$$\mathrm{br}^{\star}_{X,Y} : X \times Y \xrightarrow{\quad}_{\mathbf{Pos}} \mathcal{U}(Y \times X)$$
$$\langle x, y \rangle \mapsto \uparrow \{y\} \times \uparrow \{x\},$$