**Lemma.**  $\mathscr{U}\mathbf{P}$  is a bounded lattice (??) with  $\leq_{\mathscr{H}\mathbf{P}} := \supseteq$ ,

 $\perp_{\mathscr{U}\mathbf{P}} := \mathbf{I},$   $\mathsf{T}_{\mathscr{H}\mathbf{P}} := \emptyset,$