$$Lu, d, Uu : \mathbf{F}^{\mathrm{op}} \to_{\mathbf{Pos}} \langle \mathcal{U}\mathbf{R}, \subseteq \rangle$$