

# 14 Lectures on Visual SLAM

## From Theory to Practice

Xiang Gao, Tao Zhang, Qinrui Yan and Yi Liu

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# Preface for English Version

A lot of friends at github asked me about this English version. I'm really sorry it takes so long to do the translation, and I'm glad to make it public available to help the readers. I encountered some issues on math equation in the web pages. Since the book is originally written in LaTeX, I'm going to release the LaTeX source along with the compiled pdf. You can directly access the pdf version for English book, and probably the publishing house is going to help me do the paper version.

As I'm not a native English speaker, the translation work is basically based on Google translation and some afterwards modification. If you think the quality of translation can be improved and you are willing to do this, please contact me or send an issue on github. Any help will be welcome!

Xiang



# Chapter 1

## Preface

### 1.1 What is this book about?

This is a book introducing visual SLAM, and it is probably the first Chinese book solely focused on this specific topic.

So, what is SLAM?

SLAM stands for **S**imultaneous **L**ocalization and **M**apping. It usually refers to a robot or a moving rigid body, equipped with a specific **sensor**, estimates its own **motion** and builds a **model** (certain kinds of description) of the surrounding environment, without a *priori* information[1]. If the sensor referred here is mainly a camera, it is called "**Visual SLAM**".

Visual SLAM is the subject of this book. We deliberately put a long definition into one single sentence, so that the readers can have a clear concept. First of all, SLAM aims at solving the "positioning" and "map building" issues at the same time. In other words, it is a problem of how to estimate the location of a sensor itself, while estimating the model of the environment. So how to achieve it? This requires a good understanding of sensor information. A sensor can observe the external world in a certain form, but the specific approaches for utilizing such observations are usually different. And, why is this problem worth spending an entire book to discuss? Simply because it is difficult, especially if we want to do SLAM in **real time** and **without any a priory knowledge**. When we talk about visual SLAM, we need to estimate the trajectory and map based on a set of continuous images (which form a video).

This seems to be quite intuitive. When we human beings enter an unfamiliar environment, aren't we doing exactly the same thing? So, the question is whether we can write programs and make computers do so.

At the birth of computer vision, people imagined that one day computers could act like human, watching and observing the world, and understanding the surrounding environment. The ability of exploring unknown areas is a wonderful and romantic dream, attracting numerous researchers striving on this problem day and night [? ]. We thought that this would not be that difficult, but the progress turned out to be not as smooth as expected. Flowers, trees, insects, birds and animals, are recorded so differently in computers: they are simply matrices consisted of numbers. To make computers understand the contents of images, is as difficult as making us human understand those blocks of numbers. We didn't even know how we understand images, nor do we know how to make computers do so. However, after decades of

struggling, we finally started to see signs of success - through Artificial Intelligence (AI) and Machine Learning (ML) technologies, which gradually enable computers to identify objects, faces, voices, texts, although in a way (probabilistic modeling) that is still so different from us. On the other hand, after nearly three decades of development in SLAM, our cameras begin to capture their movements and know their positions, although there is still a huge gap between the capability of computers and human. Researchers have successfully built a variety of real-time SLAM systems. Some of them can efficiently track their own locations, and others can even do three-dimensional reconstruction in real-time.

This is really difficult, but we have made remarkable progress. What's more exciting is that, in recent years, we have seen emergence of a large number of SLAM-related applications. The sensor location could be very useful in many areas: indoor sweeping machines and mobile robots, automatic driving cars, Unmanned Aerial Vehicles (UAVs) in the air, Virtual Reality (VR) and Augmented Reality (AR). SLAM is so important. Without it, the sweeping machine cannot maneuver in a room autonomously, but wandering blindly instead; domestic robots can not follow instructions to reach a certain room accurately; Virtual Reality will always be limited within a prepared space. If none of these innovations could be seen in real life, what a pity it would be.

Today's researchers and developers are increasingly aware of the importance of the SLAM technology. SLAM has over 30 years of research history, and it has been a hot topic in both robotics and computer vision communities. Since the 21st century, visual SLAM technology has undergone a significant change and breakthrough in both theory and practice, and is gradually moving from laboratories into real-world. At the same time, we regretfully find that, at least in the Chinese language, SLAM-related papers and books are still very scarce, making many beginners of this area unable to get started smoothly. Although the theoretical framework of SLAM has basically become mature, to implement a complete SLAM system is still very challenging and requires high level of technical expertise. Researchers new to the area have to spend a long time learning a significant amount of scattered knowledge, and often have to go through a number of detours to get close to the real core.

This book systematically explains the visual SLAM technology. We hope that it will (at least in part) fill the current gap. We will detail SLAM's theoretical background, system architecture, and the various mainstream modules. At the same time, we place great emphasis on practice: all the important algorithms introduced in this book will be provided with runnable code that can be tested by yourself, so that readers can reach a deeper understanding. Visual SLAM, after all, is a technology for application. Although the mathematical theory can be beautiful, if you are not able to convert it into lines of code, it will be like a castle in the air, which brings little practical impact. We believe that practice verifies true knowledge, and practice tests true passion. Only after getting your hands dirty with the algorithms, you can truly understand SLAM, and claim that you have fallen in love with SLAM research.

Since its inception in 1986 [2], SLAM has been a hot research topic in robotics. It is very difficult to give a complete introduction to all the algorithms and their variants in the SLAM history, and we consider it as unnecessary as well. This book will be firstly introducing the background knowledge, such as projective geometry, computer vision, state estimation theory, Lie Group and Lie algebra, etc. On top of that, we will be showing the trunk of the SLAM tree, and omitting those complicated and oddly-shaped leaves. We think this is effective. If the reader can master the

essence of the trunk, they have already gained the ability to explore the details of the research frontier. So our aim is to help SLAM beginners quickly grow into qualified researchers and developers. On the other hand, even if you are already an experienced SLAM researcher, this book may still reveal areas that you are unfamiliar with, and may provide you with new insights.

There have already been a few SLAM-related books around, such as "Probabilistic Robotics" [3], "Multiple View Geometry in Computer Vision" [4], "State Estimation for Robotics: A Matrix-Lie-Group Approach"[? ], etc. They provide rich contents, comprehensive discussions and rigorous derivations, and therefore are the most popular textbooks among SLAM researchers. However, there are two important issues: Firstly, the purpose of these books is often to introduce the fundamental mathematical theory, with SLAM being only one of its applications. Therefore, they cannot be considered as specifically visual SLAM focused. Secondly, they place great emphasis on mathematical theory, but are relatively weak in programming. This makes readers still fumbling when trying to apply the knowledge they learn from the books. Our belief is: only after coding, debugging and tweaking algorithms and parameters with his own hands, one can claim real understanding of a problem.

In this book, we will be introducing the history, theory, algorithms and research status in SLAM, and explaining a complete SLAM system by decomposing it into several modules: visual odometry, back-end optimization, map building, and loop closure detection. We will be accompanying the readers step by step to implement the core algorithms of each module, explore why they are effective, under what situations they are ill-conditioned, and guide them through running the code on their own machines. You will be exposed to the critical mathematical theory and programming knowledge, and will use various libraries including Eigen, OpenCV, PCL, g2o, and Ceres, and master their use in the Linux operating system.

Well, enough talking, wish you a pleasant journey!

## 1.2 How to use this book?

This book is entitled "14 Lectures on Visual SLAM". As the name suggests, we will organize the contents into "lectures" like we are learning in a classroom. Each lecture focuses on one specific topic, organized in a logical order. Each chapter will include both a theoretical part and a practical part, with the theoretical usually coming first. We will introduce the mathematics essential to understand the algorithms, and most of the time in a narrative way, rather than in a "definition, theorem, inference" approach adopted by most mathematical textbooks. We think this will be much easier to understand, but of course with a price of being less rigorous sometimes. In practical parts, we will provide code and discuss the meaning of the various parts, and demonstrate some experimental results. So, when you see chapters with the word "practice" in the title, you should turn on your computer and start to program with us, joyfully.

The book can be divided into two parts: The first part will be mainly focused on the fundamental math knowledge, which contains:

1. Lecture 1: preface (the one you are reading now), introducing the contents and structure of the book.
2. Lecture 2: an overview of a SLAM system. It describes each module of a SLAM system and explains what they do and how they do it. The practice

section introduces basic C++ programming in Linux environment and the use of an IDE.

3. Lecture 3: rigid body motion in 3D space. You will learn knowledge about rotation matrices, quaternions, Euler angles, and practice them with the Eigen library.
4. Lecture 4: Lie group and Lie algebra. It doesn't matter if you have never heard of them. You will learn the basics of Lie group, and manipulate them with Sophus.
5. Lecture 5: pinhole camera model and image expression in computer. You will use OpenCV to retrieve camera's intrinsic and extrinsic parameters, and then generate a point cloud using the depth information through PCL (Point Cloud Library).
6. Lecture 6: nonlinear optimization, including state estimation, least squares and gradient descent methods, e.g. Gauss-Newton and Levenburg-Marquardt. You will solve a curve fitting problem using the Ceres and g2o library.

From lecture 7, we will be discussing SLAM algorithms, starting with Visual Odometry (VO) and followed by the map building problems:

7. Lecture 7: feature based visual odometry, which is currently the mainstream in VO. Contents include feature extraction and matching, epipolar geometry calculation, Perspective-n-Point (PnP) algorithm, Iterative Closest Point (ICP) algorithm, and Bundle Adjustment (BA), etc. You will run these algorithms either by calling OpenCV functions or by constructing you own optimization problem in Ceres and g2o.
8. Lecture 8: direct (or intensity-based) method for VO. You will learn the principle of optical flow and direct method, and then use g2o to achieve a simple RGB-D direct method based VO (the optimization in most direct VO algorithms will be more complicated).
9. Lecture 9: back-end optimization. We will discuss Bundle Adjustment in detail, and show the relationship between its sparse structure and the corresponding graph model. You will use Ceres and g2o separately to solve a same BA problem.
10. Lecture 10: pose graph in the back-end optimization. Pose graph is a more compact representation for BA which marginalizes all map points into constraints between keyframes. You will use g2o and gtsam to optimize a pose graph.
11. Lecture 11: loop closure detection, mainly Bag-of-Word (BoW) based method. You will use dbow3 to train a dictionary from images and detect loops in videos.
12. Lecture 12: map building. We will discuss how to estimate the depth of feature points in monocular SLAM (and show why they are unreliable). Compared with monocular depth estimation, building a dense map with RGB-D cameras is much easier. You will write programs for epipolar line search and patch matching to estimate depth from monocular images, and then build a point cloud map and octagonal tree map from RGB-D data.



13. Lecture 13: a practice chapter for VO. You will build a visual odometer framework by yourself by integrating the previously learned knowledge, and solve problems such as frame and map point management, key frame selection and optimization control.
14. Lecture 14: current open source SLAM projects and future development direction. We believe that after reading the previous chapters, you will be able to understand other people's approaches easily, and be capable to achieve new ideas of your own.

Finally, if you don't understand what we are talking about at all, congratulations! This book is right for you!

## 1.3 Source code

All source code in this book is hosted on github:

<https://github.com/gaoxiang12/slambook2>

Note the slambook2 refers to the second version which I added a lot of extra experiments.

It is strongly recommended that readers download them for viewing at any time. The code is divided by chapters, for example, the contents of the 7th lecture will be placed in folder "ch7". In addition, some of the small libraries used in the book can be found in the "3rd party" folder as compressed packages. For large and medium-sized libraries like OpenCV, we will introduce their installation methods when they first appear. If you have any questions regarding the code, click the "Issues" button on GitHub to submit. If there is indeed a problem with the code, we will make changes in a timely manner. Even if your understanding is biased, we will still reply as much as possible. If you are not accustomed to using Git, you can also click the button on the right which contains the word "download" to download a zipped file to your local drive.

## 1.4 Oriented readers

This book is for students and researchers interested in SLAM. Reading this book needs certain prerequisites, we assume that you have the following knowledge:

- Calculus, Linear Algebra, Probability Theory. These are the fundamental mathematical knowledge that most readers should have learned during undergraduate study. You should at least understand what a matrix and a vector are, and what it means by doing differentiation and integration. For more advanced mathematical knowledge required, we will introduce in this book as we proceed.
- Basic C++ Programming. As we will be using C++ as our major programming language, it is recommended that the readers are at least familiar with its basic concepts and syntax. For example, you should know what a class is, how to use the C++ standard library, how to use template classes, etc. We will try our best to avoid using tricks, but in certain situations we really can not avert. In addition, we will adopt some of C++ 11 standard, but don't worry, they will be explained as they appear.

- **Linux Basics.** Our development environment is Linux instead of Windows, and we will only provide source code for Linux. **We believe that mastering Linux is an essential skill for SLAM researchers, and please take it to begin. After going through the contents of this book, we believe you will agree with us**<sup>①</sup>. In Linux, the configuration of related libraries is so convenient, and you will gradually appreciate the benefit of mastering it. If you have never used a Linux system, it will be beneficial if you can find some Linux learning materials and spend some time reading them (to master Linux basics, the first few chapters of an introductory book should be sufficient). We do not ask readers to have superb Linux operating skills, but we do hope readers at least know how to fire an terminal, and enter a code directory. There are some self-test questions on Linux at the end of this chapter. If you have answers to them, you shouldn't have much problem in understanding the code in this book.

Readers interested in SLAM but do not have the above mentioned knowledge may find it difficult to proceed with this book. If you do not understand the basics of C++, you can read some introductory books such as *C++ Primer Plus*. If you do not have the relevant math knowledge, we also suggest that you read some relevant math textbooks first. Nevertheless, we think that most readers who have completed undergraduate study should already have the necessary mathematical arsenal. Regarding the code, we recommend that you spend time typing them by yourself, and tweaking the parameters to see how they affect outputs. This will be very helpful.

This book can be used as a textbook for SLAM-related courses, but also suitable as extra-curricular self-study materials.

## 1.5 Style

This book covers both mathematical theory and programming implementation. Therefore, for the convenience of reading, we will be using different layouts to distinguish different contents.

1. Mathematical formulas will be listed separately, and important formulas will be assigned with an equation number on the right end of the line, for example:

$$\mathbf{y} = \mathbf{A}\mathbf{x}. \quad (1.1)$$

Italics are used for scalars, e.g.,  $a$ . Bold italics are used for vectors and matrices, e.g.  $\mathbf{a}$ ,  $\mathbf{A}$ . Hollow bold represents special sets, e.g. real number  $\mathbb{R}$  and integer set  $\mathbb{Z}$ . Gothic is used for Lie Algebra, e.g.  $\mathfrak{se}(3)$ .

2. Source code will be framed into boxes, using a smaller font size, with line numbers on the left. If a code block is long, the box may continue to the next page:

```

1  #include <iostream>
2  using namespace std;
3

```

---

<sup>①</sup>Linux is not that popular in China as our computer science education starts very lately around 1990s.

```

4  int main ( int argc, char** argv ) {
5      cout<<"Hello"<<endl;
6      return 0;
7  }

```

3. When the code block is too long or contains repeated parts with previously listed code, it is not appropriate to be listed entirely. We will only give **important snippets** and mark it with "Snippet". Therefore, we strongly recommend that readers download all the source code on GitHub and complete the exercises to better understand the book.
4. Due to typographical reasons, the code shown in the book may be slightly different from the code hosted on GitHub. In that case please use the code on GitHub.
5. For each of the libraries we use, it will be explained in details when first appearing, but not repeated in the follow-up. Therefore, it is recommended that readers read this book in order.
6. An abstract will be presented at the beginning of each lecture. A summary and some exercises will be given at the end. The cited references are listed at the end of the book.
7. The chapters with an asterisk mark in front are optional readings, and readers can read them according to their interest. Skipping them will not hinder the understanding of subsequent chapters.
8. Important contents will be marked in **bold** or *italic*, as we are already accustomed to.
9. Most of the experiments we designed are demonstrative. Understanding them does not mean that you are already familiar with the entire library. So we recommend that you spend time on yourselves in further exploring the important libraries frequently used in the book.
10. The book's exercises and optional readings may require you to search for additional materials, so you need to learn to use search engines.

## 1.6 Acknowledgments

The online English version of this book is currently public available and open source. The Chinese version

## 1.7 Exercises (self-test questions)

1. There is a linear equation  $\mathbf{Ax} = \mathbf{b}$ , if  $\mathbf{A}$  and  $\mathbf{b}$  are known, how to solve for  $\mathbf{x}$ ? What are the requirements for  $\mathbf{A}$  and  $\mathbf{b}$  if we want a unique  $\mathbf{x}$ ? (Hint: check the rank of  $\mathbf{A}$  and  $\mathbf{b}$ ).
2. What is a Gaussian distribution? What does it look like in one-dimensional case? How about in high-dimensional case?

3. Do you know what a **class** is in C++? Do you know STL? Have you ever used them?
4. How do you write a C++ program? (It's completely fine if your answer is "using Visual C++ 6.0"<sup>①</sup>. As long as you have C++ or C programming experience, you are in good hand).
5. Do you know the C++11 standard? Which new features have you heard of or used? Are you familiar with any other standard?
6. Do you know Linux? Have you used at least one flavor (not including Android), such as Ubuntu?
7. What is the directory structure of Linux? What basic commands do you know? (e.g. `ls`, `cat`, etc.)
8. How to install a software in Ubuntu (without using the Software Center)? What directories are software usually installed under? If you only know the fuzzy name of a software (for example, you want to install a library with a word "eigen" in its name), how would you do it?
9. \*Spend an hour learning Vim, you will be using it sooner or later. You can type "vimtutor" into an terminal and read through its contents. We do not require you to operate it very skillfully, as long as you can use it to edit the code in the process of learning this book. Do not waste time on its plugins, do not try to turn Vim into an IDE for now, we will only use it for text editing in this book.

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<sup>①</sup> As I know many of our undergraduate students are still using this VC++ 6.0 in the university.

## Chapter 2

# First Glance of Visual SLAM

### Goal of Study

1. Understand which modules a visual SLAM framework consists of, and what task each module carries out.
2. Set up the programming environment, and prepare for experiments.
3. Understand how to compile and run a program under Linux. If there is a problem, how to debug it.
4. Learn the basic usage of cmake.

## 2.1 Introduction

This lecture summarizes the structure of a visual SLAM system as an outline of subsequent chapters. Practice part introduces the fundamentals of environment setup and program development. We will make a small "Hello SLAM" program at the end.

## 2.2 Meet "Little Carrot"

Suppose we assembled a robot called *Little Carrot*, as shown in the following figure:

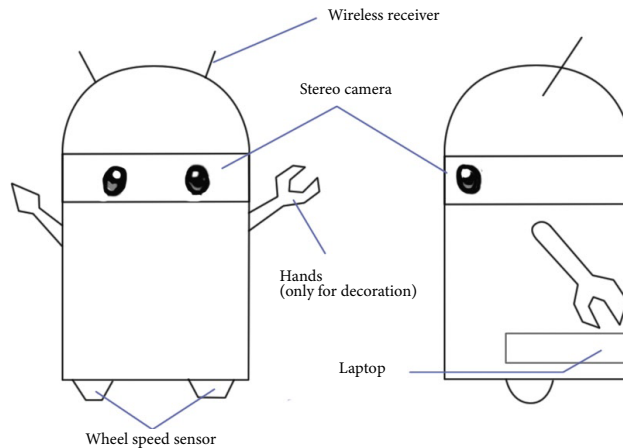


Figure 2-1: The sketch of robot *Little Carrot*

Although it looks a bit like the Android robot, it has nothing to do with the Android system. We put a laptop into its trunk (so that we can debug programs at any time). So, what is our robot capable to do?

We hope Little Carrot has the ability of *autonomous moving*. Although there are many *robots* placed statically on desktops, capable of chatting with people or playing music, but a tablet computer nowadays can also deliver the same tasks. As a robot, we hope Little Carrot can move freely in a room. Wherever we say hello to it, it can come to us right away.

First of all, such a robot needs wheels and motors to move, so we installed wheels under Little Carrot (gait control for humanoid robots is very complicated, which we will not be considering here). Now with the wheels, the robot is able to move, but without an effective navigation system, Little Carrot does not know where a target of action is, and it can do nothing but wander around blindly. Even worse, it may hit a wall and cause damage. In order to avoid this, we installed cameras on its head, with the intuition that such a robot *should look similar to human*. Certainly, with eyes, brains and limbs, human can walk freely and explore any environment, so we (somehow naively) think that our robot should be able to achieve it too. Well, in order to make Little Carrot able to explore a room, we find it at least needs to know two things:

1. Where am I? - It's about *localization*.

## 2. What is the surrounding environment like? -It's about *map building*.

*Localization* and *map building*, can be seen as the perception in both inward and outward directions. As a completely autonomous robot, Little Carrot need not only to understand its own *state* (i.e. the location), but also the external *environment* (i.e. the map). Of course, there are many different approaches to solve these two problems. For example, we can lay guiding rails on the floor of the room, or paster a lot of artificial markers such as QR code pictures on the wall, or mount radio positioning devices on the table. If you are outdoor, you can also install a GNSS receiver (like the one in a cell phone or a car) on the head of Little Carrot. With these devices, can we claim that the positioning problem has been resolved? Let's categorize these sensors (see Fig. 2-2) into two classes.

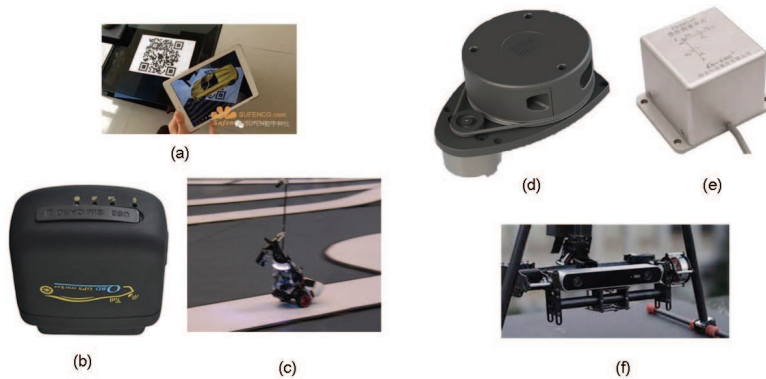


Figure 2-2: Different kinds of sensors: (a) QR code (b) GNSS receiver (c) guiding rails (d) Laser range finder (e) Inertial measurement unit (f) stereo camera

The first class are *non-intrusive* sensors which are completely self-contained inside a robot, such as wheel encoders, cameras, laser scanners, etc. They do not assume an cooperative environment around the robot. The other class are *intrusive* sensors depending on a prepared environment, such as the above mentioned guiding rails, QR codes, etc. Intrusive sensors can usually locate a robot directly, solving the positioning problem in a simple and effective manner. However, since they require changes on the environment, the scope of usage is often limited within a certain degree. For example, if there is no GPS signal, or guiding rails cannot be laid, what should we do in those cases?

We can see that the intrusive sensors place certain *constraints* to the external environment. A localization system based on them can only function properly when those constraints are met in the real world. Otherwise, the localization approach cannot be carried out anymore, like GPS positioning system normally doesn't work well in indoor environments. Therefore, although this type of sensor is simple and reliable, they do not work as a general solution. In contrast, non-intrusive sensors, such as laser scanners, cameras, wheel encoders, Inertial Measurement Units (IMUs), etc., can only observe indirect physical quantities rather than the direct locations. For example, a wheel encoder measures the wheel rotation angle, an IMU measures the angular velocity and the acceleration, a camera or a laser scanner observe the external environment in a certain form like point-clouds and images. We have to apply algorithms to infer positions from these indirect observations. While this sounds like a roundabout tactic, the more obvious benefit is that it does not make any

demands on the environment, making it possible for this localization framework to be applied to an unknown environment. Therefore, they are called as self-localization in many research area.

Looking back at the SLAM definitions discussed earlier, we emphasized an *unknown environment* in SLAM problems. In theory, we should not presume which environment the Little Carrot will be used (but in reality we will have a rough range, such as indoor or outdoor), which means that we can not assume that the external sensors like GPS can work smoothly. Therefore, the use of portable non-intrusive sensors to achieve SLAM is our main focus. In particular, when talking about visual SLAM, we generally refer to the using of *cameras* to solve the localization and map building problems.

Visual SLAM is the main subject of this book, so we are particularly interested in what the Little Carrot's eyes can do. The cameras used in SLAM are different from the commonly seen SLR cameras. It is often much simpler and does not carry expensive lens. It shoots at the surrounding environment at a certain rate, forming a continuous video stream. An ordinary camera can capture images at 30 frames per second, while high-speed cameras can do faster. The camera can be roughly divided into three categories: Monocular, Stereo and RGB-D, as shown by the following figure 2-3. Intuitively, a monocular camera has only one camera, a stereo camera has two. The principle of a RGB-D camera is more complex, in addition to being able to collect color images, it can also measure the distance of the scene from the camera for each pixel. RGB-D cameras usually carry multiple cameras, and may adopt a variety of different working principles. In the fifth lecture, we will detail their working principles, and readers just need an intuitive impression for now. In addition, there are also specialty and emerging camera types can be applied to SLAM, such as panorama camera [5], event camera [6]. Although they are occasionally seen in SLAM applications, so far they have not become the mainstream. From the appearance we can infer that Little Carrot seems to carry a stereo camera.



Figure 2-3: Different kinds of cameras: monocular, RGB-D and stereo.

Now, let's take a look at the pros and cons of using different type of camera for SLAM.



### Monocular Camera

The SLAM system that uses only one camera is called Monocular SLAM. This sensor structure is particularly simple, and the cost is particularly low, therefore the monocular SLAM has been very attractive to researchers. You must have seen the output data of a monocular camera: photo. Yes, as a photo, what are its characteristics?

A photo is essentially a *projection* of a scene onto a camera's imaging plane. It reflects a three-dimensional world in a two-dimensional form. Obviously, there is one dimension lost during this projection process, which is the so-called depth (or distance). In a monocular case, we can not obtain the *distance* between objects in the scene and the camera by using a single image. Later we will see that this distance is actually critical for SLAM. Because we human have seen a large number of images, we formed a natural sense of distances for most scenes, and this can help us determine the distance relationship among the objects in the image. For example, we can recognize objects in the image and correlate them with their approximate size obtained from daily experience. The close objects will occlude the distant objects; the sun, the moon and other celestial objects are infinitely far away; an object will have shadow if it is under sunlight. This common sense can help us determine the distance of objects, but there are also certain cases that confuse us, and we can no longer determine the distance and true size of an object. The following figure 2-4 is shown as an example. In this image, we can not determine whether the figures are real person or small toys purely based on the image itself. Unless we change our view angle, explore the three-dimensional structure of the scene. In other words, from a single image, we can not determine the true size of an object. It may be a big but far away object, but it may also be a close but small object. They may appear to be the same size in an image due to the perspective projection effect.



Figure 2-4: We cannot tell if the people are real humans or just small toys from a single image

Since the image taken by an monocular camera is just a 2D projection of the 3D space, if we want to recover the 3D structure, we have to change the camera's view angle. Monocular SLAM adopts the same principle. We move the camera and

estimate its own *motion*, as well as the distances and sizes of the objects in the scene, namely the *structure* of the scene. So how should we estimate these movements and structures? From the everyday experience we know that if a camera moves to the right, the objects in the image will move to the left which gives us an inspiration of inferring motion. On the other hand, we also know that closer objects move faster, while distant objects move slower. Thus, when the camera moves, the movement of these objects on the image forms pixel disparity. Through calculating the disparity, we can quantitatively determine which objects are far away and which objects are close.

However, even if we know which objects are near and which are far, they are still only relative values. For example, when we are watching a movie, we can tell which objects in the movie scene are bigger than the others, but we can not determine the *real size* of those objects – are the buildings real high-rise buildings or just models on a table? Is it a real monster that destructs a building, or just an actor wearing special clothing? Intuitively, if the camera’s movement and the scene size are doubled at the same time, monocular cameras see the same. Likewise, multiplying this size by any factor, we will still get the same picture. This demonstrates that the trajectory and map obtained from monocular SLAM estimation will differ from the actual trajectory and map with a factor, which is just the so-called *scale*<sup>①</sup>. Since monocular SLAM can not determine this real scale purely based on images, this is also called the *scale ambiguity*.

In monocular SLAM, depth can only be calculated with translational movement, and the real scale cannot be determined. These two things could cause significant trouble when applying monocular SLAM into real-world applications. The fundamental cause is that depth can not be determined from a single image. So, in order to obtain real-scaled depth, we start to use stereo and RGB-D cameras.

## Stereo Camera and RGB-D Camera

The purpose of using stereo and RGB-D cameras is to measure the distance between objects and the camera, to overcome the shortcomings of monocular cameras that distances are unknown. Once distances are known, the 3D structure of a scene can be recovered from a single frame, and also eliminates the scale ambiguity. Although both stereo and RGB-D cameras are able to measure the distance, their principles are not the same. A stereo camera consists of two synchronized monocular cameras, displaced with a known distance, namely the *baseline*. Because the physical distance of the baseline is known, we are able to calculate the 3D position of each pixel, in a way that is very similar to our human eyes. We can estimate the distances of the objects based on the differences between the images from left and right eye, and we can try to do the same on computers (see Fig. 2-5). We can also extend stereo camera to multi-camera systems if needed, but basically there is no much difference.

Stereo cameras usually require significant amount of computational power to (unreliably) estimate depth for each pixel. This is really clumsy compared to human beings. The depth range measured by a stereo camera is related to the baseline length. The longer a baseline is, the farther it can measure. So stereo cameras mounted on autonomous vehicles are usually quite big. Depth estimation for stereo cameras is achieved by comparing images from the left and right cameras, and does not rely on other sensing equipment. Thus stereo cameras can be applied both indoor and outdoor. The disadvantage of stereo cameras or multi-camera systems is

<sup>①</sup>Mathematical reason will be explained in the visual odometry chapter.

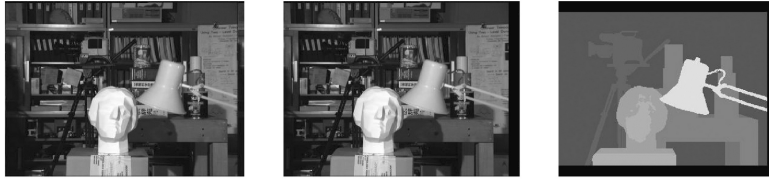


Figure 2-5: Distance is calculated from the disparity of two stereo image pair.

that the configuration and calibration process is complicated, and their depth range and accuracy are limited by baseline length and camera resolution. Moreover, stereo matching and disparity calculation also consumes much computational resource, and usually requires GPU or FPGA to accelerate in order to generate real-time depth maps. Therefore, in most of the state-of-the-art algorithms, computational cost is still one of the major problems of stereo cameras.

Depth camera (also known as RGB-D camera, RGB-D will be used in this book) is a type of new cameras rising since 2010. Similar to laser scanners, RGB-D cameras adopt infrared structure of light or Time-of-Flight (ToF) principles, and measure the distance between objects and the camera by actively emitting light to the object and receive the returned light. This part is not solved by software as a stereo camera, but by physical sensors, so it can save much computational resource compared to stereo cameras (see Fig. 2-6). Common RGB-D cameras include Kinect / Kinect V2, Xtion Pro Live, RealSense, etc. However, most of the RGB-D cameras still suffer from issues including narrow measurement range, noisy data, small field of view, susceptible to sunlight interference, and unable to measure transparent material. For SLAM purpose, RGB-D cameras are mainly used in indoor environments, and are not suitable for outdoor applications.



Figure 2-6: RGBD cameras measure the distance and can build a point cloud with a single image frame.

We have discussed the common types of cameras, and we believe you should have gained an intuitive understanding of them. Now, imagine a camera is moving in a

scene, we will get a series of continuously changing images <sup>①</sup>. The goal of visual SLAM is to localize and build a map using these images. This is not as simple task as you would think. It is not a single algorithm that continuously output positions and map information as long as we feed it with input data. SLAM requires a good algorithm framework, and after decades of hard work by researchers, the framework has been matured in recent years.

## 2.3 The Classic Visual SLAM Framework

Let's take a look at the classic visual SLAM framework, shown in the following figure 2-7:

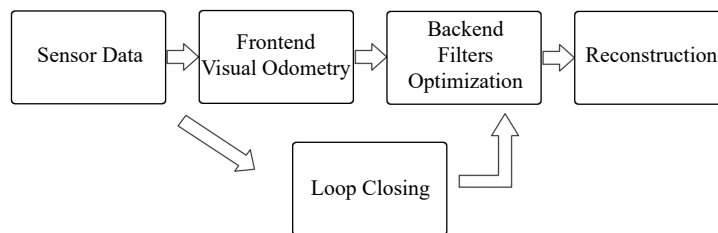


Figure 2-7: The classic visual SLAM framework.

A typical visual SLAM work-flow includes the following steps:

1. Sensor data acquisition. In visual SLAM, this mainly refers to for acquisition and preprocessing for camera images. For a mobile robot, this will also include the acquisition and synchronization with motor encoders, IMU sensors, etc.
2. Visual Odometry (VO). The task of VO is to estimate the camera movement between adjacent frames (ego-motion), as well as to generate a rough local map. VO is also known as the *Front End*.
3. Backend filtering/optimization. The back end receives camera poses at different time stamps from VO, as well as results from loop closing, and apply optimization to generate a fully optimized trajectory and map. Because it is connected after the VO, it is also known as the *Back End*.
4. Loop Closing. Loop closing determines whether the robot has returned to its previous position in order to reduce the accumulated drift. If a loop is detected, it will provide information to the back end for further optimization.
5. Reconstruction. It constructs a task specific map based on the estimated camera trajectory.

The classic visual SLAM framework is the result of more than a decade's research endeavor. The framework itself and the algorithms have been basically finalized and have been provided as basic functions in several public vision and robotics libraries. Relying on these algorithms, we are able to build visual SLAM systems performing real-time localization and mapping in static environments. Therefore, a

<sup>①</sup> You can try to use your phone to record a video clip.

rough conclusion can be reached that if the working environment is limited to static and rigid with stable lighting conditions and no human interference, visual SLAM problem is basically solved [7].

The readers may have not fully understood the concepts of the above mentioned modules yet, so we will detail the functionality of each module in the following sections. However, an deeper understanding of their working principles requires certain mathematical knowledge which will be expanded in the second part of this book. For now, an intuitive and qualitative understanding of each module is good enough.

### Visual Odometry

The visual odometry is concerned with the movement of a camera between *adjacent image frames*, and the simplest case is of course the motion between two successive images. For example, when we see the images in Fig. 2-8, we will naturally tell that the right image should be the result of the left image after a rotation to the left with a certain angle (it will be easier if we have a video input). Let's consider this question: how do we know the motion is "turning left"? Humans have long been accustomed to using our eyes to explore the world, and estimating our own positions, but this intuition is often difficult to explain, especially in natural language. When we see these images, we will naturally think that, ok, the bar is close to us, the walls and the blackboard are farther away. When the camera turns to left, the closer part of the bar started to appear, and the cabinet on the right side started to move out of our sight. With this information, we conclude that the camera should be rotating to the left.



Figure 2-8: Camera motion can be inferred from two consecutive image frames. Images are from NYUD dataset.

But if we go a step further: can we determine how much the camera has rotated or translated, in units of degrees or centimeters? It is still difficult for us to give an quantitative answer. Because our intuition is not good at calculating numbers. But for a computer, movements have to be described with such numbers. So we will ask: how should a computer determine a camera's motion only based on images?

As mentioned earlier, in the field of computer vision, a task that seems natural to a human can be very challenging for a computer. Images are nothing but numerical matrices in computers. A computer has no idea what these matrices mean (this is the problem that machine learning is also trying to solve). In visual SLAM, we can only see blocks of pixels, knowing that they are the results of projections by spatial points onto the camera's imaging plane. In order to quantify a camera's movement, we must first *understand the geometric relationship between a camera and the spatial points*.

Some background knowledge is needed to clarify this geometric relationship and the realization of VO methods. Here we only want to convey an intuitive concept. For now, you just need to take away that VO is able to estimate camera motions from images of adjacent frames and restore the 3D structures of the scene. It is named as an “odometry”, because similar to an actual wheel odometry which only calculates the ego-motion at neighboring moments, and does not estimate a global map or a absolute pose. In this regard, VO is like a species with only a short memory.

Now, assuming that we have a visual odometry, we are able to estimate camera movements between every two successive frames. If we connect the adjacent movements, this constitutes the movement of the robot trajectory, and therefore addresses the positioning problem. On the other hand, we can calculate the 3D position for each pixel according to the camera position at each time step, and they will form an map. Up to here, it seems with an VO, the SLAM problem is already solved. Or, is it?

Visual odometry is indeed an key technology to solving visual SLAM problem. We will be spending a great part to explain it in details. However, using only a VO to estimate trajectories will inevitably cause *accumulative drift*. This is due to the fact that the visual odometry (in the simplest case) only estimates the movement between two frames. We know that each estimate is accompanied by a certain error, and because the way odometry works, errors from previous moments will be carried forward to the following moments, resulting in inaccurate estimation after a period of time (see Fig. 2-9). For example, the robot first turns left  $90^\circ$  and then turns right  $90^\circ$ . Due to error, we estimate the first  $90^\circ$  as  $89^\circ$ , which is possible to happen in real-world applications. Then we will be embarrassed to find that after the right turn, the estimated position of the robot will not return to the origin. What’s worse, even the following estimates are perfectly estimated, they will always be carrying this  $1^\circ$  error compared to the true trajectory.

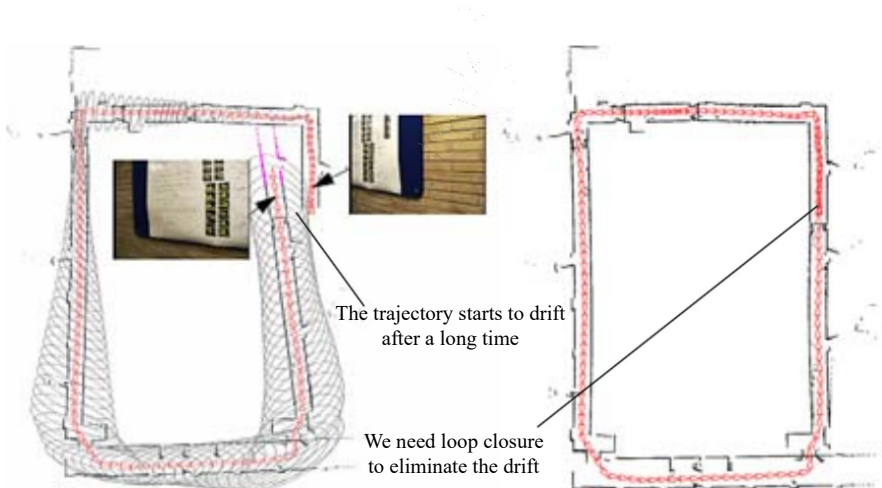


Figure 2-9: Drift will be accumulated if we only have a relative motion estimation.

The accumulated drift will make us unable to build a consistent map. A straight corridor may oblique, and a  $90^\circ$  angle may be crooked - this is really an unbearable matter! In order to solve the drifting problem, we also need other two compo-



nents: the *back-end optimization* <sup>①</sup> and *loop closing*. Loop closing is responsible for detecting whether the robot returns to its previous position, while the back-end optimization corrects the shape of the entire trajectory based on this information.

### Back-end Optimization

Generally speaking, the back-end optimization mainly refers to the process of dealing with the *noise* in SLAM systems. We wish that all the sensor data is accurate, but in reality, even the most expensive sensors still have certain amount of noise. Cheap sensors usually have larger measurement errors, while that of expensive ones may be small. Moreover, performance of many sensors are affected by changes in magnetic field, temperature, etc. Therefore, in addition to solving the problem of estimating camera movements from images, we also care about how much noise this estimation contains, how these noise is carried forward from the last time step to the next, and how confident we have on the current estimation. So the problem that back-end optimization solves can be summarized as: to estimate the state of the entire system from noisy input data and calculate how uncertain these estimations are. The state here includes both the robot's own trajectory and the environment map.

In contrast, the visual odometry part is usually referred to as the *front end*. In a SLAM framework, the front end provides data to be optimized by the back end, as well as the initial values. Because the back end is responsible for the overall optimization, we only care about the data itself instead of where it comes from. In other words, we only have numbers and matrices in backend without those beautiful images. In visual SLAM, the front end is more relevant to *computer vision* topics, such as image feature extraction and matching, while the backend is relevant to *state estimation* research area.

Historically, the back-end optimization part has been equivalent to “SLAM research” for a long time. In the early days, SLAM problem was described as a state estimation problem, which is exactly what the back-end optimization tries to solve. In the earliest papers on SLAM, researchers at that time called it “estimation of spatial uncertainty” [2, 8]. Although sounds a little obscure, it does reflect the nature of the SLAM problem: *the estimation of the uncertainty of the self-movement and the surrounding environment*. In order to solve the SLAM problem, we need state estimation theory to express the uncertainty of localization and map construction, and then use filters or nonlinear optimization to estimate the mean and uncertainty (covariance) of the states. The details of state estimation and non-linear optimization will be explained in chapter 6, 10 and 11.

### Loop Closing

Loop Closing, also known as *Loop Closure Detection*, is mainly to address the drifting problem of position estimation in SLAM. So how to solve it? Assuming that a robot has returned to its origin after a period of movement, but the estimated position does not return to the origin due to drift. How to correct it? Imagine that if there is some way to let the robot know that it has returned to the origin, then we can then “pull” the estimated locations to the origin to eliminate drifts, which is, exactly, called loop closing.

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<sup>①</sup>It is usually known as the back end. Since it is often implemented by optimization so we use the term back-end optimization.

Loop closing has close relationship with both localization and map building. In fact, the main purpose of building a map is to enable a robot to know the places it has been to. In order to achieve loop closing, we need to let the robot has the ability to identify the scenes it has visited before. There are different alternatives to achieve this goal. For example, as we mentioned earlier, we can set a marker at where the robot starts, such as a QR code. If the sign was seen again, we know that the robot has returned to the origin. However, the marker is essentially an intrusive sensor which sets additional constraints to the application environment. We prefer the robot can use its non-intrusive sensors, e.g. the image itself, to complete this task. A possible approach would be to detect similarities between images. This is inspired by us humans. When we see two similar images, it is easy to identify that they are taken from the same place. If the loop closing is successful, accumulative error can be significantly reduced. Therefore, visual loop detection is essentially an algorithm for calculating similarities of images. Note that the loop closing problem also exists in laser based SLAM, but here the rich information contained in images can remarkably reduce the difficulty of making a correct loop detection.

After a loop is detected, we will tell the back-end optimization algorithm that, OK, “A and B are the same point”. Then, based on this new information, the trajectory and the map will be adjusted to match the loop detection result. In this way, if we have sufficient and reliable loop detection, we can eliminate cumulative errors, and get globally consistent trajectories and maps.



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