

Definition (Semigroup isomorphism). Let \mathbf{S} and \mathbf{T} be semigroups. A morphism of semigroups $F : \mathbf{S} \rightarrow \mathbf{T}$ is called a *semigroup isomorphism* if there exists a morphism of semigroups $G : \mathbf{T} \rightarrow \mathbf{S}$ such that

$$F \circ G = \text{Id}_{\mathbf{S}} \quad \text{and} \quad G \circ F = \text{Id}_{\mathbf{T}}.$$