Definition (Identity design problem). For any poset A, the identity design problem id_A: $A \longrightarrow A$ is a monotone map

$$id_A: A^{op} \times A \rightarrow_{Pos} Bool.$$

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 $\langle a_1^*, a_2 \rangle \mapsto a_1 \leq_A a_2.$