Definition (General orthogonal group O(n))

The general orthogonal group of order n, written O(n), is the group of $n \times n$ square matrices that satisfy

$$\mathbf{M}\mathbf{M}^\mathsf{T} = \mathbf{M}^\mathsf{T}\mathbf{M} = \mathbb{1}.$$