

Definition (Sum of functionalities for monoidal posets)

If the poset \mathbf{P} is monoidal with monoidal product \otimes , then the “*sum*” of m copies of \mathbf{P} is a design problem given by

$$\Sigma_m : \mathbf{P} \times (\mathbf{P}^m)^{\text{op}} \longrightarrow_{\text{Pos}} \mathbf{Bool}$$

$$\langle p^*, \langle q_1, \dots, q_m \rangle \rangle \longmapsto (p \leq_{\mathbf{P}} q_1 \otimes \dots \otimes q_m).$$

Diagrammatically:

