

$$\hat{\phi}_R: \mathbf{A} \rightarrow \mathcal{P}(\mathbf{B}), \quad \hat{\phi}_R(x) \equiv \{y \in \mathbf{B} \mid \langle x, y \rangle \in R\}$$