

**Lab 7**  
**CS114 Spring 2018**  
**Markov Chains and Hidden Markov Models**

**1. Markov Chain**

$$\pi = \begin{array}{cc} & \text{Cold} & \text{Hot} \\ \pi = & 0.5 & 0.5 \end{array}$$

$$A \text{ (transition matrix)} = \begin{array}{cc} & \begin{array}{cc} \text{Cold} & \text{Hot} \end{array} \\ \begin{array}{c} \text{Cold} \\ \text{Hot} \end{array} & \begin{array}{cc} 0.6 & 0.4 \\ 0.5 & 0.5 \end{array} \end{array}$$

Compute the probability that the third day is a cold day.

**2. Hidden Markov Model**

$$\pi = \begin{array}{cc} & \text{Cold} & \text{Hot} \\ \pi = & 0.5 & 0.5 \end{array}$$

$$A \text{ (transition matrix)} = \begin{array}{cc} & \begin{array}{cc} \text{Cold} & \text{Hot} \end{array} \\ \begin{array}{c} \text{Cold} \\ \text{Hot} \end{array} & \begin{array}{cc} 0.6 & 0.4 \\ 0.5 & 0.5 \end{array} \end{array}$$

$$B \text{ (emission matrix)} = \begin{array}{cc} & \begin{array}{ccc} \text{Good} & \text{Mediocre} & \text{Bad} \end{array} \\ \begin{array}{c} \text{Cold} \\ \text{Hot} \end{array} & \begin{array}{ccc} 0.2 & 0.3 & 0.5 \\ 0.6 & 0.3 & 0.1 \end{array} \end{array}$$

- a. Suppose that the observation sequence is (Good, Good, Bad). Use the forward algorithm to compute the likelihood  $P(O)$ .
- b. Compute the probability that the third day is a cold day.