$$Y^{\vee} \xrightarrow{\operatorname{ru}_{Y}^{-1}} Y^{\vee} \otimes \mathbf{1} \xrightarrow{\operatorname{id}_{Y^{\vee}} \otimes \operatorname{coev}_{X}} Y^{\vee} \otimes (X \otimes X^{\vee})$$

$$\xrightarrow{\operatorname{as}^{-1}} (Y^{\vee} \otimes X) \otimes X^{\vee} \xrightarrow{\operatorname{(id}_{Y^{\vee}} \otimes f) \otimes \operatorname{id}_{X^{\vee}}} (Y^{\vee} \otimes Y) \otimes X^{\vee}$$

$$\xrightarrow{\operatorname{ev}_{Y} \otimes \operatorname{id}_{X^{\vee}}} \mathbf{1} \otimes X^{\vee} \xrightarrow{\operatorname{lu}_{X^{\vee}}} X^{\vee}$$