$$\begin{array}{c|c}
\mathbf{P}_1 & \xrightarrow{J_1} & \mathbf{S}_1 \\
\hline
Rel & \mathbf{Rel} & \mathbf{g} \\
\mathbf{P}_2 & \xrightarrow{f} & \mathbf{S}_2
\end{array}$$