

$$f_1 \mapsto \begin{cases} \text{Min } r_4 & r_1 \in h_a(f_1, f_2) & r_1 \preceq f_3 & f_3 = \langle f_4, f_5 \rangle \\ & r_2 \in h_b(f_4) & r_4 \preceq f_2 & r_4 = \langle r_2, r_3 \rangle \\ & r_3 \in h_c(f_5) \end{cases}$$