**Definition.** Given two metric spaces  $\langle X, d_X \rangle$ ,  $\langle Y, d_Y \rangle$ , a function  $f: X \to Y$  is Lipschitz if there exists a K > 0 such that

 $d_Y(f(x), f(y)) \le Kd_X(x, y), \quad \forall x \in X, y \in Y.$