$\geq_{\mathbf{DP}} n_h$