Definition (Binary relation). A binary relation from a set A to a set B is a subset of the Cartesian product $A \times B$.