$$L \subseteq \beta(\alpha(L))$$