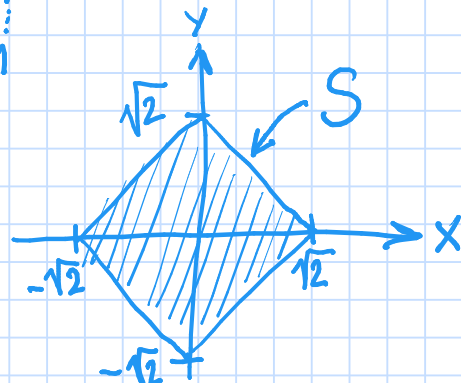


Solution using rotation:

Generate random points at  $S'$

$$\Rightarrow \begin{cases} X'_{rnd} = 2 \cdot U_1 - 1 \\ Y'_{rnd} = 2 \cdot U_2 - 1 \end{cases}$$

Rotate these coordinates  $\theta = 45^\circ \Rightarrow$



Rotation is done using the rotation matrix

$$\begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix} = \begin{bmatrix} \frac{1}{\sqrt{2}} & -\frac{1}{\sqrt{2}} \\ \frac{1}{\sqrt{2}} & \frac{1}{\sqrt{2}} \end{bmatrix}$$

$$\Rightarrow \begin{cases} X_{rnd} = \frac{1}{\sqrt{2}} \cdot (2 \cdot U_1 - 1) - \frac{1}{\sqrt{2}} \cdot (2 \cdot U_2 - 1) = \sqrt{2} \cdot (U_1 - U_2) \\ Y_{rnd} = \frac{1}{\sqrt{2}} \cdot (2 \cdot U_1 - 1) + \frac{1}{\sqrt{2}} \cdot (2 \cdot U_2 - 1) = \sqrt{2} \cdot (U_1 + U_2 - 1) \end{cases}$$

Answer:

$$X_{rnd} = \sqrt{2} \cdot (U_1 - U_2)$$

$$Y_{rnd} = \sqrt{2} \cdot (U_1 + U_2 - 1)$$

Solution using Accept-reject

Generate random points at  $S'$

i.e. let  $\begin{cases} X_{rnd} = \sqrt{8} \cdot (U_1 - \frac{1}{2}) \\ Y_{rnd} = \sqrt{8} \cdot (U_2 - \frac{1}{2}) \end{cases}$  be your candidat.

Answer:

The candidate is accepted if  
are all fulfilled

$$Y \leq \sqrt{2} - X$$

$$Y \geq -\sqrt{2} - X$$

$$Y \leq \sqrt{2} + X$$

$$Y \geq -\sqrt{2} + X$$

