

$$\mathrm{Tr}^{X\otimes Y}_{A,B}(f) = \mathrm{Tr}^X_{A,B}\left(\mathrm{Tr}^Y_{A\otimes X,B\otimes X}(f)\right)$$