

**Definition** (Equivalence of categories). An *equivalence* between two categories **C** and **D** is given by:

1. A pair of functors  $F, G$  of the form:

$$\mathbf{C} \begin{array}{c} \xleftarrow{G} \\ \xrightarrow{F} \end{array} \mathbf{D}$$

2. natural isomorphisms  $F \circ G \cong \text{Id}_{\mathbf{C}}$  and  $G \circ F \cong \text{Id}_{\mathbf{D}}$ .