

**Definition** (Locally posetal 2-category). A 2-category  $\mathbf{C}$  is *locally posetal* (or enriched in  $\mathbf{Pos}$ ) if every hom-category  $\mathbf{Hom}_{\mathbf{C}}(x, y)$  is a poset.