# 3.13 Unit Step Response

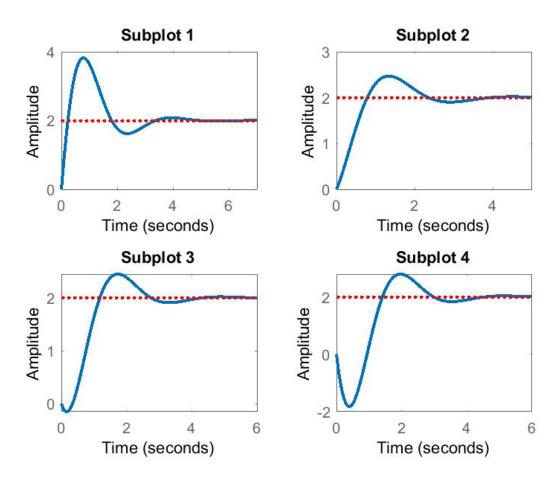
Four systems and four unit step responses are given below. Match each system to its unit step response.

(a) 
$$G_A(s) = \frac{-2s+10}{s^2+2s+5}$$

(b) 
$$G_B(s) = \frac{-10s+10}{s^2+2s+5}$$

(c) 
$$G_c(s) = \frac{2s+10}{s^2+2s+5}$$

(d) 
$$G_D(s) = \frac{10s+10}{s^2+2s+5}$$



## **Solution:**

Subplot1:  $G_D(s)$ Subplot2:  $G_C(s)$ Subplot3:  $G_A(s)$ Subplot4:  $G_B(s)$ 

#### **GPT Answer:**

To match each system with its unit step response, we consider the signs and coefficients in the transfer functions and compare them with the characteristics of the step responses.

- $G_C(s)$  corresponds to Subplot 1 due to the positive initial slope and positive steady-state.
- $G_B(s)$  or  $G_A(s)$  could correspond to Subplot 2 since it seems to approach zero, but this is ambiguous.
- $G_A(s)$  corresponds to Subplot 3 due to the negative initial slope and positive steady-state.
- $G_B(s)$  corresponds to Subplot 4 due to the negative initial slope and negative steady-state.

### **Confidence Level: 75%**

## **Reasoning Error**

#### **Calude Answer:**

Matching each subplot to one of the given transfer functions:

- Subplot 1:  $G_C(s) = \frac{2s+10}{s^2+2s+5}$
- Subplot 2:  $G_D(s) = \frac{10s+10}{s^2+2s+5}$
- Subplot 3:  $G_A(s) = \frac{-2s+10}{s^2+2s+5}$
- Subplot 4:  $G_B(s) = \frac{-10s+10}{s^2+2s+5}$

The reasoning is as follows:

- Subplots 1 and 2 have positive steady-state values, corresponding to the positive numerator coefficients in  $G_C(s)$  and  $G_D(s)$ .
- Subplot 2 has a higher steady-state value than Subplot 1, matching the larger numerator coefficient sum of 20 in  $G_D(s)$  compared to 12 in  $G_C(s)$ .
- Subplots 3 and 4 have negative dips, corresponding to the negative numerator coefficients in  $G_A(s)$  and  $G_B(s)$ .
- Subplot 4 has a larger negative dip than Subplot 3, matching the larger negative coefficient of -10 in  $G_B(s)$  compared to -2 in  $G_A(s)$ .

Confidence level: 98%

**Reasoning Error**