

$\forall V \in \mathbf{Ob} \mathbf{Vect}_{\mathbb{R}}$ is dualizable if and only if $\dim V < \infty$