Lemma. $\mathcal{A}\mathbf{P}$ is a poset with the relation $\leq_{\mathcal{A}\mathbf{P}}$ defined by





$$A \leq_{\mathcal{A}\mathbf{P}} B \qquad \equiv \qquad \uparrow A \supseteq \uparrow B.$$