$Lu \leq_{\mathbf{DP}} d \leq_{\mathbf{DP}} Uu$