Definition (Completeness). A poset is a directed complete partial order (DCPO) if each of its directed subsets has a supremum (least of upper bounds). It is a complete partial order (CPO) if it also has a bottom.