$$\alpha = \underset{\preceq_{\mathbf{R}}}{\mathrm{Min}} \bigcup_{r \in \alpha} \{r\}.$$