# Users Guide for Corrfunc

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### 1 Introduction

Correlation functions are a statistical measure of a density field and are widely used in large-scale structure formation. Generally, the measurements are done  $once^1$  on survey data and compared with model predictions in a Monte-Carlo Markov Chain. As such, the correlation functions have to be measured repeatedly during an MCMC. The codes presented here are meant to cover the typical scenarios of measuring correlation functions in theory-land. The primary consideration in writing these codes is speed<sup>2</sup>— the codes presented here should outperform any other CPU based correlation functions codes by a wide margin.

Cache locality and hand-written AVX intrinsics are the reasons why the code is very fast. However, that also means that the code is not very portable. I have tried my best to ensure that the codes work on Linux and MAC OSX. If it does not work for you, particularly if you are on a reasonable Linux install, please email me. The API for the codes can be considered frozen; I will not change the API without changing the MAJOR release version.

The paper associated with the codes is being (slowly) written by me. I hope to submit the paper to Astronomy & Computing and release the codes simultaneously. Once I submit the paper to arXiv, there will be an actual paper arXiv link here.

## 2 Installation

The only requirements for the code to install is a valid C compiler, with OpenMP support. The AVX instruction set can only be used for CPU's later than 2011 (Intel Sandy Bridge/AMD Bulldozer or later).

## 2.1 Getting the Source

You can obtain the source in two ways: i) Clone the mercurial repo (hg clone https://bitbucket.org/manodeep/corrfunc/) or ii) Download the tar archive (corrfunc.\$MAJOR.0.\$MINOR.tar. and unpack it in the directory where you wish to keep the files (tar xvzf corrfunc.\$MAJOR.0.\$MINOR.tar.gz). Here, \$MAJOR and \$MINOR refer to the major and

<sup>&</sup>lt;sup>1</sup>which is why I have not bothered with releasing the codes to measure correlation functions on data

<sup>&</sup>lt;sup>2</sup>The secondary consideration was maintainability and ease of use for others. I have versions of these codes that are even faster but are much harder to modify/maintain by any one other than me!

minor release versions (current MAJOR=1, MINOR=0). I will only change the MAJOR version in the highly unlikely event that the API changes.

# 2.2 Directory Structure

The directory structure for the code looks like this:

corrfunc	
paper	
io	Source files for reading in data.
utils	Source files for creating grids and
	helper routines.
bin	Will be created to copy executable
	files when you run 'make install'.
Ī	
lib	
	libraries and python library after
	you run 'make'.
$x_{i_{-}}$ theory	
	IDL scripts to run benchmarks.
examples	Source files for example C bindings
	using the static libraries.
python_bindings	Source files to generate python
	bindings.
x1_of_r	Source files for getting pair-counts
	to compute $\xi(r)$ .
<del>_</del>	
x1	
	periodic cube.
	Source files to compute the
xi mocks	counts-in-spheres statistic.
	IDL scripts to run benchmarks for
Dencimarks	mocks.
examples	Source files for example C bindings
1	using the static libraries for
	mocks.
python_bindings	Source files to generate python
	bindings for mocks.
tests	$\ldots\ldots$ . Correct outputs for tests for mocks.

Table I. List of c	compilations options,	what the options mea	an and their dependencies	for the codes.
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Option Type	Option Name	Default State	Requires	Notes
	PERIODIC	Enabled	None	Enables periodic boundary conditions.
Science	OUTPUT_RPAVG	Disabled	DOUBLE_PREC	Outputs the average pair-separation in each bin. $DD(r)$ and $w_p(r_p)$ can be slower by more than $2\times$ , $\xi(r_p,\pi)$ is less affected.
	DOUBLE_PREC	Disabled	None	Computations are done using double precision. Slower and requires more RAM.
Code	USE_AVX	Enabled	CPU and compiler with AVX support	CPUs later than 2011 have AVX support. Code will run much faster with this option.
	USE_OMP	Enabled	OpenMP capable compiler	Since clang does not support OpenMP yet, common.mk will stop compilation with clang when this flag is enabled.

	dataMock galaxy catalogs for tests on a
	sphere.
1	_DDrppiSource files for getting pair-counts
	to compute $\xi(r_p,\pi)$ on mocks.
1	_wthetaSource files for getting pair-counts
	to compute $\omega( heta)$ .
	_vpfSource files to compute the
	counts-in-spheres statistic on
	mocks.

### 2.3 Compilation Options

There are a few code options that control both the Science case and the code compilation. All of these options are located in 'common.mk' in the base directory ('corrfunc'). Edit the first few lines to set these options (see Table. I for details):

- Science options PERIODIC, OUTPUT\_RPAVG
- Code options DOUBLE\_PREC, USE\_AVX and USE\_OMP

Depending on your Science use-case and the cpu/compiler, you will want to set the different options. Once you set those options, you should set the C compiler, CC (available options are icc, gcc, clang). Once you have set the compiler, installing should be as simple as typing 'make' and 'make install' in the xi\_theory directory. All the libraries are intentionally chosen to be static libraries just to avoid any path conflicts. However, on MAC OSX, you may have to do more to get the library to work – so I have outlined some of the scenarios in Section 2.5.

#### 2.4 Linux

If the installation went well, you should have an executable called run\_correlations in the examples directory. Type ./run\_correlations in the examples directory and you should see the code in action. The C source file run\_correlations.c also serves as an example to use the DD(r),  $\xi(r_p, \pi)$  and  $w_p(r_p)$  libraries in C.

#### 2.5 Mac OSX

There can be two issues on MACs. One is that the default gcc assembler supplied by XCode or macports is too old and does not support AVX instructions even when the CPU does. One way to get around this is by using the clang assembler even when compiling with gcc. The easiest way to do it is by replacing the default assembler with the as script in the paper directory (taken from this url). Copy this as script to the appropriate directory (/opt/local/bin/ for me since I use macports gcc on my laptop).

Another problem might come with running the python example codes in the python\_bindings directory. If you get an error message:

• Fatal Python error: PyThreadState\_Get: no current thread

when you run python call\_correlation\_functions.py, then the following steps might fix the problem (these are also noted in the FAQ). This error occurs when the python library used at compile time is not the same as the runtime python library. In all cases that I have seen, this error occurs when using the conda package manager for python<sup>3</sup>.

- Change the relative path for the shared python library \_countpairs.so. You can change the relative path by issuing the command:

  install\_name\_tool -change libpython2.7.dylib `python-config --prefix`/lib/libpython2.7.dylib \_countpairs.so
- Add to the fallback library path environment variable.

  export DYLD\_FALLBACK\_LIBRARY\_PATH=`python-config --prefix`/lib:\$DYLD\_FALLBACK\_LIBRARY\_PATH
- If both of the above methods fail, then create a symbolic link ln -s `python-config --prefix`/lib/libpython2.7.dylib

If all went well, then you should be able to run the run\_correlations code in the examples directory as well as execute python call\_correlation\_functions.py in the python\_bindings directory. In all of the above examples, I have assumed that the relevant python library is libpython2.7.dylib (the default under conda) – you may have to replace it with your python library version.

# 2.6 Running the tests

If installation went fine, then run make tests to run a suite of tests. If any of the tests fail, then please email me. I have never seen the tests fail unless I made some coding error while modifying the source. Once the tests pass successfully, type make install to install the binaries into the bin directory.

<sup>&</sup>lt;sup>3</sup>This behaviour is by design according to conda

# 3 Running the Codes

The codes should run straight out of the box. Note, the DD(r) and  $\xi(r_p, \pi)$  can compute both auto and cross-correlations with and without PERIODIC boundary conditions whereas the  $w_p(r_p)$  code only computes the auto-correlation with PERIODIC boundary conditions. Also, since both the DD(r) and  $\xi(r_p, \pi)$  codes compute cross-correlations, pairs are double-counted in both DD(r) and  $\xi(r_p, \pi)$  codes. You could, in theory, make the auto-correlation bit faster by only computing unique pairs (as is done in  $w_p(r_p)$ , see Section 4.3.4 for details). However, since the total run-time will dominated by the cross-correlation (the number of randoms is typically an order of magnitude larger than the number of data points), I have not implemented those optimizations for the auto-correlation calculations.

### 3.1 Input File Formats

The codes currently can handle these types of input data files:

- ascii White-space separated columns, format code is 'a'.
- csv Comma-separated values, format code is 'c'.
- fast-food Fast-food, fortran binary format, format code is 'f'. The fast-food file format is described in detail in Section 3.1.1.

For the ascii and csv files, the code reads in the first three columns as the co-moving X/Y/Z arrays. Note, that more columns can be present but the code will ignore those columns.

#### 3.1.1 The fast-food file format

The fast-food format is a fortran binary format – all fields are surrounded with 4 bytes padding. These value of these padding bytes is the number of bytes of data contained in between the padding bytes. For example, to write out 20 bytes of data in a fast-food file format would require a total of 4 + 20 + 4 = 28 bytes. The first and last 4 bytes of the file will contain the value 20 – showing that 20 bytes of real data are contained in between the two paddings.

The fast-food file consists of a header:

#### **Listing 3.1** The header format for fast-food files

```
int idat[5];
float fdat[9];
float znow;
```

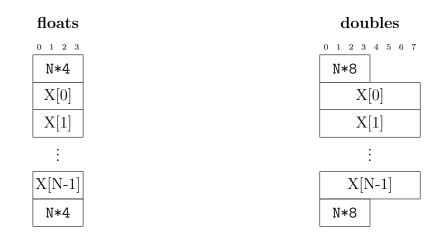
For the purposes of these correlation function codes, the only useful quantity is idat[1] which contains N – the number of particles in the data file.

0	1	2	3	4	5	6	7	8	9 10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27
	2	0			Iı	nt			N					3	Iı	nt	eg	eı	S					2	0	

The next 56 bytes contain two other fields (10 floats + 4 padding bytes of 4 bytes each) and their corresponding paddings. Since these bytes do not contain any data that are useful in the context of these codes we will skip over the contents of these bytes. In io.c, I actually fseek over these bytes.

After this header, the actual X/Y/Z values are stored. The first 4 bytes after the header contains N\*4 for float precision or N\*8 for double precision where N=idat[1], is the number of particles in the file. After all the X values there will be another 4 bytes containing N\*4 or N\*8. Note, that even when the X/Y/Z arrays are written out in double-precision, the padding is still 4 bytes. The blocks for Y/Z follow after the X block.

### Byte-structure of the X/Y/Z arrays in a fast-food file



## 3.2 Specifying the radial bins

The codes were intentionally designed to read in a set of (somewhat) arbitrary<sup>4</sup> set of bin specifications from a file. This way, you can specify disjoint bin-edges as well as use 0.0 as a bin edge (which would be impossible if log bins are assumed). The bins are to be specified in a (white-space separated) text file in this manner:

```
r_low[0] r_high[0]
r_low[1] r_high[1]
:
r_low[nbins-1] r_high[nbins-1]
```

where, r\_low[i] and r\_high[i] are the left and right edges of the i'th bin respectively. The text files should contains as many lines as the number of bins desired. The logbins

<sup>&</sup>lt;sup>4</sup>I assume bins are non-overlapping

executable can be used to create such a text file containing log bins. The syntax for running logbins is:

./logbins rmin rmax nbins > filename

An example of such a file with radial bins is the file bins in the tests directory. Note, all of the three codes print the correlation function to stdout – so be sure to redirect stdout to an output file.

# 3.3 Running DD(r)

To run the correlation function in 3-D, you will need to run the executable DD from either the bin or xi\_of\_r directory. Note, that DD(r) double-counts the pairs (as does  $\xi(r_p, \pi)$ ). The inputs to DD are:

- file1 the file name for the first file.
- format1 the file format for the first file. Options are a,c,f see Section 3.1.
- file2 the file name for the second file.
- format2 the file format for the second file. Options are a,c,f see Section 3.1.
- binfile the file name for the file containing the bins (see Section 3.2)
- nthreads the number of OpenMP threads to use (only required when the Makefile option USE\_OMP is enabled)

Thus, the code can compute an auto-correlation (when file1,format1 and file2,format2 are identical) or a cross-correlation (when file1 and file2 are different). Out of the box, some sample DD call directory) can be:

- auto-correlation ./DD ../tests/data/gals\_Mr19.ff f ../tests/data/gals\_Mr19.ff f ../tests/bins 4 > Mr19\_output.DD
- CTOSS-COTTelation ./DD ../tests/data/cmassmock\_Zspace.ff f ../tests/data/random\_Zspace.ff f ../tests/bins 4 > cmass\_output.DR

The output (printed to stdout) has nbins rows; each row contains the columns <Npairs> <rpavg> <rmin> <rmax>, where the <rpavg> column contains 0.0 unless the Makefile option OUTPUT\_RPAVG has been enabled. Here, each line of the output represents the i'th radial bin.

## 3.4 Running $\xi(r_p, \pi)$

To run the correlation function in 2-D for  $\xi(r_p, \pi)$ , you will need to run the executable DDrppi from either the bin or xi\_rp\_pi directory. Note, that  $\xi(r_p, \pi)$  double-counts the pairs (as does DD(r)). The inputs to DDrppi are:

- file1 the file name for the first file.
- format1 the file format for the first file. Options are a,c,f see Section 3.1.
- file2 the file name for the second file.
- format2 the file format for the second file. Options are a,c,f see Section 3.1.
- binfile the file name for the file containing the bins (see Section 3.2)
- pimax the maximum distance to consider in the  $\pi$  direction. The code uses Z axis as the  $\pi$  (line-of-sight) direction.
- nthreads the number of OpenMP threads to use (only required when the Makefile option USE\_OMP is enabled)

Thus, the code can compute an auto-correlation (when file1,format1 and file2,format2 are identical) or a cross-correlation (when file1 and file2 are different). Out of the box, some sample DDrppi call directory) can be:

- auto-correlation ./DDrppi ../tests/data/gals\_Mr19.ff f ../tests/data/gals\_Mr19.ff f ../tests/bins 40.0 4 > Mr19\_output\_rppi.DD
- Cross-correlation ./DDrppi ../tests/data/cmassmock\_Zspace.ff f ../tests/data/random\_Zspace.ff f ../tests/bins 80.0 4 > cmass\_output\_rppi.DR

The output (printed to stdout) has nbins rows; each row contains the columns  $\langle \text{Npairs} \rangle \langle \text{cpavg} \rangle \langle \text{cg(rmin)} \rangle \langle \text{pi\_upper} \rangle$ , where the  $\langle \text{rpavg} \rangle \rangle \langle \text{column contains 0.0}$  unless the Makefile option OUTPUT\_RPAVG has been enabled. The code bins in 1 Mpc/h in the  $\pi$  direction by default. Therefore, the total number of bins in the output file will be  $\text{nbins} \times \pi_{\text{max}}$ , where each radial bin is further broken into  $\pi_{\text{max}}$  bins along the  $\pi$  direction.

There is a code wprp in the xi\_rp\_pi directory that can combine the output of DDrppi for DD, DR and RR counts and use Landy-Szalay estimator to produce a projected correlation function.

## 3.5 Running $w_p(r_p)$

To run the projected correlation function, you will need to run the executable wp from either the bin or wp directory. The inputs to wp are:

• boxsize – the boxsize for the periodic box.

- file file name.
- format file format. Options are a,c,f see Section 3.1.
- binfile the file name for the file containing the bins (see Section 3.2)
- pimax the maximum distance to consider in the  $\pi$  direction. The code uses Z axis as the  $\pi$  (line-of-sight) direction.
- nthreads the number of OpenMP threads to use (only required when the Makefile option USE\_OMP is enabled)

The wp code only computes an auto-correlation with PERIODIC boundary conditions, irrespective of the options set in common.mk.

• ./wp 420.0 ../tests/data/gals\_Mr19.ff f ../tests/bins 40.0 4 > Mr19\_output.wp

The output (printed to stdout) has nbins rows; each row contains the columns <wp> <rpavg> <rmin> <rmax> <Npairs>, where the <rpavg> column contains 0.0 unless the Makefile option OUTPUT\_RPAVG has been enabled.

# 4 Code Design

The following sections are taken directly from the associated paper. The fundamental idea behind the code can be broken down into the following steps:

- Given the max. separation,  $r_{max}$ , for the correlation function, grid the entire the particle distribution with cell width  $r_{max}$ . In case of  $\xi(r_p, \pi)$  and  $w_p(r_p)$ , the X/Y bins are  $r_{max}$  while the Z bins is  $\pi_{max}$ .
- In each 3-D cell, store all the particles that are located in that cell in contiguous X/Y/Z arrays (see Listing 4.4). The particle data are contained in a structure defined in Listing 4.1.
- Loop over all particles in every cell (this loop uses OpenMP parallelization if USE\_OMP is enabled). This is the index1 loop in countpairs.c, countpairs\_rp\_pi.c and countpairs\_wp.c. The loop variable for the loop over each particle is i.
- Now, for every particle in the input list, we only need to look at particles in the neighbouring cells (see Fig. 1).
- Loop over neighbouring cells in all 3 dimensions. Corresponding variables are iiix, iiiy, iiiz. These variables are constructed from the loop variables iix, iiy, iiz to account for periodic boundary conditions. <sup>5</sup>

<sup>&</sup>lt;sup>5</sup>I apologize for this atrocious variable naming scheme.

- Once we have a triplet of iiix, iiiy, iiiz, we can construct the index for the neighbouring cell. Variable index2 gives the index for the neighbouring cell.
- Compute the distances between target particle and some particle bunch (where a chunk is 4 double or 8 floats) using AVX intrinsics. The slower, non-AVX version of the code computes the distances serially and does not take advantage of the CPU architecture. This is the j loop in countpairs.c, countpairs\_rp\_pi.c, countpairs\_wp.c.
- Check if any of the distances are less than  $r_{max}$ . If not, continue processing the data. If yes, then update the histograms using AVX bit-masks and popcount.
- Continue until all particles in neighbouring cell are done.

### 4.1 Partitioning the Particles based on $r_{max}$

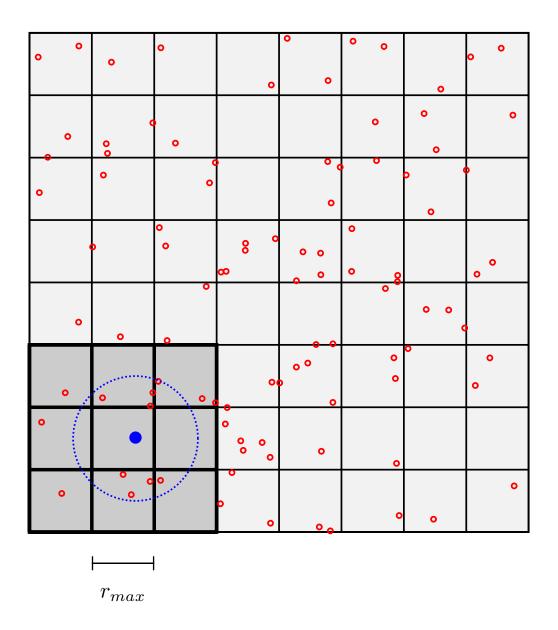
We need to compute pairwise distances to get the correlation function. A naive implementation of a correlation function would compute all possible pairwise separations with a complexity  $\mathcal{O}(N^2)$ . However, for almost all correlation functions, we are only interested in separations less than a certain  $r_{max}$ , where  $r_{max}$  is much smaller than the domain of the point distribution itself. We can then immediately see a way to prune pairs that can not possibly be within  $r_{max}$ . If we impose a 3-d grid, with cell-size  $r_{max}$ , then two points separated by more than one cell size  $(r_{max})$  in any one dimension can not be within  $r_{max}$  of each other (see Fig. 1 for a 2-D representation). Thus, given one point which is the target galaxy and a grid with cell-size  $r_{max}$ , immediately allows us to prune all of the points that are not within 1 cell offset in each dimension. However, even with this pruning, the actual implementation of the algorithm matters. For instance, the non-AVX version of the codes tend to run  $2-3\times$  slower than the AVX version.

# 4.2 How to Maintain Cache Locality within the Grid

For all pairs around a given target galaxy, we need to compute distances to all points within all neighbouring 3-d cells. We ensure that the particle locations are contiguous by moving them into the following C struct in the order in which they arrive.

**Listing 4.1** Definition of the cellarray structure. This structure contains the X/Y/Z positions of all the particles that are in one 3-D cell.

```
typedef struct{
  DOUBLE *x;
  DOUBLE *y;
  DOUBLE *z;
  int64_t nelements;
} cellarray;
```



**Figure 1.** A 2-D grid showing the bin-lattice partitioning scheme. The bigger square show the entire domain, the red circles show a random distribution of 100 particles. Let's say we want to compute all pairs for the target blue point, then we would only have to consider red points that are within one cell (the dark shaded region). A circle with radius  $r_{max}$  is also drawn to shown the actual pairs that will eventually count in the correlation function.

The code gridlink.c takes in an input list of 3 arrays X/Y/Z and grids them into a regular 3-D grid using the specified bins parameter max\_x\_size or max\_y\_size or max\_z\_size for the X/Y/Z axes respectively. <sup>6</sup> Once the number of grid cells along each axes has been determined, we allocate memory for the struct lattice. This struct lattice is a declared as an 1-D array; the conversion from the three indices in 3-D (ix,iy,iz) to a single index (index) happens through the last line in Listing 4.2. Such an 1-D array for struct lattice gives much better OpenMP scaling.

#### **Listing 4.2** Accessing as lattice[index] rather than lattice[ix][iy][iz].

```
int64_t totncells = nmesh_x * nmesh_y * nmesh_z;
cellarray *lattice = my_malloc(sizeof(cellarray), totncells);
int64_t *nallocated = my_malloc(sizeof(*nallocated), totncells);
int64_t index = ix*nmesh_y*nmesh_z + iy*nmesh_z + iz;
```

Now that we know the total number of cells in the entire domain, we need to allocated memory to store the particles in each cell. However, there is no way to know the exact number of particles in each cell without processing the entire data-set; so, we pre-allocate with an estimate of the expected number of particles from the volume of each 3-D cell (assuming a random distribution). Then, we can allocate memory for each of the X/Y/Z arrays inside each 3-D cell:

#### **Listing 4.3** Pre-allocating memory for the X/Y/Z arrays in struct cellarray.

```
for (int64_t index=0; index < totncells; index++) {
   lattice[index].x = my_malloc(sizeof(DOUBLE), expected_n);
   lattice[index].y = my_malloc(sizeof(DOUBLE), expected_n);
   lattice[index].z = my_malloc(sizeof(DOUBLE), expected_n);
   lattice[index].nelements=0;
   nallocated[index] = expected_n;
}</pre>
```

Here, nallocated is an array that keeps track of the amount of memory alread allocated for each cell. After this step, all cells have been allocated memory for expected\_n particles. Now, we can begin to process the individual particles and assigning them to the 3-D cells (if enough memory has already been allocated to assign the new particle).

#### **Listing 4.4** Assigning the particles to the struct cellarray in the cell.

```
for (int64_t i=0;i<np;i++) {
  ix=(int)((x[i]-xmin)*xinv);</pre>
```

<sup>&</sup>lt;sup>6</sup>In practice, the bins may be further subdivided using the corresponding bin refine factors. These bin refine factors seem to influence runtime the most, you should experiment with a few values of bin\_refine\_factor and zbin\_refine\_factor to see what produces the best runtimes for your typical scenario.

```
iy = (int)((y[i] - ymin) * yinv);
iz=(int)((z[i]-zmin)*zinv);
int64_t index = ix*nmesh_y*nmesh_z + iy*nmesh_z + iz;
if(lattice[index].nelements == nallocated[index]) {
  expected_n = nallocated[index] * MEMORY_INCREASE_FAC;
  lattice[index].x = my_realloc(lattice[index].x
     , sizeof(DOUBLE), expected_n, ''lattice.x'');
  lattice[index].y = my_realloc(lattice[index].y
     , sizeof(DOUBLE), expected_n,''lattice.y'');
  lattice[index].z = my_realloc(lattice[index].z
     , sizeof(DOUBLE), expected_n, ''lattice.z'');
  nallocated[index] = expected_n;
}
int64_t ipos=lattice[index].nelements;
lattice[index].x[ipos] = x[i];
lattice[index].y[ipos] = y[i];
lattice[index].z[ipos] = z[i];
lattice[index].nelements++;
```

The loop goes over all of the particles and calculates the corresponding 3-D cell indices — ix,iy,iz. With these 3 variables, the corresponding 1-D index, index, can be calculated. The next lines check (and reallocate memory, if necessary) to ensure that enough memory has been allocated to the struct lattice[index] to accommodate this new particle. The last 5 lines are simply assigning the particle into the appropriate struct lattice[index]. Once all the particles have been assigned, the cells contain contiguous X/Y/Z arrays describing the original particle distribution.

# 4.3 The Pair-Counting Algorithms

}

After running through gridlink, the particle distribution is stored in contiguous X/Y/Z inside the 1-D array of struct cellarray. To find all possible pairs, we first need to loop over all particles in the first data-set.

**Listing 4.5** Looping over all cells in the first data-set.

```
for (int64_t index1=0;index1<totncells;index1++) {
  const cellarray *first = &lattice1[index1];
  const DOUBLE *x1 = first->x;
  const DOUBLE *y1 = first->y;
  const DOUBLE *z1 = first->z;
```

Now, we have the target cell pointer and the associated x1/y1/z1 array pointers. Next, we need to get the indices for the neighbouring cells in 3-D. In order to do that, first the 1-D index, index1 needs to be converted into a set of three 3-D indices, ix, iy, iz. Listing 4.6 shows the conversion from the 1-D index to the corresponding 3-D indices.

**Listing 4.6** Reconstructing 3-D index for first cell in the first data-set.

```
const int iz = index1 % nmesh_z ;
const int ix = index1 / (nmesh_z * nmesh_y) ;
const int iy = (index1 - iz - ix*nmesh_z*nmesh_y)/nmesh_z ;
```

After executing the code segment in Listing 4.6, we have the full 3-D indices for the target cell. Now, we have to find all of the indices for the neighbouring cells that can potentially satisfy the  $r_{max}$  constraint. This requires considering all 3-D cells that are located within bin\_refine\_factor of the target cell (for each dimension). Since the target cell, first has a 3-D X index of ix, this means all cells that have X indices in the range ix  $\pm$  bin\_refine\_factor can potentially have pairs that satisfy the  $r_{max}$  constraint. However, in case of PERIODIC boundary conditions, we also have to ensure that the indices (and the actual particle positions) wrap around on the other side of the cube. Listing 4.7 shows how the looping over neighbouring cells is done for the X dimension. Similar segments follow in the actual code for the Y/Z dimensions.

**Listing 4.7** Looping over all the neighbouring cells and taking care of PERIODIC boundary conditions.

```
for(int iix=-bin_refine_factor; iix <= bin_refine_factor; iix++) {
   int iiix;
#ifdef PERIODIC

DOUBLE off_xwrap=0.0;
   if(ix + iix >= nmesh_x) {
      off_xwrap = -xdiff;
   } else if (ix + iix < 0) {
      off_xwrap = xdiff;
   }
   iiix=(ix+iix+nmesh_x)%nmesh_x;
#else
   iiix = iix+ix;
   if(iiix < 0 || iiix >= nmesh_x) {
      continue;
   }
#endif
   :
```

```
Similar chunks of code for Y/Z.

const int64_t index2 = iiix*nmesh_y*nmesh_z + iiiy*nmesh_z +
iiiz;
```

Once all of the three 3-D indices for the neighbouring cell has been determined, we can reconstruct the 1-D index, index2 for that cell. With this 1-D index, we can create a pointer, second, that contains the cellarray pointer to the neighbouring cell. In Listing 4.8, we show how the neighbouring cell and the associated x2/y2/z2 array pointers are defined.

**Listing 4.8** Dereferencing the pointers for the neighbouring (second) cell under consideration.

```
const cellarray *second = &lattice2[index2];
const DOUBLE *x2 = second->x;
const DOUBLE *y2 = second->y;
const DOUBLE *z2 = second->z;
```

At this point, we have a set of x1/y/1/z1 arrays with first->nelements elements representing the first data-set. We also have another set of x2/y2/z2 arrays with second->nelements elements representing the second data-set. Now, we have to compute all possible pair-wise separations between these two data-sets. We begin with a loop over the elements in first:

**Listing 4.9** Looping over all particles in the first cell and accounting for PERIODIC boundary conditions.

```
for(int64_t i=0;i<first->nelements;i++) {
   DOUBLE x1pos=x1[i];
   DOUBLE y1pos=y1[i];
   DOUBLE z1pos=z1[i];
#ifdef PERIODIC
   x1pos += off_xwrap;
   y1pos += off_ywrap;
   z1pos += off_zwrap;
#endif
```

If PERIODIC boundary conditions are enabled, then off\_xwrap, off\_ywrap and off\_zwrap have been declared and initialized in Listing 4.7. By wrapping the elements if the first data-set, we can avoid the wrapping operations in the j-loop over all particles in second.

**Listing 4.10** AVX intrinsics for looping over all particles in the second cell. PERIODIC boundary conditions have already been accounted for in x1pos,y1pos,z1pos variables.

```
const AVX_FLOATS m_x1pos = AVX_SET_FLOAT(x1pos);
const AVX_FLOATS m_y1pos = AVX_SET_FLOAT(y1pos);
const AVX_FLOATS m_z1pos = AVX_SET_FLOAT(z1pos);
```

```
int64_t j;
for(j=0;j<=(second->nelements-NVEC);j+=NVEC) {
  const AVX_FLOATS x2pos = AVX_LOAD_FLOATS_UNALIGNED(&x2[j]);
  const AVX_FLOATS y2pos = AVX_LOAD_FLOATS_UNALIGNED(&y2[j]);
  const AVX_FLOATS z2pos = AVX_LOAD_FLOATS_UNALIGNED(&z2[j]);

const AVX_FLOATS m_xdiff = AVX_SUBTRACT_FLOATS(m_x1pos,x2pos);
  const AVX_FLOATS m_ydiff = AVX_SUBTRACT_FLOATS(m_y1pos,y2pos);
  const AVX_FLOATS m_zdiff = AVX_SUBTRACT_FLOATS(m_z1pos,z2pos);
```

The three codes DD(r),  $\xi(r_p, \pi)$  and  $w_p(r_p)$  diverge somewhat after this point. For DD(r), we need to calculate the full 3-D separation, whereas for  $\xi(r_p, \pi)$  and  $w_p(r_p)$  the separation is the projected distance. I will discuss further implementations in the following sub-sections dedicated to each code.

#### **4.3.1** Pair-counting for DD(r)

Pair-counting for DD(r) is the most straight-forward. The squared 3-D separation, r2, is simply the sum of the squared differences in each X/Y/Z dimensions.

#### **Listing 4.11** Calculating squared separations in DD(r).

```
const AVX_FLOATS m_xdiff_sqr = AVX_SQUARE_FLOAT(m_xdiff);
const AVX_FLOATS m_ydiff_sqr = AVX_SQUARE_FLOAT(m_ydiff);
const AVX_FLOATS m_zdiff_sqr = AVX_SQUARE_FLOAT(m_zdiff);
const AVX_FLOATS m_xydiff_sqr_sum =
    AVX_ADD_FLOATS(m_xdiff_sqr,m_ydiff_sqr);
AVX_FLOATS r2 = AVX_ADD_FLOATS(m_zdiff_sqr,m_xydiff_sqr_sum);
```

Once all the NVEC separations have been computed, we use bit-masks to check if any separations fall within the range sqr\_rpmin and sqr\_rpmax. If not, we continue with the j-loop.

#### **Listing 4.12** Bit-masks in DD(r).

```
m_mask_left = AVX_COMPARE_FLOATS(r2,m_sqr_rpmax,_CMP_LT_OS);
if(AVX_TEST_COMPARISON(m_mask_left) == 0) {
   continue;
}

const AVX_FLOATS m_mask = AVX_BITWISE_AND(m_mask_left,
   AVX_COMPARE_FLOATS(r2, m_sqr_rpmin, _CMP_GE_OS));
if(AVX_TEST_COMPARISON(m_mask) == 0) {
   continue;
```

```
}
r2 = AVX_BLEND_FLOATS_WITH_MASK(m_sqr_rpmax, r2, m_mask);
m_mask_left = AVX_COMPARE_FLOATS(r2,m_sqr_rpmax,_CMP_LT_OS);
```

If the code reaches past this bit-mask section, then at least one separation is within range. In that case, we use the code in Listing 4.18 to update the npairs array (and the rpavg array if OUTPUT\_RPAVG is enabled).

#### 4.3.2 Pair-separations for the projected correlation functions $\xi(r_p, \pi), w_p(r_p)$

Listing 4.13 shows the squared distance calculation for  $\xi(r_p, \pi)$  and  $w_p(r_p)$ . r2 is simply the projected separation in the X-Y plane.

### **Listing 4.13** Calculating squared separations in $\xi(r_p, \pi)$ and $w_p(r_p)$ .

```
const AVX_FLOATS m_xdiff_sqr = AVX_SQUARE_FLOAT(m_xdiff);
const AVX_FLOATS m_ydiff_sqr = AVX_SQUARE_FLOAT(m_ydiff);
AVX_FLOATS r2 = AVX_ADD_FLOATS(m_xdiff_sqr,m_ydiff_sqr);
```

### **4.3.3** Pair-counting for $\xi(r_p, \pi)$

### **Listing 4.14** Bit-masks in $\xi(r_p, \pi)$ .

```
const AVX_FLOATS m_mask_pimax =
   AVX_COMPARE_FLOATS(m_zdiff,m_pimax,_CMP_LT_OS);
const int test = AVX_TEST_COMPARISON(m_mask_pimax);
if(test == 0) {
  continue;
}
const AVX_FLOATS m1 =
   AVX_COMPARE_FLOATS(r2, m_sqr_rpmin, _CMP_GE_OS);
r2 = AVX_BLEND_FLOATS_WITH_MASK(m_sqr_rpmax,r2,m_mask_pimax);
m_mask_left = AVX_COMPARE_FLOATS(r2,m_sqr_rpmax,_CMP_LT_OS);
const AVX_FLOATS m_mask = AVX_BITWISE_AND(m1,m_mask_left);
int test1 = AVX_TEST_COMPARISON(m_mask);
if(test1 == 0) {
  continue;
}
m_zdiff = AVX_BLEND_FLOATS_WITH_MASK(m_pimax, m_zdiff, m_mask);
#ifdef OUTPUT_RPAVG
union_mDperp.m_Dperp = AVX_SQRT_FLOAT(r2);
```

```
#endif
union_pibin.m_ibin =
    AVX_TRUNCATE_FLOAT_TO_INT(AVX_MULTIPLY_FLOATS(m_zdiff,m_inv_dpi));
```

In the  $\xi(r_p, \pi)$  code, we have to update a two dimensional npairs  $(r_p, \pi)$  array. This means we can not directly update the npairs matrix and instead have to use a separate loop (this loop is typically only invoked for DD(r) and  $w_p(r_p)$  when OUTPUT\_RPAVG is enabled). As a result of this extra loop,  $\xi(r_p, \pi)$  is  $2-3\times$  slower than DD(r) and  $w_p(r_p)$ .

### **Listing 4.15** Updating the npairs matrix in $\xi(r_p, \pi)$ .

```
for(int jj=0; jj < NVEC; jj++) {
  int rpbin = union_rpbin.ibin[jj];
  int pibin = union_pibin.ibin[jj];
  int ibin = rpbin*(npibin+1) + pibin;
  npairs[ibin]++;
#ifdef OUTPUT_RPAVG
  rpavg [ibin] += union_mDperp.Dperp[jj];
#endif
}</pre>
```

### 4.3.4 Pair-counting for $w_p(r_p)$

Since the pair-counting in  $w_p(r_p)$  always assumes PERIODIC boundary conditions and only computes an auto-correlation, extra optimizations are possible in the  $w_p(r_p)$  calculation. First, each individual cell in the struct lattice elements are sorted based on their Z arrays. The X/Y arrays are also re-ordered simultaneously. Once all the Z values inside a cell have been sorted, we can avoid double-counting the pairs by changing the iiz loop to be:

**Listing 4.16** Optimizing the loop over neighbouring cells z in  $w_p(r_p)$ .

```
for(int iiz=0;iiz<=zbin_refine_factor;iiz++)
instead of
for(int iiz=-zbin_refine_factor;iiz<=zbin_refine_factor;iiz++)</pre>
```

Another advantage of sorting the Z values is earlier termination inside the actual calculation. The Listing 4.17 shows how to break early from the j-loop. Since the z2 values are always stored in increasing order, if all values of zdiff:=z2[j:j+NVEC-1]-z1 are greater than  $\pi_{\text{max}}$ , then none of the zdiff values in future iterations of the j-loop can be smaller than  $\pi_{\text{max}}$ . When the code encounters such a scenario, it updates the j variable to second->nelements to ensure that the serial section of the code is not executed and breaks out the AVX j-loop.

**Listing 4.17** AVX intrinsics for calculating separations in  $w_p(r_p)$  and checking for early termination.

```
const AVX_FLOATS m_zdiff =
    AVX_SUBTRACT_FLOATS(m_z2,m_zpos);//z2[j:j+NVEC-1] - z1
AVX_FLOATS m_mask_pimax =
    AVX_COMPARE_FLOATS(m_zdiff,m_pimax,_CMP_LT_OS);
const int test = AVX_TEST_COMPARISON(m_mask_pimax);
if(test == 0) {
    j = second->nelements;
    break;
}
```

### 4.4 AVX intrinsics to update the npairs histogram

This section explains the AVX intrinsics used to update the pair-counts histogram, npairs.<sup>7</sup> If the code execution reaches this loop, at least one (squared) pair separation falls within the range sqr\_rpmin and sqr\_rpmax, where sqr\_rpmin is the squared lower radial limit of the first bin and sqr\_rpmax is the squared upper limit of the last bin (equivalent to  $r_{max}$ <sup>2</sup> in this user-guide). Since the pairs are more likely to occur in the largest separation bins, the loop goes backwards from the last bin to the first and uses early loop-termination in case all possible pairs have already been accounted for.

**Listing 4.18** AVX intrinsics for updating the npairs histgram for DD(r) and  $w_p(r_p)$ .

```
for(int kbin=nrpbin-1;kbin>=1;kbin--) {
  const AVX_FLOATS m1 =
     AVX_COMPARE_FLOATS(r2,m_rupp_sqr[kbin-1],_CMP_GE_OS);
  const AVX_FLOATS m_bin_mask = AVX_BITWISE_AND(m1,m_mask_left);
  m_mask_left =
     AVX_COMPARE_FLOATS(r2,m_rupp_sqr[kbin-1],_CMP_LT_OS);
                  = AVX_TEST_COMPARISON(m_bin_mask);
  const int test2
  npairs[kbin] += AVX_BIT_COUNT_INT(test2);
#ifdef OUTPUT_RPAVG
  m_rpbin = AVX_BLEND_FLOATS_WITH_MASK(m_rpbin,m_kbin[kbin],
     m_bin_mask);
#endif
  const int test3 = AVX_TEST_COMPARISON(m_mask_left);
  if(test3 == 0) break;
}
```

<sup>&</sup>lt;sup>7</sup>The thread-local version in  $w_p(r_p)$  is called local\_npair.

Note that rupp\_sqr (and its AVX equivalent, m\_rupp\_sqr) contains the squared upper limits for the bins. Thus, when considering bin kbin, m\_rupp\_sqr[kbin-1] gives the squared lower radial limit for the bin while m\_rupp\_sqr[kbin] gives the squared upper limit for bin kbin. Here, m1 is the mask that contains all separations that satisfy r2 > rupp\_sqr[kbin-1], while the mask m\_mask\_left contains those squared separations that satisfy r2 < rupp\_sqr[kbin]. Note, that m\_mask\_left is either computed before entering the kbin loop or during a previous iteration of the same kbin loop. The AVX variable m\_bin\_mask then contains the bitwise and of m1 and m\_mask\_left - the mask for the squared separations that fall into kbin. The variable test2 contains an integer composed of the upper set-bits of the mask m\_bin\_mask - thus, contains only 4/8 useful bits for float/double precision calculations respectively. The npairs pair-counts is then updated using a hardware popent instruction. The last two lines check if there are any more pairs left that satisfy the lower bin-ranges; if not, the loop is terminated with a break statement.

# 5 Calling the C Libraries

All of the correlation function codes create a corresponding static library rather than a dynamic/shared library. This was a design decision intended to minimize path-issues for the end-user. After the libraries have been created, it is fairly straightforward to use them in an external C/python code. Be absolutely sure to pass arrays for the correct type – float arrays if you did not use DOUBLE\_PREC (default) or double arrays if you did use DOUBLE\_PREC. Also, only include headers from the xi\_theory/include directory – those headers correspond to the actual static library. DO NOT include the header files from the xi\_of\_r/xi\_rp\_pi/wp directories – these headers do not contain the correct function signature for the compilation flags used to generate the static libraries.

# 5.1 C bindings

The examples contains the files run\_correlations.c that shows how to use the three types of correlation function libraries from C. Essentially, the process consists of including the appropriate header file and passing the arrays (of the correct float/double type) into the functions. Make sure to include the static library in the linking step to create a stand-alone executable (see the Makefile in the examples directory).

### **5.1.1 API** for DD(r)

The interface for the 3-D correlation function, DD(r), is through the countpairs function. Here is the corresponding function signature:

## **Listing 5.1** API for the 3-D DD(r).

results\_countpairs \* countpairs(

```
const int64_t ND1, const DOUBLE * const X1, const DOUBLE * const
    Y1, const DOUBLE * const Z1,
const int64_t ND2, const DOUBLE * const X2, const DOUBLE * const
    Y2, const DOUBLE * const Z2,
#ifdef USE_OMP
const int numthreads,
#endif
const int autocorr,
const char *binfile);
```

The parameters to the function are:

- ND1 number of elements in the first data-set.
- X1 the array of X-values in the first data-set.
- Y1 the array of Y-values in the first data-set.
- Z1 the array of Z-values in the first data-set.
- ND2 number of elements in the second data-set.
- X2 the array of X-values in the second data set.
- Y2 the array of Y-values in the second data set.
- Z2 the array of Z-values in the second data set.
- numthreads the number of threads to use (if USE\_OMP is enabled in common.mk).
- autocorr if an auto-correlation is being calculated (1 implies auto-correlation, flag is used for some runtime optimizations).
- binfile file name that contains the radial bins. See Section 3.2 for details on how to create this file.

The output from countpairs is contained in struct results\_countpairs. The structure definition is:

#### **Listing 5.2** Structure definition for the output of DD(r).

```
typedef struct{
  uint64_t *npairs;
  DOUBLE *rupp;
  DOUBLE *rpavg;
  int nbin;
} results_countpairs;

void free_results(results_countpairs **results);
```

The fields in the structure correspond to:

- npairs array containing the pair-counts.
- rupp array containing the upper limits of the bins. rupp[0] gives the lower-limit of the first radial bin.
- rpavg array containing the average value of the separations for all the pairs that fell into the bin. Will contain meaningful values if OUTPUT\_RPAVG is defined in common.mk; identically 0.0 otherwise.
- nbin the number of radial bins used. Note that the actual pair-counts are stored in the index range [1,nbin-1]. The zero'th bin contains garbage for all of the arrays in this struct results\_countpairs.

After the results structure has been used, use free\_results(&results\_countpairs) to free allocated memory.

#### 5.1.2 API for $\xi(r_p, \pi)$

The interface for the 2-D correlation function,  $\xi(r_p, \pi)$ , is through the countpairs\_rp\_pi function. Here is the corresponding function signature:

### **Listing 5.3** API for the 2-D $\xi(r_p, \pi)$

```
results_countpairs_rp_pi * countpairs_rp_pi(
const int64_t ND1, const DOUBLE *X1, const DOUBLE *Y1, const
   DOUBLE *Z1,
const int64_t ND2, const DOUBLE *X2, const DOUBLE *Y2, const
   DOUBLE *Z2,
#ifdef USE_OMP
const int numthreads,
#endif
const int autocorr,
const char *binfile,
const double pimax);
```

The parameters to the function are:

- ND1 number of elements in the first data-set.
- X1 the array of X-values in the first data-set.
- Y1 the array of Y-values in the first data-set.
- Z1 the array of Z-values in the first data-set.

- ND2 number of elements in the second data-set.
- X2 the array of X-values in the second data set.
- Y2 the array of Y-values in the second data set.
- Z2 the array of Z-values in the second data set.
- numthreads the number of threads to use (if USE\_OMP is enabled in common.mk).
- autocorr if an auto-correlation is being calculated (1 implies auto-correlation, flag is used for some runtime optimizations).
- binfile file name that contains the radial bins. See Section 3.2 for details on how to create this file.
- pimax the maximum line-of-sight distance (assumed to be the Z axis) to use.

The output from countpairs\_rp\_pi is contained in struct results\_countpairs\_rp\_pi. The structure definition is:

### **Listing 5.4** Structure definition for the output of $\xi(r_p,\pi)$

```
typedef struct{
  uint64_t *npairs;
DOUBLE *rupp;
DOUBLE *rpavg;
DOUBLE pimax;
int nbin;
int npibin;
} results_countpairs_rp_pi;
```

The fields in the structure correspond to:

- npairs array containing the pair-counts. Number of elements in the array is (npibin+1)×(nbin+1)
- rupp array containing the upper limits of the bins. rupp[0] gives the lower-limit of the first radial bin. Number of elements in the array is nbin.
- rpavg array containing the average value of the separations for all the pairs that fell into the bin. Will contain meaningful values if OUTPUT\_RPAVG is defined in common.mk; identically 0.0 otherwise. Number of elements in the array is (npibin+1) × (nbin+1).
- pimax the maximum line-of-sight distance used in the bins.

- nbin the number of radial bins used. Note that the actual pair-counts are stored in the index range [1,nbin-1]. The zero'th bin contains garbage for all of the arrays in this struct results\_countpairs\_rp\_pi.
- npibin the number of  $\pi$  bins used. The total number of elements in the arrays in the struct countpair\_rp\_pi is (npibin+1)×(nbin+1). As usual, meaningful data is only contained in the radial bin range [1,nbin-1].

After the results structure has been used, use free\_results\_rp\_pi(&results\_countpairs\_rp\_pi) to free allocated memory.

### 5.1.3 API for $w_p(r_p)$

The interface for the projected correlation function,  $w_p(r_p)$ , is through the countpairs\_wp function. The code always uses PERIODIC boundary conditions, irrespective of the settings in common.mk. Here is the corresponding function signature<sup>8</sup>:

#### **Listing 5.5** API for the $w_p(r_p)$ .

```
results_countpairs_wp *countpairs_wp(
const int64_t ND1, DOUBLE * restrict X1, DOUBLE * restrict Y1,
    DOUBLE * restrict Z1,
const double boxsize,
#ifdef USE_OMP
const int numthreads,
#endif
const char *binfile,
const double pimax);
```

The parameters to the function are:

- ND1 number of elements in the data-set.
- X1 the array of X-values in the data-set.
- Y1 the array of Y-values in the data-set.
- Z1 the array of Z-values in the data-set.
- boxsize the boxsize that fully contains the X/Y/Z values.
- numthreads the number of threads to use (if USE\_OMP is enabled in common.mk).
- binfile file name that contains the radial bins. See Section 3.2 for details on how to create this file.

<sup>&</sup>lt;sup>8</sup>The X1/Y1/Z1 arrays are not declared with const qualifiers because I sort those arrays on Z in the countpairs\_wp function.

• pimax - the maximum line-of-sight distance (assumed to be the Z axis) to use.

The output from countpairs\_wp is contained in struct results\_countpairs\_wp. The structure definition is:

### **Listing 5.6** Structure definition for the output of $w_p(r_p)$

```
typedef struct{
  uint64_t *npairs;
DOUBLE *wp;
DOUBLE *rupp;
DOUBLE *rpavg;
DOUBLE pimax;
int nbin;
} results_countpairs_wp;
```

The fields in the structure correspond to:

- npairs array containing the pair-counts. Number of elements in the array is nbin.
- wp array containing the actual wp values.
- rupp array containing the upper limits of the bins. rupp[0] gives the lower-limit of the first radial bin. Number of elements in the array is nbin.
- rpavg array containing the average value of the separations for all the pairs that fell into the bin. Will contain meaningful values if OUTPUT\_RPAVG is defined in common.mk; identically 0.0 otherwise. Number of elements in the array is nbin.
- pimax the maximum line-of-sight distance used in the bins.
- nbin the number of radial bins used. Note that the actual pair-counts are stored in the index range [1,nbin-1]. The zero'th bin contains garbage for all of the arrays in this struct results\_countpairs\_wp.

After the results structure has been used, use free\_results\_wp(&results\_countpairs\_wp) to free allocated memory.

# 5.2 Python Bindings

The python\_bindings directory contains python bindings for python 2.x. Note that python3 is not supported out of the box<sup>9</sup>. If all went well, then typing python call\_correlation\_functions.py should run the example python code. If you get an error (and you are on a MAC), then refer

<sup>&</sup>lt;sup>9</sup>In the future, I might switch to cython to cover both python2 and python3

to Section 2.5 or the FAQ. If you edit the common.mk file and compile for double precision arithmetic, then be sure to change the line dtype=np.float32 to dtype=np.float64. Otherwise, you will get a TypeError at runtime.

# 6 Benchmarks & Scaling

In this section we present the runtimes and scalings for different number of particles,  $r_{max}$  and OpenMP threads for the codes. For all of the scaling tests, only an auto-correlation calculation was used and the fiducial catalog contains  $\sim 1.2$  million galaxies on a periodic cube of side  $420~h^{-1}Mpc$ .

### 6.1 Scaling with Number of Particles

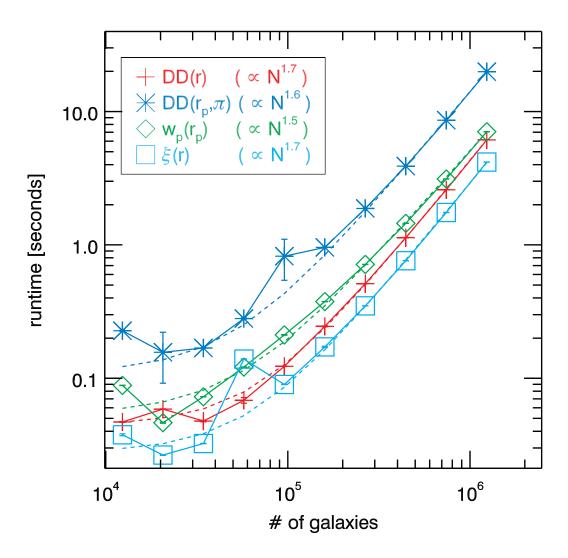
In Fig. 2, we show the scaling for the three codes with the number of particles. For this scaling, we subsampled the fiducial mock to attain 10 logarithmic steps in particle number ranging from  $1.2 \times 10^4$  to  $1.2 \times 10^6$ . All the timings are generateed using 1 thread.

### 6.2 Scaling with $r_{max}$

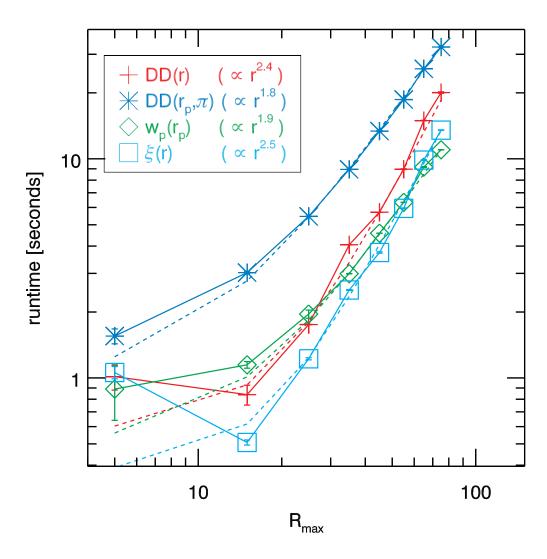
The code runtime increases drastically as the largest requested separation,  $r_{max}$  increases. Roughly speaking, the runtimes scale as  $\mathcal{O}(r_{max}^2)$  with DD(r) showing the strongest dependence on  $r_{max}$ . This is from the  $\pi_{max}$  dependence of  $\xi(r_p, \pi)$  and  $w_p(r_p)$ . Even when  $r_{max}$  is large, the effective number of particles per cell only grows as  $r_{max}^2$  and not  $r_{max}^3$  (as it does for DD(r)). If we extend the benchmarks to larger  $r_{max}$ , we will see a  $\mathcal{O}(r_{max}^3)$  dependence for

# 6.3 Scaling with OpenMP threads

All of the codes presented here scale reasonably well (efficiency  $\gtrsim 80\%$ ) up to 10 OpenMP threads. Beyond that, the work-load is scaling efficiency starts dropping off and plateaus for nthreads  $\gtrsim 20$ .



**Figure 2.** Scaling with particle number for DD(r),  $\xi(r_p, \pi)$ ,  $w_p(r_p)$ . The timings are obtained using 1 OpenMP thread.



**Figure 3.** Scaling with  $r_{max}$  for DD(r),  $\xi(r_p, \pi)$ ,  $w_p(r_p)$ . The timings are obtained with 4 OpenMP threads.

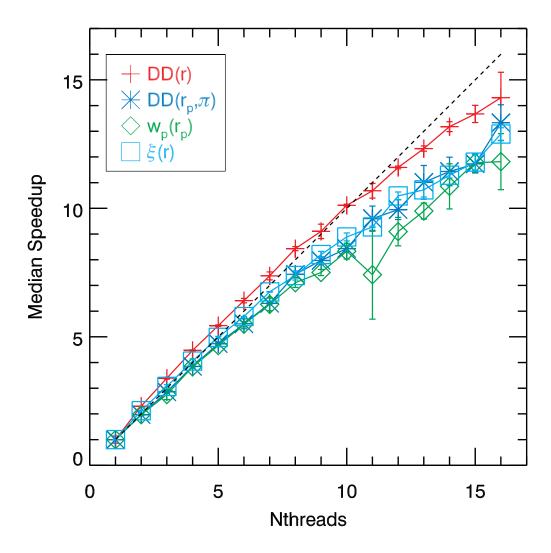


Figure 4. OpenMP scaling for DD(r),  $\xi(r_p, \pi)$ ,  $w_p(r_p)$ . The fiducial mock used here contains  $\sim 10^6$  particles in a 420.0  $h^{-1}Mpc$  cube.

**Table II.** OpenMP scaling for the three codes. Efficiencies are defined as Speedup/Nthreads. Note, that DD(r) has super-linear scaling with nthreads up to  $\sim$  8 threads.

Nthreads	$\operatorname{Efficiency}[\%]$										
	$\overline{DD(r)}$	$\xi(r_p,\pi)$	$w_p(r_p)$	$\xi(r)$							
1	100	100	100	100							
2	115	98	98	106							
3	113	95	91	102							
4	111	96	95	101							
5	108	94	93	99							
6	106	91	91	96							
7	105	90	89	96							
8	105	92	88	92							
9	101	88	83	91							
10	101	84	83	88							
11	97	87	67	84							
12	96	82	75	87							
13	94	84	76	82							
14	94	81	77	80							
15	91	78	78	78							
16	89	83	73	80							

# 7 Extending the Code

### 7.1 Different Type of Input Data File

All of the codes use io.c in the io sub-directory to read-in the data. If you want to specify a different file format, the easiest way would be to edit io.c. Decide on the file format code and add another strncmp case in io.c. Remember that the x/y/z are declared as void pointers, so you can not directly reference the x/y/z pointers. If you do add support for a different file-type, please submit a pull request and I will be happy to merge it into the code-base.

### 7.2 Computing a different type of correlation function

Let's say, you want to compute a marked correlation function. Now, you will need to read-in/create the marks for each individual point. Here are the steps you will need to create your custom correlation function code:

- 1. Add the data fields into the cellarray structure definition (see Listing 4.1.
- 2. Add in the memory allocation for the fields in gridlink.c after the malloc for X/Y/Z pointers (see Listing 4.3).
- 3. Extend gridlink.c to accept additional arrays and assign those arrays into struct lattice (see Listing 4.4).
- 4. Enable OUTPUT\_RPAVG and DOUBLE\_PREC (this is not required, but probably the easiest way to create a custom correlation function calculation).
- 5. Declare and zero-initialize a results array that will contain your custom correlation function. Follow the implementation in the code for calculating rpavg.
- 6. Add in the AVX arrays that load your custom data fields in the j loop in the countpairs\* functions.
- 7. Add your custom correlation function weight into the results array. Combine thread-local arrays into a global one in case USE\_OMP is selected.
- 8. Add the custom correlation function field to the corresponding struct results\_countpairs\*. Assign the results array into the struct results\_countpairs\*.
- 9. Add a call to free(your field) in the corresponding function free\_results\_countpairs\*.

### 7.3 Using SSE instead of AVX

If your CPU is too old and does not support AVX, then you can still use SSE instrinsics to compute the correlation functions. However, this will require replacing all of the AVX sections with corresponding SSE intrinsics. Email me and I will guide you through the conversion process.

#### 8 License

The code has been released under the MIT License.

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