



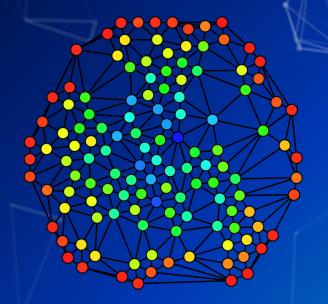
Graph Theory

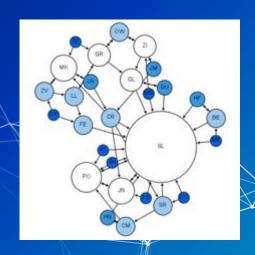
Week 1 Al Inspire Spring 2020

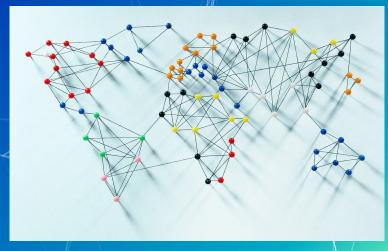




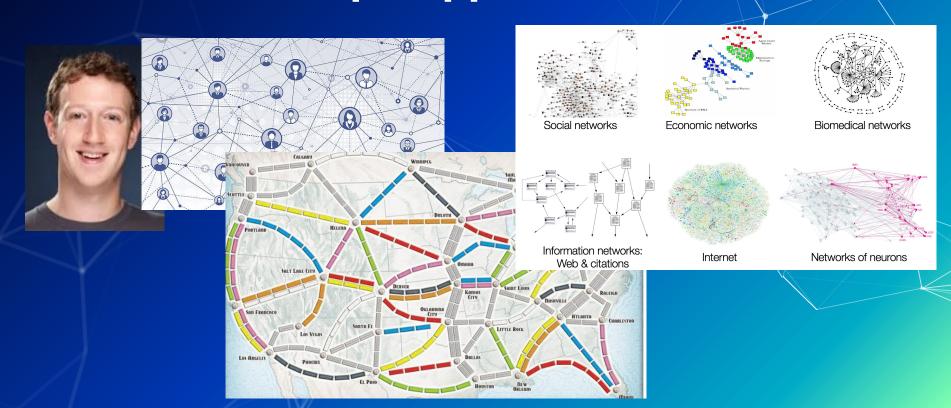
Introduction







Real World Graph Applications



Basic Java Programming + Algo concepts crash course

https://www.youtube.com/watch?v=0vyTEx1wyOY

What is a Graph?

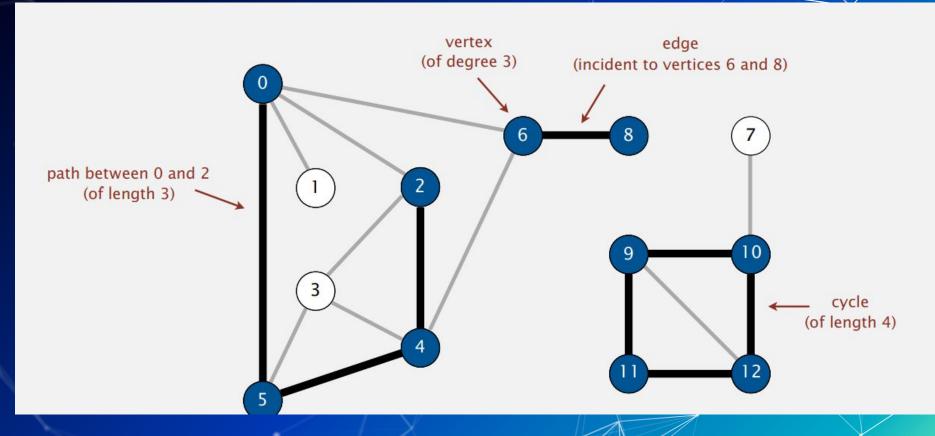
- Type of data structure to store data
 - More sophisticated than other structures learnt so far
- Set of nodes / vertices connected pairwise
 by edges (edge joins 2 nodes)
 - Node ⇒ stores some type of data
 - Edge ⇒ connection
- Total # vertices = V and total # edges = E

Vocabulary Part 1

- Connected vertices u and v = there exists
 some path between u and v
- Path = some sequence of nodes connected by edges s.t. no edge repeats (can repeat nodes)
 - Adj nodes in path seq are adj. to each other in real graph
- Cycle = pather where first and last nodes are same
- Degree of vertex = # edges touching vertex

Vocabulary Part 2

- Adjacent nodes = nodes connected by an edge
- Incident edges = edges that share vertex
- Incident vertex u & edge e IF u is one of the two vertices e connects
- Undirected Graph = graph with NO DIRECTION
 - Financial transaction graph may need direction
 - Some types of social networks may not need direction



Credits - Princeton University COS 226 Lecture

Graph API

```
public class Graph

Graph(int V) create an empty graph with V vertices

void addEdge(int v, int w) add an edge v—w

Iterable<Integer> adj(int v) vertices adjacent to v

int V() number of vertices

::
```

Credits - Princeton University COS 226 Lecture

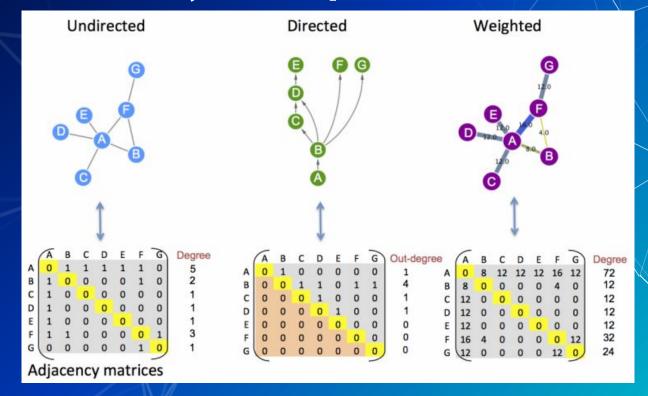
Task 1

How can we compute the degree of a vertex v in the graph G?

Representing a Graph

Understand diff graph rep. & analysis

Method 1 - Adjacency Matrix



Method 1 - Adjacency Matrix ANALYSIS

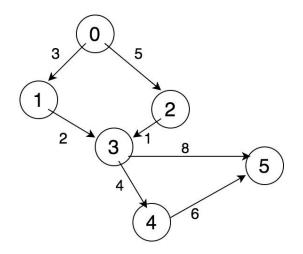
Task - print out which which vertices are adjacent.

Write code and analyze runtime

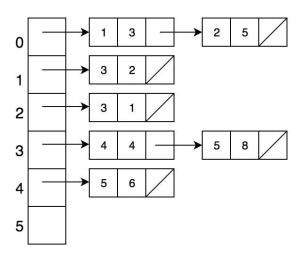
How could we reduce space complexity?

Method 2- Adjacency List

Directed Graph



Adjacency List Representation



www.kodefork.com

Method 2- Adjacency List ANALYSIS

Task - print out which which vertices are adjacent.

Write code and analyze runtime.

Note - harder analysis than adj.

matrix

Summary of Graph Rep

Use adjacency list in real life because much more efficient runtime

representation	space	add edge	edge between v and w?	iterate over vertices adjacent to v?
list of edges	E	1	E	E
adjacency matrix	V^2	1 †	1	V
adjacency lists	E+V	1	degree(v)	(degree(v)

Credits - Princeton University COS 226 Lecture

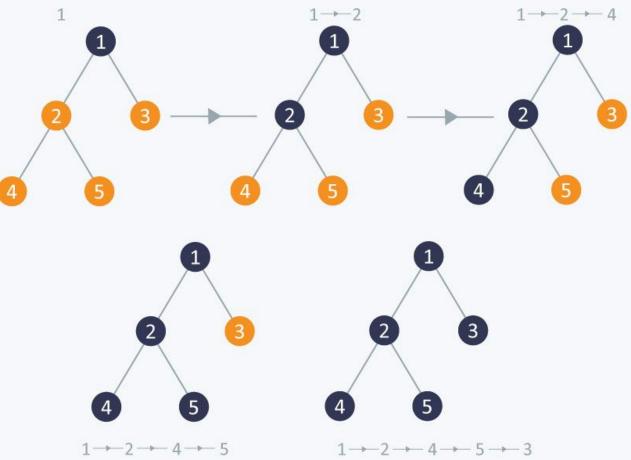
Homework

 Write Java implementation of API for adjacency list

Depth First Search

DFS - a popular traversal

DFS



Task 1

Write code or pseudocode which performs depth first search (RECURSIVELY)

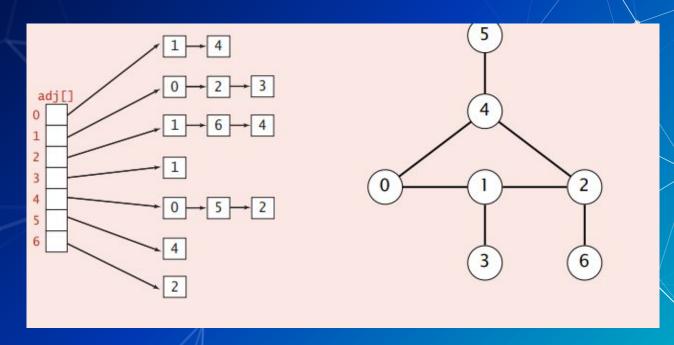
Solution

- 1) Mark the current vertex v
- Recursively visit ALL unmarked nodes w that are adjacent to v

Make sure to use the adjacency list AND an array to mark visited nodes

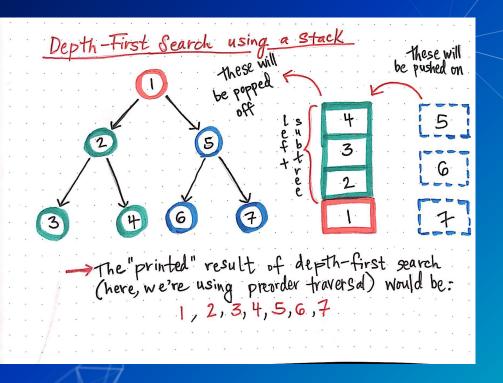
ALSO, can store another array which helps create paths

Demonstration



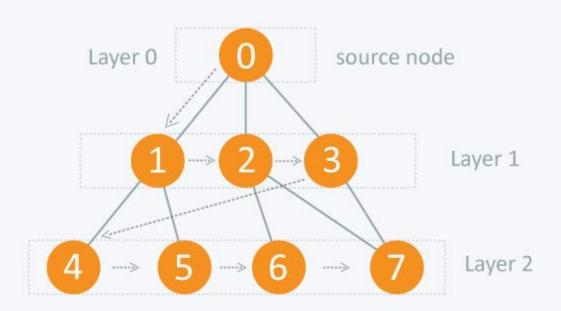
Credits - Princeton University COS 226 Lecture

Demonstration



Breadth First Search

BFS - a popular traversal



Task 1

Write code or pseudocode which performs breadth first search (using a queue)

Solution

- 1) Put first node in queue
- 2) Iterate till queue is EMPTY
 - a) Remove least recently added (FIFO) vertex
 - b) Add all of v's UNMARKED NEIGHBORS to queue AND mark them

Remember to use adjacency list to generate all possible neighbors ⇒ then from these, check which are unmarked to add them to queue (queue stores UNEXPLORED nodes)

Homework

1) Analyze algorithm to get runtime complexity of DFS and BFS (like we got runtime complexities for adjacency matrix and adjacency list representation space)

Summary

