$$\uparrow \left(\bigcup_{p \in \uparrow} \bigcup_{i \in I} \{f(p)\} \right) \supseteq \uparrow \left(\bigcup_{i \in I} \{f(s_i)\} \right).$$