Definition (Antichain in a poset). An *antichain* is a subset $\mathbf{S}$ of a poset where no elements are comparable. If $a, b \in \mathbf{S}$, then:

$$\frac{a \leq_{\mathbf{P}} b}{a = b}$$