

**Definition** (Sum of resources)

If the poset  $\mathbf{P}$  is monoidal with monoidal product  $\otimes$ , then the “*sum*” of  $n$  copies of  $\mathbf{P}$  is a design problem given by

$$\Sigma^n : (\mathbf{P}^n)^{\text{op}} \times \mathbf{P} \longrightarrow_{\text{Pos}} \mathbf{Bool},$$
$$\langle \langle p_1, \dots, p_n \rangle^*, q \rangle \longmapsto (p_1 \otimes \dots \otimes p_n \leq_{\mathbf{P}} q).$$

Clearly  $\Sigma^n$  is monotone. Diagrammatically:

