

$$\alpha = \operatorname{Min}_{\leq_{\mathbf{R}}} \bigcup_{r \in \alpha} \{r\}.$$