$H:\langle \mathbb{N},\cdot,1\rangle \to \langle \{1\},\cdot,1\rangle$