Definition (Monoid). A monoid **M** is:

Constituents

- 1. a set **M**;
- 2. a binary operation $: \mathbf{M} \times \mathbf{M} \to \mathbf{M};$ 3. a specified element $id \in M$, called neutral element.

- Conditions
 - 1. Associative law: (x ; y) ; z = x ; (y ; z)2. Neutrality Laws: id 3x = x = x 3 id

 $\forall x, y, z \in \mathbf{M};$ $\forall x \in \mathbf{M}$.