PSCF Visualization

Table of Contents

1 Initializing Data	2
1.1 Reading the PCSF Output File	2
1.2 Reading Additional User inputs	3
1.3 Fixed Inputs	4
2 Translating the Inputs into Useable Form	4
2.1 Unit Cell Properties	4
2.2 Formulating the Volume Fraction Data into 4-D arrays	5
3 Isovalue Calculation	6
3.1 Rescaling the Density	6
3.2 Drawing the Line	6
3.3 Finding the Intersections	8
3.4 Filling the Gaps	9
3.5 The 'Weight' Feature	10
3.6 Storing the Isovalue	12
4 Visualization	12
4.1 Drawing the Colour Maps	12
4.2 Drawing Discrete Density Profiles	14
4.3 Drawing the Composite Density Profile	17
4.4 Drawing the Unit Cell Outline	20
5 Scattering	20
5.1 Intensity vs Scattering Vector	20
5.2 Intensity vs Miller Indices	22
6 Density Along a Line	23

1 Initializing Data

1.1 Reading the PCSF Output File

The program begins by converting the contents of the rho_rgrid file into text, and storing each line as a cell in Matlab, using the following line of code.

```
C = textread(filename, '%s','delimiter', '\n');
```

The parameters in the file are preceded by 'keywords' or abbreviations that indicate their identity; for example, the cell parameters are preceded by 'cell_param' and the number of monomers is preceded by 'N_monomer'. All markers are summarized in Table 1.1.1.

Table 1.1.1 | Parameter Markers

Marker	Description	Type	Name
crystal_system	The crystal system	Text	type
N_monomer	The number of monomer units	Scalar	n_mnr
dim	The number of grid dimensions	Scalar	dim
ngrid	The grid dimensions	Vector	grid
cell_param	The cell parameters	Vector	param

The following code searches for these markers in the cell C using a while loop, and then converts and stores the data in the subsequent line based on its type using relevant Matlab functions, as described in Table 1.1.2.

```
while ndata <= required rep</pre>
   ic = ic +1;
   if round(sum (sscanf(C(ic),'%f')),2)== 1.00 && round(sum
sscanf(C(ic+1), '%f')), 2) == 1.00
      ndata = ndata+1;
   else
      ndata = 0;
   end
   if strcmp(strrep(char(C(ic)),' ', ''),'dim')==1
      dim = str2double(C{ic+1});
                                  % Reads the grid dimensions
   type = strrep(C(ic+1), '''', ''); % Reads the system type
   elseif strcmp(strrep(char(C(ic)),' ', ''),'cell param')==1
                                  % Reads the cell parameters
      param = sscanf(C{ic+1},'%f')';
   elseif strcmp(strrep(char(C(ic)),' ', ''),'ngrid')==1
      grid = sscanf(C{ic+1},'%f')';
                                  % Reads the grid size
   end
end
```

Table 1.1.2 | Data Conversion Functions

Data Type	Function
Text	char
Scalar	str2double
Vector	sscanf

The while loop terminates after reading five consecutive cells whose values each sum to unity that is, after reaching the density grid points. The number five is the value of the parameter required_rep. The following values are stored for later use.

```
end_info = ic - required_rep - 1;
% The row in which the supplementary information ends
start_row = ic - required_rep;
% The row in which the density values start
```

The density values at each grid point are then read into a matrix row by row.

```
A = zeros(length(C) - end_info,n_mnr);
for i =start_row:length(C)
    A(i - end_info,:) = sscanf(C{i},'%f')';
end
```

1.2 Reading Additional User inputs

Additional inputs are read from a text file in the same manner as that from the PSCF output file. A summary is presented in Table 1.2.1.

Table 1.2.1 | User Input Markers

Marker/	arker/Name Description		Туре
isova	lue	The minimum volume fraction present in the display	Vector/ Text
opacity	row 1	The desired opacity of the solid colours	Vector
	row 2	The desired opacity of the interpolated colours	Vector
thickness		The thickness of the unit cell outline	Scalar
box_c	clr	The color of the unit cell outline (RGB)	Vector
map_ch	oice	The desired map coluors	Vector
mono_c	disp	The desired monomers to be visualized independently	Vector
comp_disp		The desired monomers to be visualized in a composite display	Vector
weight		The relative weight of each monomer in the composite display	Vector
scatterdraw		The monomers through which scattering must be analyzed	Vector
h_set		Miller index range, h	Vector
k_set		Miller index range, k	Vector
l_set		Miller index range, I	Vector
inputvec		Direction through which density will be output ^a	Vector

^aSee Section 6.

It should be noted that if isovalue = 'auto', the program will determine appropriate isovalues for the system. This is discussed in Section 3.

1.3 Fixed Inputs

The following are fixed inputs into the program that need not be changed unless the program is rewritten to include more colourmaps, or to increase visual precision.

```
ncolour = 8; %Number of stored colourmaps (7 maps + 1 fill)
n dp = 3; %Number of significant decimal places for colourmapping
```

2 Translating the Inputs into Useable Form

2.1 Unit Cell Properties

The param vector contains the unit cell dimensions followed by the unit cell angles. The following code separates the two parameters and stores them in separate vectors, cell d and angle.

```
if strcmp(type, 'hexagonal') == 1
   angle = [pi/2 pi/2 (2*pi)/3];
    cell d = param;
elseif strcmp(type,'triclinic') == 1
    angle = [param(4) param(5) param(6)];
    cell d = [param(1) param(2) param(3)];
elseif strcmp(type, 'monoclinic') == 1
   angle = [pi/2 param(4) pi/2];
    cell d = [param(1) param(2) param(3)];
elseif strcmp(type,'trigonal') == 1
    angle = [param(2) param(2) param(2)];
    cell d = [param(1)];
else
   angle = [pi/2 pi/2 pi/2];
   cell d = param;
end
```

The following code then ensures that cell_d has three values (one to describe each spatial dimension of the visualized unit cell).

The following code expands the grid to three dimensions in case the calculations were done in one or two dimensions.

```
if (length (grid) ==1)
```

```
grid(2) = grid(1);
  grid(3) = grid(1);
elseif(length(grid)==2)
  grid(3) = grid(1);
end
% 3D grid for 1D crystals
% 3D grid for 2D crystals
```

2.2 Formulating the Volume Fraction Data into 4-D arrays

The following code creates three 3-D arrays containing the grid points (x, y, z) converts the matrix A into a 4-D array, R, that contains the density data at each grid point (x, y, z) for each monomer (in).

```
for iz=1:grid(3)+1,
    for iy=1:grid(2)+1,
         for ix=1:grid(1)+1,
             counter = counter + 1;
             x(ix,iy,iz) = cell d(1) * (ix-1)/grid(1) +
(\cos(\text{angle}(3)))*(\text{cell d}(2))*(\text{iy-1})/\text{grid}(2)) + ((\text{iz-}))*(\text{iz-})*(\text{inj-1})/\text{grid}(2))
1)/grid(3))*(cos(angle(1))*cell d(3));
             y(ix,iy,iz) = cell d(2) * (iy-1)/grid(2) * sin(angle(3)) +
((iz-1)/grid(3))*cos(angle(2))*cell d(3);
             z(ix,iy,iz) = cell d(3) * (iz-1)/grid(3) * sin(angle(1)) *
sin(angle(2));
             for in = 1:n mnr
                  if ix == grid(1)+1
                      R(grid(1)+1,:,:,in) = R(1,:,:,in);
                      counter = counter - (1/n mnr);
                  elseif iy == grid(2) + 1
                      R(:,grid(2)+1,:,in) = R(:,1,:,in);
                      counter = counter - (1/n mnr);
                  elseif iz == grid(3) + 1
                      R(:,:,qrid(3)+1,in) = R(:,:,1,in);
                      counter = counter - (1/n mnr);
                  else
                      R(ix, iy, iz, in) = A(round(counter), in);
                  end
             end
         end
         if(dim==1)
             counter = 0;
         end
    end
    if(dim==2)
         counter=0;
    end
end
```

Note that if the data were only calculated for one or two dimensions, the density values are repeated along the other dimensions, thus creating a 3-D grid of density values for visualization regardless of the dimensions for which the data were calculated.

3 Isovalue Calculation

The isovalue for each monomer is the lower bound of the density value to which each density profile is drawn. These are hard to appropriately determine by hand such that there is no overlap or white space in the composite density profile.

The algorithm in this code determines a set of isovalues such that the most dominant portion of each monomer can be seen in the composite density profile. This is done by drawing a line that passes through the maximum density value of each monomer, setting the isovalue to that at the highest at the intersections, and then adjusting to fill in any gaps. This is broken down in the next sections.

3.1 Rescaling the Density

In this section the R matrix is rescaled such that the density values for each monomer range from zero to one. These new values are then stored in the matrix S.

```
for in = 1:n_mnr
       polmax(in) = max(max(max((R(:,:,:,in)))));
        polmin(in) = min(min(min((R(:,:,:,in)))));
        l length(in) = polmax(in) -polmin(in);
    end
    %Creating the scaled matrix, S
    S = R;
    for in = 1:n mnr
        for iz=1:grid(3)+1,
            for iy=1:grid(2)+1,
                for ix=1:grid(1)+1,
                    S(ix,iy,iz,in) = weight(in)*(R(ix,iy,iz,in) -
polmin(in))/l length(in); % Matrix with scaled values
                end
            end
        end
    end
```

The location of the first n_lines points where the rescaled value is equal to one is then found using the following code. n_lines is set by default to a value of one, as only one value is usually sufficient for the operation of this program.

3.2 Drawing the Line

The points that the line must pass through are those that were just stored in pmax_loc. These must be interleaved to guarantee intersections between density values for different monomers. This is done as follows.

```
point_series(n_mnr*(ir-1)+in,:) = pmax_loc(ir,:,in);
%Series of points to be plotted
    end
end
```

The density values at the nearest grid points along the line are found and stored in the ' $n \times m'$ matrix line, where n is the number of monomers and m is the number of grid points that the line passes through. This is done as follows.

```
for ir = 1:(n lines*n mnr)-1 %Number of lines
           start coord = point series(ir,:);
           end coord = point series(ir+1,:);
           dir vec(ir,:) = end coord-start coord;
           step length(ir) = max(abs(dir vec(ir,:)));
           for \overline{il} = 1:step length(ir)
               ix(ir,il) = start_coord(1) + round((il-
  1) * (dir_vec(ir,1) / step_length(ir)));
               iy(ir,il) = start coord(2) + round((il-
  1) * (dir vec(ir,2)/step length(ir)));
               iz(ir,il) = start coord(3) + round((il-
  1)*(dir vec(ir,3)/step length(ir)));
               x \text{ plot}(il+1 \text{ size}) = il+1 \text{ size};
               for in= 1:n mnr
                   line (in,il+1 \text{ size}) = R
  (ix(ir,il),iy(ir,il),iz(ir,il),in);
               end
           end
           l size = l size + step length(ir);
   end
%The final point
for in= 1:n mnr
    line (in, 1 \text{ size}+1) = R (end coord(1), end coord(2), end coord(3), in);
x plot(l size+1) = l size+1;
```

The density values along this line are then rescaled.

Figure 3.2.1 displays the information contained within line_new. The label on the x-axis 'Line-Index' is simply the number of grid points that the line has passed by, whose data are contained within line new.

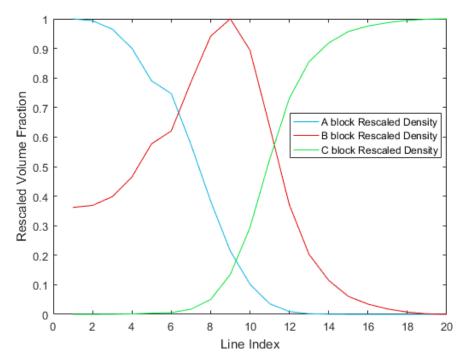


Figure 3.2.1 | Density Values Along line new

3.3 Finding the Intersections

The values of the grid points between which the rescaled density values of monomers intersect are found using and stored using the following line of code.

```
x_inter_store{k} = find(diff(sign(line_new(loop_round+j,:)-
line_new(loop_round,:))));
```

Linear interpolation is then used to find and store the rescaled density value for each monomer at each intersection.

The highest rescaled density value for each type of intersection (i.e. AB, AC, BC) is then found and stored in the vector intervalue.

```
intervalue(k) = max(inter point(k,:));
```

An initial rescaled isovalue for each monomer is then found by taking the highest intervalue that the monomer was involved in. So, for a three monomer system, the three intersection 'types' are AB, CA (which is the same as AC) and BC, which are described by the involved matrix,

```
involved = [1,2;3,1;2,3].
```

The following code stored the initial rescaled isovalue in a vector isovalue s.

```
for k = 1:n_mnr-1
    for in = 1:n_mnr
        in_mat(in,k) = intervalue(involved(in,k));
        isovalue_s(in) = max(in_mat(in,:));
    end
end
```

3.4 Filling the Gaps

Close inspection of Figure 3.2.1 will reveal that there is a gap in continuity between the current rescaled isovalue of the B block and that of the C block.

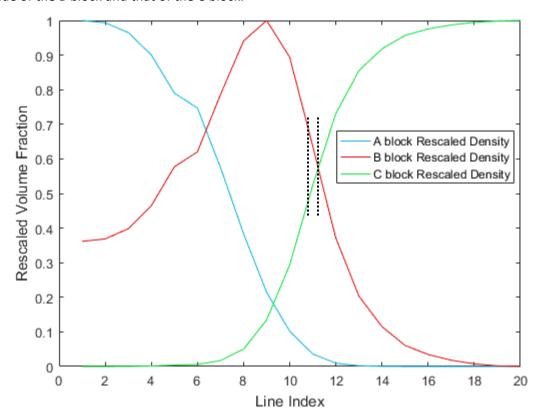


Figure 3.2.1 | Density Values Along line_new

The dotted lines represent the discontinuity in rescaled isovalue.

To bridge this gap, the following is a sample of the code that searches for discontinuities and adjusts the appropriate isovalue accordingly. The vector no_2 contains the second highest intersection value for each monomer, which is required to locate gaps. The program contains variations of this code to account for all permutations for three monomers.

```
for in = 1:n mnr
            r row = in mat(in,:);
            no 2(in) = max(r row(r row < max(r row)));
        end
        for in = 1:n mnr-1
            if isovalue s(in) == no 2(in+1)
                start mat = find(diff(sign(isovalue s(in+1) -
line new(in+1,:))));
                intersect_val = (find(diff(sign(line new(in,:)-
line new(in+1,:))), 1));
                start ind = start mat(abs(start mat -
intersect val) == min(abs(start mat - intersect val)));
                py1= line new(in+1, start ind);
                py2= line new(in+1,1+start ind);
                px1= start ind;
                px2= start ind+1;
                y int = isovalue s(in+1);
                x int = px1 + ((y int-py1)*(px2-px1))/(py2-py1);
                py1= line new(in,start_ind);
                py2= line new(in,1+start ind);
                px1= start ind;
                px2= start_ind+1;
                y \text{ new} = py1 + ((x int-px1)*(py2-py1))/(px2-px1);
                isovalue s(in) = y new;
            end
        end
```

3.5 The 'Weight' Feature

The 'weight' feature allows the user to use an available degree of freedom to increase/decrease the visual presence of any monomer. Due to the nature of the aforementioned isovalue finding algorithm, it is not usually necessary. However, as illustrated in the example below, it might be desired in some cases.

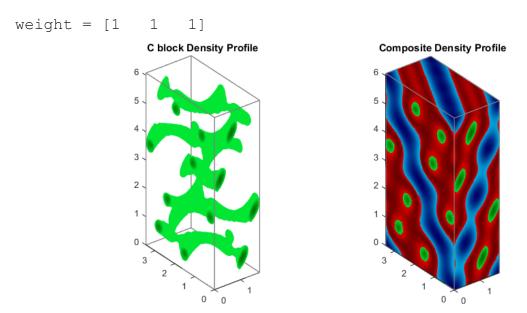


Figure 3.5.1 | Unweighted Gyroid Visualization File Source: pscf-examples/triblock/o70

An easy way to fix the issue of the relatively sparse representation of the C block is to increase its 'weight' by a small increment, and not to decrease that of the others (though the effect would be the same). Note that if the 'weight' deviates too far from 1, then the program will either run into an error, produce a graphically inaccurate representation, or completely neglect to display one of the monomers. Therefore, modifying the weight must be exhibited with caution, it should only be increased by small increments at a time. Here is the same system, with an increased weight for the 'C' block.

weight = [1 1 1.2]

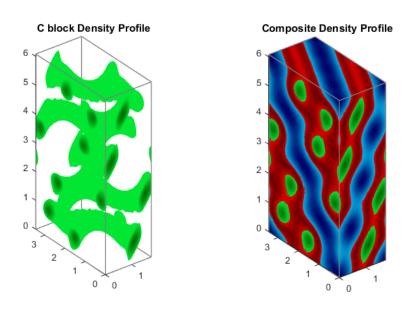


Figure 3.5.2 | Weighted Gyroid Visualization File Source: pscf-examples/triblock/o70

3.6 Storing the Isovalue

Finally, the true isovalues to be used for visualization are converted from the isovalue_s vector that contains the final rescaled isovalues. These true isovalues are stored in the vector isovalue.

```
for in=1:n_mnr
    isovalue(in) = (isovalue_s(in)*l_length(in))/weight(in) +polmin(in);
end
```

4 Visualization

4.1 Drawing the Colour Maps

The colour maps are drawn such that there is one colour for every 0.1% of the density for each monomer. This value is stored in the vector cn. So, for example, if a polymer is drawn from a maximum density of 0.7748 to an isovalue of 0.2934, there will be 1000 * (0.7748 - 0.2934) + 1 = 483 colours (round up) to display the variation of density in space for that monomer.

```
for in = 1:n mnr
   face1(:,in) = reshape(squeeze(R(1,:,:,in)),[],1);
   face2(:,in) = reshape(squeeze(R(:,1,:,in)),[],1);
   face3(:,in) = reshape(squeeze(R(:,:,1,in)),[],1);
   face4(:,in) = reshape(squeeze(R(grid(1)+1,:,:,in)),[],1);
   face5(:,in) = reshape(squeeze(R(:,grid(2)+1,:,in)),[],1);
   face6(:,in) = reshape(squeeze(R(:,:,grid(3)+1,in)),[],1);
   face data(:,in) = [face1(:,in); face2(:,in); face3(:,in);
face4(:,in); face5(:,in); face6(:,in)];
   polmax(in) = max(face data(:,in)); %Max Face Density value
   cn(map choice(in)) = 1+ceil((10^n dp)*polmax(in)-
((10^n dp)*isovalue(in))); %Effective colourmap range (+1 to buffer)
   newisovalue(in) = in + isovalue(in) - 1;
   mono label(in) = char(in+'A'-1);
   titles(in) = {[mono label(in) ' block Density Profile']};
end
```

Note that this maximum density is that on the faces of the unit cell and not that of the entire unit cell, for that is the relevant portion for the colourmap. If the density of any monomer is less than its isovalue on every face, the map is neglected in the composite density profile. The newisovalue vector contains unique density values for each monomer (stored from 0 to 1 for monomer A, 1 to 2 for monomer B, etc.), which is required for the colour map assignment in the composite image.

The colours for these maps range from pre-determined RGB values as follows.

```
% low = low fraction, i.e. light

colour_low = zeros (ncolour,3);
colour_low(1,:) = [0,0.7,0.9]; %blue
colour_low(2,:) = [0.9,0,0]; %red
colour_low(3,:) = [0,0.9,0.2]; %green
colour_low(4,:) = [1,1,0]; %yellow
colour_low(5,:) = [0.5,0,1]; %purple
colour_low(6,:) = [1,0,1]; %pink
```

```
colour_low(7,:) = [0.75,0.75,0.75]; %grey
% high = high fraction, i.e. dark

colour_high = zeros (ncolour,3);
colour_high(1,:) = [0,0,0.4]; %blue
colour_high(2,:) = [0.4,0,0]; %red
colour_high(3,:) = [0,0.4,0]; %green
colour_high(4,:) = [0.4,0.4,0]; %yellow
colour_high(5,:) = [0.15,0,0.30]; %purple
colour_high(6,:) = [0.25,0,0.25]; %pink
colour_high(7,:) = [0.3,0.3,0.3]; %grey
```

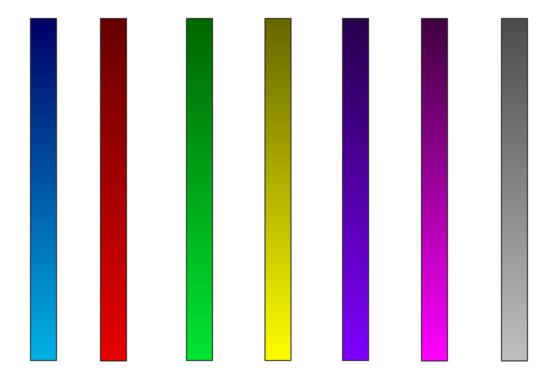


Figure 4.1.1 | Colour Bars Representing Available Colour Ranges

The maps are created using the linspace function to create a map with cn colours between colour low and colour high for each set colour.

```
for in = 1:ncolour
    temp_map = zeros(cn(in),3);
    temp_map(:,1) =
linspace(colourpad(in,1,1),colourpad(in,1,2),cn(in)); %Red
    temp_map(:,2) =
linspace(colourpad(in,2,1),colourpad(in,2,2),cn(in)); %Green
    temp_map(:,3) =
linspace(colourpad(in,3,1),colourpad(in,3,2),cn(in)); %Blue
    map_store{in}=temp_map;
end
```

4.2 Drawing Discrete Density Profiles

The following are the default axis properties, along with comments that explain their function.

The density profiles are visualized by drawing two separate patches using the patch function in Matlab. The first is an isosurface that connects all points of equal isovalue.

```
p1 = patch(isosurface(x,y,z,data,isovalue(in)), ...

'FaceColor',outcolor(map_choice(in),:),'EdgeColor','none','FaceAlpha',opacity(in,1));
```

These are independently drawn for a BCC structure with three monomer types in Figure 4.2.1.

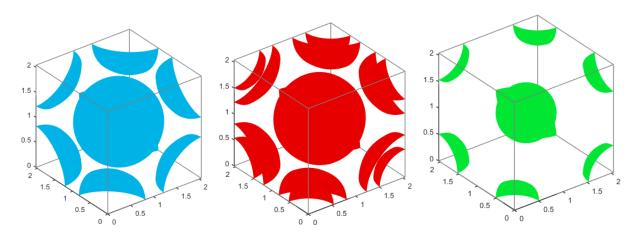


Figure 4.2.1 | Isosurface Examples

File Source: http://pscf.cems.umn.edu/tetrablocks/core-shell-spheres

The second is a patch drawn on the faces of the unit cell whose darkness increase with increasing density.

These are independently drawn for the same BCC structure in Figure 4.2.2.

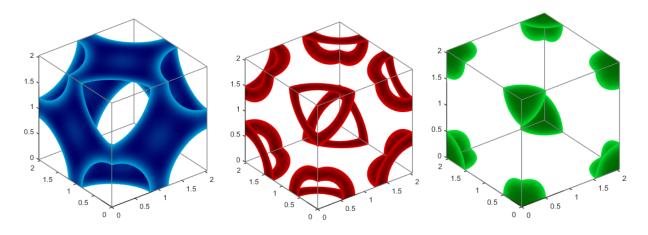


Figure 4.2.2 | Isocaps Examples

File Source: http://pscf.cems.umn.edu/tetrablocks/core-shell-spheres

When combined, the outputs look like this.

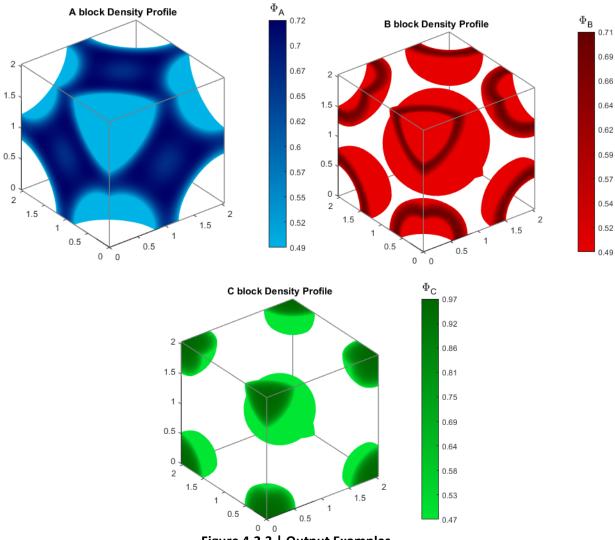


Figure 4.2.3 | Output Examples

File Source: http://pscf.cems.umn.edu/tetrablocks/core-shell-spheres

For hexagonal crystal systems, the calculations are done in the primitive unit cell (1/3 of the hexagon), which is not ideal for visualization. The following code rotates and redraws the patches (twice) so that a full hexagon may be visualized.

```
if strcmp(type, 'hexagonal') == 1
        for i =1:2
            size = (grid(1)+1)*(grid(2)+1)*(grid(3)+1);
            coord set = zeros(size,3);
            counter = 0;
            rotangle = 2*pi/3;
            for iz = 1:grid(3)+1
                for iy = 1:grid(2)+1
                    for ix = 1:grid(1)+1
                        counter = counter +1;
                         coord set(counter,1) = x(ix,iy,iz);
                         coord set(counter,2) = y(ix,iy,iz);
                         coord set(counter, 3) = z(ix, iy, iz);
                    end
                end
            end
            coord set = coord set*[cos(rotangle), sin(rotangle), 0;-
sin(rotangle), cos(rotangle), 0; 0, 0, 1];
            counter = 0;
            for iz = 1:grid(3)+1
                for iy = 1:grid(2)+1
                    for ix = 1:grid(1)+1
                         counter = counter +1;
                        x(ix,iy,iz) = coord set(counter,1);
                        y(ix,iy,iz) = coord set(counter,2);
                         z(ix,iy,iz) = coord set(counter,3);
                    end
                end
            end
            figure(in)
            data = R(:,:,:,in);
            p1 = patch(isosurface(x,y,z,data,isovalue(in)), ...
'FaceColor',outcolor(map choice(in),:),'EdgeColor','none','FaceAlpha',opacity
(in, 1));
            p2 = patch(isocaps(x,y,z,data,isovalue(in)), ...
'FaceColor', 'interp', 'EdgeColor', 'none', 'FaceAlpha', opacity(in, 2));
        end
    end
```

Figure 4.2.4 contains outputs for a simple hexagonal system.

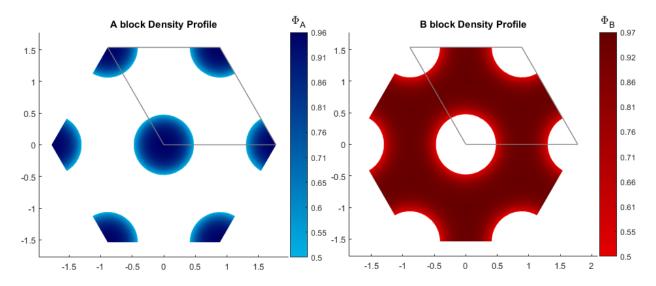


Figure 4.2.3 | Hexagonal Output Example File Source: pscf-examples/diblock/hex

4.3 Drawing the Composite Density Profile

The composite density profile is drawn using the same basic principles as that of the discrete density profile. However, to accommodate for the differing monomer colours, new array must be created, D.

```
D(:,:,:,in) = R(:,:,:,in) + in -1;
```

In this array, the (density) values from zero to one correspond to that of the A block, as usual. The (density) values from one to two correspond to that of the B block, those from two to three, that of the C block, and so on. In addition to this, a new colour map will have to be generated. Because the last patched value for any given monomer is very unlikely to be adjacent in value to that of the next monomer to be patched, some portion of the map must contain unused filler colours, whose size is determined by the matrix fill.

```
c = 0;
for in = comp_disp(1:end-1)
    c = c +1;

    if in~= n_mnr
        fill(in) = (newisovalue(comp_disp(c+1))-newisovalue(in))*(10^n_dp) -
cn(map_choice(in));
    end
```

end

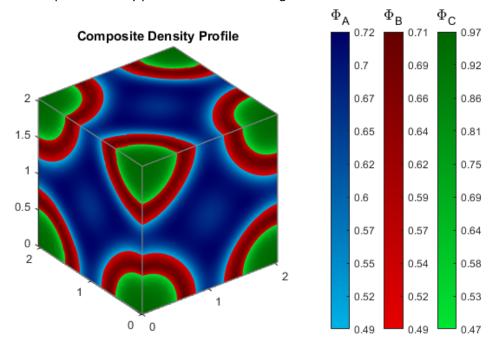
This fill matrix is then used to create the filler sections of the colour map, which spans from the darkest colour for the first monomer to the lightest colour of the next.

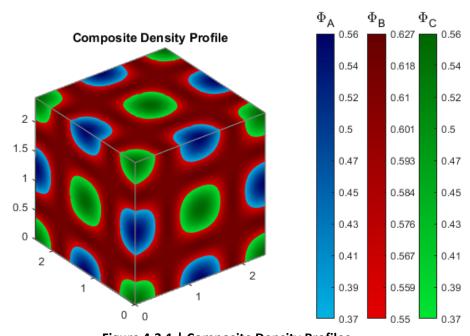
```
c = 0;
```

```
for in = comp_disp(1:end-1)
    c = c +1;
    temp_fillmap = zeros(round(fill(in)),3);
    temp_fillmap(:,1) =
linspace(colourpad(map_choice(comp_disp(c)),1,2),colourpad(map_choice(c
omp_disp(c+1)),1,1),round(fill(in))); %Red
    temp_fillmap(:,2) =
linspace(colourpad(map_choice(comp_disp(c)),2,2),colourpad(map_choice(c
omp_disp(c+1)),2,1),round(fill(in))); %Green
    temp_fillmap(:,3) =
linspace(colourpad(map_choice(comp_disp(c)),3,2),colourpad(map_choice(c
omp_disp(c+1)),3,1),round(fill(in))); %Blue
    fillmap_store{in} = temp_fillmap;
end
```

The composite colour map, newmap is then created by the following code. If the isovalue for any monomer is greater than the maximum density value at any unit cell face for that monomer, then the corresponding colour map is not necessary for visualization and will be neglected.

Two examples of composite density profiles are shown in Figure 4.3.1.





File Source (top): http://pscf.cems.umn.edu/tetrablocks/core-shell-spheres
File Source (bottom): pscf-examples/triblock/NaCl

It should be noted that the opacity of each patch of each monomer can be modified. This is one of the user inputs, <code>opacity</code> and is described in Section 1.2. For the example on the top, if the opacity is set as <code>opacity = [1,1;0,0.65;1,1]</code>, both the A and C blocks will be fully opaque, and the B block (red) will have invisible isosurfaces and isocaps with 65% opacity. This is illustrated in Figure 4.3.2.

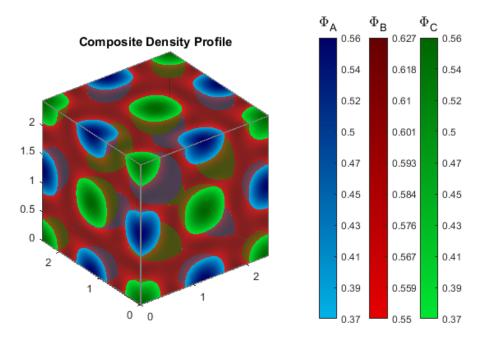


Figure 4.3.2 | Partially Transparent Composite Density Profile
File Source: pscf-examples/triblock/NaCl

4.4 Drawing the Unit Cell Outline

The subfunction draw_lattice draws the unit cell outline given the parameters cell_d, angle, box_clr and thick, whose meaning have been defined in Section 1. The default colour for the unit cell outline is set to grey and this can be seen in the images in Figure 4.2.1 through to Figure 4.3.2.

5 Scattering

The following code loops through each reflection, or set of Miller indices, as set by the user, to take the Fourier transform of the electron density in the grid and give the structure factor. The intensity, \mathbb{I} is calculated as the square of this structure factor.

```
for i f = 1:length(F store)
        h = F store(i f, 1);
        k = F store(i f,2);
        l = F store(i f, 3);
        F sum = 0;
        for in = drawscatter
            x s = zeros(grid);
            y s = zeros(grid);
            z_s = zeros(grid);
            for iz=1:grid(3)
                for iy=1:grid(2)
                     for ix=1:grid(1)
                         x s(ix,iy,iz) = x(ix,iy,iz)/cell d(1);
                         y s(ix,iy,iz) = y(ix,iy,iz)/cell d(2);
                         z s(ix,iy,iz) = z(ix,iy,iz)/cell d(3);
                         F_sum = F_sum +
R(ix,iy,iz,in) * exp(2*1i*pi*((h*x s(ix,iy,iz)) + (k*y s(ix,iy,iz)) + (l*z s(ix,iy,iz)))
ix, iy, iz))));
                     end
                end
            end
        F store(i f,4) = F sum * cell d(1)*cell d(2)*cell d(3);
        F store(i f,5) = abs(F sum)^2;
        I(i f) = F store(i f, 5);
        x index(i f) = i f;
        x index label(i f) = {[h k l]};
        x_label{i_f}=mat2str(cell2mat(x_index_label(i_f)));
        q(i f) = sqrt((b(1)*h)^2 + (b(2)*k)^2 + (b(3)*1)^2);
    end
```

5.1 Intensity vs Scattering Vector

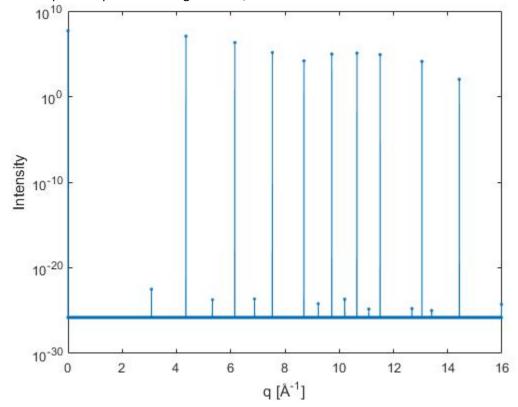
The following code finds duplicate values for q, takes the arithmetic mean of their intensities, and places the values back into a sorted matrix.

```
plotmat = sortrows([q;I]');
    [q1,~,q ind] = uniquetol(plotmat(:,1));
```

```
plotmat_avg = [q1,accumarray(q_ind,plotmat(:,2),[],@mean)];
q_sort = plotmat_avg(:,1);
I_sort = plotmat_avg(:,2);
```

Many points are then added in between those calculated so that the function plotted will approximate a delta function.

Two output examples are provided in Figure 5.1.1, that of a BCC structure and an FCC structure.



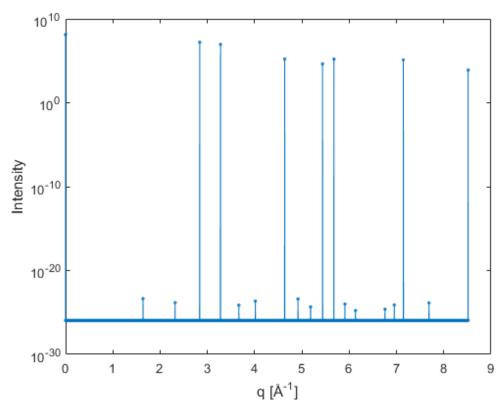
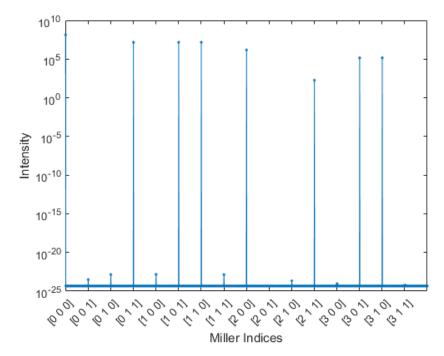


Figure 5.1.1 | I(q) plots for BCC (top) and FCC (bottom)

5.2 Intensity vs Miller Indices

The program also outputs plots of Intensity vs Miller Indices, which are stored in the main loop. Examples are shown in Figure 5.2.1 for a BCC and an FCC structure.



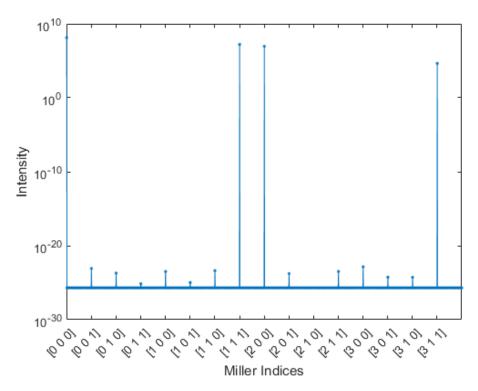


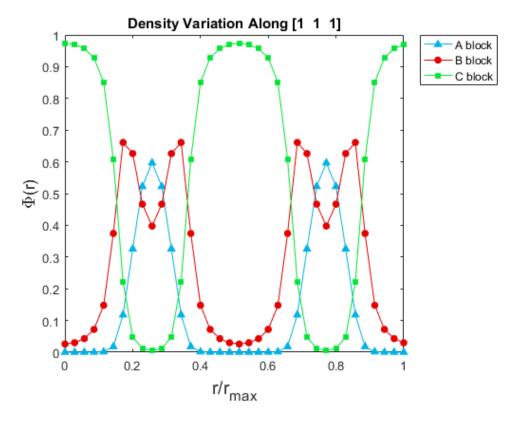
Figure 5.1.2 | Intensity vs Miller Indices plots for BCC (top) and FCC (bottom)

6 Density Along a Line

The final output of the program requires the user input inputvec. This is the direction vector along which the density values of each monomer will be found. The following code accomplishes this.

```
userinput = inputvec;
    start coord = [1 1 1];
    end coord = userinput .* grid + [1 1 1];
    dir vec = end coord-start coord;
    step length = max(abs(dir vec));
    clear ix iy iz x plot
    for il = 1:step length
        ix(il) = start coord(1) + round((il-
1) * (dir_vec(1) / step_length));
        iy(il) = start_coord(2) + round((il-
1) * (dir vec(2) / step length));
        iz(il) = start coord(3) + round((il-
1) * (dir vec(3) / step length));
        x \text{ plot(il)} = (il-1)/(step length-1);
        for in= 1:n mnr
            line plot (in,il) = R (ix(il),iy(il),iz(il),in);
        end
    end
```

Two example outputs can be seen in Figure 6.1.



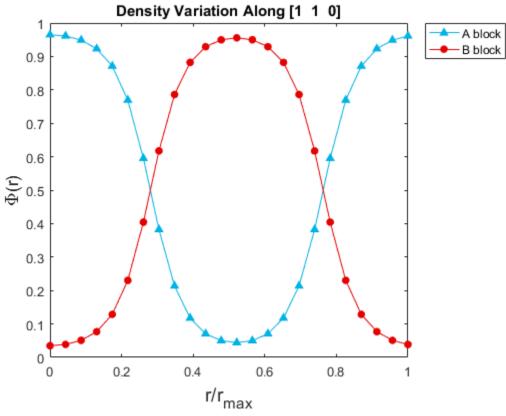


Figure 6.1 | Line Density plots for Core-Shell Spheres (top) and a Cylinder System (bottom)

File Source (top): http://pscf.cems.umn.edu/tetrablocks/core-shell-spheres

File Source (bottom): pscf-examples/diblock/hex