

Definition (Sum of resources). If the poset \mathbf{A} is monoidal, then the *sum* of n copies of \mathbf{A} is a design problem given by

$$\begin{aligned} \Sigma &: (\mathbf{A}^n)^{\text{op}} \times \mathbf{A} \xrightarrow{\text{Pos}} \mathbf{Bool} \\ \langle a_1^*, \dots, a_n^*, a_{\text{resource}} \rangle &\mapsto (a_1 + \dots + a_n \leq_{\mathbf{A}} a_{\text{resource}}). \end{aligned}$$

Clearly Σ is monotone. Diagrammatically:

