Definition (Power set). Given any set A, we can form a new set whose elements are precisely the subsets of A. This new set is called the *powerset* of A, and we denote it by $\mathscr{P}A$.