$$\operatorname{Tr}_{\mathbf{A},\mathbf{B}}^{\mathbf{C}}(\mathbf{f}_{1})(a^{*},b) = \sqrt{\mathbf{f}_{1}(\langle c,a\rangle^{*},\langle c,b\rangle)}$$

$$\leq_{\mathbf{DP}} \sqrt{\mathbf{f}_{2}(\langle c,a\rangle^{*},\langle c,b\rangle)}$$

 $= \operatorname{Tr}_{\mathbf{A},\mathbf{B}}^{\mathbf{C}}(\mathbf{f}_2)(a^*,b).$