**Definition** (Subcategory). A *subcategory* **D** of a category **C** is a category for which:

1. All the objects in Ob<sub>D</sub> are in Ob<sub>C</sub>;

If X ∈ Ob<sub>D</sub>, then Id<sub>X</sub> ∈ Hom<sub>C</sub>(X; X) is in Hom<sub>D</sub>(X; X) and acts as its identity morphism;
 If f: X → Y and g: Y → Z in D, then the composite f ; g in C is in D

2. For any objects  $X, Y \in \mathrm{Ob}_{\mathbf{D}}$ ,  $\mathrm{Hom}_{\mathbf{D}}(X; Y) \subseteq \mathrm{Hom}_{\mathbf{C}}(X; Y)$ ;

and represents the composite in **D**.