$S_{k+1} = \Phi_{f_1}(S_k)$