$A \leq_{\mathcal{A}\mathbf{P}} B$ if and only if $\uparrow A \supseteq \uparrow B$