Lemma. A monotone map f between posets $\mathbf{P}, \mathbf{Q}$ is a functor between the "posetal categories" $\mathbf{P}$ and $\mathbf{Q}$.