

Assignment-6

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Question 34.2023) Let $X_{n \geq 1}$ be a Markov chain with state space $\{1, 2, 3\}$ and transition probability matrix

$$\begin{pmatrix} \frac{1}{2} & \frac{1}{4} & \frac{1}{4} \\ \frac{1}{3} & \frac{1}{3} & \frac{1}{3} \\ 0 & \frac{1}{2} & \frac{1}{2} \end{pmatrix}$$

(by markov's property)

Let's calculate $p_{X_2, X_1}(1, 1)$ using transition probability matrix

$$\Rightarrow p_{X_2, X_1}(1, 1) = p_{11} = \frac{1}{2} \quad (3)$$

$$\Rightarrow \Pr(X_2 = 1 | X_1 = 1, X_3 = 2) = 0.5 \quad (4)$$

Then $\Pr(X_2 = 1 | X_1 = 1, X_3 = 2)$ equals

Solution: Consider transition matrix as:

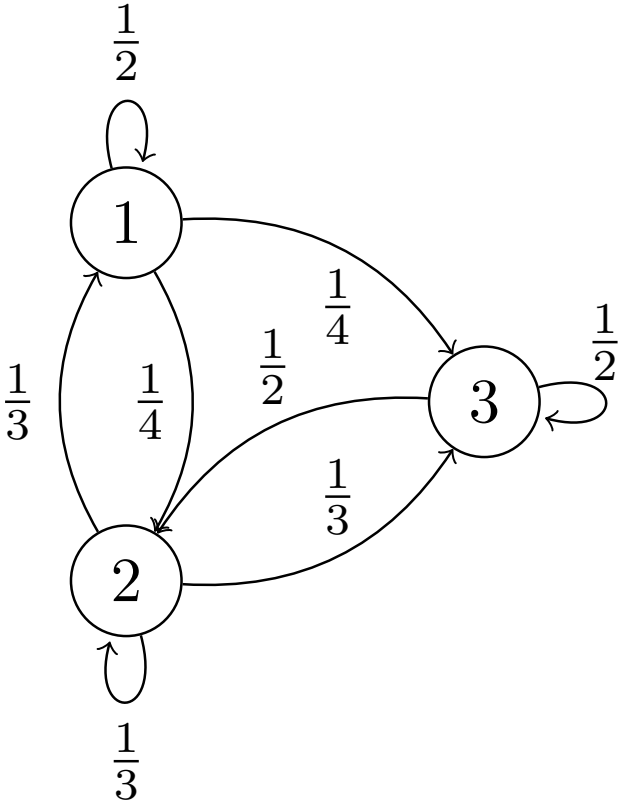


Fig. 0. Markov Chain diagram

$$\begin{pmatrix} p_{11} & p_{12} & p_{13} \\ p_{21} & p_{22} & p_{23} \\ p_{31} & p_{32} & p_{33} \end{pmatrix} \quad (1)$$

$$\Pr(X_2 = 1 | X_1 = 1, X_3 = 2) = p_{X_2, X_1}(1, 1) \quad (2)$$