

Link to Mathematica .nb file

Definitions

The proof is mostly in <http://mathworld.wolfram.com/Circle-CircleIntersection.html>

We take $R_1 = 1$ and $d = b$. The sine of the angle λ is therefore just $\frac{x}{R_1} = x = \frac{1-r^2+b^2}{2b}$, so

$$\lambda = \text{ArcSin}\left[\frac{1-r^2+b^2}{2b}\right]$$

The sine of the angle $-\phi$ is then $\frac{b-x}{r} = -\frac{1-r^2-b^2}{2br}$, so

$$\phi = \text{ArcSin}\left[\frac{1-r^2-b^2}{2br}\right].$$