Lemma. The identity functor is indeed a functor.