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- 1. Objects: objects are posets;
- 2. *Morphisms*: given objects  $X, Y \in \operatorname{Ob}_{\mathbf{Pos}_{\mathcal{Y}}}$ , morphisms  $f : X \to Y$  are monotone maps of the form  $f^* : X \to_{\mathbf{Pos}} \langle \mathcal{L} \mathbf{Y}^{\mathrm{op}}, \subseteq \rangle$ .
- 3. *Composition of morphisms*: Given morphisms  $f: X \to Y, g: Y \to Z$ , their composition  $f \circ g: X \to Z$  is given by

$$f^{\star} \circ g^{\star} : X \to_{\mathbf{Pos}} \langle \mathcal{L}\mathbf{Z}^{\mathrm{op}}, \subseteq \rangle$$
$$x \mapsto \bigcup_{y \in f^{\star}(x)} g^{\star}(y);$$

4. *Identity morphism*: given an object  $X \in \mathrm{Ob}_{\mathbf{Pos}_{\mathscr{S}}}$ , the identity morphism is given by the application of the lower closure operator:  $\mathrm{Id}_X(x) := \downarrow \{x\}$ .