

Lemma. α and β are antitone maps.