$$f(m_1 \, \, \boldsymbol{\beta_{\mathbf{M}}} \, \, n_2) = f(m_1) \, \boldsymbol{\beta_{\mathbf{N}}} \, f(n_2) \quad \forall m_1, n_2 \in \mathbf{M}$$