

**Definition** (Isomorphism). Let  $\mathbf{C}$  be a category, let  $X, Y \in \mathbf{C}$  be objects, and let  $f : X \rightarrow Y$  be a morphism. We say that  $f$  is an *isomorphism* if there exists a morphism  $g : Y \rightarrow X$  such that  $f \circ g = \text{Id}_X$  and  $g \circ f = \text{Id}_Y$ .