

1.

We can deduce a recurrence relation where $P(i)$ is the max profit we can make at every i :

$$P(i) = \max\{p_i + P(\text{previous}(i)), P(i - 1)\}$$

So if $i = 0$ to n then our max profit is $P(n)$ where $n = \text{total \# of locations}$:

Pseudo-code:

```
for i in range (2, n):
    if (m_i - m_{i-1} > k):
        previous(i) = i-1
    else:
        previous(i) = previous(i-1)
for i in range (2, n):
    P(i) = max(p_i + P(previous(i)), P(i - 1))
print P(n)
```

where the complexity is $O(n)$ (we loop twice for $n-1$ iterations) trivially due to the single run through.

2.

```
def subseq(seq):
    lens = [] #to store our longest subseqs
    for i in range(1,n):
        lens[i,i] = 1 #each character is its own palindrome (size 1)
    for i in range(1,n):
        for j in range (1, n-i):
            k = j+i
            lens[j,k] = cost(lens,seq,j,k)
            lens[k,j] = cost(lens,seq,k,j)
    return lens[1,n] #n is the last index in seq
def cost(lens, seq, x, y):
    if x == y:
        return lens[x, y]
    else if seq[x] == seq[y]:
        if x+1 >= y-1:
            return 2
        else:
            return 2 + lens[x+1, y-1]
    else:
        return maximum(lens[x+1,j], lens[x, y-1])
```

Complexity: Since we loop $n-1$ times in every n loops (in subseq), then our complexity is:
 $O(n*(n-1)) = O(n^2 - n) = O(n^2)$