$$\Psi_{f_1}^h : \mathcal{AR} \to \mathcal{AR},$$

$$R \mapsto \operatorname{Min}_{\preceq_R} \bigcup_{r \in R} h(f_1, r) \cap \mathord{\uparrow} r. \tag{0.1}$$