

$$\alpha = \operatorname{Min}_{\leq_R} \bigcup_{r \in \alpha} \{r\}.$$