$$\alpha : \mathscr{L}\mathbf{P} \to \mathscr{U}\mathbf{Q}$$

$$S \mapsto \{q \in \mathbf{Q} : \exists p \in S : d(p, q)\},$$