

Definition (Transpose of a relation). Let $\mathbf{R} \subseteq \mathbf{A} \times \mathbf{B}$ be a relation. The *transpose* (or *opposite*, *reverse*) of \mathbf{R} is the relation given by:

$$\mathbf{R}^\top := \{\langle y, x \rangle \in \mathbf{B} \times \mathbf{A} \mid \langle x, y \rangle \in \mathbf{R}\}.$$

note that $\mathbf{R}^\top : \mathbf{B} \rightarrow \mathbf{A}$, while $\mathbf{R} : \mathbf{A} \rightarrow \mathbf{B}$.