Definition (Downward closed set). An upper set S is downward-closed in a poset **P** if $S = \uparrow \text{Min } S$.