$$\begin{array}{c|c} X_1 \otimes X_2 & \xrightarrow{f_1 \otimes f_2} & Y_1 \otimes Y_2 \\ br_{X_1, X_2} & & \downarrow br_{Y_1, Y_2} \\ X_2 \otimes X_1 & \xrightarrow{f_2 \otimes f_1} & Y_2 \otimes Y_1 \end{array}$$