

## Lecture #6 Data flow.

- $C(x, s, in) = \text{value of } x \text{ before } s$
- $C(x, s, out) = \text{value of } x \text{ after } s$

Rule 1: if  $C(x, p_i, out) = *$  for any  $i$   
then  $C(x, s, in) = *$

Rule 2:  $C(x, p_i, out) = c$  &  
 $C(x, p_j, out) = d$  &  
 $d \neq c$   
then  $C(x, s, in) = *$

Rule 3: if  $\forall i, C(x, p_i, out) = c$  or  $\#$   
then  $C(x, s, in) = c$

Rule 4: if  $\forall i, C(x, p_i, out) = \#$   
then  $C(x, s, in) = \#$

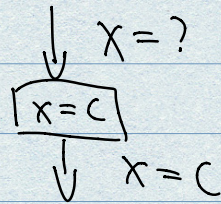
$\uparrow \quad C(x, p_i, out) \longrightarrow C(x, s, in)$

Rule 5.

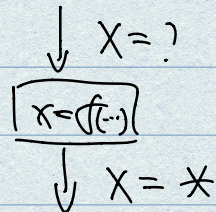
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graph TD; A["x = #"] --> B["s"]; B --> C["x = #"]
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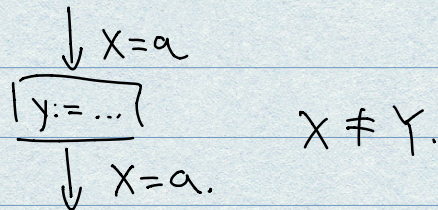
Rule 6.



Rule 7.



Rule 8.



An Algorithm:

1. for every entry  $s$  to the program

set  $C(s, x, in) = *$

2. Set  $C(s, x, in)$

$= C(s, x, out)$

$= \#$

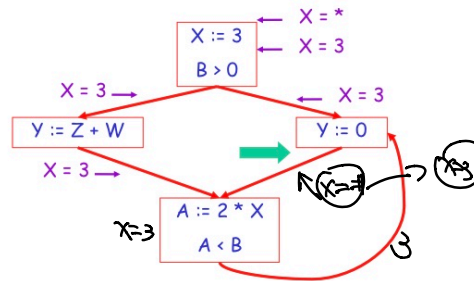
everywhere else

3. Repeat until all points satisfy 1-8.



## The Value #

- To understand why we need #, look at a loop



Dynamic dispatch: get type  
 → get method / property

Ordering.

\* is the greatest, # is the least.

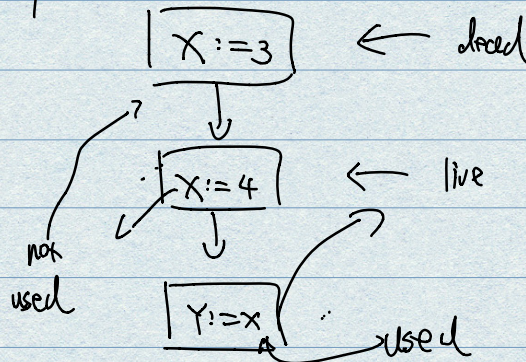
the lub be the least-upper-bound.

Rule 1 - 4 →

$C(x, s, in)$

$= \text{lub} \{ C(p, x, out) \mid p \text{ is a predecessor of } s \}$

Liveness Analysis.





live merged with live  
→ live.