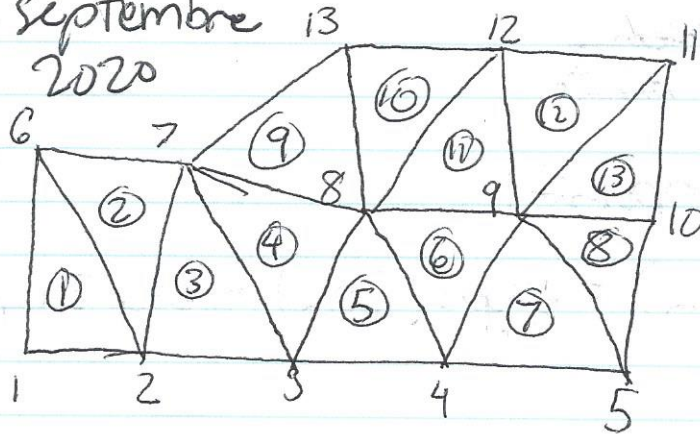


22 septembre  
2020Mailage
 $n_{elem} = 13$   
 $n_{node} = 3$ 
 $n_{point} = 13$  (hasard)

Inpael

dant

3

4

5

6

7

8

9

10

11

12

13

 nd #1  
 nd #2  
 nd #3

1	2	2	3	3	4	4	5	7	8	8	9	9
2	7	3	8	4	9	5	10	8	12	9	11	10
6	6	<del>7</del>	7	8	8	9	9	13	13	12	12	11

init.
 $esup2(1:npoint+1) = 0$ 
 $\Rightarrow [00000000000000]$   
 $14 \times 0$ 

do ielem=1, nelem

do inode=1, nnode

ipoint = mpael(inode, ielem) + 1

esup2(ipoint) = esup2(ipoint) + 1

enddo

enddo

 ex: ielem = 1 et inode = 1  $\Rightarrow$  ipoint = 2  
 $\Rightarrow esup2(2) = 1$ 

 inode = 2  
 inode = 3

 $\Rightarrow$  ipoint = 3  $esup2(3) = 1$ 
 $\Rightarrow$  ipoint = 7  $esup2(7) = 1$ 
 $[0110001000000000]$ 
0.6

~~do item = 1, nitem~~  
~~do inode = 1, nnode~~

do ipoin = 2, npoim + 1

$\text{esup2}(\text{ipoin}) = \text{esup2}(\text{ipoin}) + \text{esup2}(\text{ipoin} - 1)$   
enddo

Element Pass 1: Cont the number of elements connected to each point 33c

$$i_{elem} = 2 \quad i_{node} = 1 \quad i_{point} = 3 \quad espl(3) = 1 + 1 = 2$$

$$i_{node} = 2 \quad i_{point} = 8 \quad espl(8) = 1$$

$$i_{node} = 3 \quad i_{point} = 7 \quad espl(7) = 2$$

2 Iterations

<del>0</del>	<del>1</del>	<del>1</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>	<del>0</del>
1	2	3	4	5	6	7	8	9	10	11	12	13	14	
0	1	2	0	0	0	2	1	0	0	0	0	0	0	0
		1	1				1							
			1				1	1						
				1	1			1						
					1			1	1					
						1				1				
							1	1						
								1						
									1					
										1				
											1			
												1		
													1	
														1

à la fin  
du premier de

~~1~~

1 2 3 4 5 6 7 8 9 10 11 12 13 → # point

$$espl = [0 \ 1 \ 3 \ 3 \ 3 \ 2 \ 2 \ 4 \ 6 \ 6 \ 2 \ 2 \ 3 \ 2]$$

2e de (Storage / reshuffling pass 1):

$$espl = [0 \ 1 \ 4 \ 7 \ 10 \ 12 \ 14 \ 18 \ 24 \ 30 \ 32 \ 34 \ 37 \ 39]$$

espl est terminé !!



33d

$$\text{esup2} = [0 \ 1 \ 4 \ 7 \ 10 \ 12 \ 14 \ 18 \ 24 \ 30 \ 32 \ 34 \ 37 \ 39]$$

Element Pass 2 : Store the elements in esup1

do ielem=1, nelem  
do inode=1, nnode

ipoin = inpael (inode, ielem)  
istar = esup2 (ipoin) + 1  
esup2 (ipoin) = istar  
esup1 (istar) = ielem

enddo  
enddo

idelem=1, inode=1  $\Rightarrow$  ipoin = 1 <sup>70</sup>  
istar = esup2(1) + 1 = 1  
esup2(1) = 1  
esup1(1) = 1      [1 1 4...]

inode=2  $\Rightarrow$  ipoin = 2  
istar = 1 + 1 = 2  
esup2(2) = 2  
esup1(2) = 1      [1 2 4  
                         [1 1

inode=3  $\Rightarrow$  ipoin = 6  
istar = 12 + 1

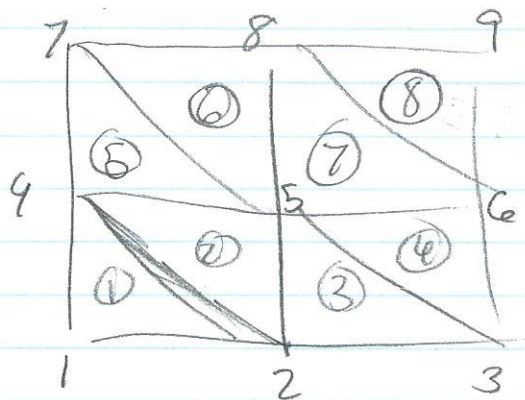
~~esup1 = [1 1 00 000000000001]~~  
~~esup1 = [1 1 00 000000000001]~~

$i_{elem} = 2, \quad n_{ode} = 1 \Rightarrow i_{point} = 2$   
 $i_{star} = 3$

[13]

$esup1 \Rightarrow$  "elements surrounding point"

OK!



$N_{NODE} = 3$   
 $N_{POINT} = 9$   
 $N_{ELEM} = 8$

$esup1 = [1 \mid 2 \ 3 \mid 3 \ 4 \mid 1 \ 2 \ 5 \mid 2 \ 3 \ 4 \ 5 \ 6 \ 7 \mid 4 \ 7 \ 8 \mid$   
 $5 \ 6 \mid 6 \ 7 \ 8 \mid 8]$

$longueur = \frac{N_{ELEM} * N_{NODE}}{i_{point} + 1}$

$i_{point} = 0$   
 $i_{star} = 1$   
 $esup2(0) = 1$   
 $esup1(0) = 0 + 1$

$i_{point} = 2 - 1 = 1$   
 $i_{star} = 1 + 1 = 2$   
 $esup2(1) = 2$   
 $esup1(1) = 0 + 1$

$i_{point} = 6 - 1 = 5$   
 $i_{star} = 12 + 1$   
 $esup2(5) = 12$

$i_{point} = ?$   
 $i_{star} = 1$

23 septembre 2020

↗ ++i pas i++

for (size\_t i = 0; i < 5; ++i)

%z affiche caractère  
%l float

Tableaux : taille N  $\Rightarrow$  indices 0  $\rightarrow$  N-1

double A1[12]

int A2[2] = {1, 2}

M1[5][4]

int main(void)  $\rightarrow$  ne retourne rien  
type universel

#include <math.h>

#include <vector>

push-back

lire et écrire dans un fichier header <fstream>



$$\begin{array}{ccccccc}
 & 1 & & 2 & & 3 & & 4 \\
 \text{psup1} = [ & 2 & 6 & | & 1 & 3 & 6 & 7 & | & 2 & 4 & 7 & 8 & | & 3 & 5 & 8 & 9 & | \\
 & 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & 8 & 9 & 10 & & & & & & & \\
 & \underbrace{4 & 9 & 10}_{5} & | & \underbrace{1 & 2 & 7}_{6} & | & \underbrace{2 & 3 & 6 & 8 & 13}_{7} & | & & & & & & 
 \end{array}$$

$$\begin{array}{ccccccc}
 \underbrace{3 & 4 & 7 & 9 & 12 & 13}_{8} & | & \underbrace{4 & 5 & 8 & 10 & 11 & 12}_{9} & | 
 \end{array}$$

$$\begin{array}{ccccccc}
 \underbrace{5 & 9 & 11}_{10} & | & \underbrace{9 & 10 & 12}_{11} & | & \underbrace{8 & 9 & 11 & 13}_{12} & | & \underbrace{7 & 8 & 12}_{13} & ] 
 \end{array}$$

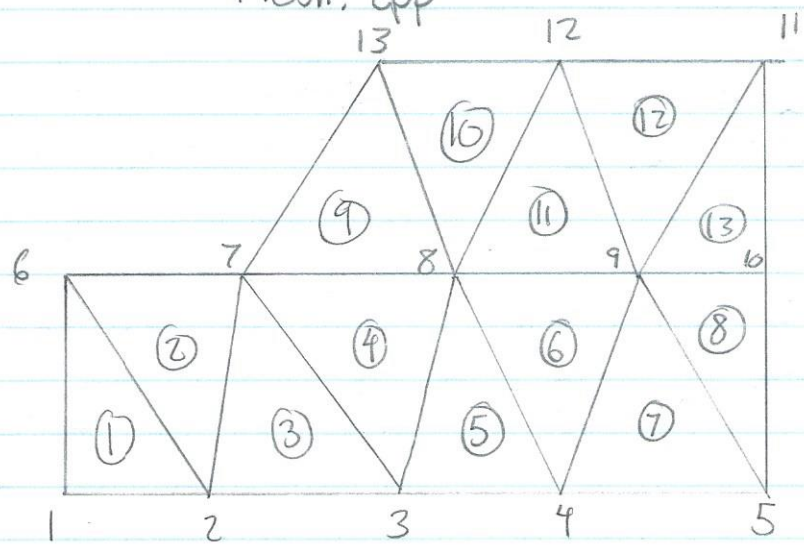
$$\boxed{50}$$

$$\text{psup2} = [0 \ 2 \ 3 \ 6 \ 6]$$

$$\text{psup2} = [0 \ 2 \ 6 \ 10 \ 14 \dots]$$

# Mesh. cpp

Ex.



CONNEX [NELEM][NNODE]

mesh  
1  
2  
3  
4  
5  
6  
7  
8  
9  
10  
11  
12

1	2	6
2	7	6
2	3	7
3	8	7
3	4	8
4	9	8
4	5	9
5	10	9
7	8	13
8	12	13
8	9	12
9	11	12
9	10	11

13 éléments

NELEM = 13  
NNODE = 3 \*  
NPOIN = 13

\* NNODE est constant dans ce maillage.  
↳ Il faudrait faire un vecteur qui stocke le nombre de nœuds par élément.

3 points par élément.



33:

$$mesup = 3 \cdot 13 = NNODE * NELEM = 39$$

\* Sum of NNODE si recteur.

# 1. Elements surrounding points - Linked lists

$esup1[mesup]$  → stores the elements  
 $esup2[NPOINT+1]$  → stores the location } linked lists

$esup1 = [$ 

1	1	2	3	3	4	5	5	6	7	7	8	1	2	2	3	4	9
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17

 $]$

4	5	6	9	10	11	6	7	8	11	12	13	8	13	12	13	10	11	12	9	10
18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38

$esup2 = [$ 

0	1	4	7	10	12	14	18	24	30	32	34	37	39
0	1	2	3	4	5	6	7	8	9	10	11	12	13

 $]$

mpsup est = à 50 ici, préférable d'utiliser 33;  
un vecteur avec push-back.

2. Points (surrounding points)

psup1[mpsup] → stores the points  
psup2[NPOIN+1] → stores the locations

lpoin[NPOIN] → helps avoid repetition

Algorithm:

lpoin[NPOIN] = {0}  
psup2(1) = 0  
istor = 0

```
do ipoin=1, npoin
  do iesup=esup2(ipoin)+1, esup2(ipoin+1)
    ielem=esup1(iesup)
    do inode=1, nnode
      jpoir=mpoel(inode, ielem)
      if (jpoir ≠ ipoin and lpoin(jpoir) ≠ ipoin)
        istor=istor+1;
        psup1(istor)=jpoir
        lpoin(jpoir)=ipoin
      endif
    enddo
  enddo
  psup2(ipoin+1)=istor
enddo
```

# Application de PSUP: Fortran

```

1, 2 = 1
ipoin = 1 —————> (de 1 à 13)
iesup = 1 —————> (de 1 à 1 par ipoin = 1)
iclem = 1
inode = 1
jpoim = 1
if (jpoim ≠ 1 & 0 ≠ 1) NON
inode = 2
jpoim = 2
if (2 ≠ 1 & 0 ≠ 1) oui
istor = 1
psup1(1) = 2
lpoim(2) = 1
→ psup1 = [2 0 0...]
lpoim = [0 1 0 0...]

inode = 3
jpoim = 6
if (6 ≠ 1 & 0 ≠ 1) oui
istor = 2
psup1(2) = 6
lpoim(6) = 1
→ psup1 = [2 6 0...]
→ lpoim = [0 1 0 0 0 1 0...]

psup2(1+1) = 2
→ psup2 = [0 2 0...]

```



ipoin = 0

C++

iesup = 0

ielem = 0

inode = 0

jpoim = 1

if (1 ≠ 1 & 0 ≠ 1) now

inode = 1

jpoim = 2

if (2 ≠ 1 & 0 ≠ 1) oui

istar = 1;

psup1(0) = 2

lpoim(1) = 1

inode = 2

jpoim = 6

if (6 ≠ 1 & 0 ≠ 1) oui

istar = 2

psup1(1) = 6

lpoim(5) = 1

psup2(1) = 2

⇒ psup1 = [2 6]

lpoim = [0 1 0 0 0 1 0 ...]

psup2 = [0 2 0 ...]

NPSUP à partir de psup2:

NPSUP [NPOIN]

✓

3. Elements surrounding elements.

(ESUEL)

ESUEL [NELEM][NFAEL]

↳ number of faces per element.

Dans l'exemple, NFAEL = 3

\* Faudrait créer un vecteur qui store cette variable par chaque élément.

lpoin [NPOIN] = {0}  
ESUEL [NELEM][NFAEL] = {0}

```

do ielem = 1, nelem
  do itael = 1, ntael
    nnota = lnota (itael)
    lhelp (1:nnota) = inpoel (lnota (1:nnota), itael), ielem)
    lpoin (lhelp (1:nnota)) = 1
    ipoin = lhelp (1)
    do istor = esup2 (ipoin) + 1, esup2 (ipoin + 1)
      jelem = esup1 (istor)
      if (jelem .ne. ielem)
        do jtael = 1, ntael
          nnotj = lnota (jtael)
          if (nnotj .ne. nnota)
            ican = 0
            do jnota = 1, nnota
              jpoin = inpoel (lnota (jnota), jtael), jelem
              ican = ican + lpoin (jpoin)
            enddo
            if (ican = nnota)
              esuel (itael, ielem) = jelem
            endif
          endif
        enddo
      endif
    enddo
    lpoin (lhelp (1:nnota)) = 0
  enddo
enddo

```

\* Je crois q'il  
manque un enddo  
ici

3enddo

Altray



Initialize:

$\text{lpoin}[\text{NPOINT}] = \{0\}$

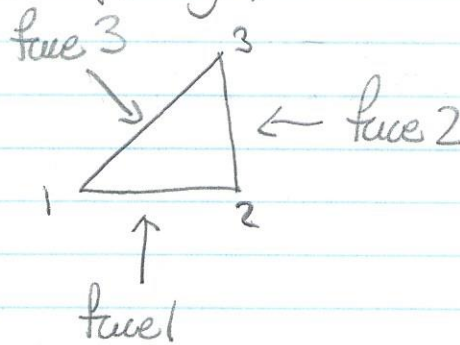
$\text{ESUEL}[\text{NELIEM}][\text{NFAEL}] = \{0\}$

\* Par un code 2D,  $n\text{nota} = 2$  (lignes)  
 $\hookrightarrow$  number of nodes per face.

$n\text{nota} \Rightarrow$  number of nodes per face = 2

$n\text{fael} \Rightarrow$  number of faces per element  
 $\hookrightarrow$  par des éléments triangulaires (2D) = 3

Ex: 2D (triangle)



\*  $\text{lpofa}$  est une matrice pré-définie qui dépend de la forme des éléments.

$\hookrightarrow$  On peut tout de suite créer une telle matrice par différents types d'éléments

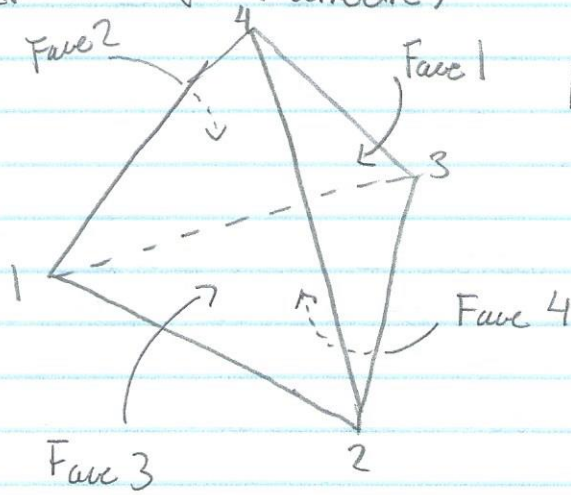
$\text{lpofa} \Rightarrow$  list (Matrix) of points per face  
 $\text{dimensions}$

$\text{lpofa}[n\text{fael}][n\text{nota}] \hookrightarrow \text{lpofa}[3][2] = \begin{bmatrix} 1 & 2 \\ 2 & 3 \\ 3 & 1 \end{bmatrix} \begin{array}{l} \rightarrow \text{face 1} \\ \rightarrow \text{face 2} \\ \rightarrow \text{face 3} \end{array}$

$\text{lnota} \Rightarrow$  list of nodes per face  $\text{lnota}[n\text{fael}]$

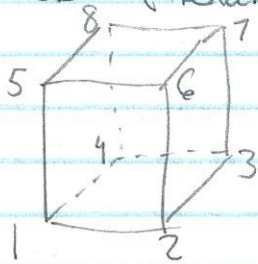
$\hookrightarrow \text{lnota}[3] = [2 \ 2 \ 2]$   
 $\text{dim}$

Ex: 3D (tétraèdre)



$$\text{potu } [4][3] = \begin{bmatrix} 2 & 3 & 4 \\ 3 & 1 & 4 \\ 1 & 2 & 4 \\ 1 & 3 & 2 \end{bmatrix} \rightarrow \begin{array}{l} \text{Face} \\ \text{Face 2} \\ \text{Face 3} \\ \text{Face 4} \end{array}$$

Ex: 3D (hexaèdre)



$$\text{potu } [6][4] = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 1 & 2 & 6 & 5 \\ 2 & 3 & 7 & 6 \\ 3 & 4 & 8 & 7 \\ 4 & 1 & 5 & 8 \\ 5 & 6 & 7 & 8 \end{bmatrix}$$

$$\text{CONNEX}(1, [1 \ 2]) = [1 \ 2]$$

jelem = 1

ifael = 1 (1 → 3)

[1 2]

nnotu = 2

lhelp [1 2] = CONNEX(1, lnotu(1, 1:2)) ⇒ lhelp = [1 2]

lpoin([1 2]) = 1

ipoin = 1

istor = 1

(début du do) 1 → 1

jelem = 1  
if (1 ≠ 1) NON

↳ ne rentre pas dans le if

endif

enddo

lpoin([1 2]) = 0

⇒ Reset lpoin

ifael = 2

nnotu = 2

lhelp [1 2] = CONNEX(1, lnotu(2, [1 2])) ⇒ lhelp = [2 6]

lpoin [2 6] = 1

⇒ lpoin = [0 1 0 0 0 1]

ipoin = 2

istor = 2

(2 → 4)

jelem = 1  
if (1 ≠ 1) NON

→ ne rentre pas dans le if

endif

istor = 3

jelem = 2  
if (2 ≠ 1) oui

jfael = 1 (for de 1 → 3)

nnotj = lnotu(jfael) = 2

if (2 == 2) oui

icam = 0

jnotu = 1

(for de 1 → 2)

(suite →)

Hilroy



ne pas oublier  
de ↗ jpoint.

$$jnode = 1$$

$$jpoint = \text{CONNEX}(2, \overbrace{\text{fpola}(1, 1)}^1) = 2$$

$$icount = \text{ipoint}(jpoint) = 0 + 1 = 1$$

$$jnode = 2$$

$$jpoint = \text{CONNEX}(2, \overbrace{\text{fpola}(1, 2)}^2) = 7 \} 6$$

$$icount = 1 + \underset{6}{\text{ipoint}(7)} = 1 + 0$$

$$\text{if } (1 == 2)^{\text{non}}$$

$$\text{esue}[1][2] = 2$$

Wow!

\* Je crois que la table CONNEX doit se présenter avec les nœuds en ordre croissant.

C'est plus qu'il doit y avoir un respect de l'ordre d'attribution des faces dans fpola ?

et fpola

ielem = 0  $\Rightarrow$  élément 1  
itael = 0  $\Rightarrow$  face 1

lnota = [2 2 2] 33r  
lpota =  $\begin{bmatrix} 1 & 2 \\ 2 & 3 \\ 3 & 1 \end{bmatrix}$   $\Delta^3_2$

face 1  $\left\{ \begin{array}{l} nnota = 2 \\ lhelp = [1 \ 2] \\ lpain = [1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0 \ 0] \\ ipoin = 1 \\ istor = 0 \end{array} \right.$  For istor = 0  $\rightarrow$  0  $\Rightarrow$  ne rentre pas dans le for  
!  
lpain = [0 0 0 0 0 0 0 0 0 0 0 0 0 0] remise à 0.

itael = 1  $\Rightarrow$  face 2

nnota = 2

lhelp = [2 6]

lpain = [0 1 0 0 0 1 0 0 0 0 0 0 0 0]

ipoin = 2

istor = 1 (For istor = 1  $\rightarrow$  3)

jelem = 1  
if (1-1  $\neq$  0) ~~oui~~

$\left. \begin{array}{l} \text{On regarde l'élément 1} \\ \text{par rapport à l'élément} \\ \text{1, on s'en fait!} \end{array} \right\}$

istor = 2

jelem = 2

if (2-1  $\neq$  0) ~~oui~~  $\Rightarrow 1 \neq 0$

jtael = 0 (For jtael = 0  $\rightarrow$  2)

nnotaj = 2 ~~oui~~ nombre de nœuds de la face "j"

if (2 == 2) ~~oui~~

ican = 0

jnota = 0 (For jnota = 0  $\rightarrow$  1)

jpain = 2

ican = ican + pain[jpain] = 0 + 1 = 1

jnota = 1

jpain = 6

\* si CANEC croissant \*

ican = 1 + 1 = 2

if (2 == 2)

esuel[0][1] = 2

Il faut regarder TOUTES LES COMBINAISONS POSSIBLES!!

Hilroy