**Definition** (Product operator  $\otimes$ ). For two maps  $h_1: F_1 \to \mathcal{A}R_1$  and  $h_2: F_2 \to \mathcal{A}R_2$ , define

 $\langle f_1, f_2 \rangle \mapsto h_1(f_1) \times h_2(f_2),$ 

 $h_1 \otimes h_2 : (F_1 \times F_2) \to \mathcal{A}(R_1 \times R_2),$ 

where  $\times$  is the product of two antichains.