$$\operatorname{Tr}_{C\otimes A,C\otimes B}^X(\operatorname{id}_C\otimes f) = \operatorname{id}_C\otimes \operatorname{Tr}_{A,B}^X(f)$$