Definition (Natural transformation)**.** Let $\mathbf{C}$ and $\mathbf{D}$ be categories, and let $F, G : \mathbf{C} \to \mathbf{D}$ be functors. A *natural transformation* $\alpha : F \Rightarrow G$

$$\begin{tikzcd} \mathbf{C} \arrow[r, bend left, "F"] \arrow[r, bend right, "G"'] \arrow[r, phantom, "\Downarrow\alpha"] & \mathbf{D} \end{tikzcd}$$

is defined by the following constituent data, satisfying the following condition.

Data:

1. For each object $X \in \mathbf{C}$, a morphism $\alpha_X : F(X) \to G(X)$ in $\mathbf{D}$, called the X*-component* of α.

Condition:

1. For every morphism $f : X \to Y$ in $\mathbf{C}$, the components of α must satisfy the *naturality condition*

$$F(f) \fatsemi \alpha_Y = \alpha_X \fatsemi G(g).$$

In other words, the following diagram must commute:

$$\begin{tikzcd} F(X) \arrow[r, "F(f)"] \arrow[d, "\alpha_X"'] & F(Y) \arrow[d, "\alpha_Y"] \\ G(X) \arrow[r, "G(f)"'] & G(Y) \end{tikzcd}$$

The situation is represented diagrammatically in **??**.