$F(\operatorname{inv}_{\mathbf{G}}(x)) = \operatorname{inv}_{\mathbf{H}}(F(x))$?