$$((br_{X,Y} \otimes Id_{Z}) \circ as_{Y,X,Z} \circ (Id_{Y} \otimes br_{X,Z}))^{*}(\langle x, y \rangle, z)$$

$$= \bigcup_{\langle y', \langle x', z' \rangle \rangle \in \uparrow \{y\} \times (\uparrow \{x\} \times \uparrow \{z\})} (Id_{Y} \otimes br_{X,Z})^{*}(y', \langle x', z' \rangle)$$

$$= \bigcup_{\langle y', \langle x', z' \rangle \rangle \in \uparrow \{y\} \times (\uparrow \{x\} \times \uparrow \{z\})} \uparrow \{y'\} \times (\uparrow \{z'\} \times \uparrow \{x'\})$$

$$= \bigcup_{\langle y', \langle x', z' \rangle \rangle \in \uparrow \{y\} \times (\uparrow \{x\} \times \uparrow \{z\})} \uparrow \{y'\} \times (\uparrow \{z'\} \times \uparrow \{x'\})$$

 $= \uparrow \{y\} \times (\uparrow \{z\} \times \uparrow \{x\}).$