3.7 Unit Step Response

The output in response to a unit step function input for a particular continuous control system is

$$c(t) = 1 - e^{-t}.$$

What is the delay time T_d ?

Solution:

The output is given as a function of time. The final value of the output is $\lim_{t\to\infty} c(t) = 1$. Hence T_d (at 50% of the final value) is the solution of

$$0.5 = 1 - e^{-T_d}$$

and is equal to $\log_e(2)$, or 0.693.

GPT Answer:

The delay time T_d in a control system is defined as the time required for the system's response to reach 50

$$c(t) = 1 - e^{-t},$$

we set c(t) = 0.5 to find the delay time. This corresponds to the system's response reaching 50

$$0.5 = 1 - e^{-t} \Rightarrow e^{-t} = 0.5 \Rightarrow -t = \ln(0.5) \Rightarrow t = -\ln(0.5).$$

Thus, the delay time T_d is given by $T_d = -\ln(0.5)$.

Confidence Level: 95%

Correct

Claude Answer:

To find the delay time T_p for this system, let's follow these steps:

- 1. The delay time is defined as the time required for the output to reach 50% of its final value in response to a unit step input.
- 2. We know the final value of the output is 1, so we need to find the time at which the output reaches 0.5.
- 3. We can set up an equation:

$$c(T_p) = 0.5 = 1 - e^{-T_p}$$

4. Solve for T_p :

$$0.5 = 1 - e^{-T_p}$$

$$e^{-T_p} = 0.5$$

$$-T_p = \ln(0.5)$$

$$T_p = -\ln(0.5) = \ln(2) \approx 0.693$$

Therefore, the delay time T_p for this system is approximately 0.693 time units. Confidence Level: 95%

Correct