$$\operatorname{Hom}_{\mathbf{C}}(f): \operatorname{Hom}_{\mathbf{C}}(X;Y) \to \operatorname{Hom}_{\mathbf{C}}(Z;U)$$

$$g \mapsto (f_1 \circ g \circ f_2).$$