

Lemma. The composition of semigroup morphisms is a morphism:

$$\frac{F : S \rightarrow T \quad G : T \rightarrow U}{F \circ G : S \rightarrow U}$$