Definition (Monoid left action). A *monoid **left** action* of a monoid **M** onto a set **A** is a monoid morphism

$$\mathbf{Lact} : \mathbf{M} \to \mathbf{End}(\mathbf{A}).$$