$$\mathbf{U}_{f \circ g} = \mathbf{U}_f,$$
 $\mathbf{X}_{f \circ g} = [\mathbf{X}_f ; \mathbf{X}_g],$
 $\operatorname{start}_{f \circ g} = [\operatorname{start}_f ; \operatorname{start}_g],$
 $\mathbf{Y}_{f \circ g} = \mathbf{Y}_g.$