Lemma. $\mathcal{A}\mathbf{P}$ is a poset with the relation $\leq_{\mathcal{A}\mathbf{P}}$ defined by

 $A \leq_{\mathcal{A}\mathbf{P}} B \equiv \uparrow A \supseteq \uparrow B.$