$$id_A: A^{op} \times A \rightarrow_{\mathbf{Pos}} \mathbf{Bool},$$

 $\langle a_1^*, a_2 \rangle \mapsto a_1 \leq_A a_2.$