

Definition (Semigroup covariant action (preliminary version)). A *semigroup covariant action* of a semigroup \mathbf{S} on a set \mathbf{A} is a map

$$\text{Covact} : \mathbf{S} \times \mathbf{A} \rightarrow \mathbf{A}$$

such that, for all $a \in \mathbf{A}$,

$$\text{Covact}(y, \text{Covact}(x, a)) = \text{Covact}(x \circ_{\mathbf{S}} y, a).$$