$f: X \to (Y \times \mathbb{R}_{\geq 0})$