$\frac{d \leq_{DP} e \quad g \leq_{DP} h}{d \, g \leq_{DP} e \, h}.$

In other words, series composition is order-preserving on **DP**.

Lemma. Given $\mathbf{d}, (\mathbf{d} \circ \mathbf{e}) \in \operatorname{Hom}_{\mathbf{DP}}(\mathbf{P}; \mathbf{Q})$ and $\mathbf{g}, \mathbf{h} \in \operatorname{Hom}_{\mathbf{DP}}(\mathbf{Q}; \mathbf{R})$ one has: