$$\operatorname{Hom}_{\mathbf{C}}(f) : \operatorname{Hom}_{\mathbf{C}}(X; Y) \to \operatorname{Hom}_{\mathbf{C}}(Z; W)$$

$$g \mapsto (f_1 \circ g \circ f_2).$$