

xCORE-200 DSP Library

This API reference manual describes the XMOS fixed-point digital signal processing software library. The library implements of a suite of common signal processing functions for use on XMOS xCORE-200 multicore microcontrollers.

Required tools and libraries

• xTIMEcomposer Tools Version 14.0.1 or later

Required hardware

Only XMOS xCORE-200 based multicore microcontrollers are supported with this library. The previsous generation XS1 based multicore microntrollers are not supported.

The xCORE-200 has a single cycle 32x32->64 bit multiply/accumulate unit, single cycle double-word load and store, dual issue instruction execution, and other instruction set enhancements. These features make xCORE-200 an efficient platform for executing digital signal processing algorithms.

Prerequisites

This document assumes familiarity with the XMOS xCORE architecture, the XMOS tool chain, the 'C' programming language, and digital signal processing concepts.



1 Overview

1.1 Introduction

This API reference manual describes the XMOS xCORE-200 fixed-point digital signal processing firmware library. The library implements of a suite of common signal processing functions for use on XMOS xCORE-200 multicore microcontrollers.

1.2 Library Organization

The library is divided into function collections with each collection covering a specific digital signal processing algorithm category. The API and implementation for each category are provided by a single 'C' header file and implementation file.

Category	Source Files	Functions
Fixed point	xmos_dsp_qformat	Q16 through Q31 formats, fixed and floating point conversions
Filters	xmos_dsp_filters	FIR, biquad, cascaded biquad, and convolution
Adaptive	xmos_dsp_adaptive	LMS and NLMS Adaptive filters
Scalar math	xmos_dsp_math	Multiply, square root, reciprocal, inverse square root
Vector math	xmos_dsp_vector	Scalar/vector add/subtract/multiply, dot product
Matrix math	xmos_dsp_matrix	Scalar/matrix add/subtract/multiply, inverse and transpose
Statistics	xmos_dsp_statistics	Vector mean, sum-of-squares, root-mean-square, variance



2 Fixed-Point Format

2.1 Q Format Introduction

The library functions support 32 bit input and output data, with internal 64 bit accumulator. The output data can be scaled to any of the supported Q Formats (Q16 through Q31). Further details about Q Format numbers is available here: https://en.wikipedia.org/wiki/Q_(number_format).

2.2 The 'q_format' Parameter

All XMOS DSP library functions that incorporate a multiply operation accept a parameter called q_format. This parameter can naively be used to specify the fixed point format for all operands and results (if applicable) where the formats are the same for all parameters. For example:

```
result_q28 = xmos_dsp_math_multiply( input1_q28, input2_q28, 28 );
```

The 'q_format' parameter, being used after one or more sequences of multiply and/or multiply-accumulate, is used to right-shift the 64-bit accumulator before truncating the value back to a 32-bit integer (i.e. the 32-bit fixed-point result). Therefore the 'q_format' parameter can be used to perform the proper fixed-point adjustment for any combination of input operand fixed-point format and desired fixed-point result format.

The output fixed-point fraction bit count is equal to the sum of the two input fraction bit counts minus the desired result fraction bit count:

```
q_format = input1 fraction bit count + input2 fraction bit count - result fraction bit count
```

For example:

```
// q_format_parameter = 31 = 30 + 29 - 28
result_q28 = xmos_dsp_math_multiply( input1_q30, input2_q29, 31 );
// q_format_parameter = 27 = 28 + 29 - 30
result_q30 = xmos_dsp_math_multiply( input1_q28, input2_q29, 27 );
```



3 Filter Functions: Finite Impulse Response (FIR) Filter

Implements the Finite Impulse Response (FIR). The function operates on a single sample of input and output data (i.e. and each call to the function processes one sample).

Parameters

Name	Direction	Description
input_sample	in	The new sample to be processed.
filter_coeffs[]	in	Pointer to FIR coefficients arranged as [b0,b1,b2,,bN-1].
state_data[]	in, out	Pointer to filter state data array of length N.
		Must be initialized at startup to all zero's.
tap_count	in	Filter tap count where $N = tap_count = filter order + 1$.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Resulting filter output sample.

Algorithm

The FIR filter algorithm is based upon a sequence of multiply-accumulate (MAC) operations. Each filter coefficient h[i] is multiplied by a state variable which equals a previous input sample x[i]:

```
y[n] = x[n] * h[0] + x[n-1] * h[1] + x[n-2] * h[2] ... + x[n-N+1] * h[N-1]
```

'filter_coeffs' points to a coefficient array of size $N = \text{'num_taps'}$. The filter coefficients are stored in forward order (e.g. h[0], h[1], ..., h[N-1]).

Behavior

The FIR algorithm involves multiplication between 32-bit filter coefficients and 32-bit state data producing a 64-bit result for each coeffient and state data pair. Multiplication results are accumulated in 64-bit accumulater with the final result shifted to the required fixed-point format. Therefore overflow behavior of the 32-bit multiply operation and truncation behavior from final shifting of the accumulated multiplication results must be considered.

```
// Five-tap (4th order) FIR filter with samples and coefficients represented in Q28 fixed-point format int filter_coeff[5] = { Q28(0.5), Q(-0.5), Q28(0.0), Q28(-0.5), Q28(0.5) }; int filter_state[4] = { 0, 0, 0, 0 }; int result = xmos_dsp_fir(sample, filter_coeff, filter_state, 5, 28 );
```



4 Filter Functions: Interpolating FIR Filter

Implements an interpolating Finite Impulse Response (FIR). The function operates on a single input sample and outputs a set of samples representing the interpolated data, whose sample count is equal to 'interp_factor'. (i.e. and each call to the function processes one sample and result in 'interp_factor' output samples).

```
void xmos_dsp_filters_interpolate
(
  int    output_samples[],
  int    input_sample,
  const int filter_coeffs[],
  int    state_data[],
  int    tap_count,
  int    interp_factor,
  int    q_format
)
```

Parameters

Name	Direction	Description
output_samples	out	The resulting interpolated samples.
input_sample	in	The new sample to be processed.
filter_coeffs[]	in	
		Pointer to FIR coefficients arranged as:
		hM,h(1L+M),h(2L+M),h((N-1)L+M),
		h1,h(1L+1),h(2L+1),h((N-1)L+1),
		h0,h(1L+0),h(2L+0),h((N-1)L+0), where $M = N-1$
state_data[]	in, out	Pointer to filter state data array of length N.
		Must be initialized at startup to all zero's.
tap_count	in	Filter tap count where $N = tap_count = filter order + 1$.
interp_factor	in	The interpolation factor/index (i.e. the up-sampling ratio).
		The interpolation factor/index can range from 2 to 16.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Resulting filter output sample.

Algorithm

The FIR filter algorithm is based upon a sequence of multiply-accumulate (MAC) operations. Each filter coefficient h[i] is multiplied by a state variable which equals a previous input sample x[i]:

```
y[n] = x[n] * h[0] + x[n-1] * h[1] + x[n-2] * h[2] ... + x[n-N+1] * h[N-1]
```

'filter_coeffs' points to a coefficient array of size $N = \text{'num_taps'}$. The filter coefficients are stored in forward order (e.g. h[0], h[1], ..., h[N-1]).

Behavior

The FIR algorithm involves multiplication between 32-bit filter coefficients and 32-bit state data producing a 64-bit result for each coefficient and state data pair. Multiplication results are accumulated in 64-bit accumulater with the final result shifted to the required fixed-point format. Therefore overflow behavior of

5



the 32-bit multiply operation and truncation behavior from final shifing of the accumulated multiplication results must be considered.



5 Filter Functions: Decimating FIR Filter

Implements an decimating Finite Impulse Response (FIR). The function operates on a single set of input samples whose count is equal to the decimation factor. (i.e. and each call to the function processes 'decim_factor' samples and results in one sample).

```
void xmos_dsp_filters_decimate
(
  int    input_samples[],
  const int filter_coeffs[],
  int    state_data[],
  int    tap_count,
  int    decim_factor,
  int    q_format
)
```

Parameters

Name	Direction	Description
output_samples	out	The resulting interpolated samples.
input_sample	in	The new sample to be processed.
filter_coeffs[]	in	
		Pointer to FIR coefficients arranged as:
		hM,h(1L+M),h(2L+M),h((N-1)L+M),
		h1,h(1L+1),h(2L+1),h((N-1)L+1),
		h0,h(1L+0),h(2L+0),h((N-1)L+0), where $M = N-1$
state_data[]	in, out	Pointer to filter state data array of length N.
		Must be initialized at startup to all zero's.
tap_count	in	Filter tap count where $N = tap_count = filter order + 1$.
decim_factor	in	The decimation factor/index (i.e. the down-sampling ratio).
		The decimation factor/index can range from 2 to 16.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	The resulting decimated sample.

Algorithm

The FIR filter algorithm is based upon a sequence of multiply-accumulate (MAC) operations. Each filter coefficient h[i] is multiplied by a state variable which equals a previous input sample x[i]:

```
y[n] = x[n] * h[0] + x[n-1] * h[1] + x[n-2] * h[2] ... + x[n-N+1] * h[N-1]
```

'filter_coeffs' points to a coefficient array of size $N = \text{'num_taps'}$. The filter coefficients are stored in forward order (e.g. h[0], h[1], ..., h[N-1]).

Behavior

The FIR algorithm involves multiplication between 32-bit filter coefficients and 32-bit state data producing a 64-bit result for each coeffient and state data pair. Multiplication results are accumulated in 64-bit accumulater with the final result shifted to the required fixed-point format. Therefore overflow behavior of the 32-bit multiply operation and truncation behavior from final shifing of the accumulated multiplication results must be considered.



6 Filter Functions: BiQuad Infinite Impulse Repsonse (IIR) Filter (direct form I)

Implements a second order Infinite Impulse Response (IIR) direct form I. The function operates on a single sample of input and output data (i.e. and each call to the function processes one sample).

```
int xmos_dsp_filters_biquad
(
  int input_sample,
  const int filter_coeffs[],
  int state_data[4],
  int q_format
)
```

Parameters

Name	Direction	Description
input_sample	in	The new sample to be processed.
filter_coeffs[]	in	Pointer to biquad coefficients arranged as [b0,b1,b2,a1,a2].
state_data[]	in, out	Pointer to filter state data array of length 4.
		Must be initialized at startup to all zero's.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Resulting filter output sample.

Algorithm

The IIR filter algorithm is based upon a sequence of multiply-accumulate (MAC) operations. Each filter coefficient b[i] is multiplied by a state variable which equals a previous input sample x[i]:

```
y[i] = x[n] * b[0] + x[n-1] * b[1] + x[n-2] * b2 + x[n-1] * a[1] + x[n-2] * a[2]
```

The filter coefficients are stored in forward order (e.g. b0, b1, b2, a1, a2).

Behavior

The IIR algorithm involves multiplication between 32-bit filter coefficients and 32-bit state data producing a 64-bit result for each coeffient and state data pair. Multiplication results are accumulated in 64-bit accumulater with the final result shifted to the required fixed-point format. Therefore overflow behavior of the 32-bit multiply operation and truncation behavior from final shifing of the accumulated multiplication results must be considered.

```
// Single Biquad filter with samples and coefficients represented in Q28 fixed-point format. int filter_coeff[5] = { Q28(+0.5), Q(-0.1), Q28(-0.5), Q28(-0.1), Q28(0.1) }; int filter_state[4] = { 0, 0, 0, 0 }; int result = xmos_dsp_biquad( sample, filter_coeff, filter_state, 28 );
```



7 Filter Functions: Cascaded BiQuad IIR Filter (direct form I)

Implements multiple second order Infinite Impulse Response (IIR) direct form I filters in series (cascaded Biquads). The function operates on a single sample of input and output data (i.e. and each call to the function processes one sample).

```
int xmos_dsp_filters_biquads
(
  int    input_sample,
  const int filter_coeffs[],
  int    state_data[],
  int    num_sections,
  int    q_format
)
```

Parameters

Name	Direction	Description
input_sample	in	The new sample to be processed.
filter_coeffs[]	in	Pointer to biquad coefficients for all BiQuad sections.
		Arranged as [section 1: b0,b1,b2,a1,a2, section N: b0,b1,b2,a1,a2].
state_data[]	in, out	Pointer to filter state data array of length 4.
		Must be initialized at startup to all zero's.
q_format	in	Fixed point format (number of bits making up fractional part).
num_sections	in	Number of BiQuad sections.
Return Value	out	Resulting filter output sample.

Algorithm

The IIR filter algorithm is based upon a sequence of multiply-accumulate (MAC) operations. Each filter coefficient b[i] is multiplied by a state variable which equals a previous input sample x[i]:

```
y[n] = x[n] * b[0] + x[n-1] * b[1] + x[n-2] * b2 + x[n-1] * a[1] + x[n-2] * a[2]
```

The filter coefficients are stored in forward order (e.g. section 1: b0, b1, b2, a1, a2, ..., section N: b0, b1, b2, a1, a2).

Behavior

The IIR algorithm involves multiplication between 32-bit filter coefficients and 32-bit state data producing a 64-bit result for each coefficient and state data pair. Multiplication results are accumulated in 64-bit accumulater with the final result shifted to the required fixed-point format. Therefore overflow behavior of the 32-bit multiply operation and truncation behavior from final shifing of the accumulated multiplication results must be considered.

```
// 4x Cascaded Biquad filter with samples and coefficients represented in Q28 fixed-point format.

int filter_coeff[20] = { Q28(+0.5), Q(-0.1), Q28(-0.5), Q28(-0.1), Q28(0.1), Q28(+0.5), Q(-0.1), Q28(-0.5), Q28(-0.1), Q28(0.1), Q28(+0.5), Q(-0.1), Q28(-0.5), Q28(-0.1), Q28(0.1), Q28(+0.5), Q(-0.1), Q28(-0.5), Q28(-0.1), Q28(0.1) };

int filter_state[16] = { 0,0,0,0, 0,0,0,0,0,0,0,0,0,0};

int result = xmos_dsp_cascaded_biquad( sample, filter_coeff, filter_state, 4, 28 );
```



8 Adaptive Filter Functions: Least-Mean-Squares Adaptive Filter

Implements a least-mean-squares adaptive FIR filter. LMS filters are a class of adaptive filters that adjust filter coefficients in order to create the a transfer function that minimizes the error between the input and reference signals. FIR coefficients are adjusted on a per sample basis by an amount calculated from the given step size and the instantaneous error.

The function operates on a single sample of input and output data (i.e. and each call to the function processes one sample and each call results in changes to the FIR coefficients).

```
int xmos_dsp_adaptive_lms
(
   int source_sample,
   int reference_sample,
   int error_sample[],
   int filter_coeffs[],
   int state_data[],
   int tap_count,
   int step_size,
   int q_format
)
```

Parameters

Algorithm

The general LMS algorithm, on a per sample basis, is to:

- 1. Apply the transfer function: output = FIR(input)
- 2. Compute the instantaneous error value: error = reference output
- 3. Compute current coefficient adjustment delta: delta = mu * error
- 4. Adjust transfer function coefficients: FIR_COEFFS[n] = FIR_COEFFS[n] + FIR_STATE[n] * delta

Behavior

The LMS filter algorithm involves multiplication between two 32-bit values and 64-bit accumulation as a result of using an FIR as well as coefficient step size calculations). Multiplication results are accumulated in 64-bit accumulater with the final result shifted to the required fixed-point format. Therefore overflow behavior of the 32-bit multiply operation and truncation behavior from final shifting of the accumulated multiplication results must be considered for both FIR operations as well as for coefficient step size calculation and FIR coefficient adjustment.

```
// 100-tap LMS filter with samples and coefficients represented in Q28 fixed-point format.
int filter_coeff[100] = { ... not shown for brevity };
int filter_state[100] = { 0, 0, 0, 0, ... not shown for brevity };
int output_sample = xmos_dsp_adaptive_lms
(
    input_sample, reference_sample, &error_sample,
    filter_coeff_array, filter_state_array, 100, Q28(0.01), 28
);
```



9 Scalar Math Functions: Multiply

Multiplies two scalar values and produces a result according to fixed-point format specified by the 'q_format' parameter.

```
int xmos_dsp_math_multiply
(
  int input1_value,
  int input2_value,
  int q_format
)
```

Parameters

Name	Direction	Description
input1_value	in	Multiply operand #1.
input2_value	in	Multiply operand #2.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	input1_value * input2_value.

Algorithm

The two operands are multiplied to produce a 64-bit result which is tested for overflow, clamped at the minimum/maximum value given the fixed-point format if overflow occurs, and finally shifted right by 'q_format' bits.

```
1) Y = X1 * X2
2) Y = min( max( Q_FORMAT_MIN, Y ), Q_FORMAT_MAX, Y )
3) Y = Y >> q_format
```

Behavior

While saturation is employed after multiplication an overflow condition when preparing the final result must still be considered when specifying a Q-format whose fixed-point numerical range do not accomodate the final result of multiplication and saturation (if applied).

```
int result = xmos_dsp_math_multiply( Q28(-0.33), sample, 28 );
```



10 Scalar Math Functions: Reciprocal

Computes the reciprocal of the input value using an iterative approximation method.

```
int xmos_dsp_math_reciprocal
(
  int input_value,
  int q_format
)
```

Parameters

Name	Direction	Description
input_value	in	Input value for computation.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Reciprocal of the input value.

Algorithm

```
    result = 1.0
    result = result + result * (1 input_value * result)
    Repeat step #2 until desired precision is achieved
```

Behavior

```
int result = xmos_dsp_math_reciprocal( sample, 28 );
```



11 Scalar Math Functions: Inverse Square Root

Computes the reciprocal of the square root of the input value using an iterative approximation method.

```
int xmos_dsp_math_invsqrroot
(
  int input_value,
  int q_format
)
```

Parameters

Name	Direction	Description
input_value	in	Input value for computation.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Reciprocal of the square root of the input value.

Algorithm

```
    result = 1.0
    result = result + result * (1 - input * result^2) / 2
    Repeat step #2 until desired precision is achieved
```

Behavior

```
int result = xmos_dsp_math_invsqrroot( sample, 28 );
```



12 Scalar Math Functions: Square Root

Computes the square root of the input value.

```
int xmos_dsp_math_squareroot
(
  int input_value,
  int q_format
)
```

Parameters

Name	Direction	Description
input_value	in	Input value for computation.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Square root of the input value.

Algorithm

result = xmos_dsp_math_reciprocal(xmos_dsp_math_invsqrroot(input))

Behavior

See behavior for the functions 'xmos_dsp_math_invsqrroot' and 'xmos_dsp_math_reciprocal'.

```
int result = xmos_dsp_math_squareroot( sample, 28 );
```



13 Vector Math Functions: Minimum Value

Locates the vector's first occurring minimum value, returning the index of the first occuring minimum value.

```
int xmos_dsp_vector_minimum
(
  const int input_vector_X[],
  int   vector_length,
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
vector_length	in	Length of the input vector.
Return Value	out	Index of the first occurring minimum value in the input vector.

Algorithm

```
index = -1, value = maximum 32 bit signed integer
for i = 0 to (vector_length - 1):
   if input_vector_X[i] < result:
     value = input_vector_X[i]
     index = i
return index</pre>
```

```
int samples[256];
int result = xmos_dsp_vector_minimum( samples, 256 );
```



14 Vector Math Functions: Maximum Value

Locates the vector's first occurring maximum value, returning the index of the first occuring maximum value.

```
int xmos_dsp_vector_maximum
(
  const int input_vector_X[],
  int   vector_length,
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
vector_length	in	Length of the input vector.
Return Value	out	Index of the first occurring maximum value in the input vector.

Algorithm

```
index = -1, value = minimum 32 bit signed integer
for i = 0 to (vector_length - 1):
   if input_vector_X[i] > result:
    value = input_vector_X[i]
   index = i
return index
```

```
int samples[256];
int result = xmos_dsp_vector_maximum( samples, 256 );
```



15 Vector Math Functions: Element Negation

Computes the negative value for each input element and sets the corresponding result element to it's negative value: result_vector[i] = -vector_X[i].

```
void xmos_dsp_vector_negate
(
  const int input_vector_X[],
  int    result_vector_R[],
  int    vector_length,
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.

Algorithm

```
result = 0
for i = 0 to (vector_length - 1): input_vector_X[i] = -input_vector_X[i]
```

Behavior

Each negated element is computed by twos-compliment negation therefore the minimum negative fixed-point value can not be negated to generate it's corresponding maximum positive fixed-point value.

For example: -Q28(-8.0) will not result in a fixed-point value representing +8.0.

```
int samples[256];
int result[256];
xmos_dsp_vector_negate( samples, result, 256 );
```



16 Vector Math Functions: Element Absolute Value

Sets each element of the result vector to the absolute value of the corresponding input vector element: $result_vector[i] = abs(vector_X[i])$.

```
void xmos_dsp_vector_abs
(
  const int input_vector_X[],
  int    result_vector_R[],
  int    vector_length,
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.

Algorithm

```
for i = 0 to (vector_length - 1): result_vector_R[i] = abs( input_vector_X[i] )
```

Behavior

If an element is less than zero it is negated to compute it's absolute value. Negation is computed via twoscompliment negation therefore the minimum negative fixed-point value can not be negated to generate it's corresponding maximum positive fixed-point value.

For example: -Q28(-8.0) will not result in a fixed-point value representing +8.0.

```
int samples[256];
int result[256];
xmos_dsp_vector_abs( samples, result, 256 );
```



17 Vector Math Functions: Scalar Addition

Adds a scalar value to each vector element: result_vector[i] = vector_X[i] + scalar_A.

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
scalar_value_A	in	Scalar value to add to each 'input' element.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_R[i] = input_vector_X[i] * scalar_value_A
```

Behavior

32-bit addition is used to compute the scaler plus vector element result. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_vector_X[256];
int scalar_value_A = Q28( 0.333 );
int result_vector_R[256];
xmos_dsp_vector_adds( input_vector_X, scalar_value_A, result_vector_R, 256 );
```



18 Vector Math Functions: Scalar Multiplication

Multiplies each vector element by a scaler value: result_vector[i] = vector_X[i] * scalar_A.

```
void xmos_dsp_vector_muls
(
  const int input_vector_X[],
  int      scalar_value_A,]
  int      result_vector_R[],
  int      vector_length,]
  int      q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
scalar_value_A	in	Scalar value to multiply each 'input' element by.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
for i = 0 to (vector_length - 1): result_vector_R[i] = input_vector_X[i] * scalar_value_A
```

Behavior

Each element in the input vectors is multiplied by a scalar using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

```
int input_vector_X[256];
int scalar_value_A = Q28( 0.333 );
int result_vector_R[256];
xmos_dsp_vector_muls( input_vector_X, scalar_value_A, result_vector_R, 256, 28 );
```



19 Vector Math Functions: Vector Addition

Subtracts two vectors element-by-element: result_vector[i] = vector_X[i] + vector_Y[i].

```
void xmos_dsp_vector_addv
(
  const int input_vector_X[],
  const int input_vector_Y[],
  int    result_vector_R[],
  int    vector_length,
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
input_vector_Y	in	Pointer to source data array Y.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_X[i] = input_vector_X[i] + input_vector_Y[i]
```

Behavior

32-bit addition is used to compute the vector element plus vector element result. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_vector_X[256];
int input_vector_Y[256];
int result_vector_R[256];
xmos_dsp_vector_addv( input_vector_X, input_vector_Y, result_vector_R, 256 );
```



20 Vector Math Functions: Vector Subtraction

Subtracts two vectors element-by-element: result_vector[i] = vector_X[i] - vector_Y[i].

```
void xmos_dsp_vector_subv
(
  const int input_vector_X[],]
  const int input_vector_Y[],
  int    result_vector_R[],
  int    vector_length,
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
input_vector_Y	in	Pointer to source data array Y.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_X[i] = input_vector_X[i] - input_vector_Y[i]
```

Behavior

32-bit subtraction is used to compute the vector element minus vector element result. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_vector_X[256];
int input_vector_Y[256];
int result_vector_R[256];
xmos_dsp_vector_subv( input_vector_X, input_vector_Y, result_vector_R, 256 );
```



21 Vector Math Functions: Vector Multiplication

Multiplies two vectors element-by-element: result_vector[i] = vector_X[i] * vector_Y[i].

```
void xmos_dsp_vector_mulv
(
  const int input_vector_X[],
  const int input_vector_Y[],
  int     result_vector_R[],
  int     vector_length,
  int     q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
input_vector_Y	in	Pointer to source data array Y.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_R[i] = input_vector_X[i] * input_vector_Y[i]
```

Behavior

Elements in each of the input vectors are multiplied together using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

```
int input_vector_X[256];
int input_vector_Y[256];
int result_vector_R[256];
xmos_dsp_vector_mulv( input_vector_X, input_vector_Y, result_vector_R, 256, 28 );
```



22 Vector Math Functions: Vector multiplication and scalar addition

result_vector[i] = vector_X[i] * vector_Y[i] + scalar_A.

```
void xmos_dsp_vector_mulv_adds
(
  const int input_vector_X[],
  const int input_vector_Y[],
  int input_scalar_A,
  int result_vector_R[],
  int vector_length,
  int q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
input_vector_Y	in	Pointer to source data array Y.
scalar_value_A	in	Scalar value to add to each X*Y result.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_R[i] = input_vector_X[i] * input_vector_Y[i] + input_scalar_A
```

Behavior

Elements in each of the input vectors are multiplied together using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

32-bit addition is used to compute the vector element plus scalar value result. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_vector_X[256];
int input_vector_Y[256];
int scalar_value_A = Q28( 0.333 );
int result_vector_R[256];
xmos_dsp_vector_mulv_adds( input_vector_X, input_vector_Y, scalar_value_A, result_vector_R, 256, 28 );
```



23 Vector Math Functions: Scalar multiplication and vector addition

result_vector[i] = vector_X[i] * A + vector_Y[i].

```
void xmos_dsp_vector_muls_addv
(
  const int input_vector_X[],
  int input_scalar_A,
  const int input_vector_Y[],
  int result_vector_R[],
  int vector_length,
  int q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
scalar_value_A	in	Scalar value to multiply each X element by.
input_vector_Y	in	Pointer to source data array Y.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_R[i] = input_scalar_A * input_vector_X[i] + input_vector_Y[i]
```

Behavior

Each element in the input vectors is multiplied by a scalar using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

32-bit addition is used to compute the vector element plus vector element result. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_vector_X[256];
int scalar_value_A = Q28( 0.333 );
int input_vector_Y[256];
int result_vector_R[256];
xmos_dsp_vector_muls_addv( input_vector_X, input_scalar_A, input_vector_Y, result_vector_R, 256, 28 );
```



24 Vector Math Functions: Scalar multiplication and vector subtraction

result_vector[i] = vector_X[i] * scalar_A - vector_Y[i].

```
void xmos_dsp_vector_muls_subv
(
  const int input_vector_X[],
  int input_scalar_A,
  const int input_vector_Y[],
  int result_vector_R[],
  int vector_length,
  int q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
scalar_value_A	in	Scalar value to multiply each X element by.
input_vector_Y	in	Pointer to source data array Y.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_R[i] = input_scalar_A * input_vector_X[i] - input_vector_Y[i]
```

Behavior

Each element in the input vectors is multiplied by a scalar using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

32-bit subtraction is used to compute the vector element minus vector element result. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_vector_X[256];
int scalar_value_A = Q28( 0.333 );
int input_vector_Y[256];
int result_vector_R[256];
xmos_dsp_vector_muls_subv( input_vector_X, input_scalar_A, input_vector_Y, result_vector_R, 256, 28 );
```



25 Vector Math Functions: Vector multiplication and vector addition

result_vector[i] = vector_X[i] * vector_Y[i] + vector_Z[i].

```
void xmos_dsp_vector_mulv_addv
(
  const int input_vector_X[],
  const int input_vector_Y[],
  const int input_vector_Z[],
  int     result_vector_R[],
  int     vector_length,
  int     q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
input_vector_Y	in	Pointer to source data array Y.
input_vector_Z	in	Pointer to source data array Z.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_R[i] = input_vector_X[i] * input_vector_Y[i] + input_vector_Z[i]
```

Behavior

Elements in each of the input vectors are multiplied together using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

32-bit addition is used to compute the vector element plus vector element result. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_vector_X[256];
int input_vector_Y[256];
int input_vector_Z[256];
int result_vector_R[256];
xmos_dsp_vector_mulv_addv( input_vector_X, input_vector_Y, input_vector_Z, result_vector_R, 256, 28 );
```



26 Vector Math Functions: Vector multiplication and vector subtraction

result_vector[i] = vector_X[i] * vector_Y[i] - vector_Z[i].

```
void xmos_dsp_vector_mulv_subv
(
  const int input_vector_X[],
  const int input_vector_Y[],
  const int input_vector_Z[],
  int     result_vector_R[],
  int     vector_length,
  int     q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
input_vector_Y	in	Pointer to source data array Y.
input_vector_Z	in	Pointer to source data array Z.
result_vector_R	out	Pointer to the resulting data array.
vector_length	in	Length of the input and result vectors.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
for i = 0 to (vector_length - 1):
    result_vector_R[i] = input_vector_X[i] * input_vector_Y[i] - input_vector_Z[i]
```

Behavior

Elements in each of the input vectors are multiplied together using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

32-bit subtraction is used to compute the vector element plus vector element result. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_vector_X [256];
int input_vector_Y [256];
int input_vector_Z [256];
int result_vector_R[256];
xmos_dsp_vector_mulv_subv( input_vector_X, input_vector_Y, input_vector_Z, result_vector_R, 256, 28 );
```



27 Matrix Math Functions: Element Negation

Computes the negative value for each input element and sets the corresponding result element to it's negative value:

result_matrix[i][j] = -matrix_X[i][j].

```
void xmos_dsp_matrix_negate
(
  const int input_matrix_X[],
  int    result_matrix_R[],
  int    row_count]
  int    column_count
)
```

Parameters

Name	Direction	Description
input_matrix_X	in	Pointer to 2-dimensional source data X.
result_matrix_R	out	Pointer to the resulting data array.
row_count	in	Number of rows in input and result matrices.
column_count	in	Number of columns in input and result matrices.

Algorithm

```
result = 0
for i = 0 to (row_count - 1):
  for j = 0 to (column_count - 1):
    k = i * column_count + j
    input_vector_X[k] = -input_vector_X[k]
```

Behavior

Each negated element is computed by twos-compliment negation therefore the minimum negative fixed-point value can not be negated to generate it's corresponding maximum positive fixed-point value.

For example: -Q28(-8.0) will not result in a fixed-point value representing +8.0.

```
int samples[8][32];
int result[8][32];
xmos_dsp_matrix_negate( samples, result, 8, 32 );
```



28 Matrix Math Functions: Scalar Addition

Adds a scalar value to each element in matrix_X and stores the result in the corresponding result matrix element:

 $result_matrix[i][j] = matrix_X[i][j] + scalar_A.$

Parameters

Name	Direction	Description
input_matrix_X	in	Pointer to 2-dimensional source data X.
scalar_value_A	in	Scalar value to add to each 'input' element.
result_matrix_R	out	Pointer to the resulting 2-dimensional data array.
row_count	in	Number of rows in input and result matrices.
column_count	in	Number of columns in input and result matrices.

Algorithm

```
result = 0
for i = 0 to (row_count - 1):
  for j = 0 to (column_count - 1):
    k = i * column_count + j
    result_matrix_R[k] = input_matrix_X[k] * scalar_value_A
```

Behavior

32-bit addition is used to compute the result for each element. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_matrix_X[8][32];
int scalar_value_A = Q28( 0.333 );
int result_vector_R[8][32];
xmos_dsp_matrix_adds( input_matrix_X, scalar_matrix_A, result_matrix_R, 8, 32 );
```



29 Matrix Math Functions: Scalar Multiplication

Multiplies each element in matrix_X by the corresponding element in matrix_Y and stores the result in the corresponding result matrix element:

result_matrix[i][j] = scalar_A * matrix_X[i][j].

Parameters

Name	Direction	Description
input_matrix_X	in	Pointer to 2-dimensional source data X.
scalar_value_A	in	Scalar value to multiply to each 'input' element by.
result_matrix_R	out	Pointer to the resulting 2-dimensional data array.
row_count	in	Number of rows in input and result matrices.
column_count	in	Number of columns in input and result matrices.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
result = 0
for i = 0 to (row_count - 1):
  for j = 0 to (column_count - 1):
    k = i * column_count + j
    result_matrix_R[k] = input_matrix_X[k] * scalar_value_A
```

Behavior

Each element of the input matrix is multiplied by a scalar value using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

```
int input_matrix_X[8][32];
int scalar_value_A = Q28( 0.333 );
int result_vector_R[8][32];
xmos_dsp_matrix_muls( input_matrix_X, scalar_value_A, result_matrix_R, 256, 8, 32, 28 );
```



30 Matrix Math Functions: Matrix Addition

Adds each element in matrix_X by the corresponding element in matrix_Y and stores the result in the corresponding result matrix element:

result_matrix[i][j] = matrix_X[i][j] + matrix_Y[i][j].

```
void xmos_dsp_matrix_addm
(
  const int input_matrix_X[],
  const int input_matrix_Y[],
  int    result_matrix_R[],
  int    row_count
  int    column_count
)
```

Parameters

Name	Direction	Description
input_matrix_X	in	Pointer to 2-dimensional source data X.
input_matrix_Y	in	Pointer to source 2-dimensional data array Y.
result_matrix_R	out	Pointer to the resulting 2-dimensional data array.
row_count	in	Number of rows in input and result matrices.
column_count	in	Number of columns in input and result matrices.

Algorithm

```
result = 0
for i = 0 to (row_count - 1):
  for j = 0 to (column_count - 1):
    k = i * column_count + j
    result_matrix_R[k] = input_matrix_X[k] + input_matrix_Y[k]
```

Behavior

32-bit addition is used to compute the result for each element. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_matrix_X[8][32];
int input_matrix_Y[8][32];
int result_vector_R[8][32];
xmos_dsp_matrix_addm( input_matrix_X, input_matrix_Y, result_matrix_R, 256, 8, 32, 28 );
```



31 Matrix Math Functions: Matrix Subtraction

Subtracts each element in matrix_Y from the corresponding element in matrix_X and stores the result in the corresponding result matrix element:

result_matrix[i][j] = matrix_X[i][j] + matrix_Y[i][j].

```
void xmos_dsp_matrix_addm
(
  const int input_matrix_X[],
  const int input_matrix_Y[],
  int    result_matrix_R[],
  int    row_count
  int    column_count
)
```

Parameters

Name	Direction	Description
input_matrix_X	in	Pointer to 2-dimensional source data X.
input_matrix_Y	in	Pointer to source 2-dimensional data array Y.
result_matrix_R	out	Pointer to the resulting 2-dimensional data array.
row_count	in	Number of rows in input and result matrices.
column_count	in	Number of columns in input and result matrices.

Algorithm

```
result = 0
for i = 0 to (row_count - 1):
  for j = 0 to (column_count - 1):
    k = i * column_count + j
    result_matrix_R[k] = input_matrix_X[k] - input_matrix_Y[k]
```

Behavior

32-bit addition is used to compute the result for each element. Therefore fixed-point value overflow conditions should be observed. The resulting values are not saturated.

```
int input_matrix_X[8][32];
int input_matrix_Y[8][32];
int result_vector_R[8][32];
xmos_dsp_matrix_addm( input_matrix_X, input_matrix_Y, result_matrix_R, 256, 8, 32, 28 );
```



32 Matrix Math Functions: Matrix Multiplication

Multiplies each element in matrix_X by the corresponding element in matrix_Y and stores the result in the corresponding element in the result matrix:

result_matrix[i][j] = matrix_X[i][j] * matrix_Y[i][j].

```
void xmos_dsp_matrix_mulm
(
  const int input_matrix_X[],
  const int input_matrix_Y[],
  int    result_matrix_R[],
  int    row_count
  int    column_count
  int    q_format
)
```

Parameters

Name	Direction	Description
input_matrix_X	in	Pointer to 2-dimensional source data X.
input_matrix_Y	in	Pointer to source 2-dimensional data array Y.
result_matrix_R	out	Pointer to the resulting 2-dimensional data array.
row_count	in	Number of rows in input and result matrices.
column_count	in	Number of columns in input and result matrices.
q_format	in	Fixed point format (number of bits making up fractional part).

Algorithm

```
result = 0
for i = 0 to (row_count - 1):
  for j = 0 to (column_count - 1):
    k = i * column_count + j
    result_matrix_R[k] = input_matrix_X[k] * input_matrix_Y[k]
```

Behavior

Elements in each of the input matrices are multiplied together using a 32bit multiply 64-bit accumulate function therefore fixed-point multiplication and q-format adjustment overflow behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

```
int input_matrix_X[8][32];
int input_matrix_Y[8][32];
int result_vector_R[8][32];
xmos_dsp_matrix_mulm( input_matrix_X, input_matrix_Y, result_matrix_R, 256, 8, 32, 28 );
```



33 Statistics Functions: Vector Mean

Computes the mean of the values contained within the input vector:

result = (vector_X[0] + ... vector_X[N-1]) / vector_length

```
int xmos_dsp_vector_mean
(
  const int input_vector_X[],
  int    vector_length,
  int    q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
vector_length	in	Length of the input vector.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Mean value of vector elements.

Algorithm

```
result = 0
for i = 0 to N-1: result += input_vector_X[i]
return result / vector_length
```

Behavior

Due to successive 32-bit additions being accumulated using 64-bit arithmetic overflow during the summation process is unlikely. The final value, being effectively the result of a left-shift by 'q_format' bits will potentially overflow the final fixed-point value depending on the resulting summed value and the chosen Q-format.

```
int result = xmos_dsp_vector_mean( input_vector, 256, 28 );
```



34 Statistics Functions: Vector Power (Sum-of-Squares)

Computes the power (also know as the sum-of-squares) of the values contained within the input vector: $result = vector_X[0]^2 + ... vector_X[(vector_length)-1]^2$

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
vector_length	in	Length of the input vector.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Sum-of-squares for all vector elements.

Algorithm

```
result = 0
for i = 0 to N-1: result += input_vector_X[i] ^ 2
return result
```

Behavior

Since each element in the vector is squared the behavior for fixed-point multiplication should be considered (see behavior for the function 'xmos_dsp_math_multiply').

Due to successive 32-bit additions being accumulated using 64-bit arithmetic overflow during the summation process is unlikely. The final value, being effectively the result of a left-shift by 'q_format' bits will potentially overflow the final fixed-point value depending on the resulting summed value and the chosen Q-format.

Example

int result = xmos_dsp_vector_power(input_vector, 256, 28);



35 Statistics Functions: Root Mean Square (RMS)

Computes the root-mean-square (RMS) of the values contained within the input vector: result = $((\text{vector}_X[0]^2 + ... + \text{vector}_X[N-1]^2) / N) ^ 0.5)$ where N = vector_length

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
vector_length	in	Length of the input vector.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	Root-mean-square of all vector elements.

Algorithm

```
result = 0
for i = 0 to N-1: result += input_vector_X[i]
return xmos_dsp_math_squareroot( result / vector_length )
```

Behavior

Since each element in the vector is squared the behavior for fixed-point multiplication should be considered (see behavior for the function 'xmos_dsp_math_multiply').

Due to successive 32-bit additions being accumulated using 64-bit arithmetic overflow during the summation process is unlikely.

The squareroot of the 'sum-of-squares divided by N value' uses the function 'xmos_dsp_math_squareroot'; see behavior for that function.

The final value, being effectively the result of a left-shift by 'q_format' bits will potentially overflow the final fixed-point value depending on the resulting summed value and the chosen Q-format.

```
int result = xmos_dsp_vector_rms( input_vector, 256, 28 );
```



36 Statistics Functions: Dot Product

Computes the dot-product of two equal length vectors:

result = $vector_X[0] * vector_Y[0] + ... vector_X[N-1] * vector_Y[N-1] where N = vector_length$

```
int xmos_dsp_vector_dotprod
(
  const int input_vector_X[],
  const int input_vector_Y[],
  int     vector_length,
  int     q_format
)
```

Parameters

Name	Direction	Description
input_vector_X	in	Pointer to source data array X.
vector_length	in	Length of the input vector.
q_format	in	Fixed point format (number of bits making up fractional part).
Return Value	out	The dot product of two equal sized vectors.

Algorithm

```
result = 0
for i = 0 to N-1: result += input_vector_X[i] * input_vector_Y[i]
return result
```

Behavior

The elements in the input vectors are multiplied before being summed therefore fixed-point multiplication behavior must be considered (see behavior for the function 'xmos_dsp_math_multiply').

Due to successive 32-bit additions being accumulated using 64-bit arithmetic overflow during the summation process is unlikely. The final value, being effectively the result of a left-shift by 'q_format' bits will potentially overflow the final fixed-point value depending on the resulting summed value and the chosen Q-format.

Example

```
int result = xmos_dsp_vector_dotprod( input_vector, 256, 28 );
```



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