

**Lemma.** Given  $\mathbf{d}, \mathbf{e} \in \text{Hom}_{\mathbf{DP}}(\mathbf{P}; \mathbf{Q})$  and  $\mathbf{g}, \mathbf{h} \in \text{Hom}_{\mathbf{DP}}(\mathbf{R}; \mathbf{S})$ , one has:

$$\frac{\mathbf{d} \leq_{\mathbf{DP}} \mathbf{e} \quad \mathbf{g} \leq_{\mathbf{DP}} \mathbf{h}}{\mathbf{d} \otimes \mathbf{g} \leq_{\mathbf{DP}} \mathbf{e} \otimes \mathbf{h}}.$$

In other words, the monoidal product preserves order on  $\mathbf{DP}$ .