

$$\Phi_{f_1} : \mathcal{A}(\mathbf{R}) \rightarrow \mathcal{A}(\mathbf{R})$$

$$S \mapsto \operatorname{Min}_{\leq \mathbf{R}} \bigcup_{r \in S} h(f_1, r) \cap \uparrow r$$