$\mathbf{d}_k: \mathbf{F}_k \longrightarrow \mathbf{R}_k$