

$$(\mathbf{br}_{U,Y} \circ (f \otimes g))^{\star}(x,z) = \left\langle \bigcup_{z' \in \uparrow\{z\}} g^{\star}(z'), \bigcup_{x' \in \uparrow\{x\}} f^{\star}(x') \right\rangle.$$