

Definition (Semi-functor). A *semi-functor* $F : \mathbf{C} \rightarrow \mathbf{D}$ between two semi-categories is defined by a map

$$F_{\text{ob}} : \text{Ob}_{\mathbf{C}} \rightarrow \text{Ob}_{\mathbf{D}}.$$

and, for every pair of objects X, Y , a map

$$F_{\text{mor}} : \text{Hom}_{\mathbf{C}}(X; Y) \rightarrow \text{Hom}_{\mathbf{D}}(F_{\text{ob}}(X); F_{\text{ob}}(Y))$$

such that

$$\frac{f : X \rightarrow_{\mathbf{C}} Y \quad g : Y \rightarrow_{\mathbf{C}} Z}{F_{\text{mor}}(f \circ g) = F_{\text{mor}}(f) \circ F_{\text{mor}}(g)}.$$