

Boolean Algebra Worksheet

Instructions

Use Java boolean notation: `&&` (AND), `||` (OR), `!` (NOT) Variables: A, B, C, D represent boolean values (true or false)

Part 1: Apply DeMorgan's Laws

Simplify the following expressions using DeMorgan's laws:

1. $\neg(A \ \&\& \ B)$
 2. $\neg(A \ || \ B)$
 3. $\neg(A \ \&\& \ B \ \&\& \ C)$
 4. $\neg(\neg A \ || \ B)$
 5. $\neg(A \ || \ \neg B) \ \&\& \ C$
 6. $\neg((A \ \&\& \ B) \ || \ C)$
 7. $\neg(A \ \&\& \ (B \ || \ C)) \ || \ D$
 8. $\neg((A \ || \ B) \ \&\& \ (C \ || \ D))$
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Part 2: Identity Verification

Determine whether each identity is **TRUE** or **FALSE**. Show your work using boolean simplification rules:

1. $A \ \&\& \ (B \ || \ C) = (A \ \&\& \ B) \ || \ (A \ \&\& \ C)$
 2. $A \ || \ (A \ \&\& \ B) = A$
 3. $(A \ || \ B) \ \&\& \ (A \ || \ C) = A \ || \ (B \ \&\& \ C)$
 4. $(A \ || \ B) \ \&\& \ (\neg A \ || \ B) = B$
 5. $A \ \&\& \ (B \ || \ C) \ \&\& \ (B \ || \ \neg C) = A \ \&\& \ B$
 6. $(A \ \&\& \ B) \ || \ (A \ \&\& \ C) \ || \ (\neg A \ \&\& \ B \ \&\& \ C) = (A \ \&\& \ B) \ || \ (A \ \&\& \ C)$
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Part 3: Simplify the Following

Reduce each expression to its simplest form:

1. $A \wedge A$
 2. $(A \vee B) \wedge (\neg A \vee B)$
 3. $A \wedge (B \vee \neg B)$
 4. $(A \wedge B) \vee (A \wedge \neg B) \vee (\neg A \wedge C)$
 5. $(A \vee B) \wedge (A \vee C) \wedge (B \vee C)$
 6. $(A \wedge B \wedge C) \vee (A \wedge B \wedge \neg C) \vee (A \wedge \neg B \wedge C) \vee (\neg A \wedge B \wedge C)$
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