Definition (Category)

A *category* **C** is a semicategory with an additional constituent and an additional rule:

Constituents

1. Identity morphisms: for each object X, there is a morphism

$$\mathrm{Id}_X:X\to X$$

called the identity morphism of X.

Conditions

1. Unitality: It holds that composing a morphism with a compatible identity leaves the morphism unchanged:

$$f: X \to Y$$

$$\operatorname{Id}_X \, \mathring{\circ} \, f = f = f \, \mathring{\circ} \, \operatorname{Id}_Y$$