

$$\text{Tr}_{C_A \otimes C_B}(\text{id}_C \otimes f) = \text{id}_C \otimes \text{Tr}_B(f)$$