$\triangleright P_{\text{track}}(\alpha)$ is decreasing with α increasing.

Lemma. Let $\mathbf{Q}(\alpha) = \alpha \mathbf{Q}_0$ and $\mathbf{R}(\alpha) = \frac{1}{\alpha} \mathbf{R}_0$, $\alpha \in \mathbb{R}_+$. Let $\mathbf{u}^*(\alpha)$ be the

solution of the LQG problem with
$$\mathbf{Q}(\alpha)$$
 and $\mathbf{R}(\alpha)$. Then, under optimal control one has:

 $\triangleright P_{\rm effort}(\alpha)$ is increasing with α increasing.