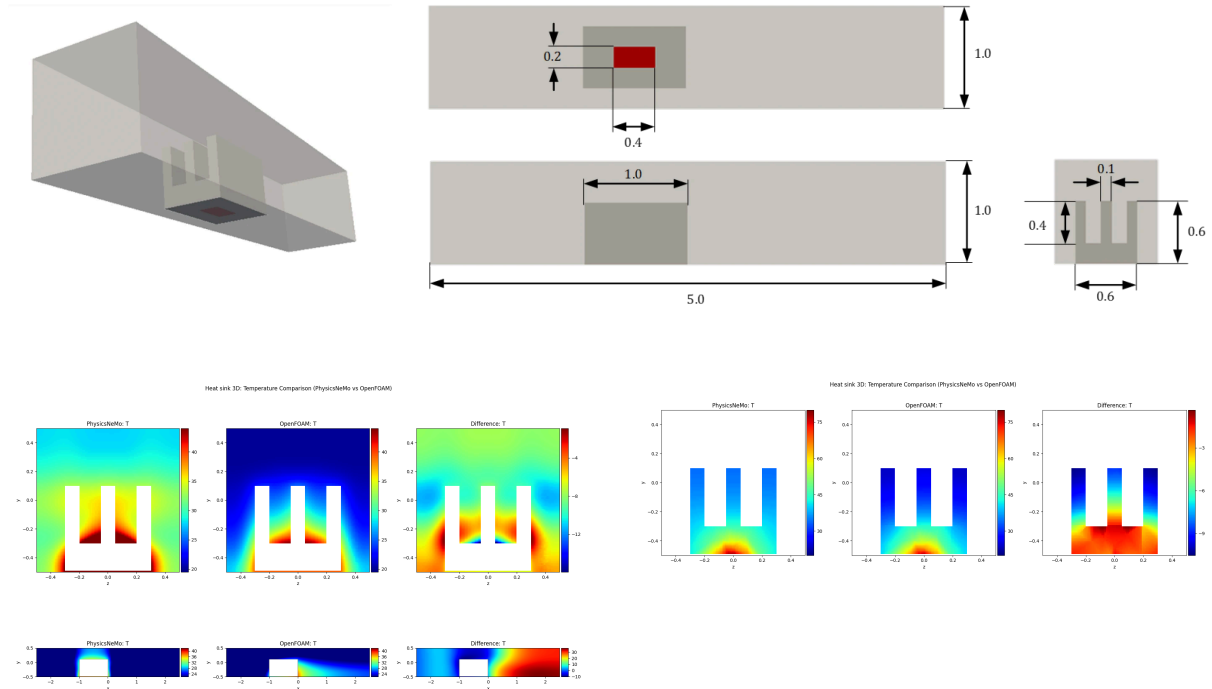


# NVIDIA PhysicsNeMo (Modulus) Part 5: Conjugate Heat Transfer



[https://docs.nvidia.com/deeplearning/modulus/modulus-sym/user\\_guide/advanced/conjugate\\_heat\\_transfer.html](https://docs.nvidia.com/deeplearning/modulus/modulus-sym/user_guide/advanced/conjugate_heat_transfer.html)

[https://catalog.ngc.nvidia.com/orgs/nvidia/teams/modulus/resources/modulus\\_sym\\_examples\\_supplemental\\_materials](https://catalog.ngc.nvidia.com/orgs/nvidia/teams/modulus/resources/modulus_sym_examples_supplemental_materials)

<https://github.com/NVIDIA/physicsnemo-sym>

<https://github.com/AI-ME-Ben/NVIDIA-Modulus-Reproduce/tree/main>

## Part 1 : Problem description

The geometry for a 3-fin heat sink placed inside a channel is shown in [Fig. 144](#). The inlet to the channel is at  $1 \text{ m/s}$ . The pressure at the outlet is specified as  $0 \text{ Pa}$ . All the other surfaces of the geometry are treated as no-slip walls.

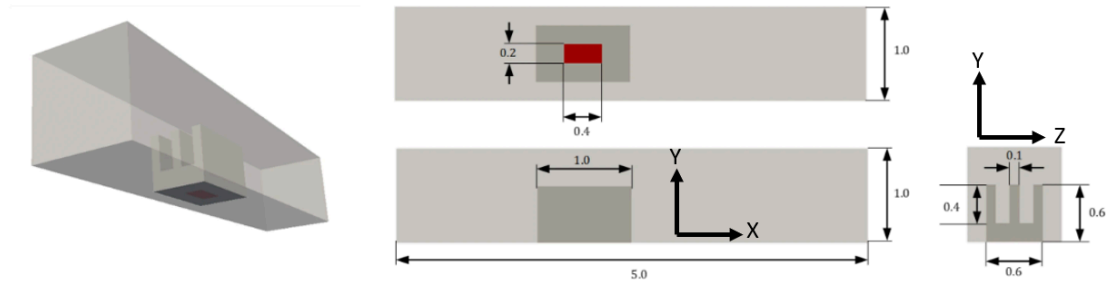


Fig. 144 Three fin heat sink geometry (All dimensions in  $m$ )

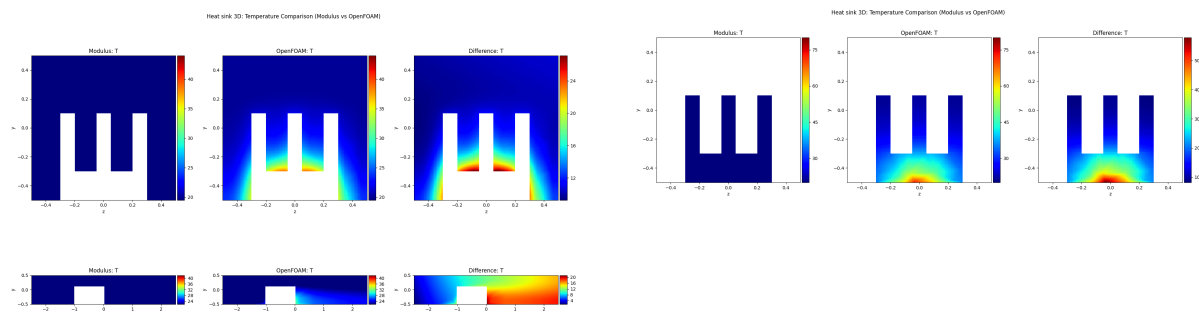
The inlet is at  $273.15 \text{ K}$ . The channel walls are adiabatic. The heat sink has a heat source of  $0.2 \times 0.4 \text{ m}$  at the bottom of the heat sink situated centrally on the bottom surface. The heat source generates heat such that the temperature gradient on the source surface is  $360 \text{ K/m}$  in the normal direction. Conjugate heat transfer takes place between the fluid-solid contact surface.

Table 5 Fluid and Solid Properties

Property	Fluid	Solid
Kinematic Viscosity ( $m^2/s$ )	0.02	NA
Thermal Diffusivity ( $m^2/s$ )	0.02	0.0625
Thermal Conductivity ( $W/m.K$ )	1.0	5.0

Material	Bulk Conductivity (W/mK)
Silver, Pure	418.0
Copper 11000	388.0
Aluminum 6061 T6	167.0
Zinc, Pure	112.2
Iron, Cast	55.0
Solder, 60% Tin	50.0
Titanium	15.6
ThermalGrease,T660	0.90
Fiberglass	0.040
Air, stp	0.025

## Part 2 : Implementation



<https://catalog.ngc.nvidia.com/orgs/nvidia/teams/physicsnemo/containers/physicsnemo>

```
1. docker run --shm-size=1g --ulimit memlock=-1 --
    ulimit stack=67108864 --runtime nvidia -p
    8888:8888 -p 7007:7007 --memory=16g -it
    nvcr.io/nvidia/physicsnemo/physicsnemo:25.03 bash
    -c "jupyter notebook --ip=0.0.0.0 --port=8888 --no-
    browser --allow-root"
```

<https://github.com/NVIDIA/physicsnemo-sym>

<https://github.com/AI-ME-Ben/NVIDIA-Modulus-Reproduce/tree/main>

[https://catalog.ngc.nvidia.com/orgs/nvidia/teams/modulus/resources/modulus\\_sym\\_examples\\_supplemental\\_materials](https://catalog.ngc.nvidia.com/orgs/nvidia/teams/modulus/resources/modulus_sym_examples_supplemental_materials)

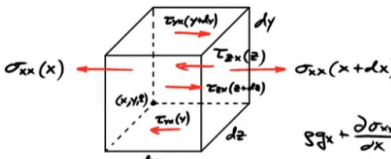
three\_fin\_flow.py  
three\_fin\_geometry.py  
three\_fin\_thermal.py

## Part 3 : Physics equation

### 1. Modified Navier-Stokes equation → Flow

```
# make navier stokes equations
if cfg.custom.turbulent:
    ze = ZeroEquation(nu=0.002, dim=3, time=False, max_distance=0.5)
    ns = NavierStokes(nu=ze.equations["nu"], rho=1.0, dim=3, time=False)
    navier_stokes_nodes = ns.make_nodes() + ze.make_nodes()
else:
    ns = NavierStokes(nu=0.01, rho=1.0, dim=3, time=False)
    navier_stokes_nodes = ns.make_nodes()
normal_dot_vel = NormalDotVec()
```

solve u, p



$$\rho g_x - \frac{\partial p}{\partial x} + \mu \left( \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} \right) = \rho \left( \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} \right) \quad \frac{\Sigma F_x = m a_x}{V}$$

$$\rho g_x + \frac{\partial \sigma_{xx}}{\partial x} + \frac{\partial \tau_{yx}}{\partial y} + \frac{\partial \tau_{zx}}{\partial z} = \rho \left( \frac{\partial u}{\partial t} + u \frac{\partial u}{\partial x} + v \frac{\partial u}{\partial y} + w \frac{\partial u}{\partial z} \right)$$

$$\rho g_y + \frac{\partial \tau_{xy}}{\partial x} + \frac{\partial \sigma_{yy}}{\partial y} + \frac{\partial \tau_{zy}}{\partial z} = \rho \left( \frac{\partial v}{\partial t} + u \frac{\partial v}{\partial x} + v \frac{\partial v}{\partial y} + w \frac{\partial v}{\partial z} \right)$$

$$\rho g_z + \frac{\partial \tau_{xz}}{\partial x} + \frac{\partial \tau_{yz}}{\partial y} + \frac{\partial \sigma_{zz}}{\partial z} = \rho \left( \frac{\partial w}{\partial t} + u \frac{\partial w}{\partial x} + v \frac{\partial w}{\partial y} + w \frac{\partial w}{\partial z} \right)$$

$$\sigma_{xx} = -p + 2\mu \frac{\partial u}{\partial x} \quad \tau_{xy} = \tau_{yx} = \mu \left( \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right)$$

$$\sigma_{yy} = -p + 2\mu \frac{\partial v}{\partial y} \quad \tau_{yz} = \tau_{zy} = \mu \left( \frac{\partial v}{\partial z} + \frac{\partial w}{\partial y} \right)$$

$$\sigma_{zz} = -p + 2\mu \frac{\partial w}{\partial z} \quad \tau_{zx} = \tau_{xz} = \mu \left( \frac{\partial w}{\partial x} + \frac{\partial u}{\partial z} \right)$$

# Navier-Stokes Equations with Zero Equation Turbulence Model

The standard Navier-Stokes equations with viscosity  $\nu$  are:

$$\frac{\partial \mathbf{u}}{\partial t} + (\mathbf{u} \cdot \nabla) \mathbf{u} = -\frac{1}{\rho} \nabla p + \nabla \cdot (\nu_{\text{eff}} \nabla \mathbf{u}) + \mathbf{f}$$

<https://www.youtube.com/watch?v=NjoMoH51UZc>

[https://docs.nvidia.com/deeplearning/modulus/modulus-sym/user\\_guide/foundational/zero\\_eq\\_turbulence.html](https://docs.nvidia.com/deeplearning/modulus/modulus-sym/user_guide/foundational/zero_eq_turbulence.html)

<https://www.youtube.com/watch?v=zf0jU25uWqo&t=4s>

## 2. Advection diffusion equation → Heat

```
# make thermal equations
ad = AdvectionDiffusion(T="theta_f", rho=1.0, D=0.02, dim=3, time=False)
dif = Diffusion(T="theta_s", D=0.0625, dim=3, time=False)
dif_interface = DiffusionInterface("theta_f", "theta_s", 1.0, 5.0, dim=3, time=False)
f_grad = GradNormal("theta_f", dim=3, time=False)
s_grad = GradNormal("theta_s", dim=3, time=False)
```

known  $u$ , solve  $C$

## 4. Interpretation of the Terms

$$\underbrace{\frac{\partial C}{\partial t}}_{\text{Time variation}} + \underbrace{\mathbf{u} \cdot \nabla C}_{\text{Advection}} = \underbrace{D \nabla^2 C}_{\text{Diffusion}} + \underbrace{S}_{\text{Source/Sink}}$$

- Time variation ( $\frac{\partial C}{\partial t}$ ): Change in  $C$  over time.
- Advection ( $\mathbf{u} \cdot \nabla C$ ): Transport of  $C$  by the velocity field.
- Diffusion ( $D \nabla^2 C$ ): Spreading of  $C$  due to random molecular motion.
- Source/Sink ( $S$ ): External sources (e.g., chemical reactions, heat generation).

## General Form of the Diffusion Equation

The diffusion equation is given by:

$$\frac{\partial C}{\partial t} = D \nabla^2 C + Q$$

where:

- $C(x, y, z, t)$  is the concentration (or temperature, or other dependent variable) at position  $(x, y, z)$  and time  $t$ .
- $D$  is the diffusion coefficient (or thermal diffusivity for heat transfer problems).
- $\nabla^2$  is the Laplacian operator, which in Cartesian coordinates is:

$$\nabla^2 = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$$

- $Q(x, y, z, t)$  is a source term, representing external sources or sinks (such as chemical reactions, heating sources, etc.).

## Diffusion Interface Boundary Conditions

### 1. Dirichlet Condition (Continuity of Variable)

- Ensures the variable (e.g., temperature or concentration) is continuous across the interface.

$$T_1 = T_2 \quad \text{at the interface}$$


### 2. Neumann Condition (Flux Conservation)

- Ensures the flux is continuous across the interface, preserving physical conservation laws.

$$D_1 \nabla T_1 \cdot \mathbf{n} = D_2 \nabla T_2 \cdot \mathbf{n}$$

### Key Takeaways:

- ✓ No sudden jumps in the variable.
- ✓ Flux must be conserved at the interface.
- ✓ Critical for heat transfer, diffusion, and multi-material simulations.

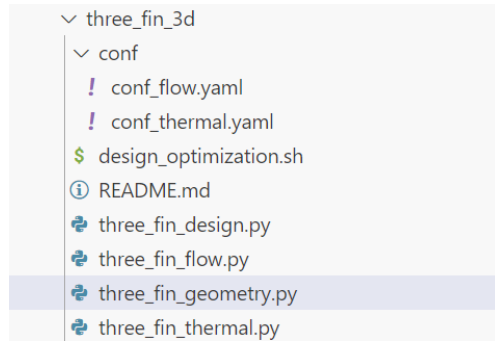
 `three_fin_thermal.py`

<https://www.youtube.com/watch?v=4EVKEImJtsg>

[https://www.youtube.com/watch?v=8ew\\_ZRNkRWU&t=219s](https://www.youtube.com/watch?v=8ew_ZRNkRWU&t=219s)

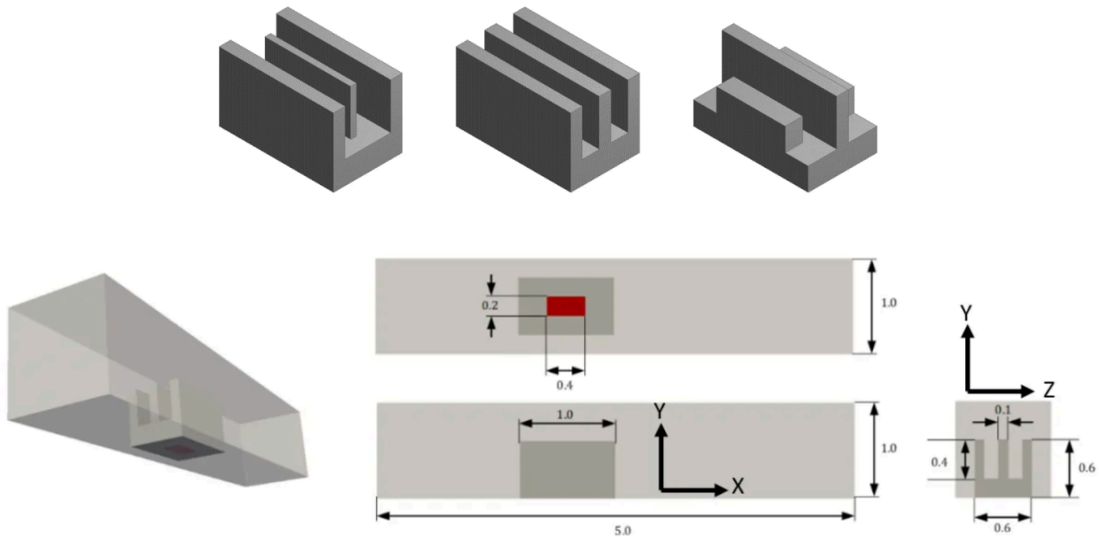
[https://en.wikipedia.org/wiki/Convection%E2%80%93diffusion\\_equation](https://en.wikipedia.org/wiki/Convection%E2%80%93diffusion_equation)

## Part 4 : Code walkthrough

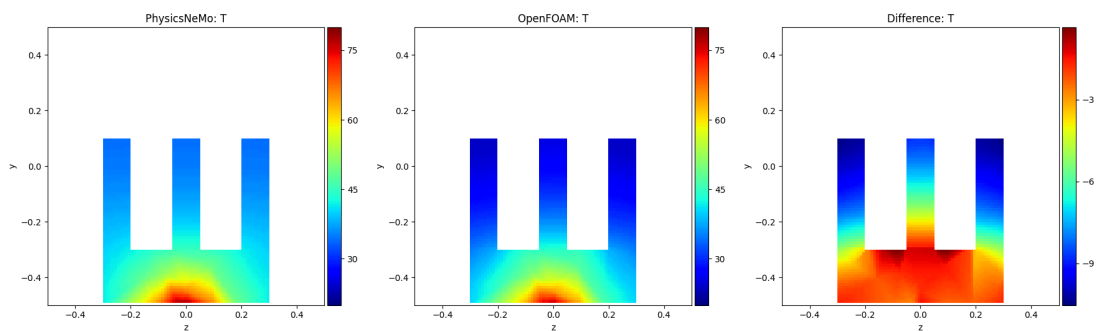


[https://docs.nvidia.com/deeplearning/physicsnemo/physicsnemo-sym/user\\_guide/advanced/parametrized\\_simulations.html](https://docs.nvidia.com/deeplearning/physicsnemo/physicsnemo-sym/user_guide/advanced/parametrized_simulations.html)

```
hcentral_fin = (0.0, 0.6),
hside_fins = (0.0, 0.6),
lcentral_fin = (0.5, 1.0)
lside_fins = (0.5, 1.0)
tcentral_fin = (0.05, 0.15)
tside_fins = (0.05, 0.15)
```



Heat sink 3D: Temperature Comparison (PhysicsNeMo vs OpenFOAM)



Heat sink 3D: Temperature Comparison (PhysicsNeMo vs OpenFOAM)

