$$((M \ \S M)(f) \ \S \ \text{mu}_{Y})([[a,b],[c,d]]) = \text{mu}_{Y}([[f(a),f(b)],[f(c),f(d)]])$$

= $[f(a),f(d)]$