Definition (Graph homomorphism). Given graphs $\mathcal{G} = \langle \mathbf{V}, \mathbf{A}, s, t \rangle$ and $\mathcal{G}' = \langle \mathbf{V}', \mathbf{A}', s', t' \rangle$, a graph homomorphism $f : \mathcal{G} \to \mathcal{G}'$ is given by maps $f_0 : \mathbf{V} \to \mathbf{V}'$ and $f_1 : \mathbf{A} \to \mathbf{A}'$, such that the following diagrams commute:

