$$id_{\mathbf{P}}: \mathbf{P}^{op} \times \mathbf{P} \rightarrow_{\mathbf{Pos}} \mathbf{Bool},$$
 
$$\langle p_1^*, p_2 \rangle \mapsto p_1 \leq_{\mathbf{P}} p_2.$$