Lemma. The composition of semigroup morphisms is a morphism:

$F: \mathbf{S} \to \mathbf{T} G: \mathbf{T} \to \mathbf{U}$
$F \cappa G : \mathbf{S} o \mathbf{T}$