

# Application of finding maximal cliques

(not – not the maximum)

# Reasoning about graph problems – wins awards!

- CVPR is the highest-ranking computer vision conference in the world.
- By common metrics, it is also typically the highest ranking conference across disciplines – that doesn't mean it is THE BEST (rankings/metrics have their imperfections – but it is certainly one of the best...)



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CVPR2023  
Best Paper  
Award

## 3D Registration with Maximal Cliques

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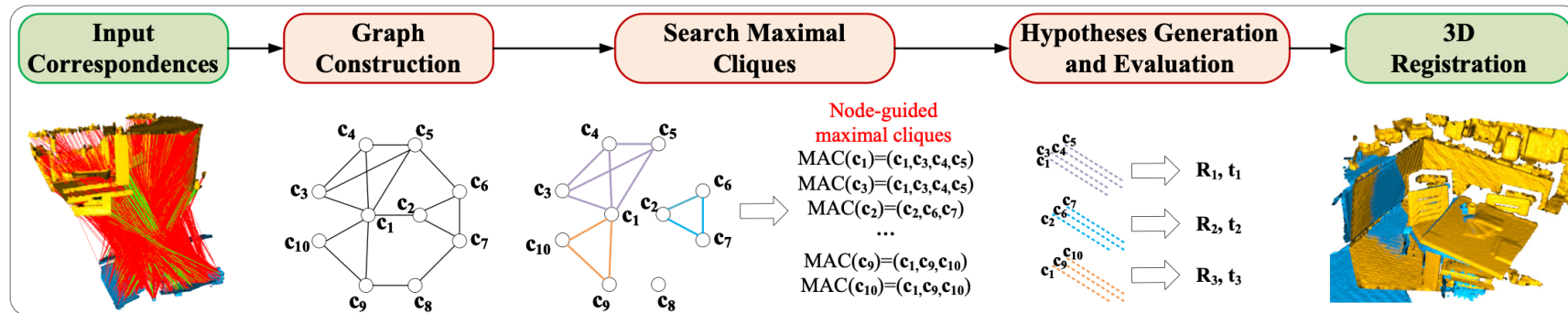


Figure 2. **Pipeline of MAC.** 1. Construct a graph for the initial correspondence set. 2. Select a set of maximal cliques from the graph as the consistent sets. 3. Generate and evaluate the hypotheses according to the consistent sets. 4. Select the best hypothesis to perform 3D registration.

- For every pair of “potential correspondences” ( $\rightarrow$  vertex in graph) place an edge if these correspondences are “compatible” (can both arise from 3D rigid transformation).
- Find maximal (not only the maximum but other large ones) cliques (of some size or quality thresholded)
- Evaluate the maximal cliques by the quality of registration yielded by the rigid motion they “vote for”. Select the best one.
- Simple (in principle) – but because finding all cliques (above a certain size/quality is likely hard – need a lot of approximations and hacks to make it work well.... BUT the motivation comes from simple graph theory.

# THIS IS CONNECTED TO (maximal) independent sets!

- A clique is a set of totally connected vertices...
- What can you say about these vertices in the complement graph?
  - They have no edges between them in the complement graph  $\rightarrow$  they are an independent set in the complement graph.
  - Thus...finding a maximal clique in the graph  $G$  is the same as finding a maximal independent set in the graph  $G_{\text{complement}}$ .
  - $G$  is the graph of compatible pairs of potential matches
  - So  $G_{\text{complement}}$  is the graph of incompatible pairs of potential matches
  - So...the paper COULD have been written as finding maximal independent sets....
  - But  $G$  might be (for the data setting) simpler/smaller to deal with than  $G_{\text{complement}}$ ....so there might be computational/practical reasons for preferring one of the two (theoretically equivalent) characterisations...