

**Definition** (Semantics of MCDP). Given an MCDP in algebraic form  $\langle \mathcal{A}, \mathbf{T}, \mathbf{v} \rangle$ , the semantics

$$\varphi[\langle \mathcal{A}, \mathbf{T}, \mathbf{v} \rangle] \in \mathbf{DP}$$

is defined as follows:

$$\varphi[\langle \mathcal{A}, a, \mathbf{v} \rangle] \doteq \mathbf{v}(a), \quad \text{for all } a \in \mathcal{A}, \quad (0.1)$$

$$\varphi[\langle \mathcal{A}, \text{series}(\mathbf{T}_1, \mathbf{T}_2), \mathbf{v} \rangle] \doteq \varphi[\langle \mathcal{A}, \mathbf{T}_1, \mathbf{v} \rangle] \odot \varphi[\langle \mathcal{A}, \mathbf{T}_2, \mathbf{v} \rangle], \quad (0.2)$$

$$\varphi[\langle \mathcal{A}, \text{par}(\mathbf{T}_1, \mathbf{T}_2), \mathbf{v} \rangle] \doteq \varphi[\langle \mathcal{A}, \mathbf{T}_1, \mathbf{v} \rangle] \otimes \varphi[\langle \mathcal{A}, \mathbf{T}_2, \mathbf{v} \rangle], \quad (0.3)$$

$$\varphi[\langle \mathcal{A}, \text{loop}(\mathbf{T}), \mathbf{v} \rangle] \doteq \varphi[\langle \mathcal{A}, \mathbf{T}, \mathbf{v} \rangle]^\dagger. \quad (0.4)$$