

Lemma. Let $R \subseteq A \times B$ and $S \subseteq B \times C$ be relations which are functions. Then their composition $R \circ S \subseteq A \times C$ is again a function.