

Definition (Downward closed set)

An upper set A is *downward-closed* in a poset P if

$$A = \uparrow \text{Min } A.$$

The set of downward-closed upper sets of P is denoted $\overline{\text{UpperSets}P}$.