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# Assignment-8

## EE22BTECH11012-A.Chhatrapati

Question 9.3.4)In an examination, 20 questions of true-false type are asked. Suppose a student tosses a fair coin to determine his answer to each question. If the coin falls heads, he answer true; if it falls tails, he answer false. Find the probability that he answers at least 12 questions correctly.

### **Solution:**

TABLE 0 Variables

| Variable              | Value            | Description                           |
|-----------------------|------------------|---------------------------------------|
| n                     | 20               | Number of questions                   |
| p                     | 0.5              | probability of question being correct |
| $\mu = np$            | 10               | mean of distribution                  |
| $\sigma = \sqrt{npq}$ | √5               | variance of distribution              |
| X                     | $0 \le X \le 20$ | Number of correct questions           |

#### Gaussian

$$X \approx Y \sim \mathcal{N}(10, 5)$$
 (1)

1) With a 0.5 correction:

$$\Pr(Y \ge 12) = Q\left(\frac{11.5 - \mu}{\sigma}\right) \tag{2}$$

$$\Pr(Y \ge 12) = Q(0.3 \times \sqrt{5}) = Q(0.67)$$
(3)

$$\implies \Pr(Y \ge 12) = 0.2511 \tag{4}$$

2) Without correction:

$$\Pr(Y \ge 12) = Q\left(\frac{12 - \mu}{\sigma}\right) \tag{5}$$

$$\Pr(Y \ge 12) = Q(0.894) \tag{6}$$

$$\implies \Pr(Y \ge 12) = 0.1855$$
 (7)

#### **Binomial**

$$Pr(X \ge 12) = 1 - Pr(X < 12)$$
 (8)

$$= \sum_{k=12}^{20} {}^{n}C_{k}p^{k} (1-p)^{n-k}$$
 (9)

$$= 0.2517$$
 (10)

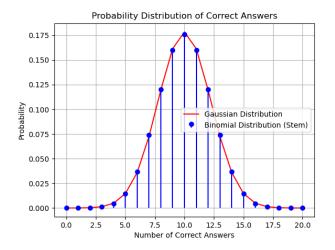


Fig. 2. Binomial vs Gaussian