Definition (Directed set)

A set $S \subseteq \mathbf{P}$ is *directed* if each pair of elements in S has an upper bound: for all $a, b \in S$, there exists $c \in S$ such that $a \preceq c$ and $b \preceq c$.