Definition (Lattice homomorphism)
Given two lattices $\mathbf{P}, \mathbf{Q}$, a *lattice homomorphism* is a map $f : \mathbf{P} \to \mathbf{Q}$ which preserves meets and joins:

$$f(p \wedge_{\mathbf{P}} q) = f(p) \wedge_{\mathbf{Q}} f(q)$$
$$f(p \vee_{\mathbf{P}} q) = f(p) \vee_{\mathbf{Q}} f(q).$$