Definition (Downward closed set). An upper set *S* is *downward-closed* in a poset **P** if

 $S = \uparrow \text{Min } S$.