$$\hat{\phi}_R : \mathbf{A} \to \mathcal{P}(\mathbf{B}),$$

$$x \mapsto \{y \in \mathbf{B} \mid xRy\},$$