**Lemma.** The *U* endofunctor is indeed a functor.