

**Definition** (Category of  $M$ -algebras). Let  $\langle M, \text{un}, \text{mu} \rangle$  be a monad on a category  $\mathbf{C}$ . The *category of  $M$ -algebras*  $\mathbf{C}^M$  of the monad  $M$  is specified by:

1. *Objects*:  $M$ -algebras;
2. *Morphisms*:  $M$ -algebra morphisms;
3. *Identities*: given an  $M$ -algebra  $\langle X, a \rangle$ , its identity morphism is  $\text{Id}_X$ ;
4. *Composition*: is induced by the composition of morphisms in  $\mathbf{C}$ .