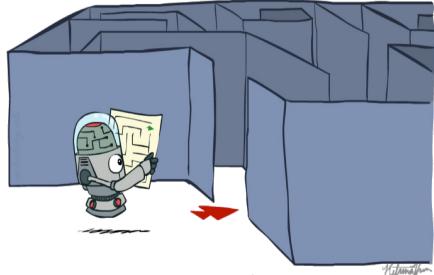
Search



Instructor: David Suter

Course Delivered for Xidian University

[Many slides adapted from those created by Dan Klein and Pieter Abbeel for CS188 Intro to AI at UC Berkeley. Some others from colleagues at Adelaide University.]

Topics

Agents that Plan Ahead

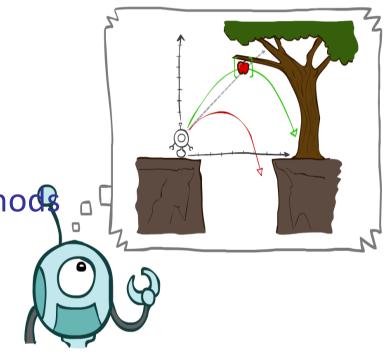
Search Problems

Uninformed Search Methods

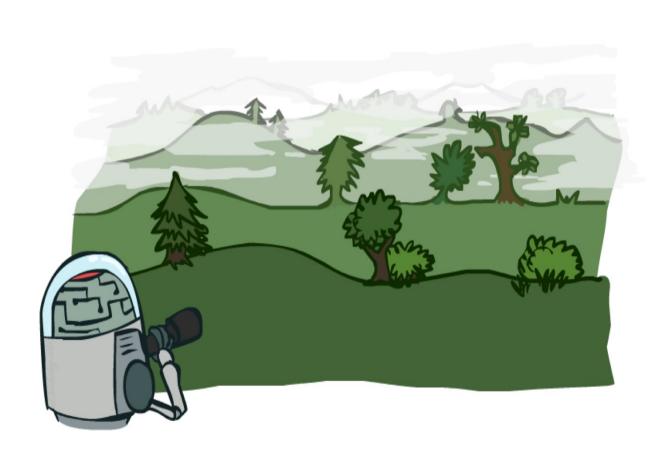
Depth-First Search

Breadth-First Search

Uniform-Cost Search



Search Problems



Search Problems

- A search problem consists of:
 - A state space



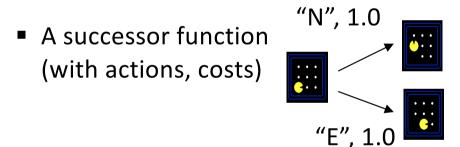






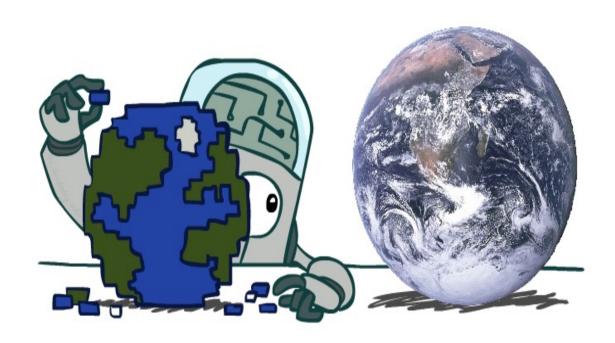




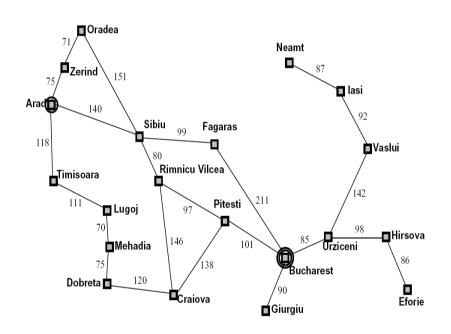


- A start state and a goal test
- A solution is a sequence of actions (a plan) which transforms the start state to a goal state

Search Problems Are Models



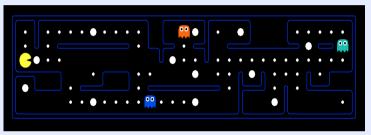
Example: Traveling in Romania



- State space:
 - Cities
- Successor function:
 - Roads: Go to adjacent city with cost = distance
- Start state:
 - Arad
- Goal test:
 - Is state == Bucharest?
- Solution?

What's in a State Space?

The world state includes every last detail of the environment



A search state keeps only the details needed for planning (abstraction)

- Problem: Path Finding
 - States: (x,y) location
 - Actions: NSEW
 - Successor: update location only
 - Goal test: is (x,y)=END

- Problem: Eat-All-Dots
 - States: {(x,y), dot booleans}
 - Actions: NSEW
 - Successor: update location and possibly a dot boolean
 - Goal test: dots all

State Space Sizes?

World state:

Agent positions: 120

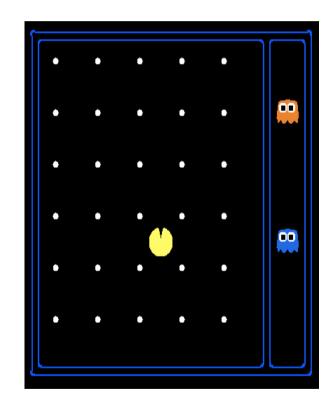
• Food count: 30

Ghost positions: 12

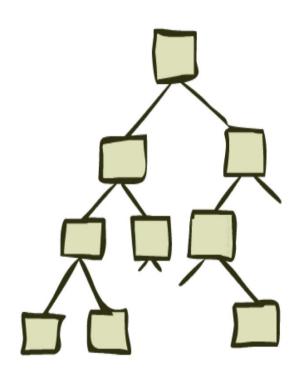
Agent facing: NSEW

How many

- World states?
 120x(2³⁰)x(12²)x4
- States for path finding?120
- States for eat-all-dots? 120x(2³⁰)

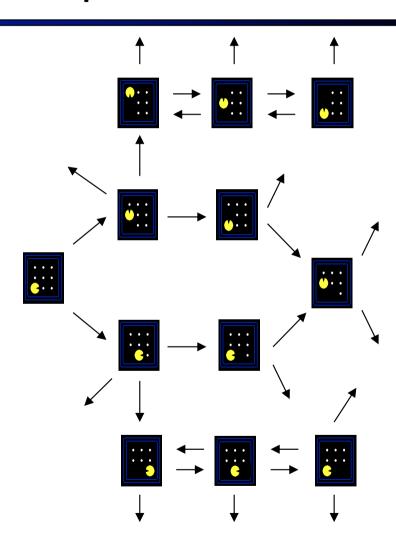


State Space Graphs and Search Trees



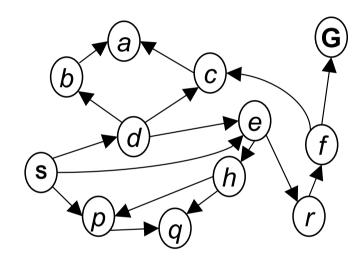
State Space Graphs

- State space graph: A mathematical representation of a search problem
 - Nodes are (abstracted) world configurations
 - Arcs represent successors (action results)
 - The goal test is a set of goal nodes (maybe only one)
- In a state space graph, each state occurs only once!
- We can rarely build this full graph in memory (it's too big), but it's a useful idea



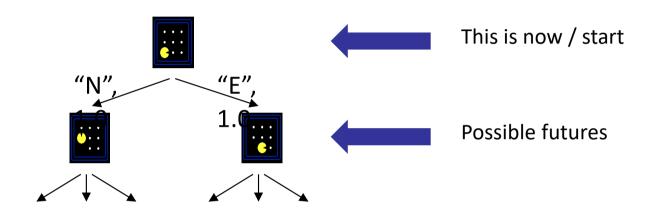
State Space Graphs

- State space graph: A mathematical representation of a search problem
 - Nodes are (abstracted) world configurations
 - Arcs represent successors (action results)
 - The goal test is a set of goal nodes (maybe only one)
- In a search graph, each state occurs only once!
- We can rarely build this full graph in memory (it's too big), but it's a useful idea



Tiny search graph for a tiny search problem

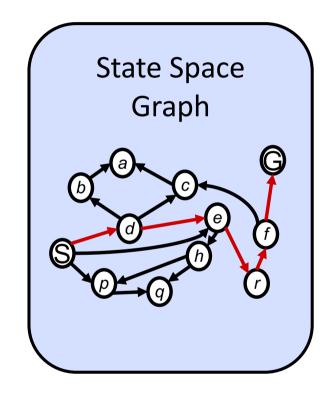
Search Trees



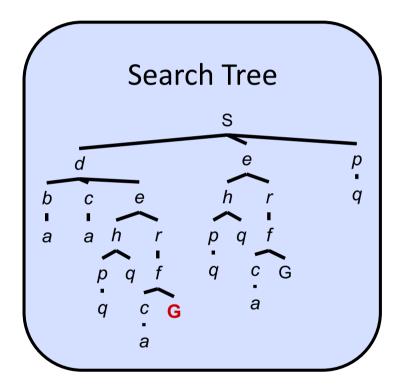
A search tree:

- A "what if" tree of plans and their outcomes
- The start state is the root node
- Children correspond to successors
- Nodes show states, but correspond to PLANS that achieve those states
- For most problems, we can never actually build the whole tree

State Space Graphs vs. Search Trees

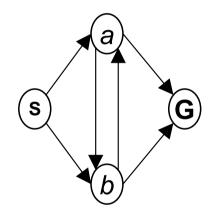


Each NODE in in the search tree is an entire PATH in the state space grapph. construct both on demand – and we construct as little as



Quiz: State Space Graphs vs. Search Trees

Consider this 4-state graph:

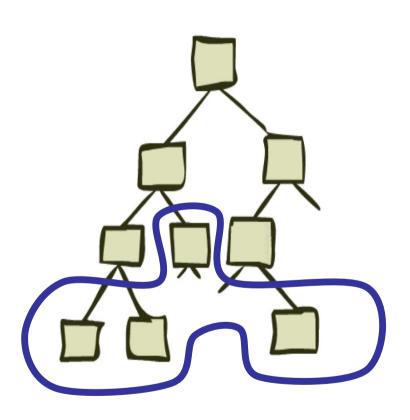


How big is its search tree (from S)?

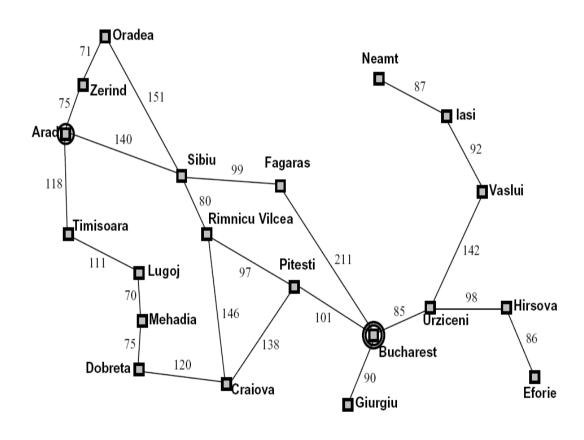


Important: Lots of repeated structure in the search tree!

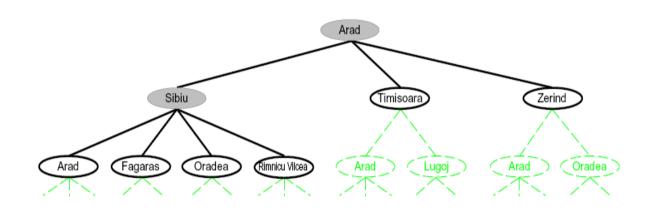
Tree Search



Search Example: Romania



Searching with a Search Tree



Search:

- Expand out potential plans (tree nodes)
- Maintain a fringe of partial plans under consideration
- Try to expand as few tree nodes as possible

General Tree Search

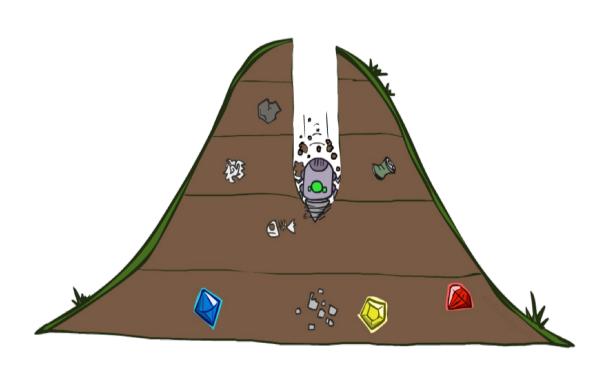
```
function Tree-Search (problem, strategy) returns a solution, or failure initialize the search tree using the initial state of problem loop do

if there are no candidates for expansion then return failure choose a leaf node for expansion according to strategy

if the node contains a goal state then return the corresponding solution else expand the node and add the resulting nodes to the search tree end
```

- Important ideas:
 - Fringe
 - Expansion
 - Exploration strategy
- Main question: which fringe nodes to explore?

Depth-First Search

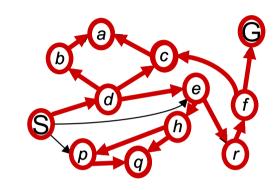


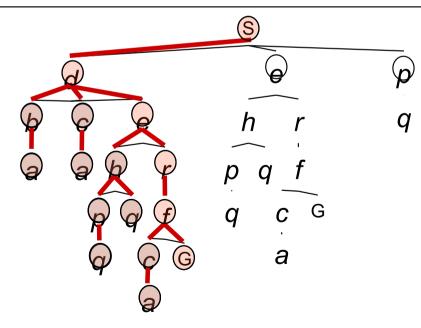
Depth-First Search

Strategy:
expand a
deepest node
first

<u>Implementati</u>

on: Fringe is a LIFO stack





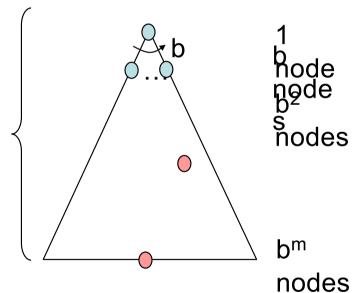
Search Algorithm Properties



Search Algorithm Properties

- Complete: Guaranteed to find a solution if one exists?
- Optimal: Guaranteed to find the least cost path?
- Time complexity?
- Space complexity?
- Cartoon of search tree:
 - b is the branching factor
 - m is the maximum depth
 - solutions at various depths

m tiers

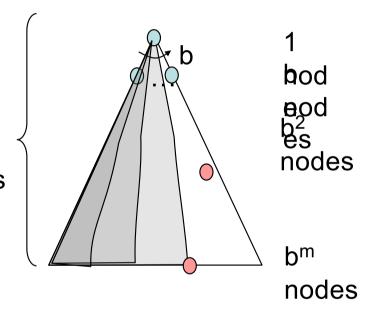


- Number of nodes in entire tree?
 - $1 + b + b^2 + b^m = O(b^m)$

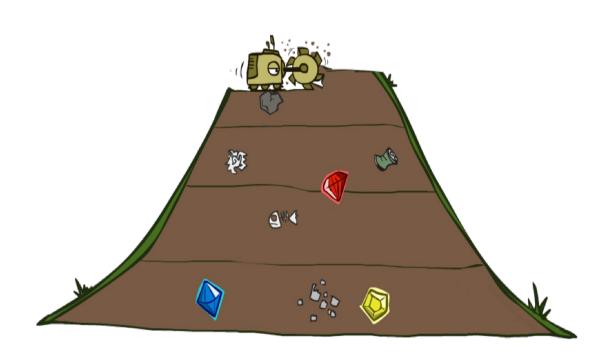
Depth-First Search (DFS) Properties

What nodes DFS expand?

- Some left prefix of the tree.
- Could process the whole tree!
- If m is finite, takes time O(b^m)
- How much space does the fringe take?
 - Only has siblings on path to root, so O(bm)
- Is it complete?
 - m could be infinite, so only if we prevent cycles (more later)
- Is it optimal?
 - No, it finds the "leftmost" solution, regardless of depth or cost

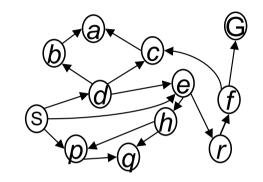


Breadth-First Search

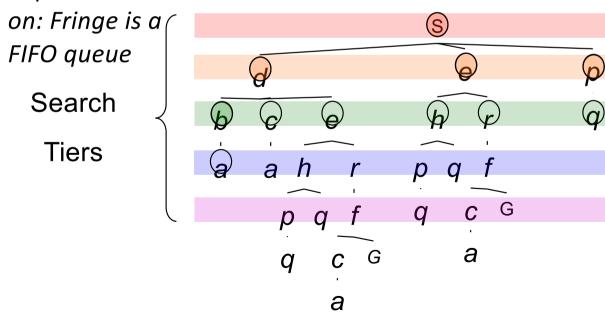


Breadth-First Search

Strategy: expand a shallowest node first

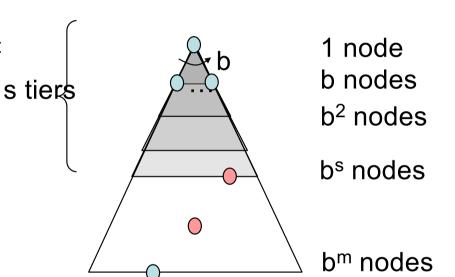


<u>Implementati</u>

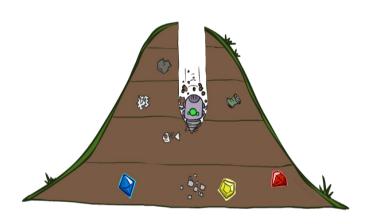


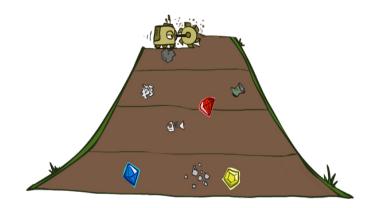
Breadth-First Search (BFS) Properties

- What nodes does BFS expand?
 - Processes all nodes above shallowest solution
 - Let depth of shallowest solution be s
 - Search takes time O(b^s)
- How much space does the fringe take?
 - Has roughly the last tier, so O(b^s)
- Is it complete?
 - s must be finite if a solution exists, so yes!
- Is it optimal?
 - Only if costs are all 1 (more on costs later)



Quiz: DFS vs BFS





Quiz: DFS vs BFS

When will BFS outperform DFS?

When will DFS outperform BFS?

[Demo: dfs/bfs maze

Video of Demo Maze Water DFS/BFS (part 1)



Video of Demo Maze Water DFS/BFS (part 2)

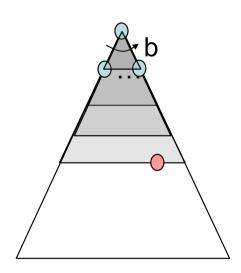


Iterative Deepening

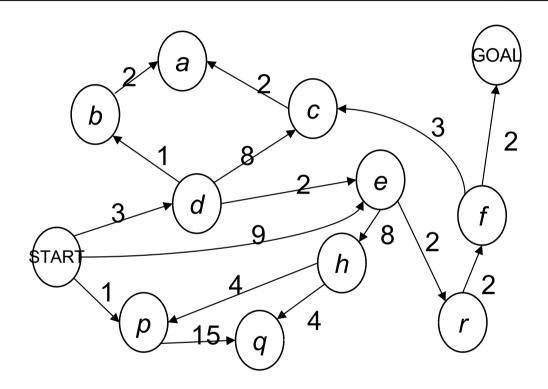
- Idea: get DFS's space advantage with BFS's time / shallow-solution advantages
 - Run a DFS with depth limit 1. If no solution...
 - Run a DFS with depth limit 2. If no solution...
 - Run a DFS with depth limit 3.



Generally most work happens in the lowest level searched, so not so bad!

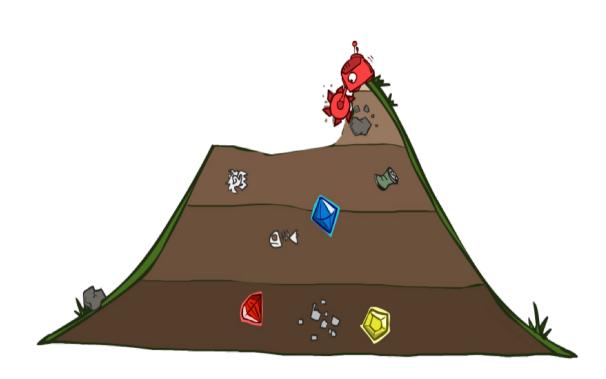


Cost-Sensitive Search

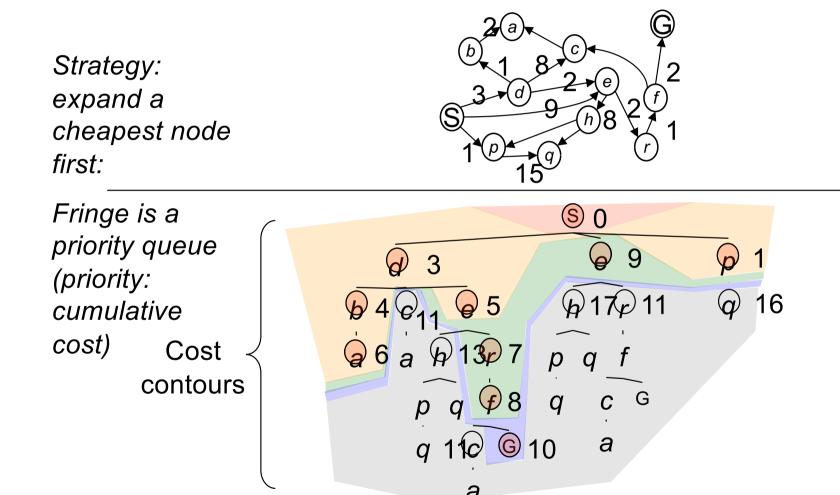


BFS finds the shortest path in terms of number of actions. It does not find the least-cost path. We will now cover a similar algorithm which does find the least-cost path.

Uniform Cost Search

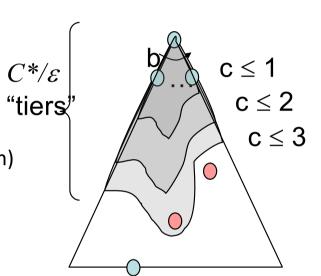


Uniform Cost Search



Uniform Cost Search (UCS) Properties

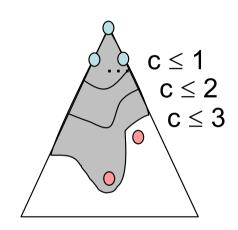
- What nodes does UCS expand?
 - Processes all nodes with cost less than cheapest solution!
 - If that solution costs C^* and arcs cost at least ε , then the "effective depth" is roughly C^*/ε
 - Takes time $O(b^{C*/\varepsilon})$ (exponential in effective depth)
- How much space does the fringe take?
 - Has roughly the last tier, so $O(b^{C^*/\varepsilon})$
- Is it complete?
 - Assuming best solution has a finite cost and minimum arc cost is positive, yes!
- Is it optimal?
 - Yes! (Proof via A*)



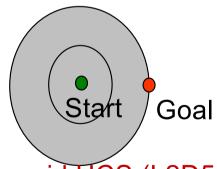
Uniform Cost Issues

Remember: UCS explores increasing cost contours

The good: UCS is complete and optimal!



- The bad:
 - Explores options in every "direction"
 - No information about goal location
- We'll fix that soon!



[Demo: empty grid UCS (L2D5)] [Demo: maze with deep/shallow water DFS/BFS/UCS (L2D7)]

Video of Demo Empty UCS



Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 1)



Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 2)

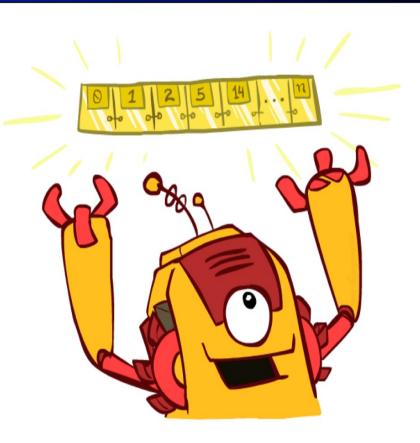


Video of Demo Maze with Deep/Shallow Water --- DFS, BFS, or UCS? (part 3)



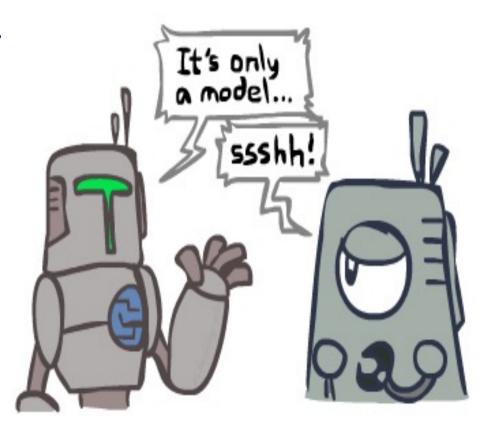
The One Queue

- All these search algorithms a the same except for fringe strategies
 - Conceptually, all fringes are priority queues (i.e. collections nodes with attached priorities)
 - Practically, for DFS and BFS, yo can avoid the log(n) overhead from an actual priority queue, using stacks and queues
 - Can even code one implementation that takes a variable queuing object



Search and Models

- Search operates over models of the world
 - The agent doesn't actually try all the plans out in the real world!
 - Planning is all "in simulation"
 - Your search is only as good as your models...



Search

Prof. Abbeel steps through a few

search examples