

**Lemma.** For  $A, B \in \mathcal{AP}$ , and  $S \subseteq P$ ,  $A \leq_{AR} B$  implies  $A \cap S \leq_{AR} B \cap S$ .