$$id_{\mathbf{A}}: \mathbf{A}^{op} \times \mathbf{A} \rightarrow_{\mathbf{Pos}} \mathbf{Bool},$$

$$\langle a_1^*, a_2 \rangle \mapsto a_1 \leq_{\mathbf{A}} a_2.$$