$$\mathbf{d}_k(f^*_k, r_k) = \top$$