$F(x \circ_{\mathbf{S}} y) = F(x) \circ_{\mathbf{T}} F(y)$