# Variable Importance Plots—An Introduction to the vip Package

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**Abstract** In the era of "big data", it is becoming more of a challenge to not only build state-of-the-art predictive models, but also gain an understanding of what's really going on in the data. For example, it is often of interest to know which, if any, of the predictors in a fitted model are relatively influential on the predicted outcome. Some modern algorithms—like random forests (RFs) and gradient boosted decision trees (GBMs)—have a natural way of quantifying the importance or relative influence of each feature. Other algorithms—like naive Bayes classifiers and support vector machines—are not capable of doing so and *model-agnostic approaches* are generally used to measure each predictor's importance. Enter **vip**, an R package for constructing variable importance scores/plots for many types of supervised learning algorithms using model-specific and novel model-agnostic approaches. We'll also discuss a novel way to display both feature importance and feature effects together using *sparklines*, a very small line chart conveying the general shape or variation in some feature that can be directly embedded in text or tables.

## Introduction

Too often machine learning (ML) models are summarized using a single metric (e.g., cross-validated accuracy) and then put into production. Although we often care about the predictions from these models, it is becoming routine to also understand the predictions! Understanding how an ML model makes its predictions helps build trust in the model and is the fundamental idea of the emerging field of *interpretable machine learning* (IML). For an in-depth discussion on IML, see Molnar (2019). In this paper, we focus on global methods for quantifying the importance of features in an ML model. Computing variable importance (VI) and communicating them through variable importance plots (VIPs) is a fundamental component of IML and is the main topic of this paper.

VI scores and VIPs can be constructed for general ML models using a number of packages. The **iml** package (Molnar et al., 2018) provides the `FeatureImp()` function which computes feature importance for general prediction models using the permutation approach (discussed later). It is written in **R6** (Chang, 2019) and allows the user to specify a generic loss function or select one from a pre-defined list (e.g., `loss = "mse"` for mean squared error). It also allows the user to specify whether importance is measured as the difference or as the ratio of the original model error and the model error after permutation. The user can also specify the number of repetitions used when permuting each feature to help stabilize the variability in the procedure.

The **ingredients** package (Biecek, 2019) also provides permutation-based VI scores through the `feature_importance()` function. (Note that this function recently replaced the now deprecated **DALEX** function `variable_importance()` (Biecek, 2018).) Similar to `iml::FeatureImp()`, this function allows the user to specify a loss function and how the importance scores are computed (e.g., using the difference or ratio). It also provides an option to sample the training data before shuffling the data to compute importance (the default is to use `n_sample = 1000`). This can help speed up computation.

The **caret** package (Kuhn, 2017) includes a general `varImp()` function for computing model-specific and filter-based VI scores. Filter-based approaches, which are described in Kuhn and Johnson (2013), do not make use of the fitted model to measure VI. They also do not take into account the other predictors in the model. For regression problems, a popular filter-based approach to measuring the VI of a numeric predictor $x$ is to first fit a flexible nonparametric model between $x$ and the target $Y$; for example, the locally-weighted polynomial regression (LOWESS) method developed by Cleveland (1979). From this fit, a pseudo-$R^2$ measure can be obtained from the resulting residuals and used as a measure of VI. For categorical predictors, a different method based on standard statistical tests (e.g., $t$-tests and ANOVAs) can be employed; see Kuhn and Johnson (2013) for details. For classification problems, an area under the ROC curve (AUC) statistic can be used to quantify predictor importance. The AUC statistic is computed by using the predictor $x$ as input to the ROC curve. If $x$ can reasonably separate the classes of $Y$, that is a clear indicator that $x$ is an important predictor (in terms of class separation) and this is captured in the corresponding AUC statistic. For problems with more than two classes, extensions of the ROC curve or a one-vs-all approach can be used.

If you use the **mlr** interface for fitting ML models (Bischl et al., 2016), then you can use the `getFeatureImportance()` function to extract model-specific VI scores from various tree-based models (e.g., RFs and GBMs). Unlike **caret**, the model needs to be fit via the **mlr** interface; for instance, you cannot use `getFeatureImportance()` on a **gbm** model (Ridgeway, 2017) unless it was fit using **mlr**.

While the **iml** and **DALEX** packages provide model-agnostic approaches to computing VI, **caret**, and to some extent **mlr**, provide model-specific approaches (e.g., using the absolute value of the $t$-statistic for linear models) as well less accurate filter-based approaches . Furthermore, each package has a completely different interface (e.g., **iml** is written in R6). The **vip** package (Greenwell and Boehmke, 2018) strives to provide a consistent interface to both model-specific and model-agnostic approaches to feature importance that is simple to use. The three most important functions exported by **vip** are described below:

- `vi()` computes VI scores using model-specific or model-agnostic approaches (the results are always returned as a tibble (Müller and Wickham, 2019));
- `vip()` constructs VIPs using model-specific or model-agnostic approaches with **ggplot2**-style graphics (Wickham, 2016);
- `add_sparklines()` adds a novel sparkline representation of feature effects (e.g., *partial dependence plots*) to any VI table produced by `vi()`.

There's also a function called `vint()` (for variable interactions) but is experimental and will not be discussed here; the interested reader is pointed to Greenwell et al. (2018). Note that `vi()` is actually a wrapper around four workhorse functions, `vi_model()`, `vi_ice()`, `vi_pdp()`, and `vi_permute()`, that compute various types of VI scores. The first computes model-specific VI scores, while the latter three produce model-agnostic ones. The workhorse function that actually gets called is controlled by the `method` argument in `vi()`; the default is `method = "model"` which corresponds to model-specific VI (see `?vip::vi` for details and links to further documentation).

### Constructing VIPs in R

We'll illustrate major concepts using the Friedman 1 benchmark problem described in Friedman (1991) and Breiman (1996):

$$Y_i = 10 \sin\left(\pi X_{1i} X_{2i}\right) + 20\left(X_{3i} - 0.5\right)^2 + 10 X_{4i} + 5 X_{5i} + \epsilon_i, \quad i = 1, 2, \ldots, n, \tag{1}$$

where $\epsilon_i \overset{iid}{\sim} N\left(0, \sigma^2\right)$. Data from this model can be generated using the `vip::gen_friedman()`. By default, the features consist of 10 independent variables uniformly distributed on the interval $[0, 1]$; however, only 5 out of these 10 are actually used in the true model. The code chunk below simulates 500 observations from the model in Equation~(1) with $\sigma = 1$; see `?vip::gen_friedman` for details.

```
trn <- vip::gen_friedman(500, sigma = 1, seed = 101)  # simulate training data
tibble::as_tibble(trn)  # inspect output
```

```
#> # A tibble: 500 x 11
#>        y     x1    x2    x3    x4     x5      x6    x7    x8    x9   x10
#>    <dbl>  <dbl> <dbl> <dbl> <dbl>  <dbl>   <dbl> <dbl> <dbl> <dbl> <dbl>
#>  1 14.9  0.372  0.406 0.102 0.322 0.693  0.758   0.518 0.530 0.878 0.763
#>  2 15.3  0.0438 0.602 0.602 0.999 0.776  0.533   0.509 0.487 0.118 0.176
#>  3 15.1  0.710  0.362 0.254 0.548 0.0180 0.765   0.715 0.844 0.334 0.118
#>  4 10.7  0.658  0.291 0.542 0.327 0.230  0.301   0.177 0.346 0.474 0.283
#>  5 17.6  0.250  0.794 0.383 0.947 0.462  0.00487 0.270 0.114 0.489 0.311
#>  6 18.3  0.300  0.701 0.992 0.386 0.666  0.198   0.924 0.775 0.736 0.974
#>  7 14.6  0.585  0.365 0.283 0.488 0.845  0.466   0.715 0.202 0.905 0.640
#>  8 17.0  0.333  0.552 0.858 0.509 0.697  0.388   0.260 0.355 0.517 0.165
#>  9  8.54 0.622  0.118 0.490 0.390 0.468  0.360   0.572 0.891 0.682 0.717
#> 10 15.0  0.546  0.150 0.476 0.706 0.829  0.373   0.192 0.873 0.456 0.694
#> # ... with 490 more rows
```

From Equation~(1), it should be clear that features $X_1$–$X_5$ are the most important! (The others don't influence $Y$ at all.) Also, based on the form of the model, we'd expect $X_4$ to be the most important feature, probably followed by $X_1$ and $X_2$ (both comparably important), with $X_5$ probably less important. The influence of $X_3$ is harder to determine due to its quadratic nature, but it seems likely that this nonlinearity will suppress the variable's influence over its observed range (i.e., 0–1).

## Model-specific VI

Some machine learning algorithms have their own way of quantifying the importance of each feature. We describe some of these in the subsections that follow. The issue with model-specific VI scores

is that they are not necessarily comparable across different types of models. For example, directly comparing the impurity-based VI scores from tree-based models to the $t$-statistic from linear models.

### Decision trees and tree ensembles

Decision trees probably offer the most natural model-specific approach to quantifying the importance of each feature. In a binary decision tree, at each node $t$, a single predictor is used to partition the data into two homogeneous groups. The chosen predictor is the one that maximizes some measure of improvement $i^t$. The relative importance of predictor $X$ is the sum of the squared improvements over all internal nodes of the tree for which $X$ was chosen as the partitioning variable; see Breiman et al. (1984) for details. This idea also extends to ensembles of decision trees, such as RFs and GBMs. In ensembles, the improvement score for each predictor is averaged across all the trees in the ensemble. Fortunately, due to the stabilizing effect of averaging, the improvement-based VI metric is often more reliable in large ensembles; see Hastie et al. (2009, p. 368). RFs offer an additional method for computing VI scores. The idea is to use the leftover out-of-bag (OOB) data to construct validation-set errors for each tree. Then, each predictor is randomly shuffled in the OOB data and the error is computed again. The idea is that if variable $X$ is important, then the validation error will go up when $X$ is perturbed in the OOB data. The difference in the two errors is recorded for the OOB data then averaged across all trees in the forest. Later on, we'll discuss a more general permutation method that can be applied to any supervised learning model.

To illustrate, we fit a CART-like regression tree, RF, and GBM to the simulated training data. (Note: there are a number of different packages available for fitting these types of models, we just picked popular implementations for illustration.)

```
# Load required packages
library(rpart)          # for fitting CART-like decision trees
library(randomForest)   # for fitting RFs
library(xgboost)        # for fitting GBMs

# Fit a single regression tree
tree <- rpart(y ~ ., data = trn)

# Fit an RF
set.seed(101)
rfo <- randomForest(y ~ ., data = trn, importance = TRUE)

# Fit a GBM
set.seed(102)
bst <- xgboost(
  data = data.matrix(subset(trn, select = -y)),
  label = trn$y,
  objective = "reg:linear",
  nrounds = 100,
  max_depth = 5,
  eta = 0.3,
  verbose = 0  # suppress printing
)
```

Each of the above packages include the ability to compute VI scores for all the features in the model; however, the implementation is rather package specific, as shown in the code chunk below. The results are displayed in Figure~1 (the code to reproduce these plots has been omitted but can be made available upon request).

```
# Extract VI scores from each model
vi_tree <- tree$variable.importance
vi_rfo <- rfo$variable.importance
vi_bst <- xgb.importance(model = bst)
```

As we would expect, all three methods rank the variables `x1`–`x5` as more important than the others. While this is good news, it is unfortunate that we have to remember the different functions and ways of extracting and plotting VI scores from various model fitting functions. This is one place where **vip** can help…one function to rule them all! Once **vip** is loaded, we can use `vi()` to extract a tibble of VI scores.

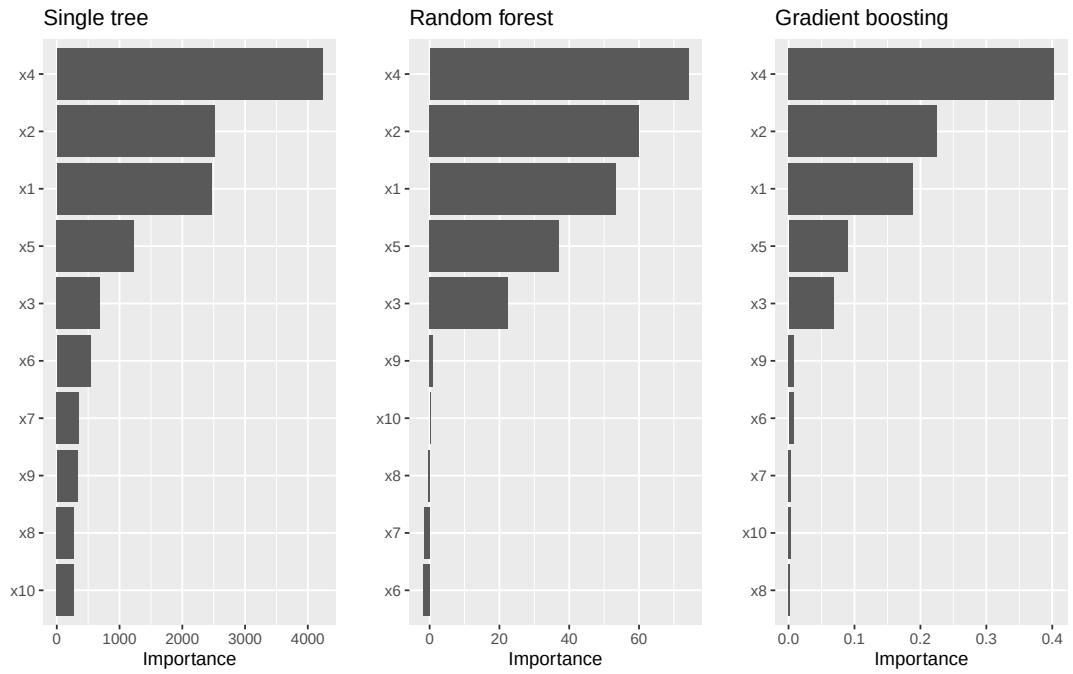


**Figure 1:** Model-specific VIPs for the three different tree-based models fit to the simulated Friedman data.

```
# Load required packages
library(vip)

# Compute model-specific VI scores
vi(tree)  # CART-like decision tree
```

```
#> # A tibble: 10 x 2
#>    Variable Importance
#>    <chr>         <dbl>
#>  1 x4            4234.
#>  2 x2            2513.
#>  3 x1            2461.
#>  4 x5            1230.
#>  5 x3             688.
#>  6 x6             533.
#>  7 x7             357.
#>  8 x9             331.
#>  9 x8             276.
#> 10 x10            275.
```

```
vi(rfo)   # RF
```

```
#> # A tibble: 10 x 2
#>    Variable Importance
#>    <chr>         <dbl>
#>  1 x4           74.2
#>  2 x2           59.9
#>  3 x1           53.3
#>  4 x5           37.1
#>  5 x3           22.5
#>  6 x9            1.05
#>  7 x10           0.254
#>  8 x8           -0.408
#>  9 x7           -1.56
#> 10 x6           -2.00
```

```
vi(bst)   # GBM
```

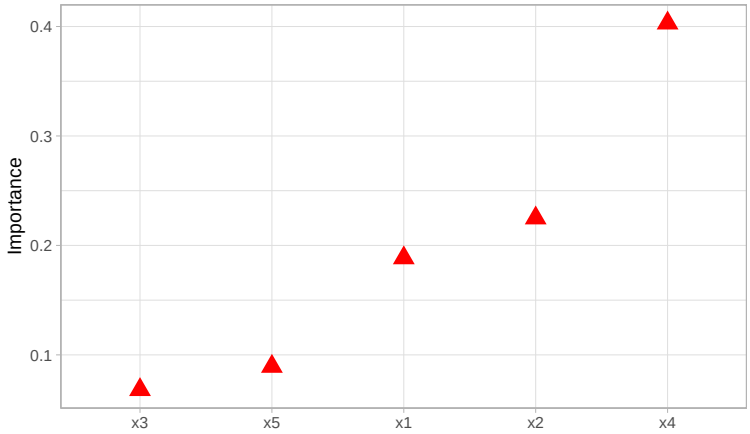


**Figure 2:** Illustrating various plotting options.

```
#> # A tibble: 10 x 2
#>    Variable Importance
#>    <chr>         <dbl>
#>  1 x4          0.403
#>  2 x2          0.225
#>  3 x1          0.189
#>  4 x5          0.0894
#>  5 x3          0.0682
#>  6 x9          0.00802
#>  7 x6          0.00746
#>  8 x7          0.00400
#>  9 x10         0.00377
#> 10 x8          0.00262
```

Notice how the `vi()` function always returns a tibble[1] with two columns: `Variable` and `Importance` (the exceptions are coefficient-based models which also include a `Sign` column giving the sign of the corresponding coefficient and permutation importance involving multiple Monte Carlo simulations, but more on that later). Also, by default, `vi()` always orders the VI scores from highest to lowest; this, among other options, can be controlled by the user (see `?vip::vi` for details). Plotting VI scores with `vip()` is just as straightforward. For example, the following code can be used to reproduce Figure~1.

```
p1 <- vip(tree) + ggtitle("Single tree")
p2 <- vip(rfo) + ggtitle("Random forest")
p3 <- vip(bst) + ggtitle("Gradient boosting")

# Figure 1
grid.arrange(p1, p2, p3, nrow = 1)
```

Notice how the `vip()` function always returns a `"ggplot"` object (by default, this will be a bar plot). For large models with many features, a Cleveland dot plot is more effective (in fact, a number of useful plotting options can be fiddled with). Below we call `vip()` and change a few useful options (the resulting plot is displayed in Figure~2). Note that we can also call `vip()` directly on a `"vi"` objects if it's already been constructed.

```
# Load required packages
library(ggplot2)  # for theme_light() function
theme_set(theme_light())  # set theme for all ggplot2-based plots

vip(bst, num_features = 5, geom = "point", horizontal = FALSE,
    aesthetics = list(color = "red", shape = 17, size = 4))
```

### Linear models

In multiple linear regression, or linear models (LMs), the absolute value of the $t$-statistic (or some other scaled variant of the estimated coefficients) is commonly used as a measure of VI. The same idea also

[1]Technically, it's a tibble with an additional `"vi"` class.

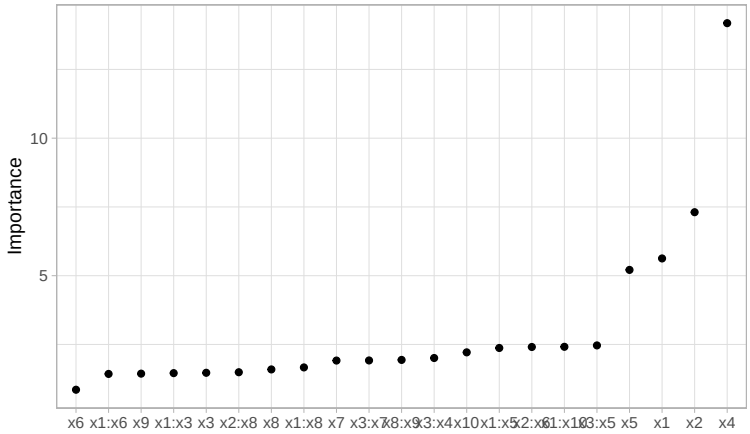


**Figure 3:** Example VIP from a linear model fit to the simulated Friedman data.

extends to generalized linear models (GLMs). In the code chunk below, we fit an LM to the simulated `trn` data set allowing for all main effects and two-way interactions, then use the `step()` function to perform backward elimination. The resulting VIP is displayed in Figure~3.

```
# Fit a LM
linmod <- lm(y ~ .^2, data = trn)
backward <- step(linmod, direction = "backward", trace = 0)

# Extract VI scores
(vi_backward <- vi(backward))
```

```
#> # A tibble: 21 x 3
#>    Variable Importance Sign
#>    <chr>         <dbl> <chr>
#>  1 x4            14.2  POS
#>  2 x2             7.31 POS
#>  3 x1             5.63 POS
#>  4 x5             5.21 POS
#>  5 x3:x5          2.46 POS
#>  6 x1:x10         2.41 NEG
#>  7 x2:x6          2.41 NEG
#>  8 x1:x5          2.37 NEG
#>  9 x10            2.21 POS
#> 10 x3:x4          2.01 NEG
#> # ... with 11 more rows
```

```
# Plot VI scores; by default, `vip()` displays the top ten features
vip(vi_backward, num_features = length(coef(backward)),
    geom = "point", horizontal = FALSE)
```

One issue with computing VI scores for LMs using the $t$-statistic approach is that a score is assigned to each term in the model, rather than to each individual feature! We can solve this problem using one of the model-agnostic approaches discussed later.

Multivariate adaptive regression splines (MARS), which were introduced in Friedman (1991), is an automatic regression technique and can be seen as a generalization of LMs and GLMs. In the MARS algorithm, the contribution (or VI score) for each predictor is determined using a generalized cross-validation (GCV) statistic (though, other statistics can also be used; see `?vip::vi_model` for details). An example using the **earth** package (Milborrow, 2017) is given below (the results are plotted in Figure~4):

```
# Load required packages
library(earth)

# Fit a MARS model
mars <- earth(y ~ ., data = trn, degree = 2, pmethod = "exhaustive")

# Extract VI scores
vi(mars, type = "gcv")
```

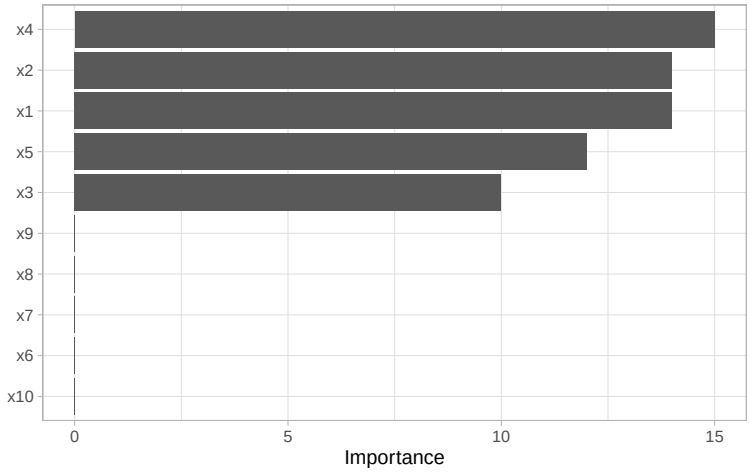


**Figure 4:** Example VIP from a MARS model fit to the simulated Friedman data.

```
#> # A tibble: 10 x 2
#>    Variable Importance
#>    <chr>         <dbl>
#>  1 x4            100
#>  2 x1             83.2
#>  3 x2             83.2
#>  4 x5             59.3
#>  5 x3             43.5
#>  6 x6              0
#>  7 x7              0
#>  8 x8              0
#>  9 x9              0
#> 10 x10             0

# Plot VI scores
vip(mars)
```

To access VI scores directly in **earth**, you can use the `earth::evimp()` function.

### Neural networks

For neural netwroks (NNs), two popular methods for constructing VI scores are the Garson algorithm (Garson, 1991), later modified by Goh (1995), and the Olden algorithm (Olden et al., 2004). For both algorithms, the basis of these VI scores is the network's connection weights. The Garson algorithm determines VI by identifying all weighted connections between the nodes of interest. Olden's algorithm, on the other hand, uses the products of the raw connection weights between each input and output neuron and sums these products across all hidden neurons. This has been shown to outperform the Garson method in various simulations. For DNNs, a similar method due to Gedeon (1997) considers the weights connecting the input features to the first two hidden layers (for simplicity and speed); but this method can be slow for large networks. We illustrate these two methods below using `vip()` with the **nnet** package (Venables and Ripley, 2002) (see the results in Figure~5).

```
# Load required packages
library(nnet)

# Fit a neural network
set.seed(0803)
nn <- nnet(y ~ ., data = trn, size = 7, decay = 0.1, linout = TRUE)

#> # weights:  85
#> initial  value 126298.176281
#> iter  10 value 5148.185025
#> iter  20 value 3563.828062
#> iter  30 value 3095.876922
#> iter  40 value 2638.672528
```

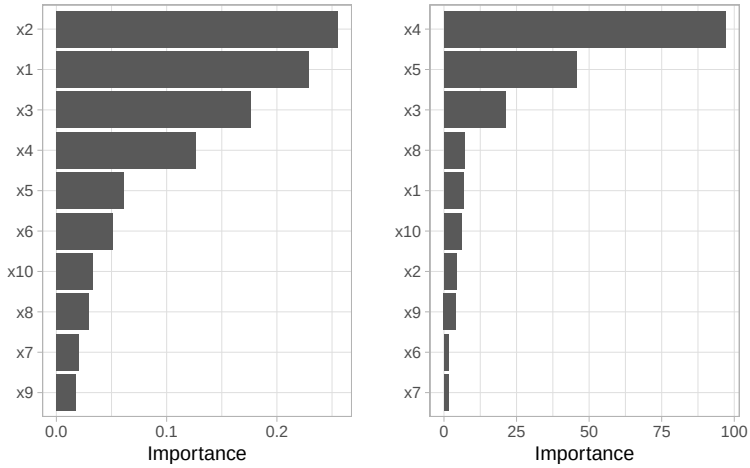


**Figure 5:** Example VIPs from a single-hidden-layer NN fit to the simulated Friedman data.

```
#> iter  50 value 1983.009001
#> iter  60 value 1759.428911
#> iter  70 value 1483.284575
#> iter  80 value 1112.219052
#> iter  90 value 835.941067
#> iter 100 value 748.120719
#> final  value 748.120719
#> stopped after 100 iterations

# VIPs
p1 <- vip(nn, type = "garson")
p2 <- vip(nn, type = "olden")

# Figure 5
grid.arrange(p1, p2, nrow = 1)
```

## Model-agnostic VI

Model-agnostic interpredibility separates interpretation from the model. Compared to model-specific approaches, model-agnostic VI methods are more flexible and can be applied to any supervised learning algorithm. In this section, we discuss model-agnostic methods for quantifying global feature importance using three different approaches: 1) partial dependence plots (PDPs), 2) *individual conditional expectation* (ICE) curves, and 3) permutation-based feature importance. For specific details on approaches 1)–2), see Greenwell et al. (2018).

### PDP method

Our first model-agnostic approach is based on quantifying the "flatness" of the PDPs of each feature. PDPs help visualize the effect of low cardinality subsets of the feature space on the estimated prediction surface (e.g., main effects and two/three-way interaction effects.). PDPs provide model-agnostic interpretations and can be constructed in the same way for any supervised learning algorithm; for an overview, see Greenwell (2017). Below, we fit a projection pursuit regression (PPR) model and construct PDPs for each feature using the **pdp** package Greenwell (2017). The results are displayed in Figure~6. Notice how the PDPs for the uninformative features are relatively flat compared to the PDPs for features `x1`–`x2`!

```
# Load required packages
library(pdp)

# Fit a PPR model (nterms was chosen using the caret package with 5 repeats of
# 5-fold cross-validation)
pp <- ppr(y ~ ., data = trn, nterms = 11)
```

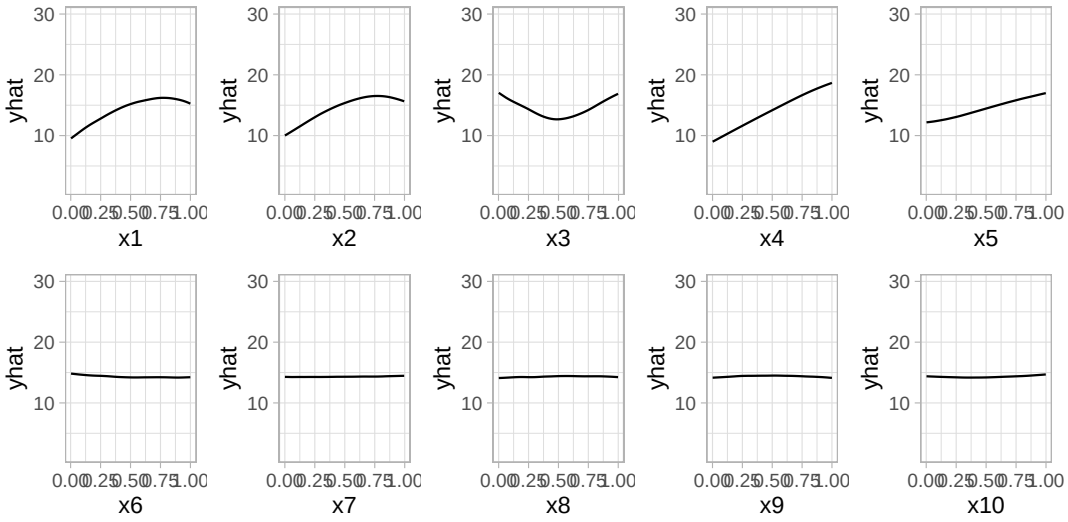


**Figure 6:** PDPs of main effects in the PPR model fit to the simulated Friedman data.

```
# PDPs for all 10 features
features <- paste0("x", 1:10)
pdps <- lapply(features, FUN = function(feature) {
  pd <- partial(pp, pred.var = feature)
  autoplot(pd) +
    ylim(range(trn$y)) +
    theme_light()
})
grid.arrange(grobs = pdps, ncol = 5)
```

Next, we compute PDP-based VI scores for the PPR and NN models. The PDP method constructs VI scores that quantify the relative "flatness" of each PDP (by default, this is defined by computing the standard deviation of the $y$-axis values for each PDP). To use the PDP method, specify `method = "pdp"` in the call to `vi()` or `vip()`:

```
# Fit a PPR model (nterms was chosen using the caret package with 5 repeats of
# 5-fold cross-validation)
pp <- ppr(y ~ ., data = trn, nterms = 11)

# Plot VI scores
p1 <- vip(pp, method = "pdp") + ggtitle("PPR")
p2 <- vip(nn, method = "pdp") + ggtitle("NN")

# Figure 7
grid.arrange(p1, p2, ncol = 2)
```

In Figure~7 we display the PDP-based feature importance for the previously obtained PPR and NN models. These VI scores essentially capture the variability in the partial dependence values for each main effect.

### ICE curve method

The ICE curve method is similar to the PDP method. The only difference is that we measure the "flatness" of each ICE curve and then aggregate the results (e.g., by averaging). If there are no (substantial) interaction effects, using `method = "ice"` will produce results similar to using `method = "pdp"`. However, if strong interaction effects are present, they can obfuscate the main effects and render the PDP-based approach less useful (since the PDPs for important features can be relatively flat when certain interactions are present; see Goldstein et al. (2015) for details). In fact, it is probably safest to always use `method = "ice"`.

Below, we display the ICE curves for each feature in the PPR model using the same $y$-axis scale; see Figure~8. Again, there is a clear difference between the ICE curves for features `x1`–`x5` and `x6`–`x10`; the later being relatively flat by comparison. Also, notice how the ICE curves within each feature are relatively parallel (if the ICE curves within each feature were perfectly parallel, the standard deviation

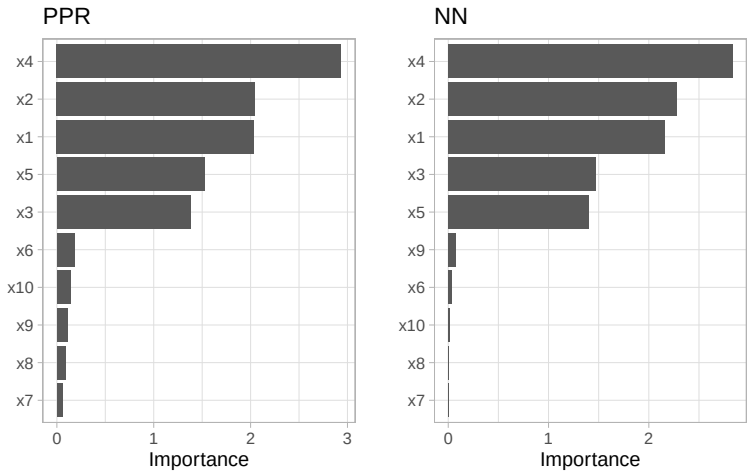


**Figure 7:** PDP-based feature importance for the PPR and NN models fit to the simulated Friedman data.

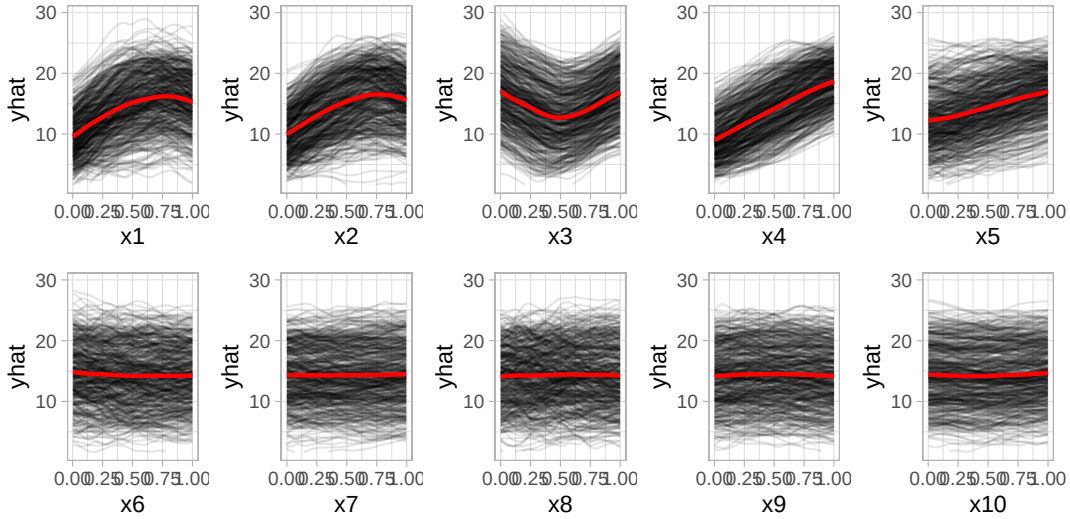


**Figure 8:** ICE curves for each feature in the PPR model fit to the simulated Friedman data. The red curve represents the PDP (i.e., the averaged ICE curves).

for each curve would be the same and the results will be identical to the PDP method). In this example, the interaction term between `x1` and `x2` does not obfuscate the PDPs for the main effects and the results are not much different.

```
# ICE curves for all 10 features
ice_curves <- lapply(features, FUN = function(feature) {
  ice <- partial(pp, pred.var = feature, ice = TRUE)
  autoplot(ice, alpha = 0.1) +
    ylim(range(trn$y)) +
    theme_light()
})

# Figure 8
grid.arrange(grobs = ice_curves, ncol = 5)
```

Obtaining the ICE-based feature importance scores is also straightforward, just specify `method = "ice"` in the call to `vip::vi()` or `vip::vip()`. This is illustrated in the code chunk below and the results are Figure~9 are similar to those obtained using the PDP method.

```
# Plot VI scores
p1 <- vip(pp, method = "ice") + ggtitle("PPR")
p2 <- vip(nn, method = "ice") + ggtitle("NN")
```

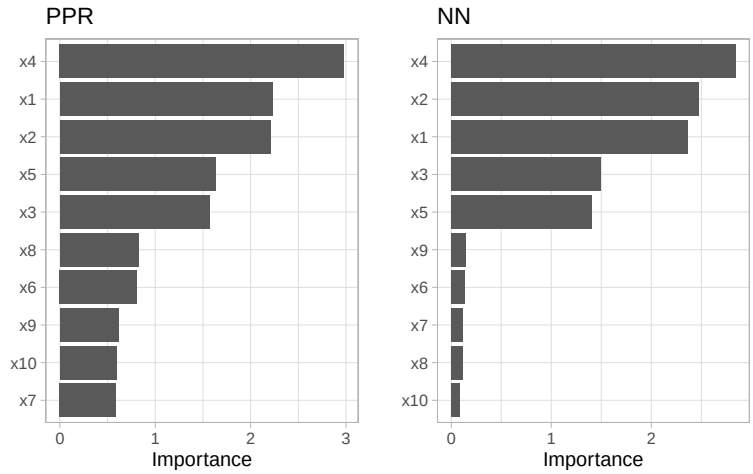


**Figure 9:** ICE-based feature importance for the PPR and NN models fit to the simulated Friedman data.

```
# Figure 9
grid.arrange(p1, p2, ncol = 2)
```

When using `method = "pdp"` or `method = "ice"`, the feature effect values are stored as attributes `"pdp"` and `"ice"`, respectively. This is a convenience so that the feature effect plots (e.g., PDPs and ICE curves) can easily be reconstructed and compared with the VI scores, as demonstrated in the example below (see Figure~10):

```
# Construct PDP-based variable importance scores
(vis <- vi(pp, method = "pdp"))
```

```
#> # A tibble: 10 x 2
#>    Variable Importance
#>    <chr>         <dbl>
#>  1 x4           2.93
#>  2 x2           2.05
#>  3 x1           2.04
#>  4 x5           1.53
#>  5 x3           1.38
#>  6 x6           0.183
#>  7 x10          0.139
#>  8 x9           0.113
#>  9 x8           0.0899
#> 10 x7           0.0558
```

```
# Reconstruct PDPs for all 10 features
par(mfrow = c(2, 5))
for (name in paste0("x", 1:10)) {
  plot(attr(vis, which = "pdp")[[name]], type = "l", ylim = c(9, 19), las = 1)
}
```

### Permutation method

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### Shapley method

Starting with **vip** 0.1.4 you can now construct VI scores based on *Shapley values* REF. Suppose we make a prediction for an observation $x\prime$, denoted $f(x\prime)$. The Shapley values for $f(x\prime)$...

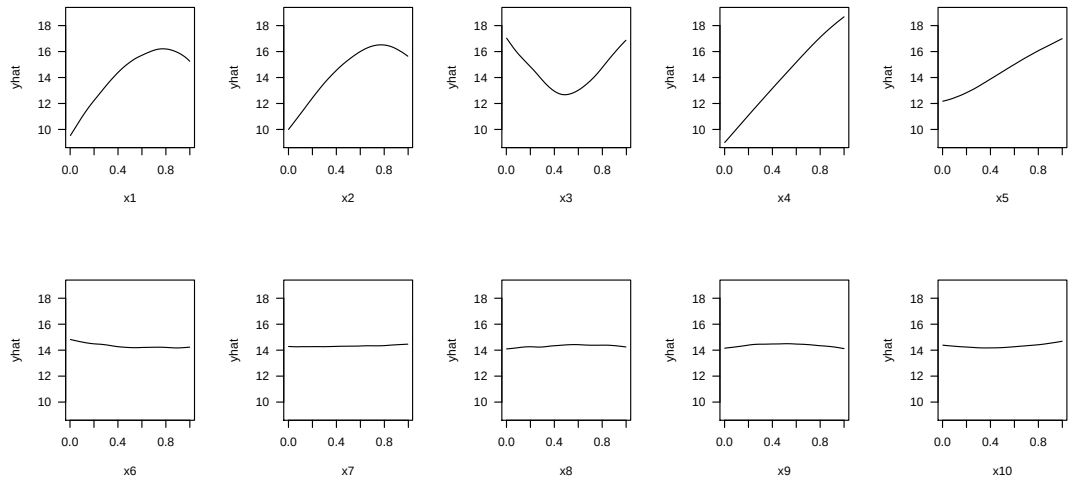


**Figure 10:** PDPs for all ten features reconstructed from the `pdp` attribute of the `vis` object.

1. For $i = 1, 2, \ldots, j$:
   (a) Permute the values of feature $X_i$ in the training data.
   (b) Recompute the performance metric on the permuted data $\mathcal{M}_{perm}$.
   (c) Record the difference from baseline using $imp\left(X_i\right) = \mathcal{M}_{perm} - \mathcal{M}_{orig}$.
2. Return the VI scores $imp\left(X_1\right), imp\left(X_2\right), \ldots, imp\left(X_j\right)$.

<!–
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**Algorithm 1:** A simple algorithm for constructing permutation-based VI scores.

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