

**Definition** (Generated semigroups). Let  $\langle S, \circ \rangle$  be a semigroup, and let  $A \subseteq S$  be a subset. We say that  $S$  is *generated* by  $A$  if every element of  $S$  can be expressed as a finite multiplication of elements of  $A$ .