

$$\text{Lact}(x) \circ_{\text{End}(A)} \text{Lact}(y) = \text{Lact}(x \circ_S y)$$