$$\text{Tr}_{A,B}^{X \otimes Y}(f) = \text{Tr}_{A,B}^{X}\left(\text{Tr}_{A \otimes X, B \otimes X}^{Y}(f)\right)$$