$$\langle f^{\text{op}}, r \rangle \mapsto \exists i \in \mathbf{I} : (f \leq_{\mathbf{F}} \text{prov}(i)) \land (\text{req}(i) \leq_{\mathbf{R}} r)$$