$$\left(\bigcup_{p \in \uparrow} \{f(p)\}\right) \supseteq \uparrow \left(\bigcup_{i \in I} \{f(s_i)\}\right)$$