



Machine Learning

Linear Regression with multiple variables

Gradient descent in
practice I: Feature Scaling

Feature Scaling

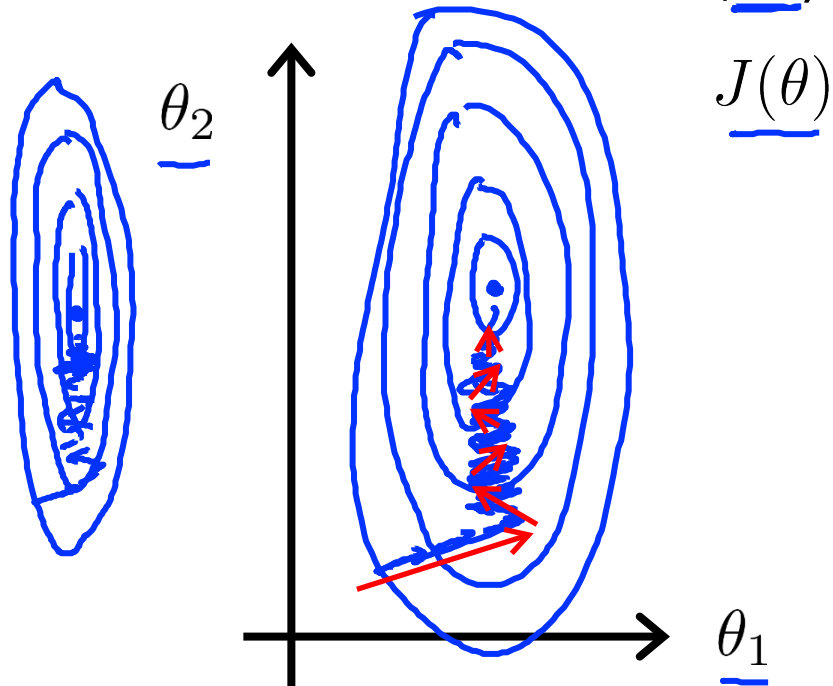
ao mudarmos a
escala o GD
converge + rapido

with similar range values GD can converge
more quickly

Idea: Make sure features are on a similar scale.

E.g. $x_1 = \text{size (0-2000 feet}^2)$ ←

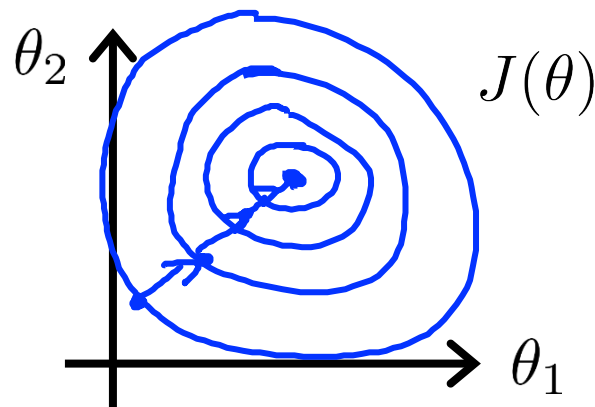
$x_2 = \text{number of bedrooms (1-5)}$ ←



→ $x_1 = \frac{\text{size (feet}^2)}{2000}$ ←

→ $x_2 = \frac{\text{number of bedrooms}}{5}$ ✓

$0 \leq x_1 \leq 1$ $0 \leq x_2 \leq 1$



Feature Scaling

Get every feature into approximately a $-1 \leq x_i \leq 1$ range.

$$x_0 = 1$$

$$0 \leq x_1 \leq 3 \quad \checkmark$$

$$-2 \leq x_2 \leq 0.5 \quad \checkmark$$

$$-100 \leq x_3 \leq 100 \quad \times$$

$$-0.0001 \leq x_4 \leq 0.0001 \quad \times$$

$$-3 \text{ to } 3 \quad \checkmark$$

$$-\frac{1}{3} \text{ to } \frac{1}{3} \quad \checkmark$$

Mean normalization

Replace x_i with $x_i - \mu_i$ to make features have approximately zero mean
(Do not apply to $x_0 = 1$).

E.g. $\rightarrow x_1 = \frac{\text{size} - 1000}{2000}$

$$x_2 = \frac{\# \text{bedrooms} - 2}{5}$$

Average size = 1000
1-5 bedrooms

$$\rightarrow -0.5 \leq x_1 \leq 0.5, -0.5 \leq x_2 \leq 0.5$$

$$x_1 \leftarrow \frac{x_1 - \mu_1}{\sigma_1} \quad \begin{array}{l} \text{average value} \\ \text{of } x \\ \text{in training set} \end{array} \quad \bigg| \quad x_2 \leftarrow \frac{x_2 - \mu_2}{\sigma_2}$$

range (max-min)
(or standard deviation)