$$\text{Tr}^{Z}_{V \otimes X, V \otimes Y}(\text{Id}_V \otimes f) = \text{Id}_V \otimes \text{Tr}^{Z}_{X,Y}(f)$$