

**Definition.** Given two metric spaces  $\langle X, d_X \rangle, \langle Y, d_Y \rangle$ , a function  $f : X \rightarrow Y$  is *Lipschitz* if there exists a  $K > 0$  such that

$$d_Y(f(x), f(y)) \leq K d_X(x, y), \quad \forall x \in X, y \in Y.$$