

**Lemma.** The  $\mathcal{U}$  endofunctor is indeed a functor.