Definition (Metric space) A metric space $\langle A, d \rangle$ consists of:

- 1. A set A, elements of which are called *points*;
- 2. A map $d : A \times A \to \mathbb{R}_{\geq 0}$, called *distance*. The constituents must satisfy:
- $\Rightarrow d(a, a) = 0$, for all $a \in A$;
- - If d(a,b) = 0, then a = b, for all $a,b \in A$
- $d(a,b) = d(b,a), \text{ for all } a,b \in \mathbf{A};$ $d(a,b) + d(b,c) \ge d(a,c), \text{ for all } a,b,c \in \mathbf{A}.$