Lemma. Let A be an antichain in **P**. Then

$$a \in A \quad \equiv \quad \{a\} = A \cap {\uparrow} a.$$