## **Definition** (*U* endofunctor)

The U endofunctor has the form U:  $Pos \rightarrow Pos$  and acts on objects and morphisms as follows:

1. On objects: Given a poset  $P \in Ob_{Pos}$ , U maps P to its upper set.

{bhfn:1}

2. *On morphisms*: Given posets **P**, **Q**, and a monotone map  $f: \mathbf{P} \to \mathbf{Q}$ , the U endofunctor acts as:

$$U(f): \mathcal{U}\mathbf{P} \to \mathcal{U}\mathbf{Q}$$

$$\mathbf{P}' \mapsto \uparrow \left( \bigcup_{p \in \mathbf{P}'} \{f(p)\} \right).$$