**Definition** (Diagonal function). Define the diagonal function diag<sub>p</sub>:  $P \rightarrow$  $P \times P$ :  $\operatorname{diag}_{\mathcal{D}}: P \to P \times P$ ,

 $p \mapsto \langle p, p \rangle$ .