

Naive Bayes Classifier

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i am luis serrano and this video is
about the naive

Spam Detector



“Buy”

25 Spam



75 No spam



so there's five so let's forget about
all the others and just

Spam Detector



“Buy”

Spam



80%

No spam



20%

Quiz: If an e-mail contains the word “buy”, what is the probability that it is spam?

- 40%
- 60%
- 80%
- 100%

Solution:
80%

probability is gonna be 80 percent that it's spam if it contains

Spam Detector



“Cheap”

Spam



No spam



be in 15 of them and from the non-spam
ten of them !

Bayes Theorem



“Cheap”

Spam



60%

No spam



40%

Quiz: If an e-mail contains the word “cheap”, what is the probability that it is spam?

- 40%
- 60%
- 80%
- 100%

Solution:
60%

split and therefore the solution is 60%
so

Spam Detector



“Buy” and “Cheap”

Spam



No spam



the words buy and cheap so that's some
good data and

Spam Detector



“Buy” and “Cheap” → 100% ?

Spam



100%

No spam

0%

Quiz: If an e-mail contains the words “buy” and “cheap”, what is the probability that it is spam?

- 40%
- 60%
- 80%
- 100%

Solution:
100%

right well maybe you're being skeptical like

Spam Detector



100 e-mails

5 “Buy”

10 “Cheap”

would contain the words buy and cheap so
let's think 5 out of 100 is

Spam Detector



100 e-mails

5 “Buy”

10 “Cheap”

5% “Buy”

10% “Cheap”

0.5% “Buy” and “Cheap”

Spam Detector

Spam



25 e-mails

20 "Buy"

15 Cheap

4/5 → 12/25
3/5

Spam Detector

Spam



25 e-mails

20 “Buy”

15 Cheap

$$\frac{4}{5} \rightarrow \frac{12}{25} \times 25 = 12 \text{ “Buy” and “Cheap”}$$

$\frac{3}{5}$

Spam Detector

No spam



75 e-mails

5 "Buy"

10 "Cheap"

$\frac{1}{15}$

$$\frac{1}{15} \rightarrow \frac{2}{225} \times 75 = \frac{2}{3} \text{ "Buy" and "Cheap"}$$

Spam Detector



“Buy” and “Cheap”

Spam

No spam

Quiz: If an e-mail contains the words “buy” and “cheap”, what is the probability that it is spam?



12



2/3

94.737%

$$\frac{12}{12 + 2/3} = \frac{36}{38}$$

$$= 94.737\%$$

Naive Bayes

| | Spam | | No spam | |
|-------------|------|-------|---------|-------|
| Total | 25 | | 75 | |
| Buy | 20 | 4/5 | 5 | 1/15 |
| Cheap | 15 | 3/5 | 10 | 2/15 |
| Buy & Cheap | 12 | 12/25 | 2/3 | 2/225 |

Naive Bayes

| | Spam | | No spam | |
|-------------|------|-------|---------|-------|
| Total | 25 | | 75 | |
| Buy | 20 | 4/5 | 5 | 1/15 |
| Cheap | 15 | 3/5 | 10 | 2/15 |
| Buy & Cheap | 12 | 12/25 | 2/3 | 2/225 |

$$\frac{12}{12 + 2/3} = \frac{36}{38} = 94.737\%$$

Bayes Theorem

S: Spam

H: Ham (not spam)

B: 'Buy'

$$P(S | B) = \frac{P(B | S) P(S)}{P(B | S) P(S) + P(B | H) P(H)}$$

Naive Bayes

$$P(\text{"Buy"} \& \text{"Cheap"}) = P(\text{"Buy"}) P(\text{"Cheap"})$$

$$P(B \cap C) = P(B) P(C)$$

↑
Naive

S: Spam

H: Ham (not spam)

B: 'Buy'

C: 'Cheap'

Naive Bayes

$$P(S | B \cap C) = \frac{P(B|S)P(C|S) P(S)}{P(B|S)P(C|S) P(S) + P(B|H)P(C|H) P(H)}$$

$$P(\text{spam if "Buy" \& "Cheap"}) = \frac{\frac{20}{25} \frac{15}{25} \frac{25}{100}}{\frac{20}{25} \frac{15}{25} \frac{25}{100} + \frac{5}{75} \frac{10}{75}}$$