

Lemma. $(\textcolor{orange}{L}x)^{\dagger} \leq_{\text{DP}} (\textcolor{red}{U}x)^{\dagger}.$