$$\mathbf{d}_k : \mathbf{F}_k \longrightarrow \mathbf{R}_k$$