Assignment-3

EE22BTECH11012-A.Chhatrapati

Question 10.13.3.37) A child's game has 8 triangles of which 3 are blue and rest are red, and 10 squares of which 6 are blue and rest are red. One piece is lost at random. Find the probability that it is a

- (i) triangle
- (ii) square
- (iii) square of blue colour
- (iv) triangle of red colour

Solution:

Variable	Value	Description
X	1	Triangle
X	0	Square
Y	1	Blue coloured
Y	0	Red coloured

$$p_X(X = 0) = \frac{10}{15}$$

$$p_X(X = 1) = \frac{8}{15}$$

$$p_X(Y = 0) = \frac{9}{15}$$

$$p_X(I = I) = \frac{18}{18}$$

(ii)
$$p_X(0) = \frac{10}{18}$$

$$p_{X}(X = 0) = \frac{10}{18}$$

$$p_{X}(X = 1) = \frac{8}{18}$$

$$p_{X}(Y = 0) = \frac{9}{18}$$

$$p_{X}(Y = 1) = \frac{9}{18}$$

$$(i) p_{X}(1) = \frac{8}{18}$$

$$(ii) p_{X}(0) = \frac{10}{18}$$

$$(iii) p_{XY}(X = 0, Y = 1) = \Pr(Y = 1|X = 0) p_{X}(0)$$

$$= \frac{6}{10} \times \frac{10}{18} = \frac{6}{18}$$

$$= \frac{6}{10} \times \frac{10}{18} = \frac{6}{18}$$
(iv) $p_{XY}(X = 1, Y = 0) = \Pr(Y = 0|X = 1) p_X(1)$

$$= \frac{5}{8} \times \frac{8}{18} = \frac{5}{18}$$