

**Lemma.** Functions from  $X$  to  $\mathcal{P}Y$  are exactly the relations from  $X$  to  $Y$ .