Definition (Semicategory)

A semicategory **C** is specified by:

Constituents

- 1. Objects: A collection $Ob_{\mathbf{C}}$ whose elements are called *objects*.
- 2. Morphisms: For every pair of objects X, Y in $\mathsf{Ob}_{\mathbb{C}}$, there is a set called "homset" and indicated as $\mathsf{Hom}_{\mathbb{C}}(X;Y)$, elements of which are called *morphisms*. We write

$$f: X \rightarrow_{\mathbf{C}} Y$$

to indicate

$$f \in \operatorname{Hom}_{\mathbb{C}}(X; Y)$$
.

3. Composition operations: For every three objects X, Y, Z in $\mathsf{Ob}_{\mathbf{C}}$ there is a composition map

$$\S_{X,Y,Z}$$
: $\operatorname{Hom}_{\mathbf{C}}(X;Y) \times \operatorname{Hom}_{\mathbf{C}}(Y;Z) \to \operatorname{Hom}_{\mathbf{C}}(X;Z)$.

We usually just write $\frac{1}{9}$ instead of $\frac{1}{9}X,Y,Z$:

$$f: X \to Y \quad g: Y \to Z$$

$$(f \circ g): X \to Z$$

Conditions

1. Associativity: it holds that

$$f: X \to Y \quad g: Y \to Z \quad h: Z \to U$$

$$(f \ g) \ h = f \ (g \ h)$$