

$$\langle f^*, r \rangle \mapsto \{i \in I : (f \leq_F \text{prov}(i)) \wedge (\text{req}(i) \leq_R r)\}$$