

Definition. A symmetric matrix $\mathbf{M} \in \mathbb{R}^{n \times n}$ is *positive semi-definite* if $x^\top \mathbf{M} x \geq 0$ for all non-zero $x \in \mathbb{R}^n$. We call the set of all such matrices \mathcal{P}^n .