

$$\mathrm{Tr}^{Z\otimes U}_{X,Y}(f) = \mathrm{Tr}^Z_{X,Y}\left(\mathrm{Tr}^U_{X\otimes Z,Y\otimes Z}(f)\right)$$