## Given any two morphisms $f, g: X \to Y$ in $\mathbf{Pos}_{\mathcal{H}}$ , we define an order between

**Definition** (Order on morphisms in **Pos**<sub>9/</sub>)

 $f \leq_{\mathbf{Pos}_{9/}} g$ 

 $f^*(x) \leq_{\mathcal{H}Y} g^*(x), \quad \forall x \in X$