

Definition (Locally posetal 2-category). A 2-category \mathbf{C} is *locally posetal* (or enriched in \mathbf{Pos}) if every hom-category $\mathbf{Hom}_{\mathbf{C}}(x, y)$ is a poset.