

**Lemma.**  $\alpha$  and  $\beta$  are antitone maps.