Definition (*U* endofunctor)

The U endofunctor has the form U: $Pos \rightarrow Pos$ and acts on objects and morphisms as follows:

1. On objects: Given a poset $P \in Ob_{Pos}$, U maps P to its upper set.

{bhfn:1}

2. *On morphisms*: Given posets P, Q, and a monotone map $f: P \rightarrow Q$, the U endofunctor acts as:

$$U(f): \mathcal{U}\mathbf{P} \to \mathcal{U}\mathbf{Q}$$

$$\mathbf{P'} \mapsto \mathbf{\uparrow} \left(\bigcup_{p \in \mathbf{P'}} \{f(p)\} \right).$$