

**Lemma.**  $\vdash : DP \rightarrow DP$  is monotone on  $\langle DP, \leq_{DP} \rangle$ .