$$Lu_a, Lu_b, Uu_a, Uu_b : \mathbf{F}^{\mathrm{op}} \to_{\mathbf{Pos}} \langle \mathcal{U}\mathbf{R}, \subseteq \rangle$$