Lemma (Coproduct in **Cat**). The disjoint union of categories is the coproduct in **Cat**.