

Definition (Functions as relations). Let \mathbf{A} and \mathbf{B} be sets. A relation $R \subseteq \mathbf{A} \times \mathbf{B}$ is a *function* if it satisfies the following two conditions:

1. for all $x \in \mathbf{A} \quad \exists y \in \mathbf{B} : xRy$;
2. for all x_1Ry_1, x_2Ry_2 holds:

$$\frac{x_1 = x_2}{y_1 = y_2}$$