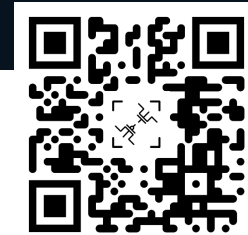




Design and Simulation of RF Integrated Circuits with Open-Source CAD Tools and Process Design Kits

SLIDES >>>>>>>>>



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Tutorial Outline

- **Part 1:**

Advanced Compact MOSFET Model 2 - ACM2 model

- **Part 2:**

Implementing the ACM2 model

- **Part 3:**

ACM2 - Parameter extraction

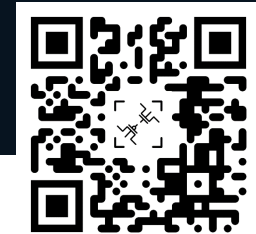
- **Part 4:**

Design Methodology-Application to Low Noise Amplifier



Part 1

Advanced Compact MOSFET Model: ACM2



Carlos Galup-Montoro

https://github.com/ACMmodel/MOSFET_model

Outline

- **Introduction: ACM timeline**
- **ACM2 model**
- **Long-channel: I_D and g_m/I_D models**

ACM timeline

- 1993 ϕs -based model (SBMICRO, Campinas, Br)
- 1995 Long-channel charge-based model (SSE, Nov.)
- 1998 Most referenced ACM paper (JSSC, Oct.)
- 2000 ACM model in SMASH simulator (CICC, Orlando)

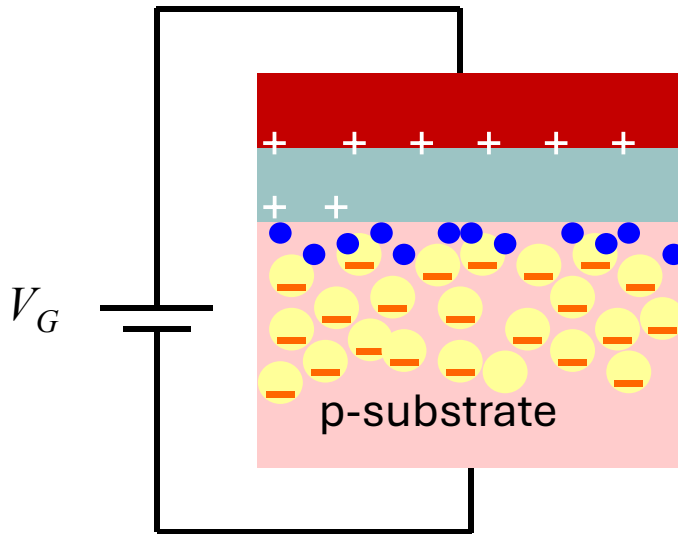


- 2018 Short course on ACM for ST organized by Prof. Silvain at Grenoble
- 2021 4-parameter single-piece model (NorCAS, Oslo)
- 2023 ACM2 in VERILOG-AMS (NEWCAS, Edinburgh)

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The capacitive model of the MOSFET



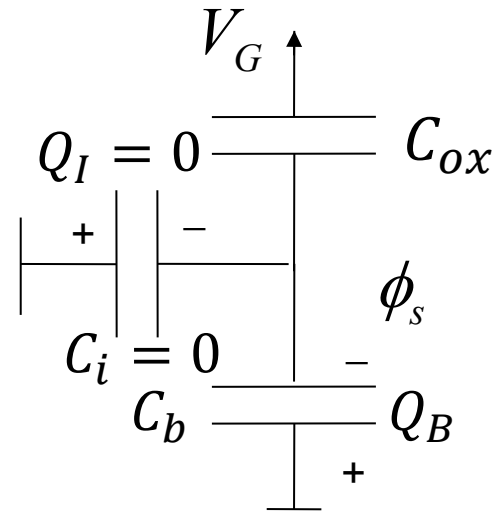
ϕ_s surface potential

C_{ox} oxide capacitance per unit area

C_b depletion capacitance per unit area

Q_I carrier charge density

V_{T0} threshold voltage



$$\frac{\Delta\phi_s}{\Delta V_G} = \frac{C_{ox}}{C_{ox} + C_b} = \frac{1}{n}$$

$$\phi_s = 2\phi_F + \frac{V_G - V_{T0}}{n} = 2\phi_F + V_P$$

ACM2 current law

From 3 approximations: normalized current vs. normalized charge densities at source and drain



$$i_D = \frac{(q_S + q_D + 2)}{1 + \zeta(q_S - q_D)} (q_S - q_D)$$

$$i_D = I_D/I_S \quad I_S = \frac{W}{L} \mu_s n C_{ox} \frac{\phi_t^2}{2}$$

normalization (specific) current

$$q_{S(D)} = Q_{S(D)} / (-n C_{ox} \phi_t)$$

$-n C_{ox} \phi_t$ thermal charge

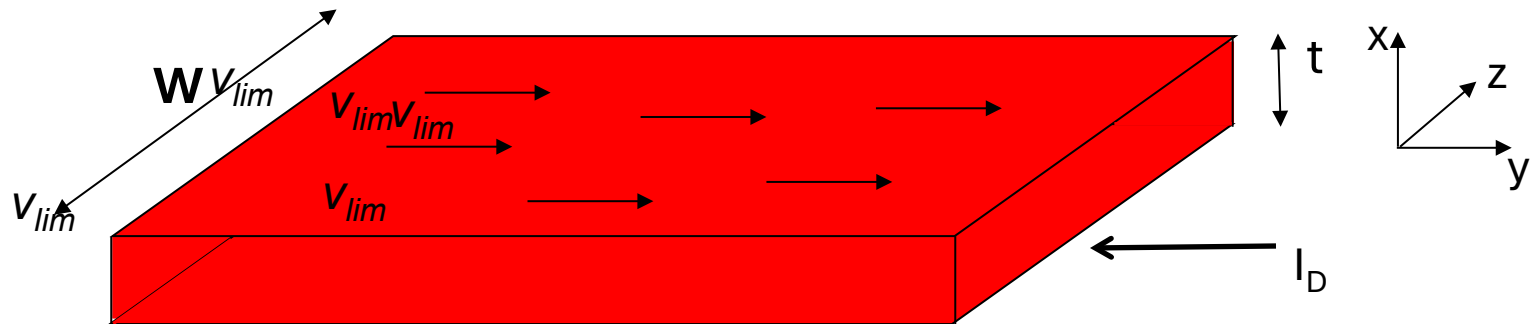
$$SI : q_{S(D)} \gg 1 \quad WI : q_{S(D)} \ll 1$$

Short-channel parameter ζ :

$$\zeta = \frac{(\mu_s \phi_t / L)}{v_{lim}}$$

ratio of diffusion-related velocity to saturation velocity

Physics-based saturation



Saturation current due to saturation velocity of the carriers

$$I_{Dsat} = -W Q_{Dsat} v_{lim}$$

Q_{Dsat} is the saturation inversion charge per unit area

or, using normalized variables

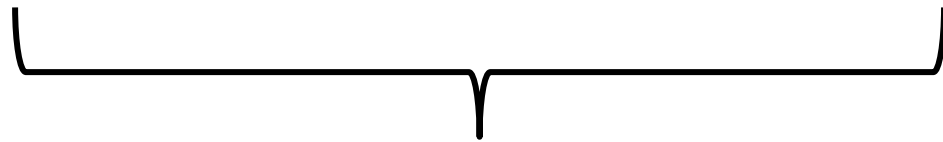
$$i_{Dsat} = \frac{2}{\zeta} q_{dsat}$$

“Carrier velocity approaches v_{sat} , but never reaches v_{sat} ”

Y.Taur TED March 2019

Physics-based saturation: design model

$$i_{Dsat} = \frac{2}{\zeta} q_{dsat} \qquad i_{Dsat} = \frac{(q_s + q_{Dsat} + 2)}{1 + \zeta(q_s - q_{Dsat})} (q_s - q_{Dsat})$$



$$q_{Dsat} = q_s + 1 + \frac{1}{\zeta} - \sqrt{\left(1 + \frac{1}{\zeta}\right)^2 + \frac{2q_s}{\zeta}}$$

or equivalently

$$q_s = \sqrt{1 + \frac{2}{\zeta} q_{dsat}} - 1 + q_{dsat}$$

The Unified Charge Control Model (UCCM)

$$\frac{V_P - V_C}{\phi_t} = q_I - 1 + \ln q_I$$

$$V_S \leq V_C \leq V_D$$

$$q_S \leq q_I \leq q_D$$



$$\frac{V_{DS}}{\phi_t} = q_S - q_D + \ln \frac{q_S}{q_D}$$

The “Regional” Weak (WI) and Strong Inversion (SI) Approximations

WI

SI

$$q_I \ll 1 \rightarrow V_P - V_C \ll -\phi_t$$

$$q_I \gg 1 \rightarrow V_P - V_C \gg \phi_t$$

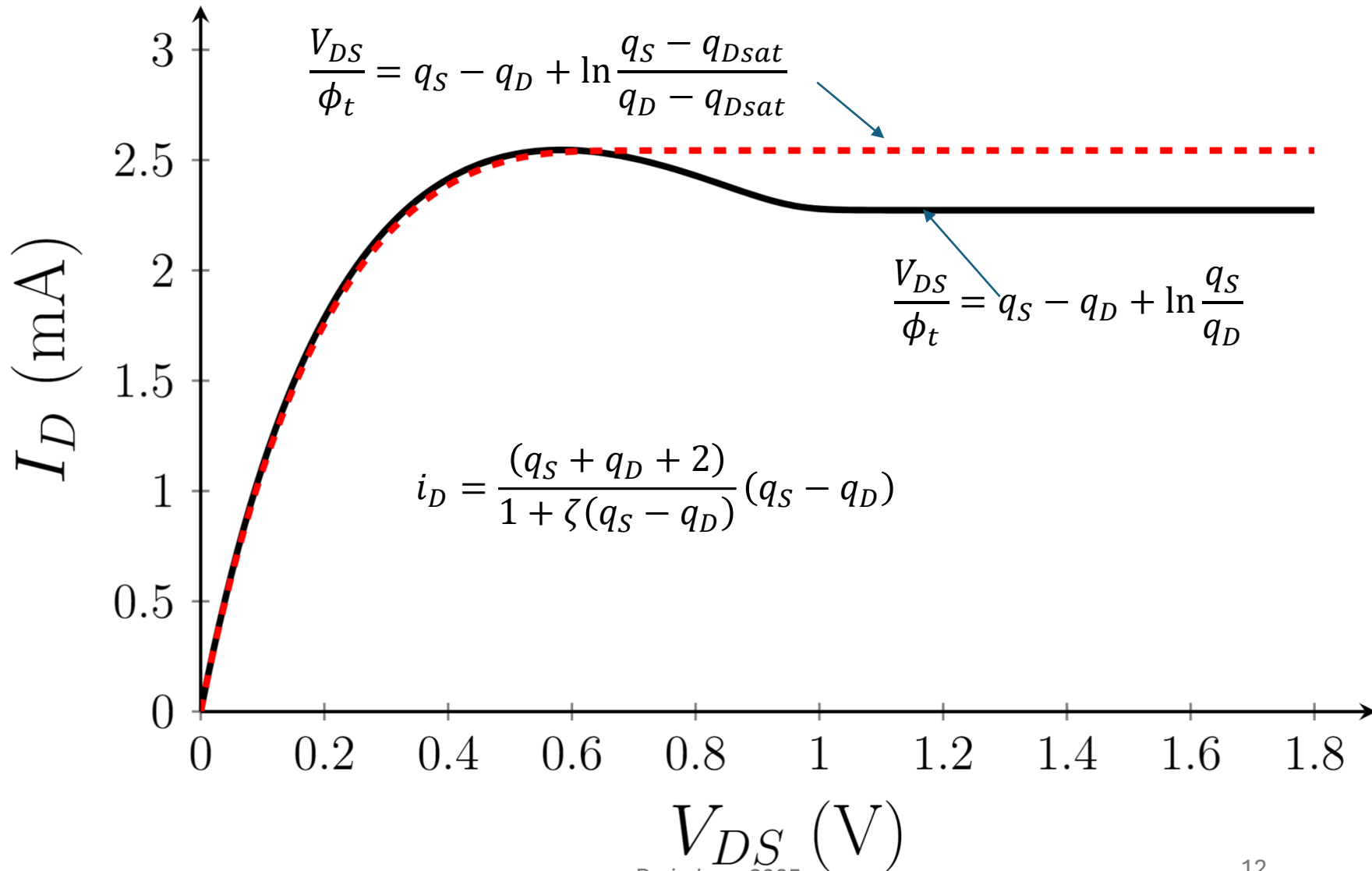
$$q_I \cong e^{\frac{V_P - V_C + \phi_t}{\phi_t}}$$

$$q_I \cong \frac{V_P - V_C + \phi_t}{\phi_t}$$

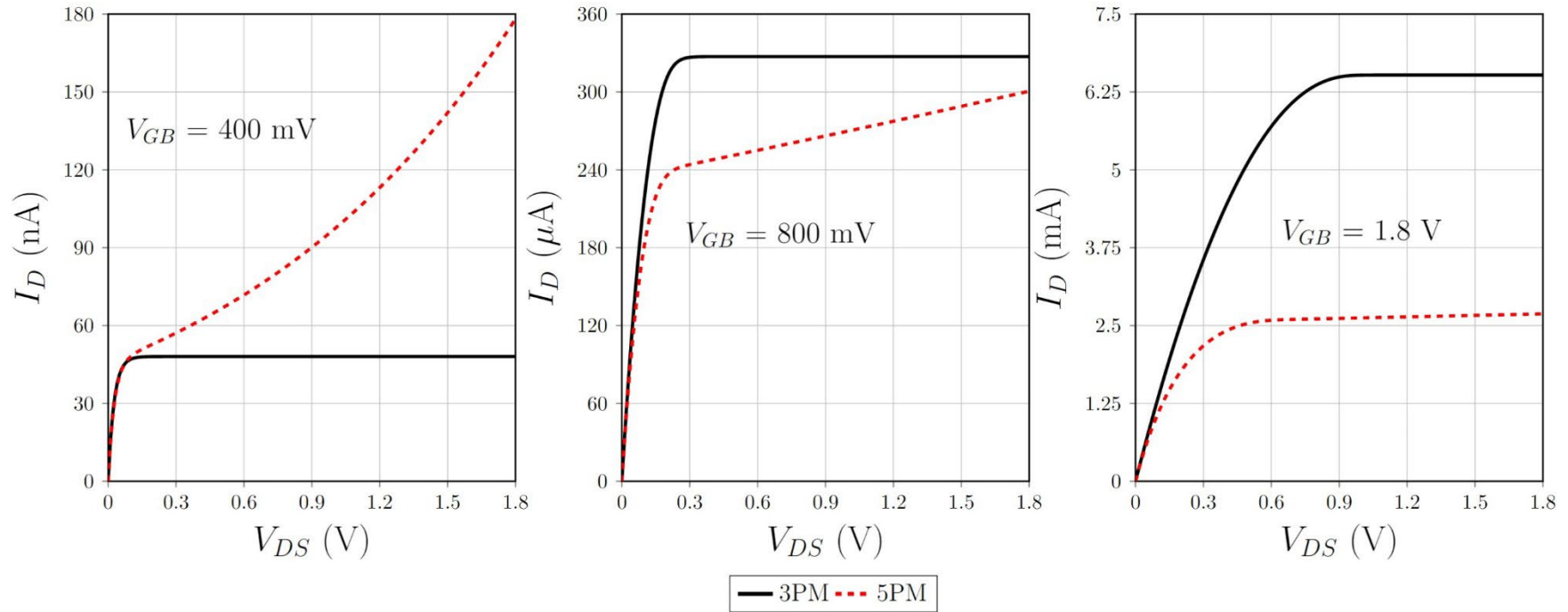
Error <10% for $q_I < 0.22$

Error <10% for $q_I > 20$

UCCM including the effect of velocity saturation



Output curves including DIBL and v_{sat}



DIBL model: $V_T = V_{T0} - \sigma(V_S + V_D)$

Transistor	W/L ($\mu\text{m}/\mu\text{m}$)	V_{T0} (mV)	I_S (μA)	n	σ	ζ
NMOS2V	5/0.18	528	5.52	1.37	0.025	0.056

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- Introduction: ACM timeline
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Long-channel charge-based model

For short channel MOS

$$I_D = I_S \frac{(q_S + q_D + 2)}{1 + \zeta(q_S - q_D)} (q_S - q_D)$$

$$\frac{V_P - V_S}{\phi_t} = q_S - 1 + \ln q_S \quad \frac{V_{DS}}{\phi_t} = q_S - q_D + \ln \frac{q_S - q_{Dsat}}{q_D - q_{Dsat}}$$

For long channel MOS $\zeta=0 \rightarrow q_{Dsat}=0$

$$I_D = I_S(q_S + q_D + 2)(q_S - q_D) = I_S[(q_S^2 + 2q_S) - (q_D^2 + 2q_D)]$$

$$\frac{V_P - V_{S(D)}}{\phi_t} = q_{S(D)} - 1 + \ln q_{S(D)}$$

$$\text{Obs: } \frac{dq_{S(D)}}{dV_G} = -\frac{1}{n} \frac{dq_{S(D)}}{dV_{S(D)}} \quad \frac{dq_D}{dV_D} = -\frac{1}{\phi_t} \frac{q_D}{q_D + 1} \quad \frac{dI_D}{dq_D} = -2I_S(q_D + 1)$$

Small-signal transconductances

$$g_{md} = \frac{dI_D}{dV_D} = \frac{dI_D}{dq_D} \frac{dq_D}{dV_D} = 2I_S(q_D + 1) \frac{1}{\phi_t} \frac{q_D}{q_D + 1} = \frac{2I_S}{\phi_t} q_D$$

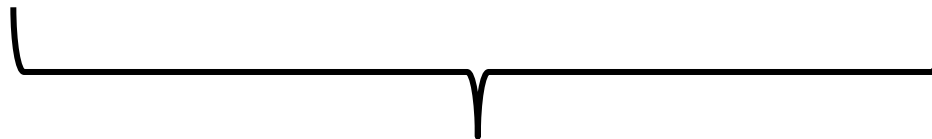
Symmetry



$$g_{ms} = \frac{2I_S}{\phi_t} q_S$$

**Amazingly simple
(see Appendix)**

$$g_m = \frac{dI_D}{dV_G} = \frac{dI_D}{dq_S} \frac{dq_S}{dV_G} + \frac{dI_D}{dq_D} \frac{dq_D}{dV_G} \qquad \frac{dq_{S(D)}}{dV_G} = -\frac{1}{n} \frac{dq_{S(D)}}{dV_{S(D)}}$$



$$g_m = \frac{g_{ms} - g_{md}}{n}$$

$$g_m = \frac{g_{ms}}{n} \longrightarrow \text{in saturation}$$

Unified Current Control Model (UICM)-I

$$I_D = I_S[(q_S^2 + 2q_S) - (q_D^2 + 2q_D)] \quad (A)$$

(A) can also be written as

$$I_D = I_F - I_R = I_S[i_f - i_r] \quad (B)$$

I_F, I_R : forward and reverse currents

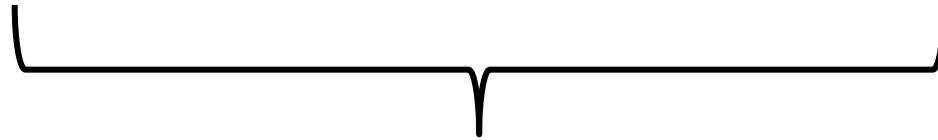
$i_{f(r)} = q_{S(D)}^2 + 2q_{S(D)}$: forward (reverse) inversion coefficients

$$\downarrow$$
$$q_{S(D)} = \sqrt{1 + i_{f(r)}} - 1$$

Unified Current Control Model (UICM)-II

$$\frac{V_P - V_{S(D)}}{\phi_t} = q_{S(D)} - 1 + \ln q_{S(D)}$$

$$q_{S(D)} = \sqrt{1 + i_{f(r)}} - 1$$



Normalized UICM

$$\frac{V_P - V_{S(D)}}{\phi_t} = \sqrt{1 + i_{f(r)}} - 2 + \ln \left(\sqrt{1 + i_{f(r)}} - 1 \right)$$



$$\frac{V_{DS}}{\phi_t} = q_S - q_D + \ln \frac{q_S}{q_D} = \sqrt{1 + i_f} - \sqrt{1 + i_r} + \ln \left(\frac{\sqrt{1 + i_f} - 1}{\sqrt{1 + i_r} - 1} \right)$$

$$g_m/I_D$$

$$g_{ms(d)} = \frac{2I_S}{\phi_t} \left(\sqrt{1 + i_{f(r)}} - 1 \right) = \frac{W}{L} \mu C_{ox} n \phi_t \left(\sqrt{1 + i_{f(r)}} - 1 \right)$$

$$g_m = \frac{g_{ms} - g_{md}}{n}$$

$$\frac{g_m}{I_D} = \frac{2}{n \phi_t (\sqrt{1 + i_f} + \sqrt{1 + i_r})}$$

For $V_{DS}/\phi_t \ll 1$ we have $i_f \approx i_r$

In saturation $i_f \gg i_r$

$$\frac{g_m}{I_D} \cong \frac{1}{n \phi_t \sqrt{1 + i_f}}$$

$$\frac{g_m}{I_D} \cong \frac{2}{n \phi_t (\sqrt{1 + i_f} + 1)}$$

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- A. I. A. Cunha, M. C. Schneider and C. Galup-Montoro, "Derivation of the Unified Charge Control Model and Parameter Extraction Procedure", Solid-State Electronics, March 1999.
- O. C. Gouveia Filho, A. I. A. Cunha, M. C. Schneider and C. Galup-Montoro, "Advanced compact model for short-channel MOS transistors", IEEE Custom Integrated Circuits Conference, Orlando, FL, USA, May 2000.
- C. Galup-Montoro and M. C. Schneider, *MOSFET Modeling for Circuit Analysis and Design*, World Scientific, 2007.
- C. M. Adornes, D. G. Alves Neto, M. C. Schneider and C. Galup-Montoro, "Bridging the Gap between Design and Simulation of Low-Voltage CMOS Circuits", Journal of Low Power Electronics and Applications, June 2022.
- D. G. Alves Neto *et al*, "Design-oriented single-piece 5-DC parameter MOSFET model," *IEEE Access*, 2024.

Appendix: the exact model of the long-channel MOSFET¹

$$I_D = -\frac{W}{L} \int_{V_S}^{V_D} \mu Q_I(V_C) dV_C$$

Consequently, the **exact** expressions for g_{ms} and g_{md} are

$$g_{md} = \frac{dI_D}{dV_D} = -\frac{W}{L} \mu Q_D = \frac{2I_S}{\phi_t} q_D$$

$$g_{ms} = -\frac{dI_D}{dV_S} = -\frac{W}{L} \mu Q_S = \frac{2I_S}{\phi_t} q_S$$

¹ H. C. Pao and C. T. Sah, 'Effects of diffusion current on characteristics of metal-oxide (insulator)-semiconductor transistors' Solid-State Electronics, Oct 1966