



Considerations On Futility Rules For Adaptive Dose-Finding Designs

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Futility – Where Do We Stop?

- Futility stopping in two-armed confirmatory trials:
 - Stop the trial if interim results are worse than a predefined threshold (e.g., in terms of first stage p -value)
- Futility stopping in multi-armed confirmatory trials:
 - Stop the trial if global interim results are worse than a predefined threshold (e.g., in terms of first stage p -value for global hypothesis test)
 - Stop the trial if no treatment arm fulfills selection criteria (in case of conditional selection → implied futility stop)
 - Stop specific treatment arms
- Futility stopping in dose-finding trials?

Goals for Interim Analyses in Dose-Finding Trials

- Goals for interim analyses in dose-finding trials are generally different from those in confirmatory trials
- There is generally no early stopping for efficacy but rather...
 - Expanding a study if there is evidence for a drug-related effect (e.g., top-down design)
 - Gathering information on the dose-response relation in order to expand recruitment on the most promising doses
- In either case, it is desirable if a futile development programme does not advance to the second stage

Futility Stopping in Dose-Finding Trials

- Futility Stopping in dose-finding trials can have a different implication than it has in confirmatory trials
- Instead of stopping one trial only, the entire development programme can be affected
- Reasons for futility stopping in such trials can be
 - No evidence against a flat dose-response relationship
 - Evidence against a commercially viable effect

Motivating Example

- Development of a new compound in the Osteoarthritis indication
- Two-stage design is planned:
 - For the first stage, placebo and up to four active doses are available
 - Second stage can add one active dose if no futility stopping after first stage
 - 1.1 on the target scale is considered a commercially viable effect
- Which futility rules to choose?
- Does the number of doses affect the futility stop?
- What about first stage sample size?

Approach 1: Pairwise Testing For Any Difference

- Derived from later stage multiple comparison trials with limited number of doses
- Apply a futility boundary of α_0 to the global intersection null hypothesis

$$H_0 = \cap H_{0i}, H_{0i}: \mu_i \leq \mu_0$$

- Multiplicity correction needed (here, Dunnett considered throughout)
- What is the impact of the number of doses in the first stage?
 - E.g., comparison of top-down approach vs equal allocation to all available doses

Approach 2: Model-Based Testing for Any Difference

- Uses MCPMod approach:
 - Prespecify a number of candidate models
 - Derive optimal contrasts for these models in dependence of the planned allocation to the first stage doses
- Apply a futility boundary to the resulting multiple contrast test for the existence of a drug-related effect
- Multiplicity penalty is lower than in Approach 1

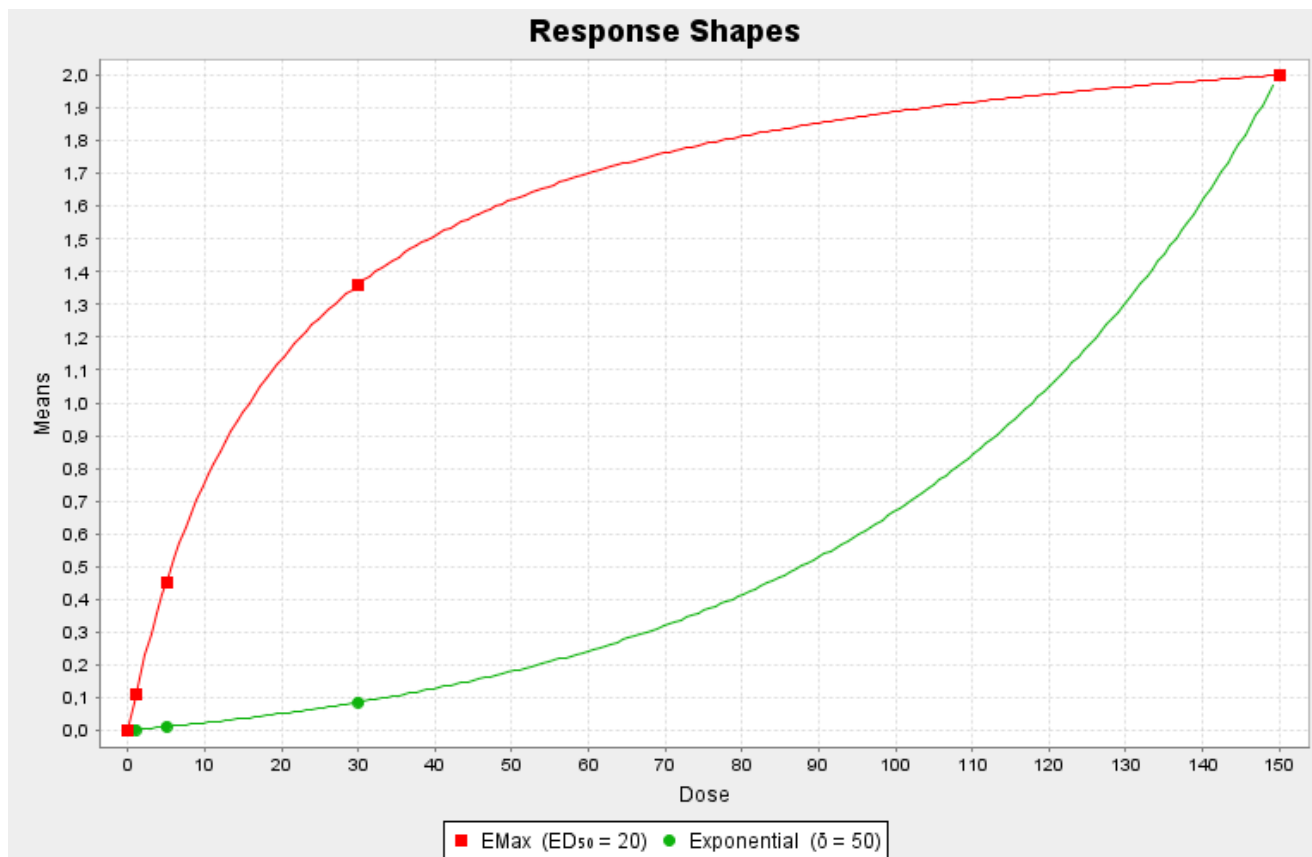
Approach 1 & Approach 2

- Both approaches control the probability of continuing development when there is no drug-related effect
- Probability of continuing development when there is a true benefit is not controlled
- Impacting the latter probability requires appropriate sample size for the first stage

Revisit Example

- Active doses for first stage are 1 mg, 5 mg, 30 mg, 150 mg
- Total sample size for first stage is set to 120 patients (including placebo patients)
- For simulations, we assume a maximum effect of 2 on the target scale (standard deviation: 4) and two different true dose-response shapes:
 - An EMax model with ED_{50} at 20 mg ($\eta(d) = e_{\max} \times d / (d + 20)$)
 - An exponential model with $\delta=50$ ($\eta(d) = e_{\max} \times (\exp\{d/50\} - 1)$)

Example Response Shapes



Example Revisited

- Consider the following possible allocations in the first stage:

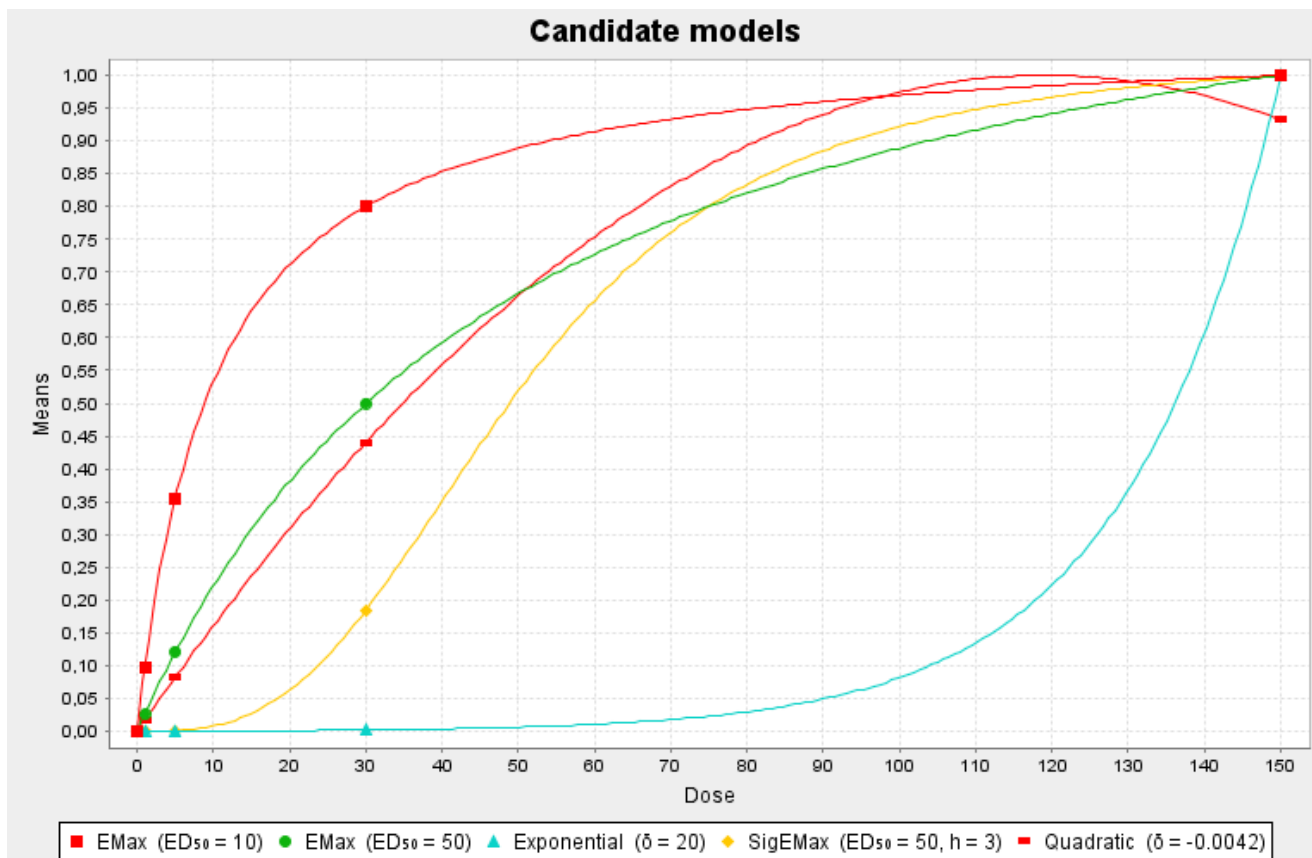
	PLA	1 mg	5 mg	30 mg	150 mg
D1	0.5	0	0	0	0.5
D2	0.2	0.2	0.2	0.2	0.2
D3	0.4	0	0	0.2	0.4

Example Revisited

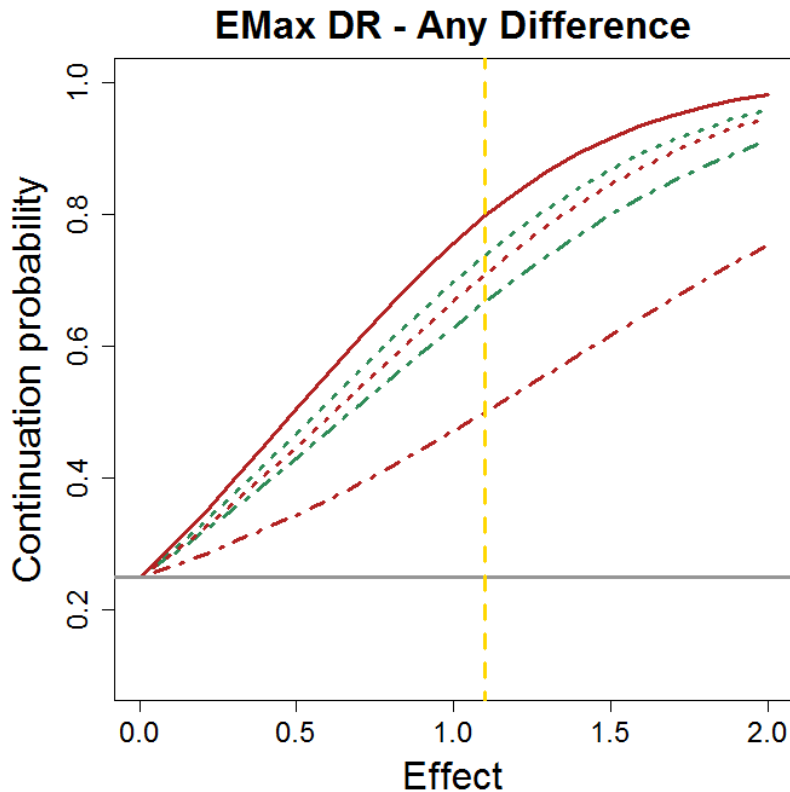
- For the model-based contrasts, assume the following candidate dose-response shapes:

Model	Parameter(s)
EMax	$ED_{50} = 10$
EMax	$ED_{50} = 50$
Sigmoid EMax	$ED_{50} = 50, h = 3$
Exponential	$\delta = 20$
Quadratic	$\delta = -1/240$

Candidate Models

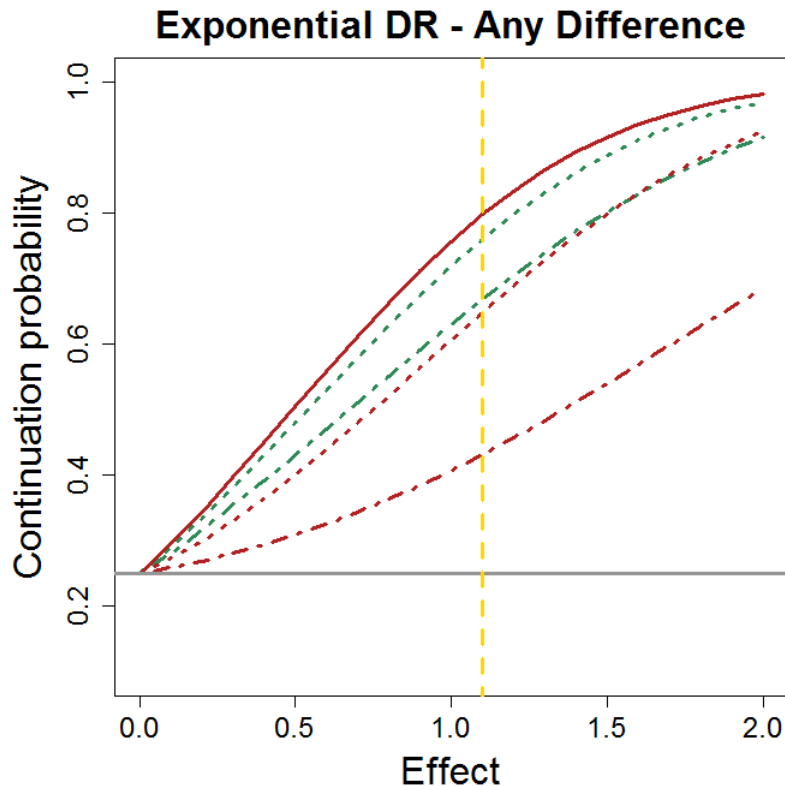


Approach 1 & 2: True Shape EMax



- Red: Pairwise comparisons
- Green: Model-based contrasts
- Solid: D1 (top down)
- Dash-dot: D2 (equal)
- Dotted: D3
- Grey reference line: α_0
- Yellow reference line: TV

Approach 1 & 2: True Shape Exponential



- Red: Pairwise comparisons
- Green: Model-based contrasts
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Approach 3: Pairwise Testing for Target Value

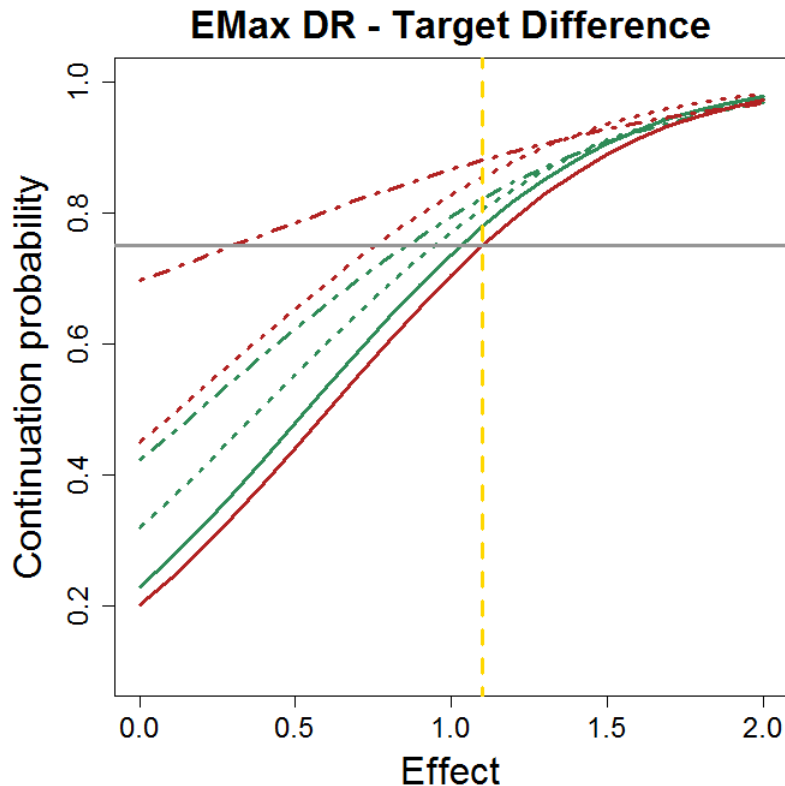
- Complementary approach: Control probability of a development stop in case of true benefit
- Consider testing the following null hypothesis:
$$H_0: \{\mu_1 \geq \mu_0 + TV\} \cup \{\mu_2 \geq \mu_0 + TV\} \cup \dots \cup \{\mu_k \geq \mu_0 + TV\}$$
- Stop for futility if H_0 can be rejected at level α_0 (implies that true effect for all doses is below TV)
- No multiplicity adjustment required

Approach 4: Model-Based Testing for Target Value

- The model-based approach uses the model-based estimators for the maximum treatment effect
- $\hat{\Delta}_g$ denotes the estimated maximum treatment effect for model g
- Then recommend stopping for futility if

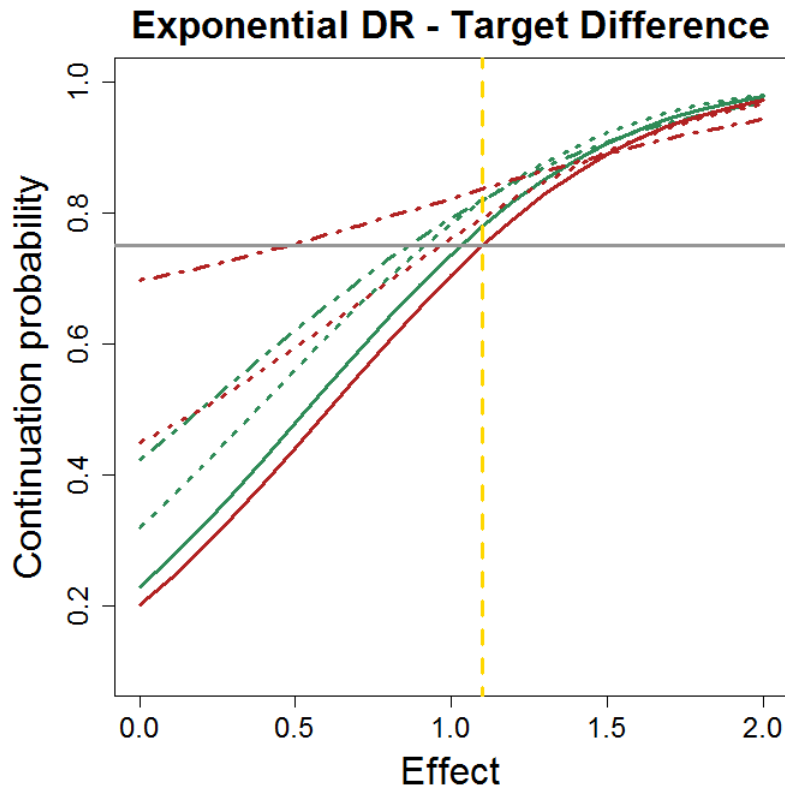
$$\min_{g=1,\dots,5} \sqrt{N_1} \frac{TV - \hat{\Delta}_g}{\sqrt{\sigma^2 c_g^T W^{-1} c_g}} > z_{1-\alpha_0}$$

Approach 3 & 4: True Shape EMax



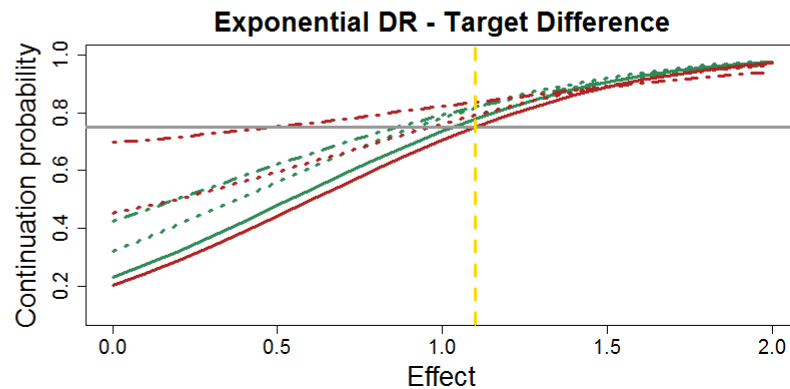
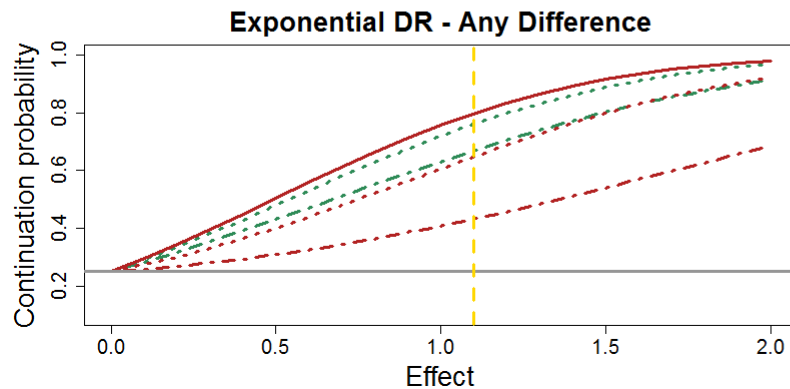
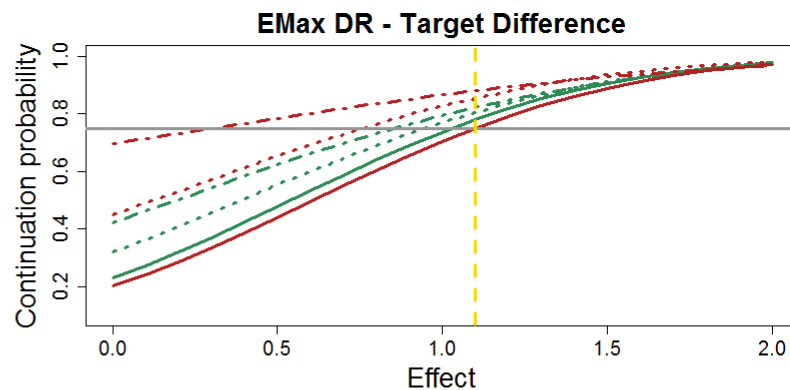
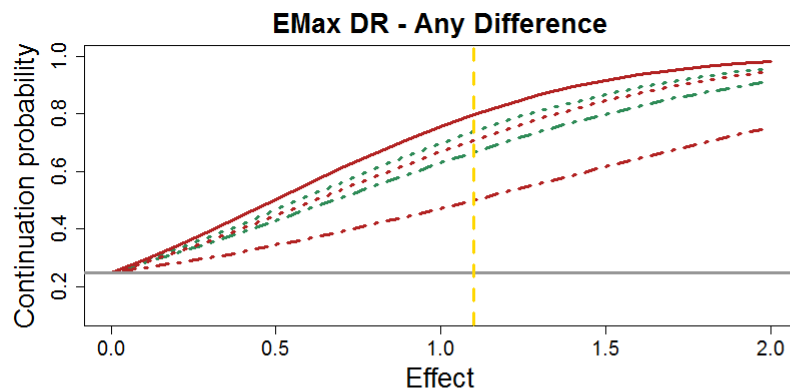
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Approach 3 & 4: True Shape Exponential



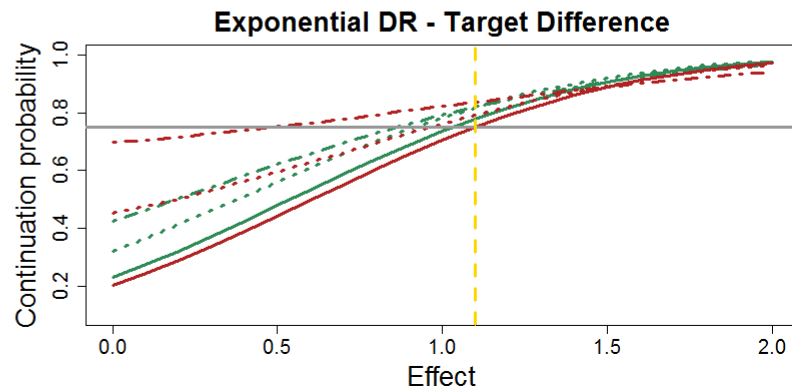
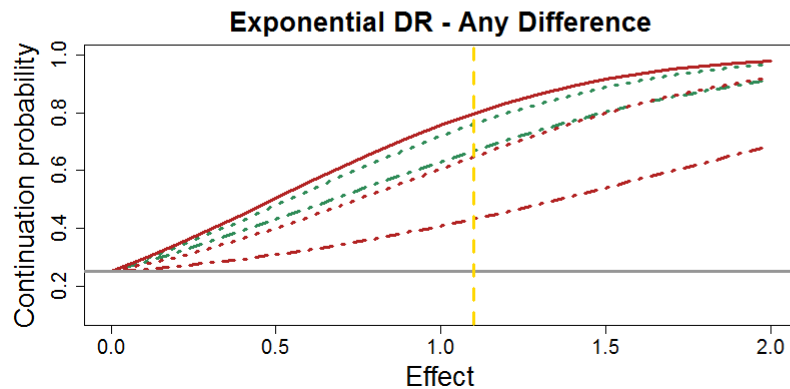
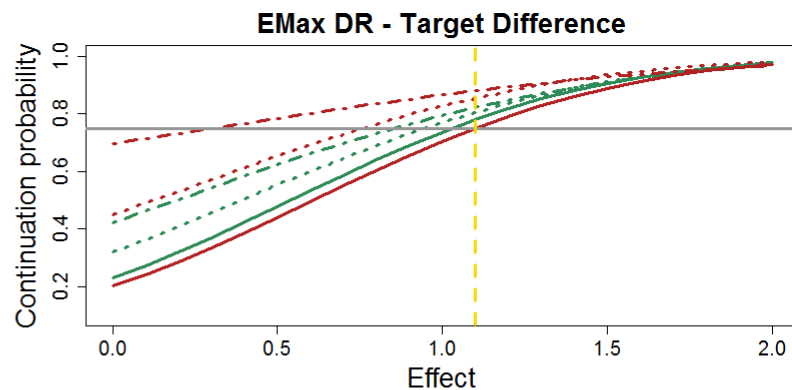
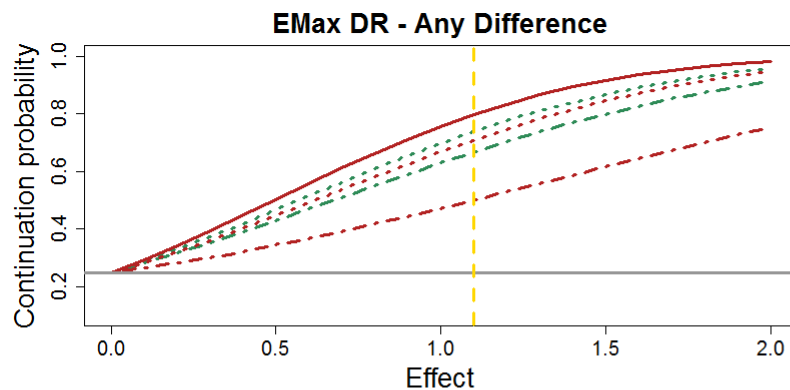
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All Together...

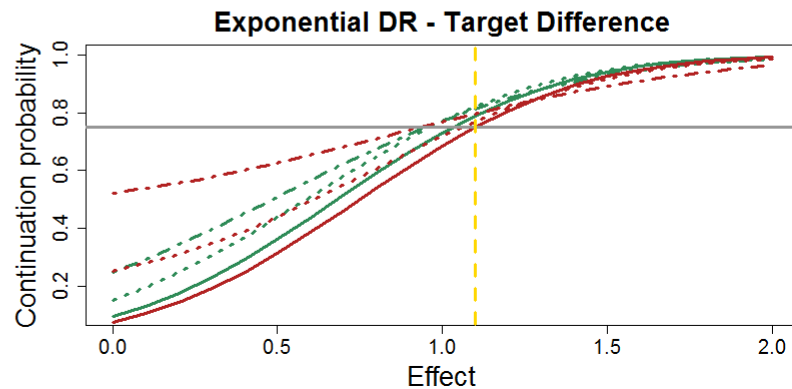
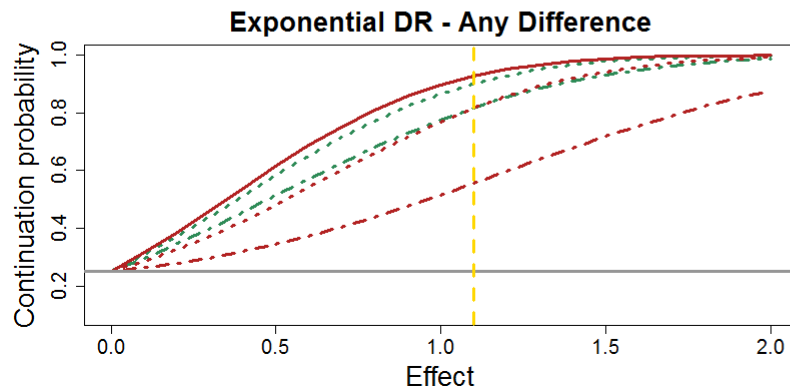
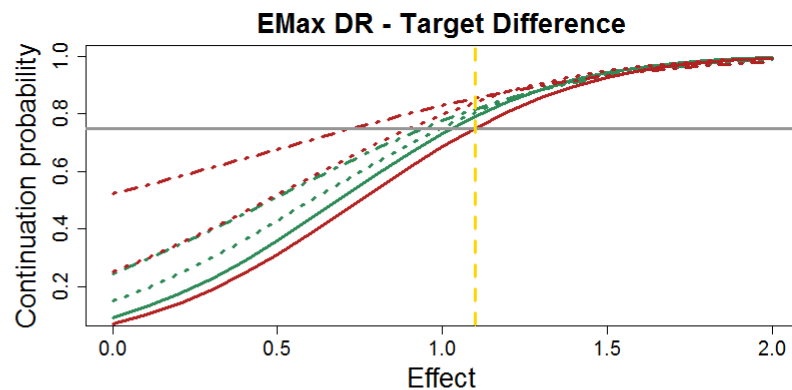
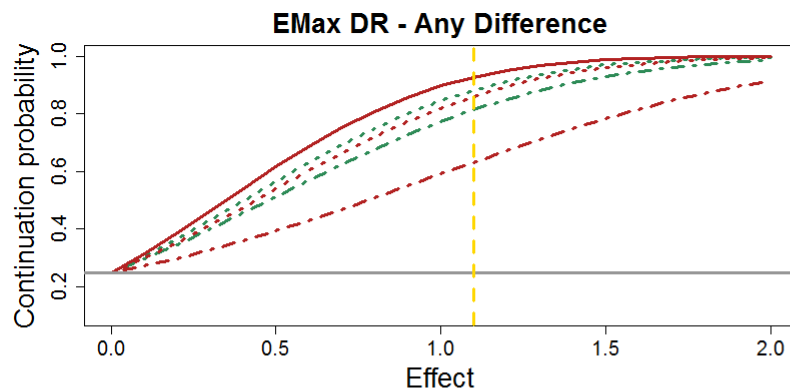


Interim Summary

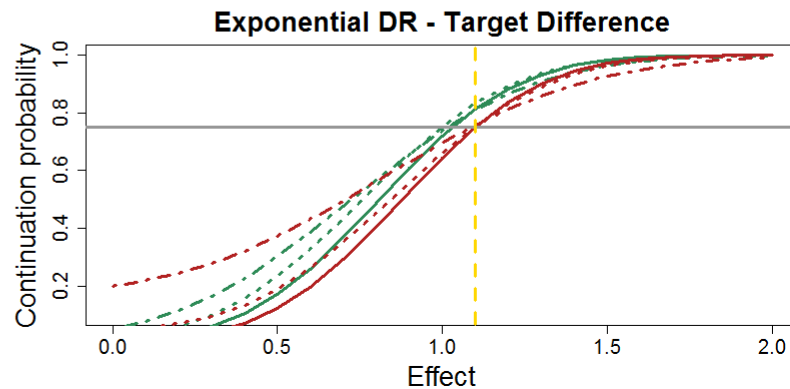
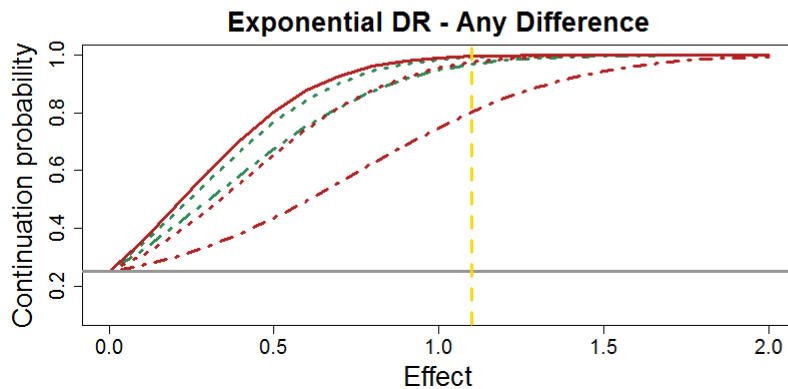
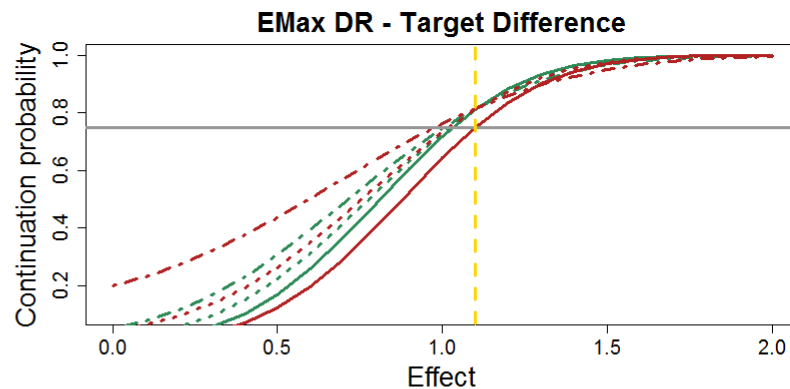
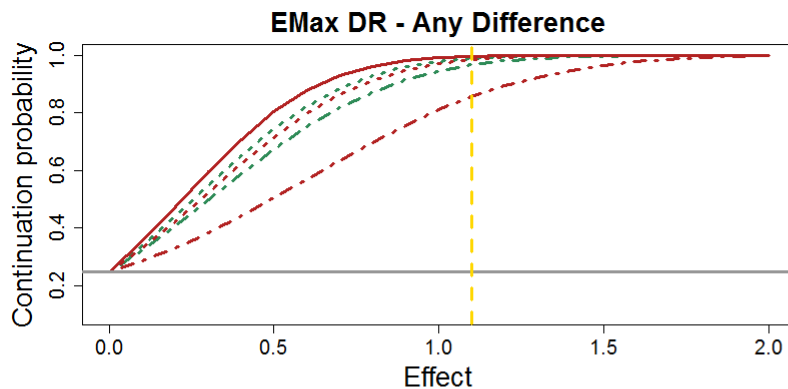
- Hard requirements are fulfilled in both cases:
 - Stopping probability is controlled at α_0 in the Any Difference case
 - Continuation probability is controlled at $1 - \alpha_0$ in the Target Value case
- With the considered sample size, curves for Target Value case are too smooth
- For investigation of sample size impact, consider sample sizes of 120 (as before), 240 and 600



Total N 240



Total N 600



Summary

- Sensitivity of futility stopping boundaries depend on number of doses tested and sample size
- Pairwise comparison procedures suffer from multiplicity penalty (Any Difference) and from lack of power for individual hypotheses (Target Value)
- The „Target Value“ approach can improve identification of promising developments
- Model based techniques can improve discrimination between promising and futile developments, especially in the case of many doses
- Increasing the first stage sample size increases the continuation probability uniformly in the Any Difference case but increases the selectivity in the Target Value case

Software Solution

- ADDPLAN DF 4.0 partly incorporates these methods:
 - Multi stage designs available in simulation module for MCPMod and Nonlinear Regression
- Options for futility stopping are
 - Pairwise comparisons at α_0
 - Model-based test at α_0
 - Test for target effect difference at α_0

Multi Stage Designs

✓ Computation options ✓ Recruitment options ✓ Design options »2

of stages
K = 2

of treatment arms
G = 5

Significance level
 $\alpha =$ 0.025

Alternative
☒ one-sided ☐ two-sided

Direction
☒ increasing ☐ decreasing

Model selection
☒ AIC ☐ average AIC ☐ maxT

Fit all models
☐ Fit all models

TD/ED
☒ TD $\Delta =$ 0.1 ☐ ED $p =$ 0.5
Effect difference Means

Treatment arms

✓	Dose 1	Dose 2	Dose 3	Dose 4	Dose 5	
Doses	0	1	5	30	150	

of simulations
of simulations = 100

Ongoing trial
☐ Simulate trial Start stage = 2

Random seed
Seed =

Design Options for Stage 1

✓ Design stage 1 ✕ ✓ Design stage 2

Early futility stopping

Futility rule Pairwise comparison ▼

☐ Proof of concept $\alpha_0 =$

✓ Design stage 1 ✕ ✓ Design stage 2

Early futility stopping

Futility rule Model based test ▼

☐ Proof of concept $\alpha_0 =$

✓ Design stage 1 ✕ ✓ Design stage 2

Early futility stopping

Futility rule Target effect difference ▼

☐ Proof of concept $\alpha_0 =$ Continuation prob. = Target diff. =

References

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Thank you!

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