

$A \leq_{AP} B$  if and only if  $\uparrow A \supseteq \uparrow B$