**Lemma.** Functions from X to  $\mathcal{P}Y$  are exactly the relations from X to Y.