$$F(\text{inv}_{\mathbf{G}}(x)) = \text{inv}_{\mathbf{H}}(F(x))$$
?