$$\operatorname{Tr}_{X,Y}^{Z \otimes U}(f) = \operatorname{Tr}_{X,Y}^{Z} \left(\operatorname{Tr}_{X \otimes Z,Y \otimes Z}^{U}(f) \right)$$