$$(\mathbf{f} \circ \mathbf{g}) : \mathbf{A}^{\mathrm{op}} \times \mathbf{C} \to_{\mathbf{Pos}} \mathbf{Bool},$$
 
$$\langle a^*, c \rangle \mapsto \bigvee_{b \in \mathbf{B}} f(a^*, b) \wedge g(b^*, c).$$

Alternatively:

$$(\mathbf{f} \, {}^{\circ}_{9}\mathbf{g}) : \mathbf{A}^{\mathrm{op}} \times \mathbf{C} \to_{\mathbf{Pos}} \mathbf{Bool},$$
 
$$\langle a^{*}, c \rangle \mapsto \bigvee_{\substack{b_{1} \leq b_{2}, b_{1}, b_{2} \in \mathbf{B}}} \mathbf{f}(a^{*}, b_{1}) \wedge \mathbf{g}(b_{2}^{*}, c).$$