$A \preceq_{\mathcal{A}^{\mathbb{P}}} B$ if and only if $\uparrow A \supseteq \uparrow B$