$$S(\mathbf{X}_f * \mathbf{X}_g) \xrightarrow{-1} S(\mathbf{X}_f) \times S(\mathbf{X}_g) \xrightarrow{\pi_2} S(\mathbf{X}_g) \xrightarrow{ro_g} \mathbf{Y}_g$$