

Lemma. Let A and B be subsets of \mathbf{P} that are antichains. Then

$$\uparrow A = \uparrow B \quad \Rightarrow \quad A = B.$$