Definition (Lower set). A *lower set* **L** is a subset of a poset **P** if, if a point is inside, all points below it are inside as well. In other words:

$$\frac{x \in \mathbf{L} \quad y \leq_{\mathbf{P}} x}{y \in \mathbf{L}}$$