$$(\operatorname{un}_{\mathcal{U}}^{\mathbf{A}} \circ \operatorname{Unc}(\mathbf{f}))(p^*, [q_1, q_2]) = \bigvee_{[p_1, p_2] \in \mathbf{Int}(\mathbf{A})} \operatorname{un}_{\mathcal{U}}^{\mathbf{A}}(p^*, [p_1, p_2]) \wedge \operatorname{Unc}(f)([p_1, p_2]^*, [q_1, q_2])$$

$$= \bigvee_{[p_1, p_2] \in \mathbf{Int}(\mathbf{A})} (p \leq p_1) \wedge \mathbf{f}(p_1^*, q_1) \wedge \mathbf{f}(p_2^*, q_2)$$

 $[p_1,p_2]\in \mathbf{Int}(\mathbf{A})$