Lemma. $\mathbf{Pos}_{\mathcal{U}}$ is the Kleisli category of $\mathcal{U}$.