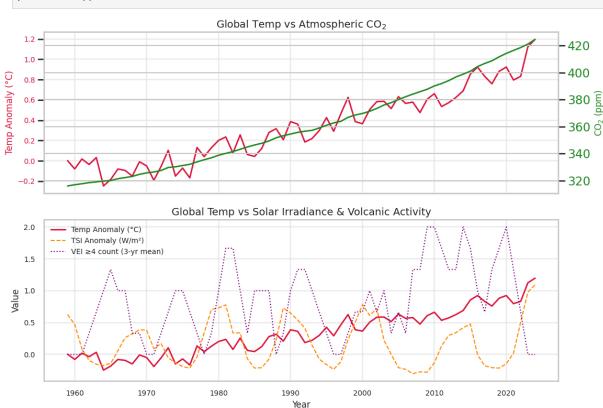
summary_table = summary_table.rename(columns={
    "mean": "Mean",
    "std": "Std Dev",
```

Multi-Panel Overview of Key Climate Relationships

We create a final multi-panel summary plot that combines the most important visualizations from our analysis into a single figure. This compact layout allows for quick comparison of trends, relationships, and model results, providing a clear visual narrative of how CO_2 , solar activity, volcanic activity, and temperature anomalies interact over time.

```
In [18]: sns.set_theme(style="whitegrid", context="talk")
         fig, axes = plt.subplots(2, 1, figsize=(12, 8), sharex=True)
         # Temp vs CO
         ax1 = axes[0]
         ax1.plot(combined_corr["Year"], combined_corr["Global_Anom_C"], color="crims"
         ax1.set_ylabel("Temp Anomaly (°C)", color="crimson", fontsize=12)
         ax1.tick_params(axis='y', labelcolor="crimson")
         ax1b = ax1.twinx()
         ax1b.plot(combined_corr["Year"], combined_corr["CO2_ppm"], color="forestgree"
         ax1b.set_ylabel("CO$_2$ (ppm)", color="forestgreen", fontsize=12)
         ax1b.tick_params(axis='y', labelcolor="forestgreen")
         ax1.set_title("Global Temp vs Atmospheric CO$_2$", fontsize=14)
         # Temp vs Solar & Volcanic
         ax2 = axes[1]
         ax2.plot(combined_corr["Year"], combined_corr["Global_Anom_C"], color="crims"
         ax2.plot(combined_corr["Year"], combined_corr["TSI_anom"], color="darkorange"
         ax2.plot(combined_corr["Year"], combined_corr["VEI_count_rm3"], color="purpl
         ax2.set_ylabel("Value", fontsize=12)
         ax2.set_title("Global Temp vs Solar Irradiance & Volcanic Activity", fontsiz
         ax2.legend(frameon=False, fontsize=10)
         for ax in axes:
             ax.grid(alpha=0.3)
```

```
ax.tick_params(axis='both', labelsize=10)
axes[1].set_xlabel("Year", fontsize=12)
plt.tight_layout()
plt.show()
```



- From 1960 to 2024, global temperature anomalies (red line) rise closely alongside atmospheric ${\rm CO_2}$ concentrations (green line), showing a strong long-term upward trend in both variables.
- The parallel trajectory reinforces the very high correlation between CO_2 and temperature (r \approx 0.96), consistent with regression results where CO_2 is the dominant predictor of warming.
- While TSI (orange dashed line) shows cyclical peaks and troughs linked to the ~ 11 -year solar cycle, its magnitude of variation is small compared to the CO_2 -driven warming trend.
- Periods of high volcanic activity (purple dotted line) often coincide with short-term dips in temperature anomalies, reflecting temporary cooling effects from large eruptions.
- After major volcanic events, temperatures generally rebound within a few years, resuming the CO_2 -driven warming trajectory.

• Natural factors (solar cycles & volcanic eruptions) influence short-term variability, but the long-term warming pattern is overwhelmingly governed by the persistent rise in atmospheric ${\rm CO}_2$

Interpretations and conclusions

- \bullet Our analysis shows a clear and statistically significant positive correlation between atmospheric ${\rm CO}_2$ concentrations and global surface temperature anomalies.
- \bullet The data indicate that the recent and sustained warming trend aligns closely with rising ${\rm CO}_2$ levels, while solar irradiance and volcanic activity explain far less of the observed variation.
- \bullet Regression models with robust errors confirm ${\rm CO_2}$ as the dominant predictor, and ANOVA results show only marginal improvement when adding solar and volcanic variables.
- These findings are consistent with the scientific consensus that human-driven increases in greenhouse gases, particularly CO_2 , are the primary cause of modern global warming

References

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