



Machine Learning

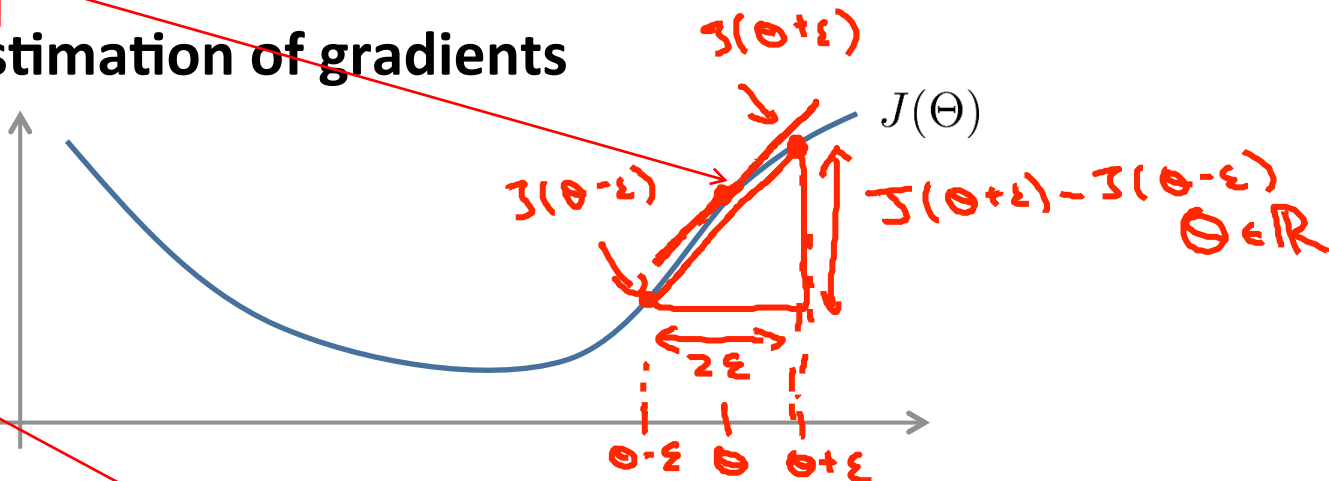
Neural Networks: Learning

Gradient checking

usamos inclinação recta como
aproximação derivada

Numerical estimation of gradients

estimar derivada



$$\frac{d}{d\theta} J(\theta) \approx \frac{J(\theta + \epsilon) - J(\theta - \epsilon)}{2\epsilon}$$

$\epsilon = 10^{-4}$

~~$$\frac{J(\theta + \epsilon) - J(\theta)}{\epsilon}$$~~

Implement: gradApprox = (J(theta + EPSILON) - J(theta - EPSILON)) / (2*EPSILON)

Parameter vector θ

VECTOR

→ $\theta \in \mathbb{R}^n$ (E.g. θ is “unrolled” version of $\underline{\Theta^{(1)}}$, $\underline{\Theta^{(2)}}$, $\underline{\Theta^{(3)}}$)

→ $\theta = [\theta_1, \theta_2, \theta_3, \dots, \theta_n]$

APROXIMAR DERIVADAS

→ $\frac{\partial}{\partial \theta_1} J(\theta) \approx \frac{J(\theta_1 + \epsilon, \theta_2, \theta_3, \dots, \theta_n) - J(\theta_1 - \epsilon, \theta_2, \theta_3, \dots, \theta_n)}{2\epsilon}$

Handwritten annotations: "thetaPlus" under $\theta_1 + \epsilon$ and "thetaMinus" under $\theta_1 - \epsilon$.

→ $\frac{\partial}{\partial \theta_2} J(\theta) \approx \frac{J(\theta_1, \theta_2 + \epsilon, \theta_3, \dots, \theta_n) - J(\theta_1, \theta_2 - \epsilon, \theta_3, \dots, \theta_n)}{2\epsilon}$

Handwritten annotations: an upward arrow under $\theta_2 + \epsilon$ and a box around $\theta_2 - \epsilon$.

⋮

→ $\frac{\partial}{\partial \theta_n} J(\theta) \approx \frac{J(\theta_1, \theta_2, \theta_3, \dots, \theta_n + \epsilon) - J(\theta_1, \theta_2, \theta_3, \dots, \theta_n - \epsilon)}{2\epsilon}$

Handwritten annotations: boxes around $\theta_n + \epsilon$ and $\theta_n - \epsilon$.

```

for i = 1:n, ←
    thetaPlus = theta;
    thetaPlus(i) = thetaPlus(i) + EPSILON;
    thetaMinus = theta;
    thetaMinus(i) = thetaMinus(i) - EPSILON;
    gradApprox(i) = (J(thetaPlus) - J(thetaMinus))
                    / (2*EPSILON);
end;

```

$$\begin{bmatrix} \theta_1 \\ \theta_2 \\ \vdots \\ \theta_i + \epsilon \\ \vdots \\ \theta_n \end{bmatrix} \rightarrow \theta_i - \epsilon$$



$$\frac{\partial}{\partial \theta_i} J(\theta).$$

Check that gradApprox \approx DVec ←

↑
From back prop.

backpropagation

Implementation Note:

- - Implement backprop to compute DVec (unrolled $D^{(1)}, D^{(2)}, D^{(3)}$).

- - Implement numerical gradient check to compute gradApprox.

- - Make sure they give similar values. fazer aprox é muito exigente e lento
- - Turn off gradient checking. Using backprop code for learning.

quando verificamos que funciona removemos



Important:

- - Be sure to disable your gradient checking code before training your classifier. If you run numerical gradient computation on every iteration of gradient descent (or in the inner loop of `costFunction(...)`) your code will be very slow.