## **Definition** (Category **UPos**). The category **UPos** consists of:

- 1. Objects: objects are posets;
- 2. *Morphisms*: given objects  $X, Y \in Ob_{UPos}$ , morphisms from X to Y are monotone maps of the form  $f: X \to \mathcal{U}Y$ .
- 3. Composition of morphisms: Given morphisms  $f: X \to \mathcal{U}Y \ g: Y \to \mathcal{U}Z$ , their composition is given as

$$f \circ g : X \to \mathcal{U}Z$$

$$x \mapsto \bigcup_{y \in f(x)} g(y);$$

4. *Identity morphism*: given an object  $X \in \mathrm{Ob}_{\mathrm{UPos}}$ , the identity morphism is given by the application of the upper closure operator:  $\mathrm{Id}_X(x) := \uparrow \{x\}$ .