

Definition (General orthogonal group $O(n)$). The general orthogonal group of order n , written $O(n)$, is the group of $n \times n$ square matrices that satisfy

$$\mathbf{M}\mathbf{M}^\top = \mathbf{M}^\top\mathbf{M} = \mathbb{1}.$$