**Definition** (Boolean profunctors). Given two posets **P** and **Q**, a boolean profunctor from **P** to **Q** is a monotone function of the form

 $F: \mathbf{P}^{\mathrm{op}} \times \mathbf{Q} \rightarrow_{\mathbf{Pos}} \mathbf{Bool}.$ 

This is also written as  $F: \mathbf{P} \longrightarrow \mathbf{Q}$ .