Definition (Twisted arrow category). Given a category **C**, we denote its *twisted* arrow category by Tw (**C**). This is a category which is composed of:

- 1. Objects: Arrows (morphisms) in C.
- 2. *Morphisms*: A morphism between two arrows $f: X \to Y, g: Z \to W$ is given by the pair of arrows $\langle h, i \rangle$ such that the following diagram commutes:

