

$$\text{br}_{c,d} \circ \text{br}_{d,c} = \text{Id}_c \otimes \text{Id}_d$$