

$$\mathrm{Tr}_{v \otimes X, v \otimes Y}^Z (\mathrm{Id}_v \otimes f) = \mathrm{Id}_v \otimes \mathrm{Tr}_{X, Y}^Z(f)$$