

$$\uparrow \left( \bigcup_{\substack{p \in \uparrow \\ i \in I} S_i} \{f(p)\} \right) \supseteq \uparrow \left( \bigcup_{i \in I} \{f(s_i)\} \right)$$