Definition (Category). A *category* **C** is a semicategory with an additional constituent and rule:

Constituents

1. Identity morphisms: for each object X, there is a morphism $\mathrm{Id}_X : X \to X$ called *the identity morphism of X*.

Conditions

1. Unitality: It holds that:

$$\frac{f : X \to Y}{\mathrm{Id}_X \ \fatsemi \ f = f = f \ \fatsemi \ \mathrm{Id}_Y}$$