$$(\mathrm{Id}_U \otimes \mathrm{Tr}_{X,Y}^Z(f))^\star (u,x) = \uparrow \{u\} \times \left\{ y \in Y \mid \bigvee_{z \in Z} \langle y, z \rangle \in f^\star(x,z) \right\}.$$