# Revised Paragraphs of Crypto2023-Paper280

### Reviewer#B-Q2:

The revised introduction of references [4] (for replacing lines 114-121 in our paper) is as follows:

Recently, Beierle et al. proposed a technique to reduce the complexity [4]. The high-level idea of the technique is as follows. Denote the set of all right pairs for the differential  $\Delta_{in} \xrightarrow{E_1} \Delta_m$  by  $\mathcal{X}$ . To amplify the correlation of the distinguisher  $\Delta_{in} \xrightarrow{E_1} \gamma_{out}$ , we choose  $\epsilon r^{-2}q^{-4}$  right pairs in the set  $\mathcal{X}$  to observe its correlation. To efficiently get right pairs, we exploit the structure of the set  $\mathcal{X}$ . Concretely, the set  $\mathcal{X}$  might have a special structure, such that for any  $x \in \mathcal{X}$ , one can obtain a set  $X = \{(x \oplus u, x \oplus u \oplus \Delta_{in}) | u \in \mathcal{U}\}$ , where  $\mathcal{U}$  is a subspace, such that all elements in X are right pairs for the differential  $\Delta_{in} \to \Delta_m$ . For a differential whose set of right pairs has such a special structure, once one right pair is obtained, one can generate a set of  $2^{\dim \mathcal{U}}$  right pairs for free. To find such subspace  $\mathcal{U}$  for a differential, one can use the concept of the differential's neutral bits [BC04]. In particular, we require  $2^{\dim \mathcal{U}} \geqslant \epsilon r^{-2}q^{-4}$ . For some differentials for which obtaining a large enough  $\mathcal{U}$  is difficult, one might use a probabilistic approach related to the concept of probabilistic neutral bits [JS+08]. Assume that the probability that a randomly generated input x belongs to  $\mathcal{X}$  is  $\overline{p}$ . Then the complexity of the distinguisher is  $\epsilon \overline{p}^{-1}r^{-2}q^{-4}$ .

#### References

[BC04] Biham, E., Chen, R. (2004). Near-Collisions of SHA-0. In: Franklin, M. (eds) Advances in Cryptology – CRYPTO 2004. CRYPTO 2004. Lecture Notes in Computer Science, vol 3152. Springer, Berlin, Heidelberg.

[JS+08] Aumasson, JP., Fischer, S., Khazaei, S., Meier, W., Rechberger, C. (2008). New Features of Latin Dances: Analysis of Salsa, ChaCha, and Rumba. In: Nyberg, K. (eds) Fast Software Encryption. FSE 2008. Lecture Notes in Computer Science, vol 5086. Springer, Berlin, Heidelberg.

## Reviewer#B-Q3:

The revised tablenotes of Table 4 is as follows:

$(r_m, r_2)$	$\Delta_m \to \gamma_m \to \gamma_{out}$	Cor of $\Delta_m \to \gamma_{out}$
(8,3)	$[26] \to * \to [0, 9, 61, 91, 105]$	$2^{-4.679}$
(8,4)	$[31] \to * \to [0, 9, 61, 91, 105]$	$-2^{-10.970}$
(8,5)	$[31] \rightarrow [8, 41, 42, 73, 74] \rightarrow$	$-2^{-6.04} \times 2^{-10 \times 2}$
	[0, 29, 37, 38, 61, 68, 88, 91, 101, 102, 105, 114]	- /\-

 $<sup>^1</sup>$  \*: There are many choices searched by Algorithm 2. The maximum hamming weight of returned  $\gamma_m$  is 7. Since many differential-linear approximations share the same output mask  $\gamma_{out}$ , we directly present the experimental correlation of  $\Delta_m \to \gamma_{out}$ , i.e.,  $2^{-4.679}$  and  $-2^{-10.970}$ .

#### Reviewer#C-Q1:

A more detailed argument for Lemma 3 (for replacing lines 432-437 in our paper) is as follows:

Table 6 summarizes the result of the search. Given any plaintext pair  $(P, P \oplus \Delta_{in})$  conforming to the 4-round differential characteristic as shown in Table 5, using the 34 basis elements, one can create from the plaintext pair a plaintext structure consisting of  $2^{34}$  plaintext pairs that are expected to pass the differential characteristic together, with a theoretical probability  $2^{-3.7}$  under the assumption that the effects of the 34 basis elements are independent. For verifying the theoretical probability  $2^{-3.7}$ , we generate  $2^{10}$  plaintext pairs conforming to the 4-round differential characteristic, and find that the empirical probability is  $2^{-3.18}$  (resp.  $2^{-3.17}$ ,  $2^{-3.33}$ ) for LEA-128 (resp. LEA-192, LEA-256). Thus, we obtain Lemma 3. The 17-round key recovery attack introduced later uses this linear subspace.

**Lemma 3.** There is a set  $\mathcal{X} \subseteq \mathbb{F}_2^{128}$  of size  $2^{128-33-3.7}$  and a 34-dimension linear subspace  $\mathcal{U}$ , such that for any element  $x \in \mathcal{X}$  and any  $u \in \mathcal{U}$  it holds that  $E_1(x \oplus u) \oplus E_1(x \oplus u \oplus \Delta_{in}) = \Delta_m$  where  $E_1$  denotes 4 rounds of LEA.

<sup>&</sup>lt;sup>2</sup> Denote by  $r_m, r_2$  the number of rounds covered by  $E_m, E_2$ .

The three correlations  $2^{-4.679}$ ,  $-2^{-10.970}$ ,  $-2^{-6.04}$  are estimated again using N plaintext pairs and 100 keys. The three values are the median of 100 experimental correlations. For  $2^{-4.679}$  and  $-2^{-6.04}$ ,  $N=2^{24}$ . For  $-2^{-10.970}$ ,  $N=2^{32}$ . The number  $2^{-10}$  in the third row is the correlation of the linear approximation  $\gamma_m \to \gamma_{out}$ .