$S_1 \preceq_{\mathcal{AP}} S_2 \ \equiv \uparrow S_1 \supseteq \uparrow S_2.$