Definition (Lattice homomorphism)

Given two bounded lattices **P**, **Q**, a *lattice homomorphism* is a map $f: \mathbf{P} \rightarrow \mathbf{P}$ **Q** which preserves meets, joins, top, and bottom:

$$f(p \wedge_{\mathbf{P}} q) = f(p) \wedge_{\mathbf{Q}} f(q)$$

$$f(p \vee_{\mathbf{P}} q) = f(p) \vee_{\mathbf{Q}} f(q)$$

$$f(p \lor_{\mathbf{P}} q) = f(p) \lor_{\mathbf{Q}} f(q)$$
$$f(\bot_{\mathbf{P}}) = \bot_{\mathbf{Q}}$$

 $f(\mathsf{T}_{\mathbf{P}}) = \mathsf{T}_{\mathbf{O}}$