

$$\text{Id}_S(x \circ_S y) = x \circ_S y = \text{Id}_S(x) \circ_S \text{Id}_S(y)$$