

■ CRT Monitor (cathode ray tube) : —

The CRT is a vacuum tube that contains one or more electron guns. In these CRT there is a phosphorescent screen. And its use to display images it modulates, accelerates and deflects electron beam on to the screen to create the image, the image may be represent electrical wave form, pictures, radar targets or other phenomena.

In television sets and computer monitors the entire front area is scanned multiple times, and symmetrically in a fixed pattern called a raster . And image is produce by controlling the intensity of each of the 3- electron beams, 1 for each additive primary colour red, green and blue and with a video signal. In all modern CRT monitors and computers; And beams are bent by magnetic deflection. In a variety magnetic field generated by coils.

• CRT Resolution : — Dot pitch defines the maximum resolution of the display assuming delta gun CRTs.

1) What is Graphics?

→ Computer graphics is a branch of computer science that deal with images, figures, drawing and their analysis; Computer graphics mean drawing picture artificially by setting the pixels with different colour. For doing these, we need a lot of mathematical things.

2) How computer graphics is different from image processing?

→ It differs from image processing in the sense, image processing starts after the image is in the image space whereas computer graphics starts with the drawing of the object. Image processing generally means the pixel based operation on an already existing image and generate a new image.

3) How computer graphics is different from animation?

→ It differs from animation because animation starts with the motion of an image. The animation is very closely related with computer graphics. There are still few differences. Computer animation means generating graphical object in such a way that there is a motion in the picture sequence of picture generated by computer.

Graphics can generate a motion.

4 Discuss about different graphics hardware?
→ Softcopy display:-

• CRT (cathode ray tube):- It displays high quality images. It uses cathode ray to form generating picture monitors.

• HDTV:- High definition television uses very high technology and supports 60 Hz interlaced and non-interlaced high resolution display.

• plasma display:- It uses plasma gas discharge technique for display. In high voltage it dissociates gas and plasma is then used for display.

• LCD:- Liquid crystal display used liquid crystals for its display. The polarising characteristics of certain organic compound are to modify the characteristics of incident light in these way it displays a very high resolution picture.

■ Hardcopy output devices : —

- Electronic plotters : — plotter is use to print the output on a large page on sheet. It is specially used in engineering design.

- Printers : — It is the most popular hardcopy devices it's of two type one impact printer another is non impact printer.

■ Input devices : —

- Mouse : — It is specially use in windows environment it's also use to drawing.

- Joystick : — It is mainly use in game playing.

- Light pen : — It is use for graphics design.

■ Graphics software: — Graphics uses two types of software.

One is general purpose software written in high level programming language with graphics library function and example of graphics is open GL. These type of packages include basic function like straight line drawing, curve drawing etc. Exp — JAVA/C/C++.

Other is special purpose graphics software. Here user can generate graphics output easily. Here several ready-made option available. 'Autocad' is an example dedicated graphics software these use for engineering design.

Application of computer graphics?

(i) Computer Arts: — It is widely prints arts and modern commercial arts. Artists use several hardware and software packages to draw their picture then give the effects to their picture.

(ii) Entertainment: — computers are use to generating movies, cartoons etc, and now a days television shows, music videos are also use in Computer graphics.

(iii) Computer aided education: —

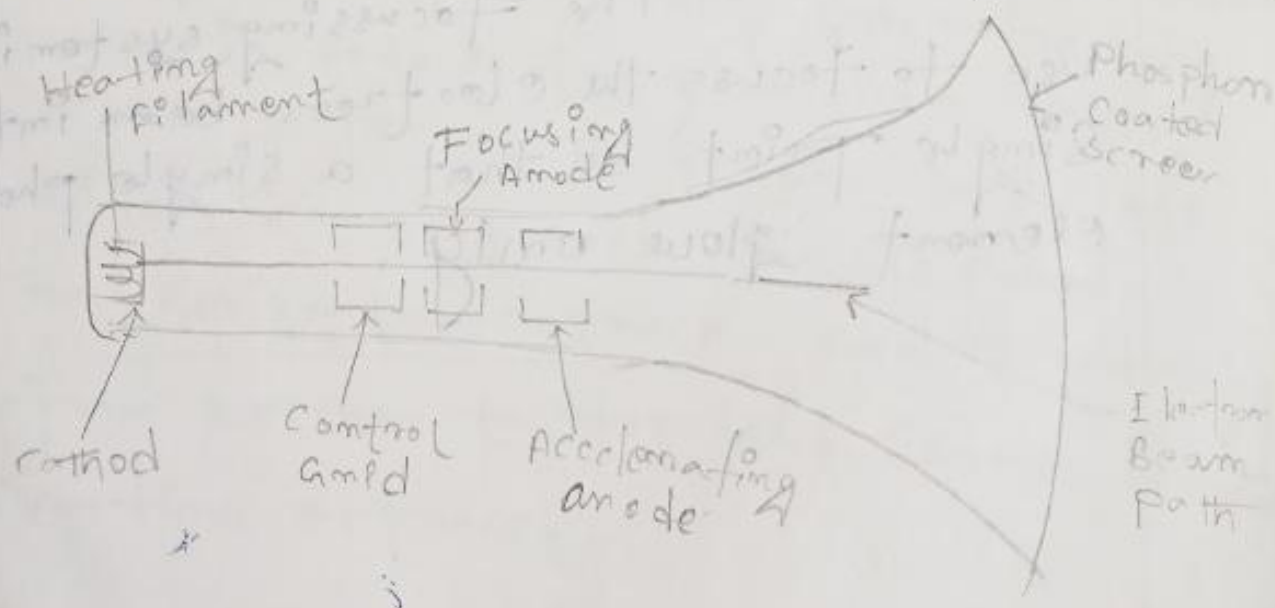
It generates models for different branches and train are use for education and training purpose.

Ex: — Biological structure, Plotting of graph etc.

(iv) GUI: — Computer graphics is use in computer for graphical user design. Multiple window, buttons, scroll bars, Combo box and tool bar are the example of Computer graphics.

■ Refresh Cathod Ray Tubes:-

The first monitor was made of refresh Cathod ray tube in these type of terminal an electron beam on Cathod ray is focussed on phosphor coated screen. Phosphor glows and emits a small spot of light when a large number of phosphor glows with different colors we see a picture on the screen. The phosphor fades very quickly so, one way to keep them glow for a long time is to redraw the picture repeatedly and very quickly by focussing the electron beam back over the same phosphor point. For these reason these type of CRT is called refresh CRT.



when heat is generated by the filament the cathode emits free negatively charged electrons towards the phosphor plate.

The tube is vacuum so, electrons move freely the focussing anode focuses the electron beam and accelerating anode accelerates the electron particle towards screen or phosphor plate by generating high positive voltages.

The intensity of the electron beam is controlled by the control grid which is a metal cylinder a negative voltage is applied to its control grid. The negative voltage of the control grid will decrease the no. of electrons on the electron beam.

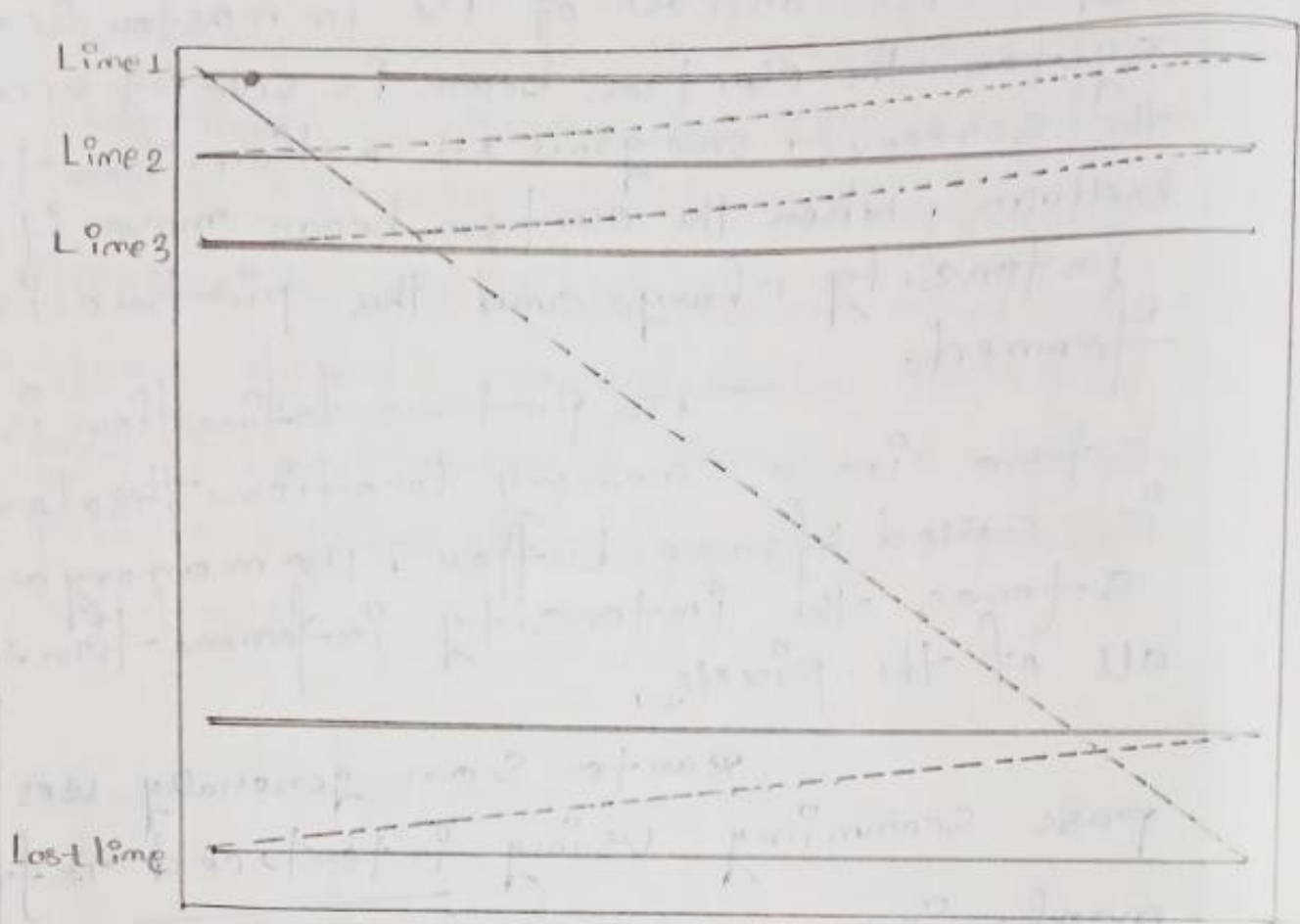
The focussing system is used to focus the electron beam into a single point so that a single phosphor element glows only.

■ Raster Scan CRT:- This is the most common type CRT in case of TV. In raster scan system the electron beam is swept across the screen, one row at a time from top to bottom. When the electron beam moves its intensity changes and the picture is formed.

The picture definition is stored in a memory location. This location is called frame buffer. The memory area stores the intensity information for all of the pixels.

Raster scan generally uses to pass scanning using interlaced refresh mechanism. In the first pass the ^{beam} sweeps every second line from the top to bottom to produce the half of the total picture. Then it draws the next line in the second pass. This improves the ~~second~~ image quality. Normally the refreshing rate is 60 to 80 frame/sec in a raster scan system. The return to the left after scanning each line is called horizontal retrace and returning from bottom to top left corner is called vertical retrace.

What do you mean



Electron beam

Horizontal deflection

Vertical deflection

Raster Scan CRT

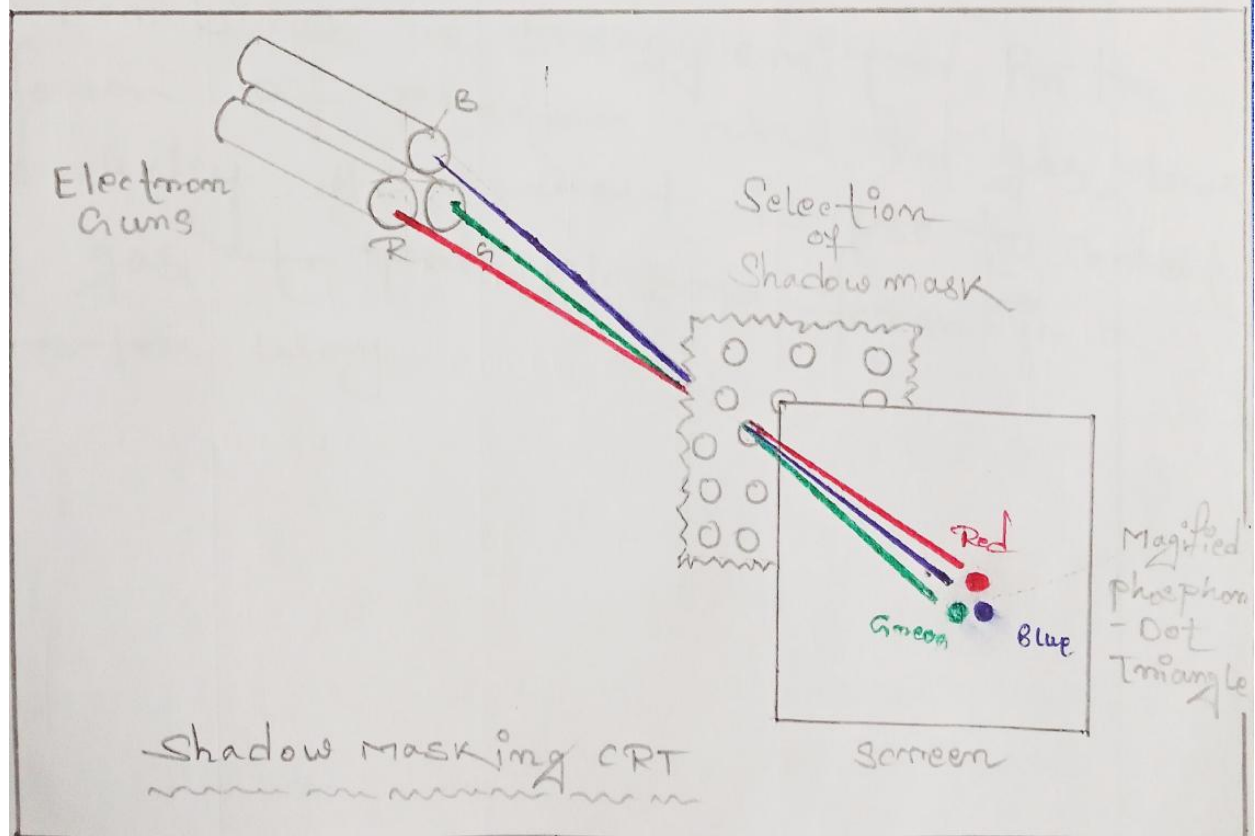
■ Briefly discuss about colour CRT monitor?

→ There are two methods for colour CRT —

• Beam penetration method! — In these method, two layers of phosphors are coated inside the CRT screen. One layer is an red phosphor and other is for green phosphor. When the electron beam falls on the phosphor, the colour of the pixel depends on the penetration power, of the electron beam. If the power of the electron beam is low then the beam can penetrate only the red layer and if the beam power is high the beam can reach to inner most green layer and excites the green phosphor. If the electron beam power is medium it shows the combination of red and green phosphor colour, generally orange and yellow. The electron beam power is controlled by controlling the voltage of electricity.

Shadow mask method! — These method has 3 phosphor colour dots at each pixel position. The 3 phosphor emits 3 different lights red, green and blue. This type of CRT has 3 electron guns one for red, one for green and one for blue dots. one grid with number of fine holes is placed just behind the phosphor coating. This grid plate is called Shadow mask. when 3 electron guns emits electron beams the beam is pass through a hole of shadow mask grid. The phosphor dots are arranged in such a way that the corresponding beams activated it's own dots. The dots are placed in triangular shaped is called delta arrangement. Following is the list of complete 8 colours.

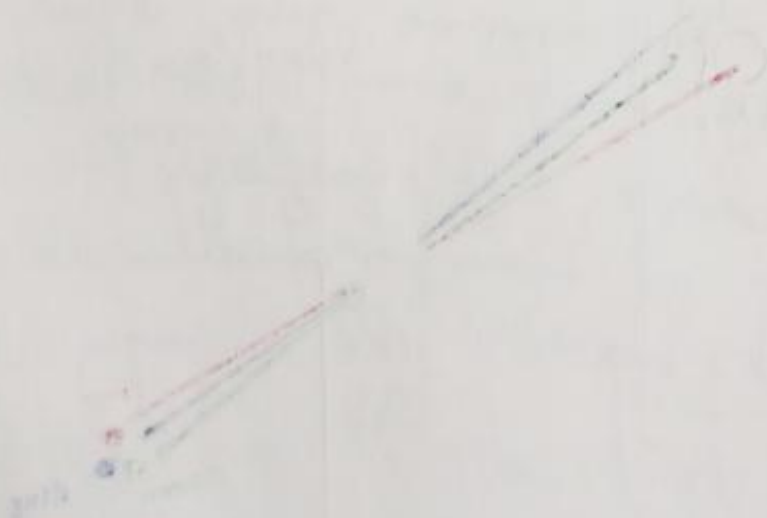
Red	Green	Blue	produced colour
off	off	off	Black
on	on	on	white
off	on	on	Cyan
on	off	on	Magenta
on	on	off	Yellow
on	off	off	Red
off	on	off	Green
off	off	on	blue



Total no. of colours that can be produce after combining 3 dot of different intensity is 256 for red dots \times 256 for green dot \times 256 for blue dot i.e.

$$256 \times 256 \times 256 = 2^8 \times 2^8 \times 2^8 = 2^{24}$$

So, approximately 17 million colours can be produced.



■ Plasma monitor:- It is also called plasma panel or gas discharge display. It is made of two glass plates to make a glass envelop. In these glass envelop there is matrix of cells each cell is filled with gas, the gas is generally inert gas. In general neon or neon argon mixture is placed, the gas is placed at low pressure in the cell. When high voltage is applied to the gas the electrons are stripped from the atom. These form of gas is called plasma, when electron recombines the energy emitted in the form of photon and the gas glows. Generally AC current is used to convert the gas to plasma form in a faster way.

■ LCD Monitor: — The LCD monitor are different from all the monitor types it does not emits light instead of passes the polarized light from the light sources through the LCD. This type of monitor uses a special type of liquid which molecules acts as crystals. It generally uses nematic liquid crystal compound. These liquid is placed between two glass plates. These glass plates have light polarizes at right angle to the ~~on~~ other plate one glass plate is made of a series of horizontal transparent conductors. The intersection of two conductors define a pixel position when power is applied the crystals are applied in such a way that light is not ~~&~~ twisted, so it will be reflected back to the viewers when no power is applied the crystals are ~~aline~~ in such a way that the light is reflected back to the viewer.

■ Printing Devices: — (Impact printer)

• Dot matrix printer → It is one of the oldest hardcopy design. In these of printer one printing head runs back forth from left side to the paper to right side. And inked ribbon is placed between the paper and the writing head. The head is populated with a number pins normally the no. of pin is 64. They form an 8x8 square matrix when a character need to be printed. Say for example A, some pins come forward and forms the pattern A, the head then harmonizes on the ribbon and the impression of A is printed on the paper. The head then moves to the right side and prints the next character in the same mechanism. As the pins strike the paper to print the impression. These printers are often called impact printer. The printing quality is very poor but it cheaper.

Inkjet printer: (Non Impact printer)

It is used to print high quality graphics. Here head is made with several tiny nozzles, behind the nozzles, there are tiny chambers of ink. These elements of ink are connected with ink reservoir. When a character is to be printed say for example some nozzles are selected; these nozzles form a pattern of A. Behind the nozzles there is a ink chamber. Heat is applied using the power of electricity stream explosion and the ink comes rapidly through the nozzle and falls on the paper. The vacuum chamber is now filled up by another drop of ink coming from the reservoir. These type of printer can produce finer and smoother details but it has its advantages too. Its printing cost is very high and it is not an impact printer, it can not produce carbon copy output. Also very thin nozzles are prone to clogging with dry ink.

- laser printer! — (Non impact printer)

It has 7 step working principal.

- Raster image processing! — Each horizontal strip across the page is called raster line, it uses the page description language to generate bit map of the page in the master ~~mem~~ memory.

- charging! — A wire, named as Corona wire projects an electrostatic charge on a revolving photo sensitive drum. This drum is capable of storing electrostatic charge on its surface is called photo resistor.

- Exposing: — A beam of laser is focus on the photo resistor through the photo ~~mirror~~ lenses. The stream of masterized data stored in the memory, ^{turns} ~~turns~~ the ^{laser} ~~laser~~ on ~~off~~ ^{on} to form the image pattern.

• Developing! — The surface of drum with image definition with charge and neutral is then expose to tonner.

Tonner is basically fine particles of dry plastic powder mixed with the black carbon, these tonner ~~are~~ -ve ly charge that it will not ~~change~~ the touch the +ve particles of the drum.

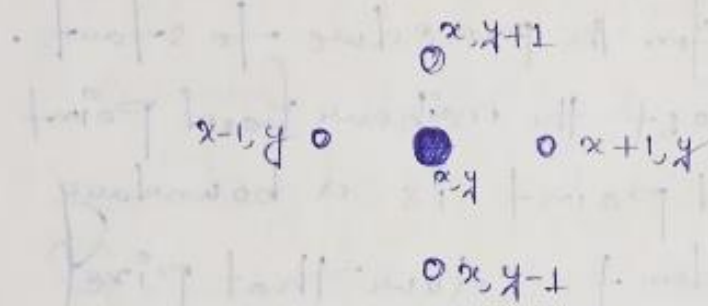
• Transfer! → photo receptor is pressed or rolled over paper to transfer the image on the paper.

• Fusing! → The paper then passes to rollers where heat and pressure bond the dry plastic powder to the paper permanently.

• Cleaning! → when the print is complete and electrically neutral soft blade cleans the excess tonner from the photo receptor drum and the discharge lamp removes the remaining charge from the drum.

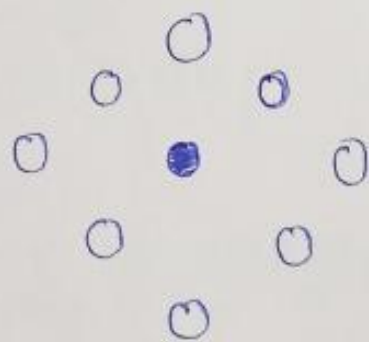
■ what do you mean by four Connected and eight Connected approach in filling algorithm

→ There are two ways in which pixels are considered to be connected, to one another, four Connected and eight Connected. In four Connected method pixel may have ^{upto} four neighbors



These are up, down, left, right; if the current pixel is (x, y) the neighbors are $(x, y+1)$, $(x, y-1)$, $(x-1, y)$, $(x+1, y)$

In eight Connected approach the pixel may have up to eight neighbors.



These are up, down, left, right and forth
Common points i.e. $(x, y-1)$, $(x, y+1)$,
 $(x+1, y)$, $(x-1, y)$, $(x-1, y-1)$, $(x-1, y+1)$,
 $(x+1, y+1)$, $(x+1, y-1)$.

Boundary fill algorithm: -

In case of boundary fill recursive algorithm takes an initial interior point (x, y) , for the procedure to start.

The procedure test the neighbourhood point. If neighbourhood point is a boundary pixel then we don't colour that pixel. Otherwise, the pixel are colour & will fill colour and any of the neighbour pixel is then chosen to continue the same process again and again.

The procedure stops when all pixel up to boundary are tested.



Boundaryfill (int x, int y, int fillcolour, int
boundary colour)

{

int colour = getpixel(x, y)

if (current colour \neq boundary colour &&

then : current colour \neq fill colour)

putpixel(x, y, fillcolour)

Boundaryfill(x+1, y, fillcolour, boundary colour)

Boundaryfill(x-1, y, fillcolour, boundary colour)

Boundaryfill(x, y+1, fillcolour, boundary colour)

Boundaryfill(x, y-1, fillcolour, boundary colour)

end if

}



■ Disadvantage of boundary fill algorithm:-

① These algorithm may not fill the region correctly, if some initial pixels had already be painted in the fill colour. If any point is encounter with the fill colour that recursive bound stops there and a part of the region may not be filled. To avoid these, one may change the colour of any initial point, if it is set to fill colour before applying these process.

② Another drawback of these algorithm is its extensive recursive function calls and therefore stacking of ~~no~~ neighbouring points. Points.



Flood Fill algorithm :-

when the boundary of a region is painted with several colours we cannot apply boundary fill algorithm, In these we apply flood fill algorithm. Here we take starting starting interior point then we check whether it has the old interior colour or not; If the answer is yes then we replace the old colour as fill colour and ~~for~~ consider all its neighbourhood points from the same procedure.

```
Flood Fill (int x, int y, int oldcolour, int  
            fill colour)
```

```
if (getpixel(x, y) == oldcolour) then  
    putpixel(x, y, fill colour)
```

```
    Flood Fill (x+1, y, oldcolour, fill colour)
```

```
    Flood Fill (x-1, y, oldcolour, fill colour)
```

```
    Flood Fill (x, y+1, oldcolour, fill colour)
```

```
    Flood Fill (x, y-1, oldcolour, fill colour)
```

```
end if
```

```
}
```

• Disadvantages!

① There is no stopping criteria for these algorithm for these reason colour may get ~~fall~~ flooded out side boundary.

② Extensive ~~to~~ recursive call.

■ what do you ^{mean by} aliasing effect?

→ we know that the lights, lines, geometric shape, colour boundary are continuous where as a raster device is a discrete one, for these reason the picture is distorted. These distortion is due to the under sampling there are various types of distortion these distortion are collectively called aliasing.

• unequal brightness

• A slanted line appears to be less bright ~~than~~ than a horizontal or vertical line.

There is because the slanted pixels are far apart than the horizontal and vertical pixel.

mapping of preotic figures:— In these case

we may also have understanding.

In case of preotic information we need the sampling frequency at least twice the highest frequency of the object, this is called Nyquist frequency.

■ 2D Transformation ■

The fundamental of all computer graphics is the manipulation of objects. These manipulation of several types, orientation, size, shape, main. These can be done by changing the co-ordinate description of the object. These alteration of the co-ordinate description is known as geometric transformation.

• Translation: — A translation is moving the object along a straight line from one location to another without changing the shape or direction. The distance between the old position of the object and the new position of the object is called translation distance.

Let (x, y) is the original co-ordinate of a point the object, Let the translation along the x axis is t_x and translation along y

axis is t_y . The new co-ordinate of that point (x', y') is —

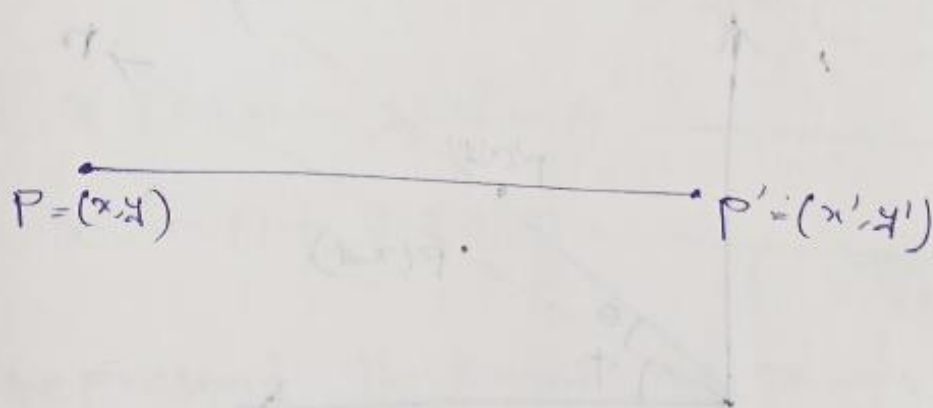
$$x' = x + t_x \quad \text{--- (i)}$$

$$y' = y + t_y \quad \text{--- (ii)}$$

The t translation distance pair (t_x, t_y) is called translation vector or shift vector and it's denoted by

~~T~~ T_v So, $P' = T_v + P$ where

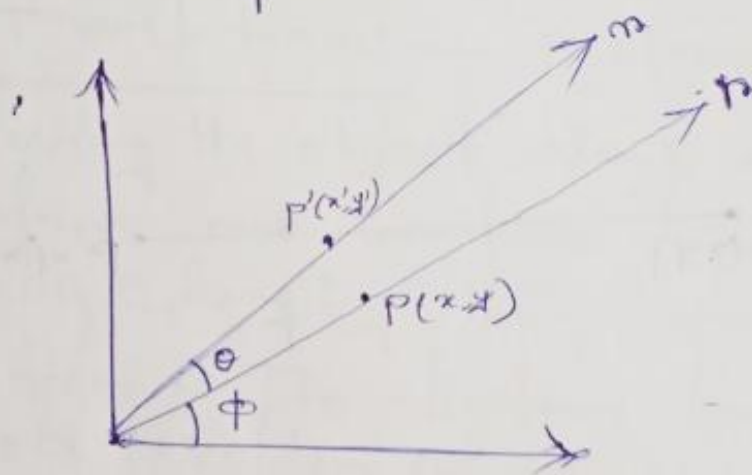
$$P' = (x', y'), \quad P = (x, y)$$



■ Rotation: — Rotation means motion ~~among~~ along its circular path without changing the ~~st~~ shape of the circular path.

(7) • Rotation about origin: —

we shall first take the origin as the pivot point and perform the transformation; let the angle of rotation of a point is θ . And originally made an angle ϕ with the origin.



Let, the old original ~~old~~ point is $P(x, y)$ and the change point is $P'(x', y')$. Also let the distance of the point from the origin (Pivot point) is r .

$$x' = r \cos(\theta + \phi) \quad \text{--- (i)}$$

$$y' = r \sin(\theta + \phi) \quad \text{--- (ii)}$$

$$\text{So, } x' = r \cos \theta \cos \phi - r \sin \theta \sin \phi$$

$$y' = r \sin \theta \cos \phi + r \cos \theta \sin \phi \quad \text{--- (iv)}$$

It is clear from the above picture,

$$x = r \cos \phi \quad \text{--- (v)}$$

$$y = r \sin \phi \quad \text{--- (vi)}$$

Putting the value of (v) and (vi) in the eqⁿ (iii) and (iv) we get

$$x' = x \cos \theta - y \sin \theta \quad \text{--- (vii)}$$

$$y' = x \sin \theta + y \cos \theta \quad \text{--- (viii)}$$

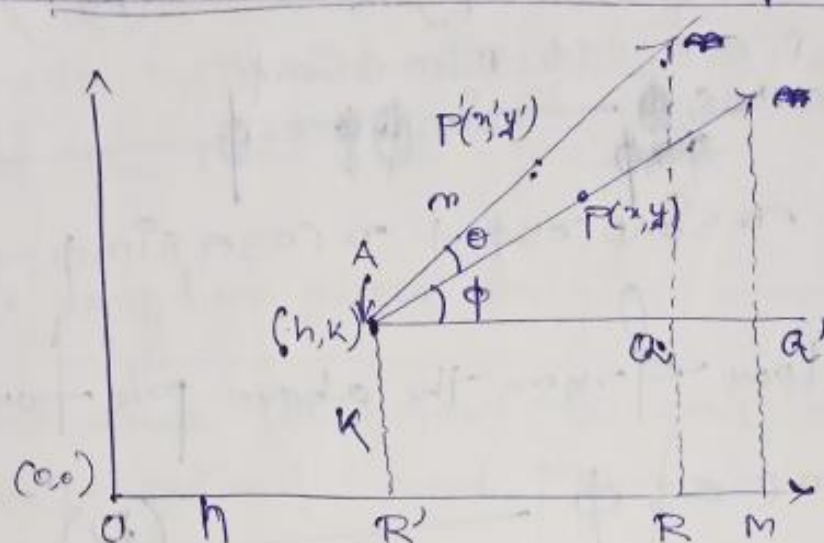
\therefore we represent the same as matrix form

$$P' = R(\theta) \cdot P$$

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

(16)

• Rotation about an arbitrary pivot point:-



We shall take an arbitrary point (h, k) as the pivot point.

Clearly from the figure $AQ = AP'$
 ~~$AP = AP'$~~

$$AQ = AP' \cos(\theta + \phi) \quad \text{--- (i)}$$

$$n \cos(\theta + \phi) \quad \text{--- (ii)}$$

$$\text{So, } OR = h + n \cos(\theta + \phi) \quad \text{--- (iii)}$$

$$x' = h + (n \cos \theta \cos \phi - n \sin \theta \sin \phi)$$

(iv)

$$\text{Similarly, } P'(x') = n \sin(\theta + \phi)$$

$$RP' = k + n \sin(\theta + \phi)$$

$$y' = k + (n \sin \theta \cos \phi + n \cos \theta \sin \phi)$$

(v)

Now from $\Delta PQ'$ triangle we get

$$AQ' = m \cos \phi$$

$$\therefore OM - OR' = m \cos \phi$$

$$\therefore (x - h) = m \cos \phi \quad \text{--- (vi)}$$

Similarly, $PQ' = m \sin \phi$

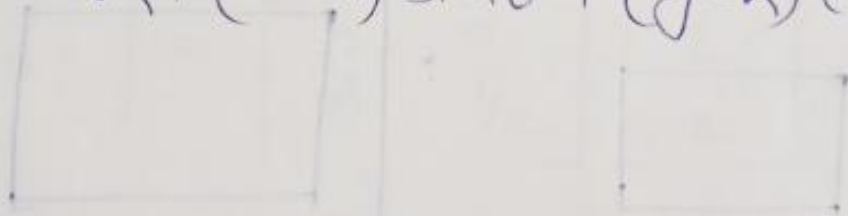
$$\therefore PM - Q'M = m \sin \phi$$

$$\therefore (y - k) = m \sin \phi \quad \text{--- (vii)}$$

Putting eqs. (6) and (7) in (5)
In eqs. (4) and (5) we get

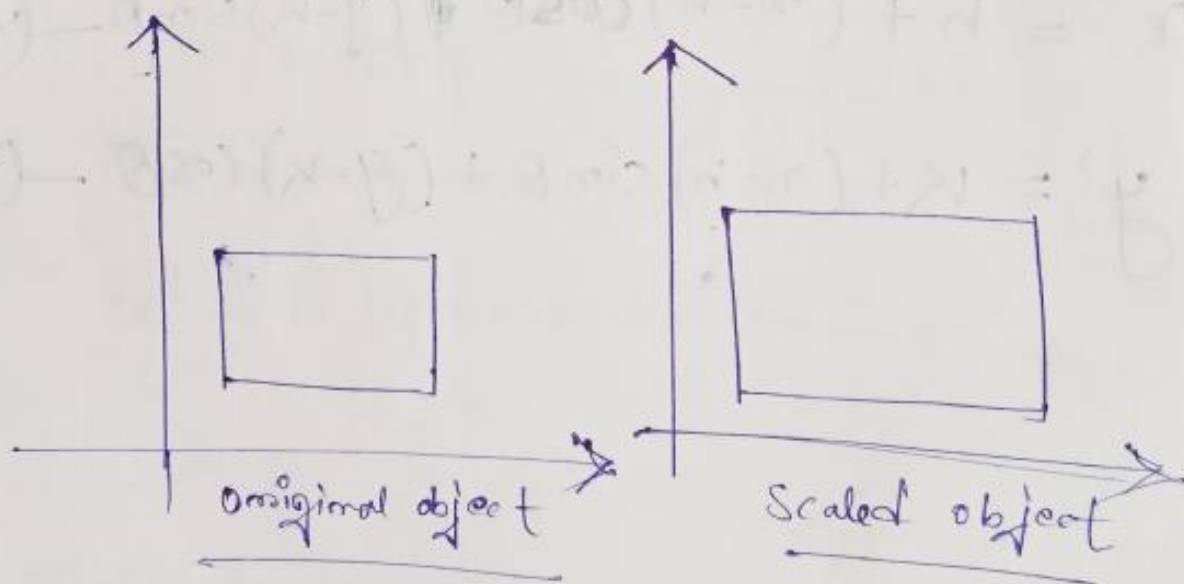
$$x' = h + (x - h) \cos \theta + (y - k) \sin \theta \quad \text{--- (viii)}$$

$$y' = k + (x - h) \sin \theta + (y - k) \cos \theta \quad \text{--- (ix)}$$



■ Scaling : \Rightarrow (18)

Scaling means changing the size of the object i.e. scaling means expanding ~~under line~~ and compressing the dimension of an object. The constants that decide the changes in dimension are called scaling factors. The scaling factors in x and y direction are known as S_x and S_y respectively. If the scaling factor is < 1 then the object will be compressed otherwise if it is > 1 then the object will be expanded.



Let $P(x, y)$ is the original point and the scaling factors along x and y are S_x and S_y . The point will be transformed to $P' = (x', y')$

where, $x' = S_x x$ ——— (i)

~~y'~~ $y' = S_y y$ ——— (ii)

$$\begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} S_x & 0 \\ 0 & S_y \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix}$$

~~for~~

Scaling matrix

■ What is reposition problem?

→ Consider the case of a straight line
Scaling with scaling factors $S_x = \frac{1}{2}$,
 $S_y = \frac{1}{2}$ where, the straight line is

perpendicular to x axis. Let the co-ordinates
of the end point P(2,2) and
Q(2,4)

The transformed point for P i.e.

$$P' = \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \frac{1}{2} & 0 \\ 0 & \frac{1}{2} \end{bmatrix} \begin{bmatrix} 2 \\ 2 \end{bmatrix}$$

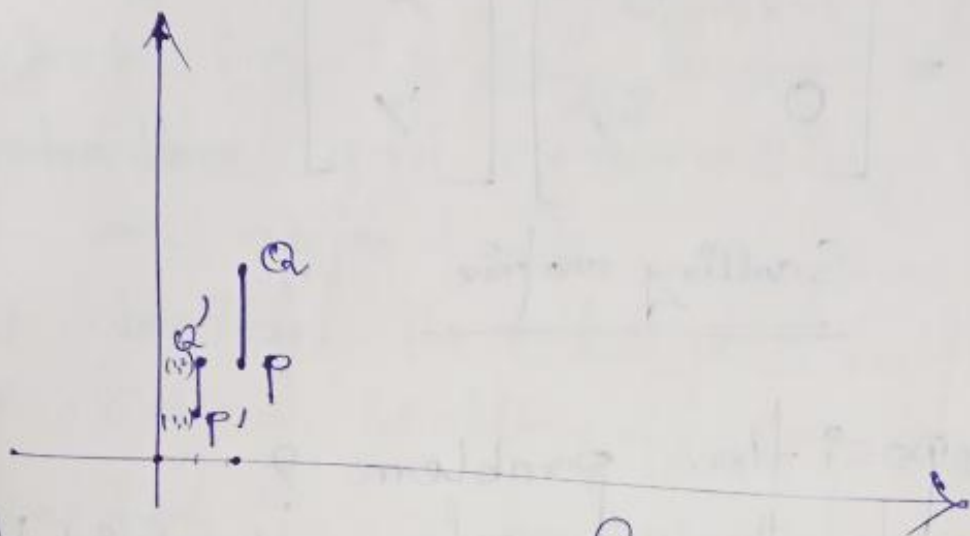
$$= \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Similarly, for Q point the changed location
is,

$$Q' = \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} \frac{1}{2} & 0 \\ 0 & \frac{1}{2} \end{bmatrix} \begin{bmatrix} 2 \\ 4 \end{bmatrix}$$

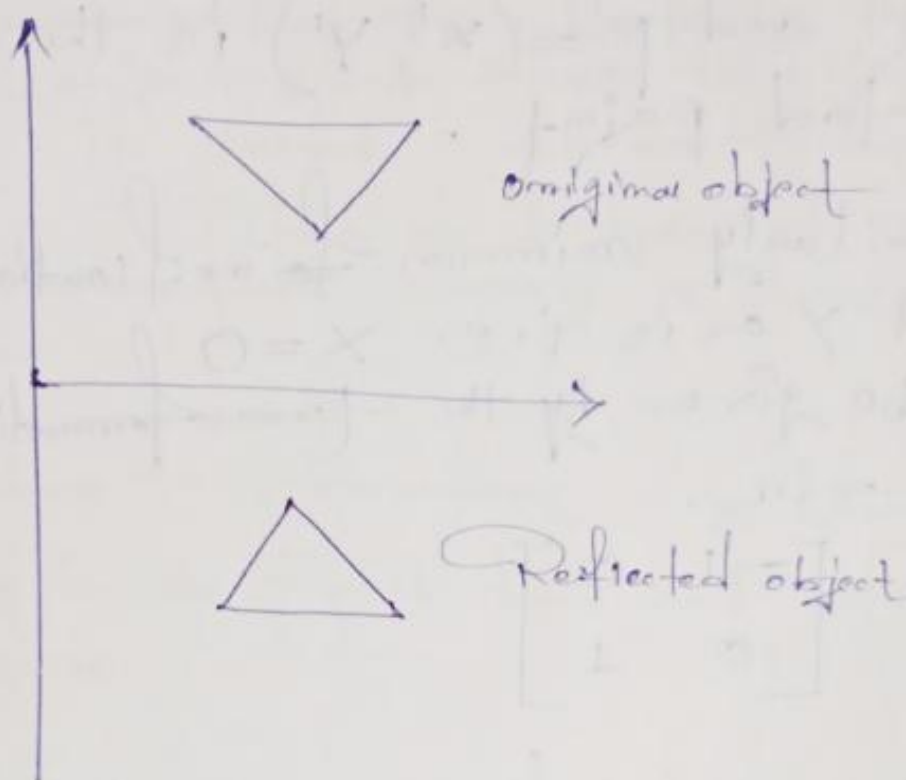
$$= \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

So, the new line ends points
are $(1, 1)$, $(1, 2)$



from the above figure it is clear
that the size of the straight line
is reduce if it is shifted towards
the origin. this is called
repositioning problem.

Mirror transformation:-



These transformation produces the mirror image of an object with respect to a given mirror axis. Reflexion means rotating the object 180° with respect to the mirror axis.

Reflexion about x-axis i.e. $y=0$ can be determined by transformation matrix

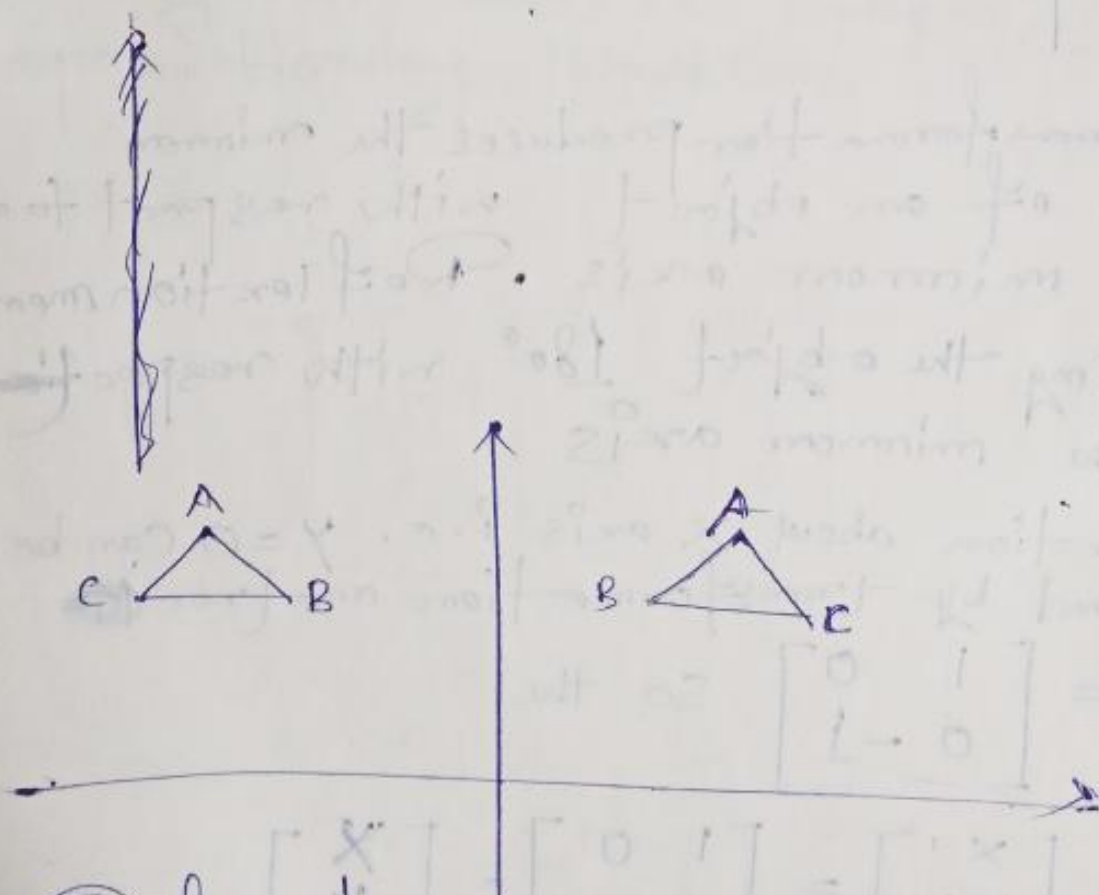
$$M = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \text{ So, the}$$

$$P = \begin{bmatrix} x' \\ y' \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} \\ = \begin{bmatrix} x \\ -y \end{bmatrix}$$

therefore $x' = x$ and $y' = -y$
 here. $p = (x, y)$ is the original
 point and $p' = (x', y')$ is the
 reflected point.

Similarly mirror reflection
 about y axis i.e. $x = 0$
 can be given by the transformation
 matrix.

$$M = \begin{bmatrix} -1 & 0 \\ 0 & 1 \end{bmatrix}$$



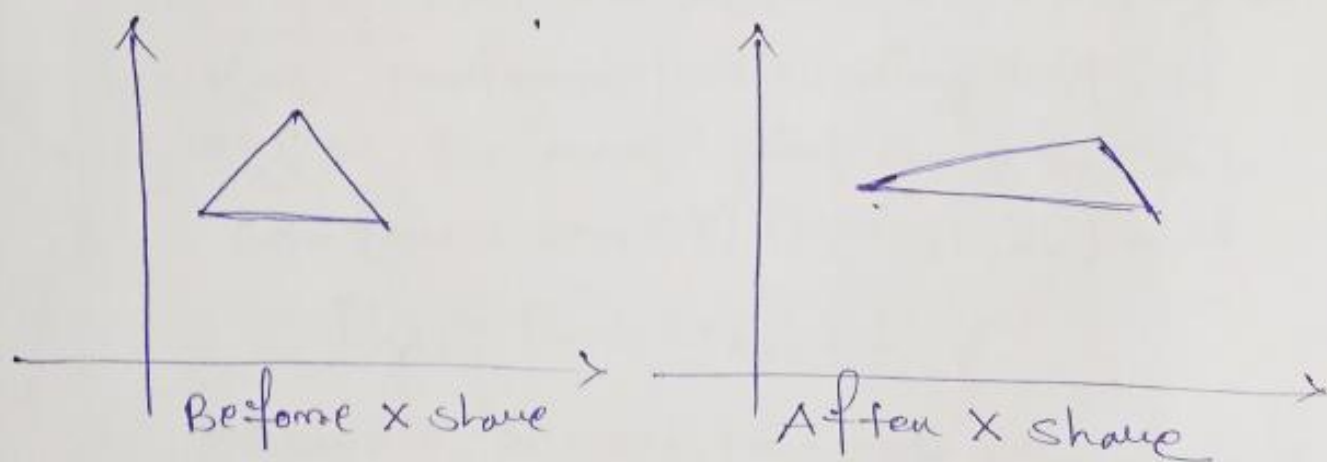
Reflection about y axis.

Shear transformation:

A transformation that distorts the shape of the object and makes the object slant is called a shear transformation.

There are 2 types of shear transformation namely X shear and Y shear.

X shear transformation: — X shear means slanting in the right hand and left hand side.



$$S_{hx} = \begin{bmatrix} 1 & SF_x \\ 0 & 1 \end{bmatrix}$$

where SF_x is the X shearing factor.

So, $P(x, y)$ will be changed to $P'(x', y')$

$$\text{where } x' = x + SF_x \cdot y$$

$$y' = y$$

Similarly, γ share with respect to y axis can be given by the matrix $S_{hy} =$

$$S_{hy} = \begin{bmatrix} 1 & 0 \\ SF_y & 1 \end{bmatrix}$$



Homogenous Quadrimates

we shall represent the Cartesian coordinate P
 (X, Y) by homogenous quadrimate X_h, Y_h, h
where X equal to $\frac{X_h}{h}$
and $Y = \frac{Y_h}{h}$

we shall choose any non 0. h . Let
 $h = 1$

The homogenous quadrimate
representation for translation is as follows.

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_x \\ 0 & 1 & t_y \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

The homogenous quadrimate
representation for translation rotation as follows

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta & -\sin \theta & 0 \\ \sin \theta & \cos \theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

The homogenous quadrimate
representation for scaling as follows

$$\begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} S_x & 0 & 0 \\ 0 & S_y & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

Composite transformation: —

• Multiple translation: —

Let there be two translation with translation vectors t_{x1}, t_{x2} and t_{y1}, t_{y2} ,

$$P' = T(t_{x2}, t_{y2}) [T(t_{x1}, t_{y1}) \cdot P]$$

$$T(t_{x2}, t_{y2}) \cdot T(t_{x1}, t_{y1}) \cdot P$$

As matrix multiplication is associative.

$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & t_{x2} \\ 0 & 1 & t_{y2} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & t_{x1} \\ 0 & 1 & t_{y1} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$
$$\neq \begin{bmatrix} 1 & 0 & t_{x1} + t_{x2} \\ 0 & 1 & t_{y1} + t_{y2} \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\text{So, } P' = T(t_{x1} + t_{x2}, t_{y1} + t_{y2}) \cdot P$$

(15)

• Successive Rotation : —

$$P' = R(\theta_2) [R(\theta_1) \cdot P]$$

$$= R(\theta_2) \cdot R(\theta_1) \cdot P$$

$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} \cos \theta_2 & -\sin \theta_2 & 0 \\ \sin \theta_2 & \cos \theta_2 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \theta_1 & -\sin \theta_1 & 0 \\ \sin \theta_1 & \cos \theta_1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} \cos(\theta_1 + \theta_2) & -\sin(\theta_1 + \theta_2) & 0 \\ \sin(\theta_1 + \theta_2) & \cos(\theta_1 + \theta_2) & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

So, $P' = R(\theta_1 + \theta_2) \cdot P$

• Successive Scaling : —

$$P' = S(S_{x_2}, S_{y_2}) [S(S_{x_1}, S_{y_1}) \cdot P]$$

$$= S(S_{x_2}, S_{y_2}) S(S_{x_1}, S_{y_1}) \cdot P$$

$$P' = \begin{bmatrix} x' \\ y' \\ 1 \end{bmatrix} = \begin{bmatrix} S_{x_2} & 0 & 0 \\ 0 & S_{y_2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} S_{x_1} & 0 & 0 \\ 0 & S_{y_1} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$= \begin{bmatrix} S_{x_1} \cdot S_{x_2} & 0 & 0 \\ 0 & S_{y_1} \cdot S_{y_2} & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ 1 \end{bmatrix}$$

$$\text{So, } P' = S(S_{x_1}, S_{x_2}, S_{y_1}, S_{y_2}) \cdot P$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\left[\begin{array}{ccc|ccc} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \end{array} \right] \begin{bmatrix} x \\ y \\ z \end{bmatrix}$$

$$\begin{bmatrix} x \\ y \\ z \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

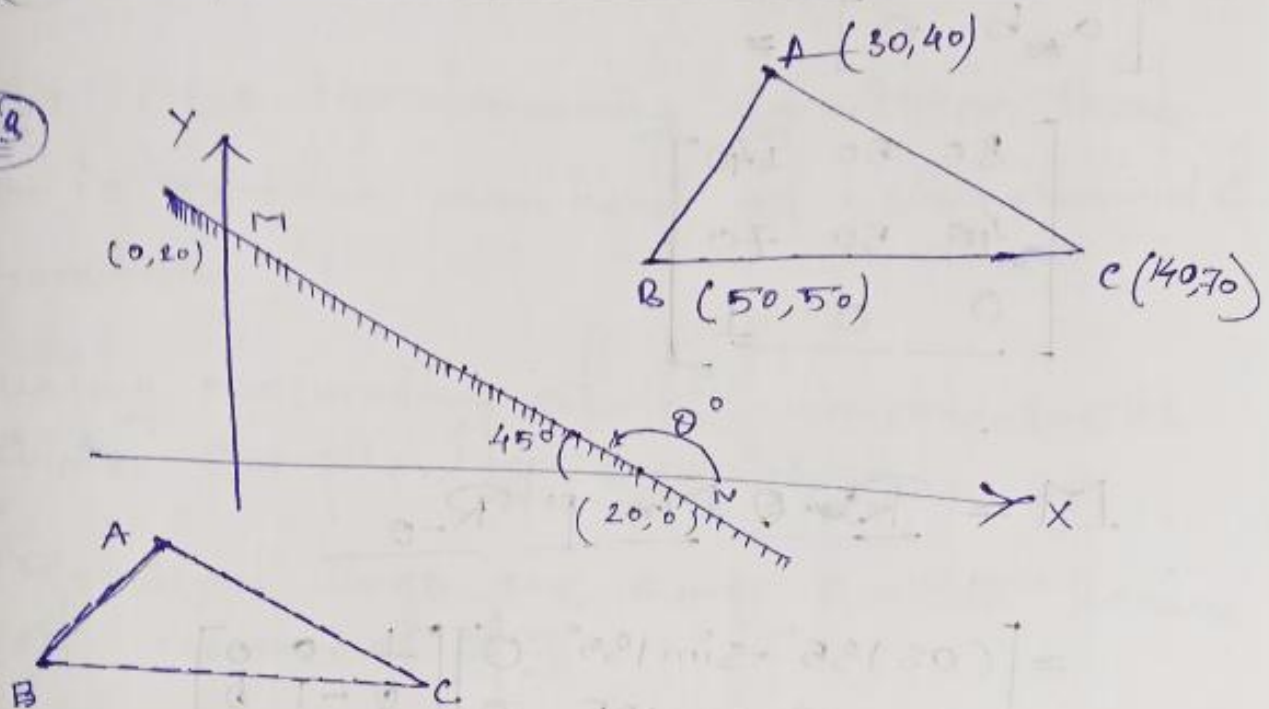
$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$(41, 42, 43) \rightarrow$ same / different digits

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$$\theta = 180 - 45$$

$$\theta = 135^\circ$$

The mirror has x intercept $(20, 0)$ and y intercept $(0, 20)$,

we know that $m = -\tan \theta$

$$= \frac{y_2 - y_1}{x_2 - x_1}$$

$$= \frac{20 - 0}{0 - 20}$$

$$= -1$$

$$\text{So, } -\tan \theta = -1 = \tan 135^\circ$$

$$\text{So, } \theta = 135^\circ$$

∴ Now, the triangle is given by the matrix

$$[a \ b \ c]$$

$$= \begin{bmatrix} 30 & 50 & 140 \\ 40 & 50 & 70 \\ 0 & 0 & 1 \end{bmatrix}$$

$$M = R_{-135} M_0 R_{-135}$$

$$= \begin{bmatrix} \cos 135^\circ & \sin 135^\circ & 0 \\ \sin 135^\circ & \cos 135^\circ & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\begin{bmatrix} 30 & 50 & 140 \\ 40 & 50 & 70 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 30 & 40 \\ 50 & 50 \\ 140 & 70 \end{bmatrix} \begin{bmatrix} \cos 135^\circ & \sin 135^\circ \\ -\sin 135^\circ & \cos 135^\circ \\ 0 & 0 & 1 \end{bmatrix}$$

$$= \begin{bmatrix} \dots & \dots & \dots \\ \dots & \dots & \dots \\ \dots & \dots & \dots \end{bmatrix}$$

5, 6 Same

In DDA line drawing algorithm there is extra overhead of using round of function.

- using rounding of $f_{\frac{m}{n}}$ increases the time complexity algorithm.
- Resulted lines are not smooth because of round of $f_{\frac{m}{n}}$.
- The points generated by the algorithm is not accurate.

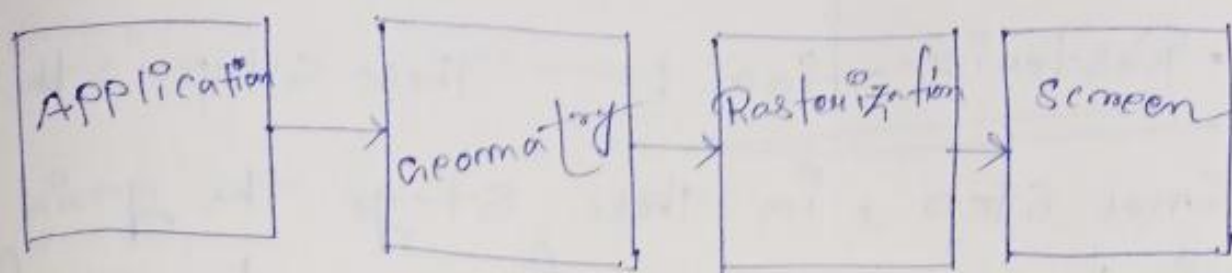
Advantage of DDA algo.

- It is a simple algorithm.
- It's easy to implement.
- It avoid using multiplication operation which is costly in term of time complexity.

36 In computer graphics, a computer graphics pipeline, rendering pipeline or, simply graphics pipeline is a conceptual model that describes what steps a graphics system needs to perform to convert a 3D scene to a 2D screen screen, once a 3D model has been created. For instance in video game or any other 3D computer animation the graphics pipeline is the process of turning that 3D model into what the computer displays. The model of graphics pipeline is usually used in real time rendering.

A graphics pipeline can be divided into 3 main parts →

- Application
- Geometry
- Rasterization.



• Application : — The application state is executed by the software of the main processor (CPU). In the application step changes are made to the scene as required.

Example of the task that are done in the application steps are collision detection, animation, morphing etc.

• Geometry : — The geometry step which is responsible majority of the operation with polygon of their vertices.

(The world co-ordinate system)

• Rasterization! — This step is the final step, in this stage the grid points are called fragments. Each fragment corresponds to one pixel in the frame buffer these can be coloured. The colour of a fragment depends on the illumination, texture and other material properties.

(29) Interlacing is where the horizontal lines of a video display are updated on odd and even lines alternately.
+ RasterScan CRT