**Lemma.** Let A be an antichain in **P**. Then  $a \in A \equiv \{a\} = A \cap \uparrow a.$