Lemma. \odot : $\mathbf{DP} \times \mathbf{DP} \to \mathbf{DP}$ is monotone on $\langle \mathbf{DP}, \leq_{\mathbf{DP}} \rangle$.