

**Lemma.**  $\mathcal{AP}$  is a poset with the relation  $\leq_{\mathcal{AP}}$  defined by

$$A \leq_{\mathcal{AP}} B \quad \equiv \quad \uparrow A \supseteq \uparrow B.$$