$$\operatorname{act}_f: (\mathbb{N} \to \mathbf{A}) \to (\mathbb{N} \to \mathbf{A})$$