Quiz 5

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$$f(t) = \begin{cases} t & \text{if } 0 < t < 1\\ 1 & \text{if } t > 1 \end{cases}$$

Solution:

$$\begin{split} &= \int_0^1 t e^{-st}\,dt + \int_1^t e^{-st}\,dt \\ \text{LHS integral:} \\ &= \int_0^1 t e^{-st}\,dt = -\frac{t e^{-st}}{s} + \int_0^1 \frac{e^{-st}}{s}\,dt \\ &= \left(-\frac{t}{s e^{st}} - \frac{1}{s^2 e^{st}}\right) \end{split}$$