

# Definition (Min)

$\text{Min} : \mathcal{P}\mathbf{P} \rightarrow \mathcal{A}\mathbf{P}$  is the map that sends a subset  $\mathbf{A}$  of a poset to the minimal elements of that subset (those elements  $a \in S$  such that  $a \leq_{\mathbf{P}} b$  for all  $b \in \mathbf{A}$ ).  
In formulas:

$$\text{Min} : \mathcal{P}\mathbf{P} \rightarrow \mathcal{A}\mathbf{P}$$

$$\mathbf{A} \mapsto \{c \in \mathbf{A} : (d \in \mathbf{A}) \wedge (d \leq_{\mathbf{P}} c) \Rightarrow (c = d)\}.$$

Note that  $\text{Min}(\mathbf{A})$  could be empty.