## **Definition** (Monoid). A monoid **M** is:

## Constituents

- 1. a set **M**;
- 2. a binary operation  $\S: \mathbf{M} \times \mathbf{M} \to \mathbf{M}$ ;
- 3. a specified element  $id \in M$ , called neutral element.

## Conditions

- 1. Associative law:  $(x \circ y) \circ z = x \circ (y \circ z)$ ;
- 2. Neutrality Laws: id  $\frac{1}{9}x = x = x \frac{1}{9}$  id.