Definition (Power set as lattice). Given a set S, its power set $\mathscr{P}S$ (the set of all subsets) is a lattice where, given $A, B \in \mathscr{P}S$:

▶ Order is given by inclusion:

$$A \leq B := A \subseteq B$$
;

► The join is given by the union of sets:

$$A \lor B := A \cup B$$
;

▶ The meet is given by the intersection of sets:

$$A \wedge B := A \cap B$$
;

▶ The top element is the set S itself:

$$T = S;$$

▶ The bottom element is the empty set:

$$\perp = \emptyset$$
.