**Definition** (Discrete-time linear systems)

A discrete-time linear time-invariant proper open system is defined by three matrices **A**, **B**, **C**. Together they give a recurrence of the type

$$\mathbf{x}_{k+1} = \mathbf{A}\mathbf{x}_k + \mathbf{B}\mathbf{u}_k,$$

$$\mathbf{y}_k = \mathbf{C}\mathbf{x}_k.$$

If x has dimension  $n \ge 1$ , u dimension  $m \ge 1$  and y dimension  $p \ge 1$ , then A

has dimension  $n \cdot n$ , **B** has dimension  $n \cdot m$ , and **C** has dimension  $p \cdot n$ .