

Lemma. Given a poset \mathbf{P} and a family of upper sets of \mathbf{P} , denoted $\{\mathbf{P}_i\}_{i \in I}$ (with index set I), their union is also an upper set.