$$\mathrm{id}_A: A^{\mathrm{op}} \times A \to_{\mathbf{Pos}} \mathbf{Bool},$$
  
 $\langle a_1^*, a_2 \rangle \mapsto a_1 \leq_A a_2.$