

Lemma. The \mathcal{U} endofunctor is indeed a functor.