

Random variables

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Let

Variable	Value	Description
X_i	0	i^{th} player doesn't win a prize
	1	i^{th} player wins a prize

If n^2 is the value of the chosen number that is greater than 500 and also a perfect square, then

$$n^2 \in (500, 1000] \quad (1)$$

$$\implies n \in (22.36, 31.62] \quad (2)$$

n can take 9 integer values in the above interval.

$$Pr(X_1 = 1) = \frac{9}{1000} \quad (3)$$

$$= 0.009 \quad (4)$$

If first player gets a number greater than 500 which is a perfect square then the second player can get a number from the remaining 8 numbers in the above interval to win a prize.

(i) Probability that first player wins a prize

$$= Pr(X_1 = 1) \quad (5)$$

$$= 0.009 \quad (6)$$

(ii) Probability that second player wins given that the first player has won prize

$$= Pr((X_2 = 1)|(X_1 = 1)) \quad (7)$$

$$= 0.008 \quad (8)$$