$$\operatorname{Hom}_{\mathbf{C}}(\operatorname{Id}_{\langle X^*, Y \rangle}) = \operatorname{Id}_{\operatorname{Hom}_{\mathbf{C}}(\langle X^*, Y \rangle)}$$