Lemma. Functions from X to $\mathscr{P}Y$ are in one-to-one correspondence with relations from X to Y.