Definition (Trace of an endomorphism)

Let $\langle \mathbf{C}, \boldsymbol{\otimes}, \mathbf{1}_{\mathbf{C}}, \mathrm{br} \rangle$ be a symmetric monoidal category. Let $X \in \mathrm{Ob}_{\mathbf{C}}$ be dualizable and let $f \in \mathrm{Hom}(X,X)$. The *trace* of f is the morphism $\mathrm{Tr}(f) \in \mathrm{Hom}(\mathbf{1},\mathbf{1})$

defined by $1 \xrightarrow{\operatorname{coev}_X} X \otimes X^{\vee} \xrightarrow{f \otimes \operatorname{id}_{X^{\vee}}} X \otimes X^{\vee} \xrightarrow{\operatorname{br}} X^{\vee} \otimes X \xrightarrow{\operatorname{ev}_X} 1$