$$f(m_1 \, \S_{\mathbf{M}} \, n_2) = f(m_1) \, \S_{\mathbf{N}} \, f(n_2) \quad \forall m_1, n_2 \in \mathbf{M}$$