



Machine Learning

Linear Regression with multiple variables

Normal equation
and non-invertibility
(optional)

Normal equation

$$\theta = \underline{(X^T X)^{-1} X^T y}$$

$$\underline{X^T X}$$

- What if $\boxed{X^T X}$ is non-invertible? (singular/
degenerate)

- Octave: `pinv(X' * X) * X' * y`

θ

$\boxed{\text{pinv}}$
inv

What if $X^T X$ is non-invertible? causas de n ser invertivel?

- 1• Redundant features (linearly dependent).

E.g. $x_1 = \text{size in feet}^2$

~~$x_2 = \text{size in m}^2$~~

eliminar variaveis redundantes

$$x_1 = (3.28)^2 x_2$$

$$1\text{m} = 3.28\text{ feet}$$

$$\rightarrow m = 10 \leftarrow$$

$$\rightarrow n = 100 \leftarrow$$

$$\Theta \in \mathbb{R}^{101}$$

- 2• Too many features (e.g. $m \leq n$).

- Delete some features, or use regularization.

↓ later
technical