

$$f: \mathbf{X} \rightarrow (\mathbf{Y} \times \mathbb{R}_{\geq 0})$$