

$$\mathrm{Tr}_{v \otimes x, v \otimes y}^z (\mathrm{Id}_v \otimes f) = \mathrm{Id}_v \otimes \mathrm{Tr}_{x, y}^z(f)$$