$\operatorname{br}_{c,d} \circ \operatorname{br}_{d,c} = \operatorname{Id}_{c \otimes d}$