

Definition (Enriched category). We say that a category \mathbf{C} is enriched in \mathbf{D} if:

1. For all objects X, Y of \mathbf{C} , the set $\text{Hom}_{\mathbf{C}}(X; Y)$ can be considered an object of \mathbf{D} ;
2. \mathbf{D} is a monoidal category (??), with monoidal product $\otimes_{\mathbf{D}}$;
3. For all objects X, Y, Z of \mathbf{C} , there exists a certain morphism $m_{X,Y,Z}$ in \mathbf{D} , which goes from the object $\text{Hom}_{\mathbf{C}}(X; Y) \otimes_{\mathbf{D}} \text{Hom}_{\mathbf{C}}(Y; Z)$ to the object $\text{Hom}_{\mathbf{C}}(X; Z)$:

$$m_{X,Y,Z} : \text{Hom}_{\mathbf{C}}(X; Y) \otimes_{\mathbf{D}} \text{Hom}_{\mathbf{C}}(Y; Z) \rightarrow \text{Hom}_{\mathbf{C}}(X; Z).$$