Definition (Identity homomorphism). Let **M** be a monoid. Similar to the case of semigroups, the identity function $id_{\mathbf{M}}: \mathbf{M} \to \mathbf{M}$ is also a homomorphisms of monoids.