**Definition** (Chain in a poset). Given a poset  $\mathbf{P}$ , a *chain* is a sequence of elements  $p_i$  in  $\mathbf{P}$  where two successive elements are comparable:

$$\frac{i \leq j}{p_i \leq_{\mathbf{P}} p_i}$$