Lemma. The lower closure operator \downarrow is a monotone map.