Definition (Chain in a poset). Given a poset $\mathbf{P}$, a *chain* is a sequence of elements s_i in $\mathbf{P}$ where two successive elements are comparable:

$$i \leq j \Rightarrow s_i \leq_{\mathbf{P}} s_j.$$