monoidal category. Let  $X \in \mathrm{Ob}_{\mathbb{C}}$  be dualizable and let  $f \in \mathrm{Hom}(X,X)$ . The *trace* of f is the morphism  $\mathrm{Tr}(f) \in \mathrm{Hom}(\mathbf{1},\mathbf{1})$  defined by

$$\mathbf{1} \xrightarrow{\eta_X} X \otimes X^{\vee} \xrightarrow{f \otimes \operatorname{id}_{X^{\vee}}} X \otimes X^{\vee} \xrightarrow{\operatorname{br}} X^{\vee} \otimes X \xrightarrow{\epsilon_X} \mathbf{1}$$

**Definition** (Trace of an endomorphism). Let  $\langle \mathbf{C}, \boldsymbol{\otimes}_{\mathbf{C}}, \mathbf{1}_{\mathbf{C}}, \mathbf{br} \rangle$  be a symmetric