

$$\mathrm{Tr}_{v \otimes c_X, v \otimes c_Y}^Z (\mathrm{Id}_v \otimes c f) = \mathrm{Id}_v \otimes c \mathrm{Tr}_{X,Y}^Z (f)$$