

An Introduction to

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Why I like Julia

- It's like MATLAB in that
 - Basic syntax is similar
 - Great for linear algebra: BLAS libraries in base namespace
- It's like Python in that
 - It's interoperable powerful glue
 - Good interaction with Jupyter
 - No need for explicit memory management
 - It's open source
- It's like C in that
 - It's pretty fast
 - (Julia is JIT-compiled)
- Very strong user community
 - Interaction takes place on Github

What's not to like?

- Debugging is wanting
- Error messages can be hard to interpret
- Parallelism has yet to fulfill its promise
- Not yet 1.0
 - I've been using Julia since 2012
 - For me, “breaking changes” have not been very breaking

Features

- [Multiple dispatch](#): providing ability to define function behavior across many combinations of argument types
- Dynamic type system: types for documentation, optimization, and dispatch
- Good performance, approaching that of statically-compiled languages like C
- Built-in package manager
- [Lisp-like macros](#) and other [metaprogramming facilities](#)
- Call Python functions: use the [PyCall](#) package
- [Call C functions](#) directly: no wrappers or special APIs
- Powerful shell-like capabilities for [managing other processes](#)
- Designed for [parallelism and distributed computation](#)
- [Coroutines](#): lightweight “green” threading
- [User-defined types](#) are as fast and compact as built-ins
- Automatic generation of efficient, specialized code for different argument types
- Elegant and extensible [conversions and promotions](#) for numeric and other types
- Efficient support for [Unicode](#), including but not limited to [UTF-8](#)
- [MIT licensed](#): free and open source

Installing and using Julia

- Install current version from julialang.org
- Many ways to invoke:
 - command line interface
 - Juno IDE
 - Jupyter notebooks
 - Atom text editor can evaluate chunks
 - ...
- Try it out on JuliaBox.com
 - Sync with <https://github.com/madeleineudell/intro-to-julia>

On the command line interface: try typing “.” or “?”

Basic syntax

- [Demo](#)

The Two Language Problem

- 1) Begin project writing simple, easy code in a prototyping language
 - eg, Python, MATLAB, R
- 2) Realize you need the code to be fast
- 3) Rewrite code in a fast language
 - C, Scala, Fortran
- 4) Wrap the code
 - Cython, Mex, ...

Julia's solution to the two-language problem

- Start with basic MATLAB-like syntax
- Speed it up: take advantage of JIT compilation
 - Add type annotations
 - Devectorize (!)

The Many-Language Problem

Problem: want to use code written in a bunch of different languages

Julia is a good **glue language**:

- Native support for Fortran and C
- Fast in-memory interfaces for Python, R, MATLAB, C++, Java, ...
- Can also [call Julia from C](#)!

Advanced feature demo

- Demo:
 - JIT
 - Introspection
 - Packages
 - Calling out

Parallel Computing

- Embarrassingly parallel operations are embarrassingly easy
- Fine-grained control over data movement and interprocess communication
 - RemoteRefs, Channels, ...
- What about multithreading?
 - There's no GIL, so it's possible
 - In the bad old days: I've done it via SharedArrays
 - Now: experimental multithreading implementation...!

Optimization in Julia

- Julia is currently the best programming language for mathematical optimization
 - Why?
 - Convex.jl
 - JuMP
 - MathProgBase
 - Solver interfaces
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Optimization: from math to solution

- 1) Write down a mathematical description
 - 2) Identify structure in objective/constraints
 - 3) Perform transformations to change structure
 - 4) Identify a solution method (algorithm, solver)
 - 5) Massage transformed problem into something the algorithm can work with
 - 6) Code it up and pass it along
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Optimization schematic in Julia

```
type OptProb{T}; blob; end
```

```
solve(x::OptProb{:Linear}) = simplex_method(x.blob)
```

```
solve(x::OptProb{:Semidefinite}) = interior_point(x.blob)
```

```
solve(x::OptProb{:Integer}) = branch_and_bound(x.blob)
```

```
solve(x::OptProb{:Lasso}) = glmnet(x.blob)
```

The details

A couple questions:

1. How do we recognize the problem class?
 2. How do we translate `blob` into something useful?
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The details

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How do you create blob in the first place?

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 2. How do we translate blob into something useful?
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The details

A couple questions:

How do you create `blob` in the first place?

1. How do we recognize the problem class?
2. How do we translate `blob` into something useful?

JuMP and Convex are tools to help you build `blob` (and then do 1 and 2

Algebraic modeling languages

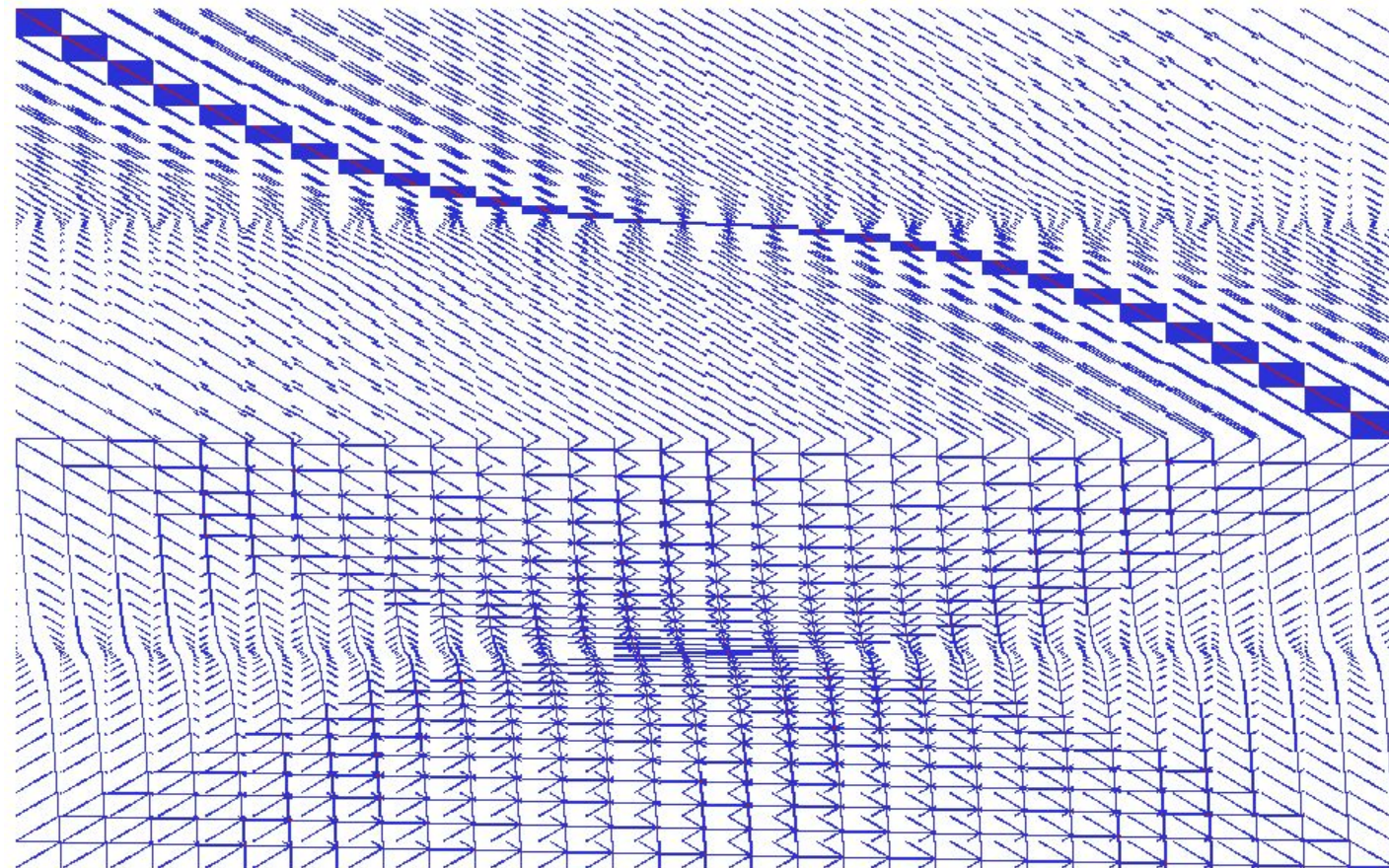
- JuMP and Convex are *algebraic modeling languages* (AMLs)

- AMPL

$$\begin{aligned}
 \min_{\mathbf{u}, \mathbf{y}} \quad & \frac{1}{4} \Delta_x \left((y_{m,0} - y_0^t)^2 + 2 \sum_{j=1}^{n-1} (y_{m,j} - y_j^t)^2 + (y_{m,n} - y_n^t)^2 \right) + \\
 & \frac{1}{4} a \Delta_t \left(2 \sum_{i=1}^{m-1} u_i^2 + u_m^2 \right) \\
 \text{s.t.} \quad & 1/\Delta_t (y_{i+1,j} - y_{i,j}) = \\
 & \frac{1}{2h_2} (y_{i,j-1} - 2y_{i,j} + y_{i,j+1} + y_{i+1,j-1} - 2y_{i+1,j} + y_{i+1,j+1}) \quad \forall i \in I', j \in J' \\
 & y_{0,j} = 0 \quad \forall j \in J \\
 & y_{i,2} - 4y_{i,1} + 3y_{i,0} = 0 \quad \forall i \in I \\
 & 1/2\Delta_x (y_{i,n-2} - 4y_{i,n-1} + 3y_{i,n}) = u_i - y_{i,n} \quad \forall i \in I \\
 & -1 \leq u_i \leq 1 \quad \forall i \in I \\
 & 0 \leq y_{i,j} \leq 1 \quad \forall i \in I, j \in J
 \end{aligned}$$

...into this:

```
type QuadProgData
  Q::SparseMatrixCSC{Float64,Int}
  c::Vector{Float64}
  A::SparseMatrixCSC{Float64,Int}
  lb::Vector{Float64}
  ub::Vector{Float64}
  l::Vector{Float64}
  u::Vector{Float64}
end
```



coeff ■ ■ ■ 1 ■ ■ ■ 1 to 100

Algebraic modeling

- Very useful for medium-to-large scale constrained optimization
 - Automates a process that is
 - Tedious
 - Error-prone
 - Opaque
 - Not portable
 - The goal is a direct translation of math to valid code
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JuMP vs. Convex

JuMP

- Larger-scale
- Complex indexing
- Advanced solver features
- Autodiff for exact derivatives

Convex

- Reformulates complex nonlinear expressions
 - Automatic convexity proof
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Why Julia?

- **C FFI** lets us work with solvers in memory
 - **Macros** let us build up models efficiently (avoid operator overloading and copying)
 - **Multiple dispatch** allows an easy, generic interface layer (MathProgBase)
 - **Performance** (duh)
 - A **real programming language** for data wrangling, post-processing, etc.
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More information and examples

- [JuliaOpt](#)
 - [Intro to Convex.jl](#)
 - [Convex.jl example](#)
 - [JuMP example](#)
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