$\left\{ f(p) \right\} = \uparrow \left\{ \bigcup_{i \in I} \{ f(s_i) \} \right\}$

 $\bigcup_{i \in I} S_i$