$$J^{\star} = \text{Tr}\bar{\mathbf{S}}\bar{\mathbf{\Sigma}}\mathbf{C}^{*}\mathbf{V}^{-1}\mathbf{C}\bar{\mathbf{\Sigma}} + \bar{\mathbf{\Sigma}}\mathbf{Q}$$
$$= \text{Tr}\bar{\mathbf{\Sigma}}\bar{\mathbf{S}}\mathbf{B}\mathbf{R}^{-1}\mathbf{B}^{*}\bar{\mathbf{S}} + \bar{\mathbf{S}}\mathbf{W},$$