## **Definition** (Metric space) A metric space $\langle A, d \rangle$ consists of:

- 1. A set A, elements of which are called *points*;
- 2. A map  $d: \mathbf{A} \times \mathbf{A} \to \mathbb{R}_{\geq 0}$ , called *distance*.

The constituents must satisfy:

- $b d(a,a) = 0, \text{ for all } a \in A;$
- $ightharpoonup ext{If } d(a,b) = 0, ext{ then } a = b, ext{ for all } a,b \in \mathbf{A};$