

**Lemma.** Let **A** and **B** be subsets of **P** that are antichains. Then

$$\frac{\uparrow \mathbf{A} = \uparrow \mathbf{B}}{\mathbf{A} = \mathbf{B}} .$$