$$\begin{array}{c}
\mathbf{U}_{f} \times (\mathbf{X}_{f} * \mathbf{X}_{g} * \mathbf{X}_{h}) & \xrightarrow{\mathrm{dyn}_{(f_{\S}(g_{\S}h))}} & (\mathbf{X}_{f} * \mathbf{X}_{g} * \mathbf{X}_{h}) \\
\mathrm{id}_{\mathbf{U}_{f}} \times (\mathrm{coh}_{(f_{\S}g)_{\S}h} \times \mathrm{id}_{(\mathbf{X}_{h})}) \uparrow & \uparrow \mathrm{coh}_{(f_{\S}g)_{\S}h} \\
\mathbf{U}_{f} \times ((\mathbf{X}_{f} * \mathbf{X}_{g}) \times (\mathbf{X}_{h})) & (\mathbf{X}_{f} * \mathbf{X}_{g}) \times (\mathbf{X}_{h}) \\
\mathrm{id}_{\mathbf{U}_{f}} \times (\mathrm{coh}_{f_{\S}g} \times \mathrm{id}_{(\mathbf{X}_{h})}) \uparrow & \uparrow \mathrm{coh}_{f_{\S}g} \times \mathrm{id}_{(\mathbf{X}_{h})} \\
\mathbf{U}_{f} \times (((\mathbf{X}_{f}) \times (\mathbf{X}_{g})) \times (\mathbf{X}_{h})) & \xrightarrow{\bullet} ((\mathbf{X}_{f}) \times (\mathbf{X}_{g})) \times (\mathbf{X}_{h})
\end{array}$$