Definition (Lower set). A *lower set* **L** is a subset of a poset **P** such that, if $x \in L$, then all elements of **P** that are below x are also in **L**. In other words:

$$\frac{x \in L \quad y \leq_P x}{y \in L}$$