



Machine Learning

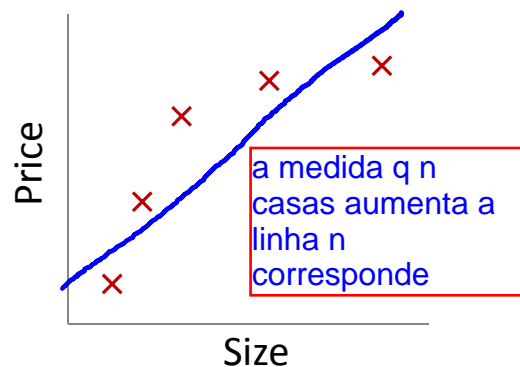
# Regularization

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The problem of  
overfitting

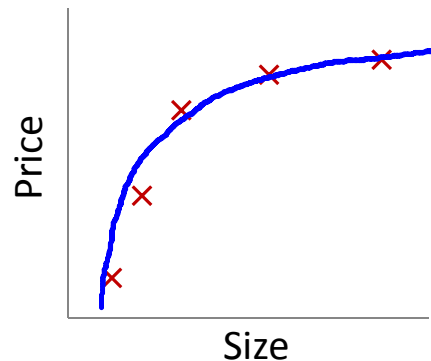
para exemplos ts funciona bem mas novos  
exemplos NAO

## Example: Linear regression (housing prices)



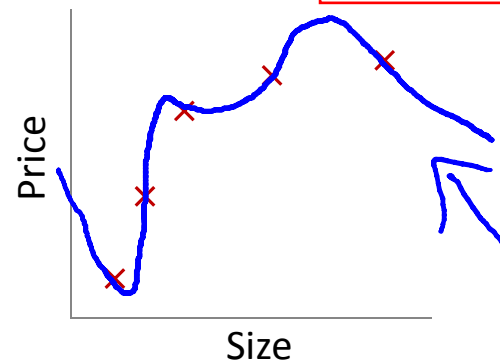
$$\rightarrow \theta_0 + \theta_1 x$$

"Underfit" "High bias"



$$\rightarrow \theta_0 + \theta_1 x + \theta_2 x^2$$

"Just right"

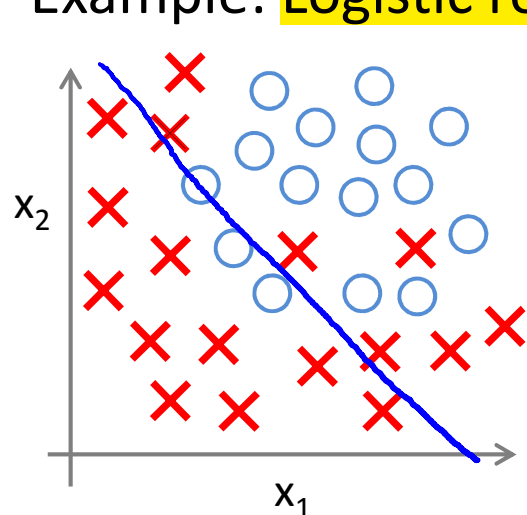


$$\rightarrow \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 + \theta_4 x^4$$

"Overfit" "High variance"

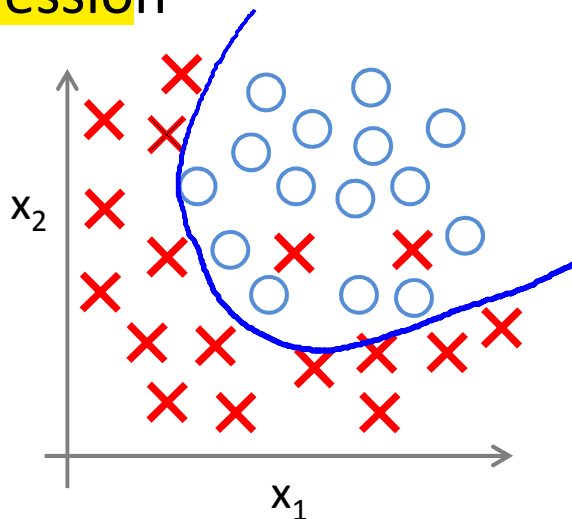
**Overfitting:** If we have too many features, the learned hypothesis may fit the training set very well ( $J(\theta) = \frac{1}{2m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)})^2 \approx 0$ ), **but fail to generalize** to **new examples** (predict prices on new examples).

## Example: Logistic regression



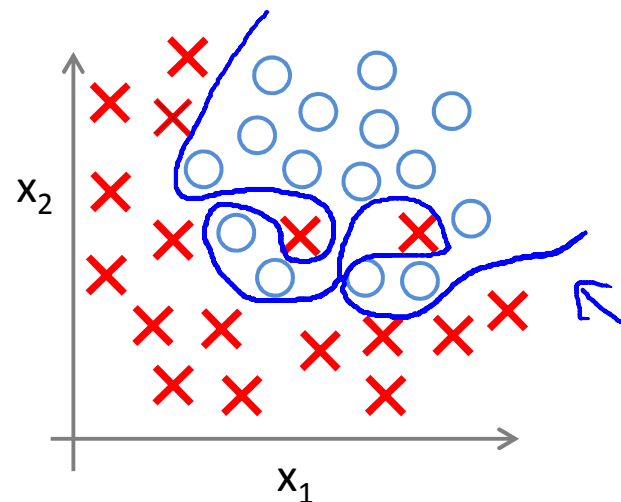
$\rightarrow h_{\theta}(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_2)$   
( $g$  = sigmoid function)

"Underfit"



$g(\theta_0 + \theta_1 x_1 + \theta_2 x_2$   
 $+ \theta_3 x_1^2 + \theta_4 x_2^2$   
 $+ \theta_5 \underline{x_1 x_2})$

razoavel



$g(\theta_0 + \theta_1 x_1 + \theta_2 x_1^2$   
 $+ \theta_3 \underline{x_1^2 x_2} + \theta_4 \underline{x_1^2 x_2^2}$   
 $+ \theta_5 \underline{x_1^2 x_2^3} + \theta_6 \underline{x_1^3 x_2} + \dots)$

"Overfit"

mt variancia

## Addressing overfitting:

$x_1$  = size of house

$x_2$  = no. of bedrooms

$x_3$  = no. of floors

$x_4$  = age of house

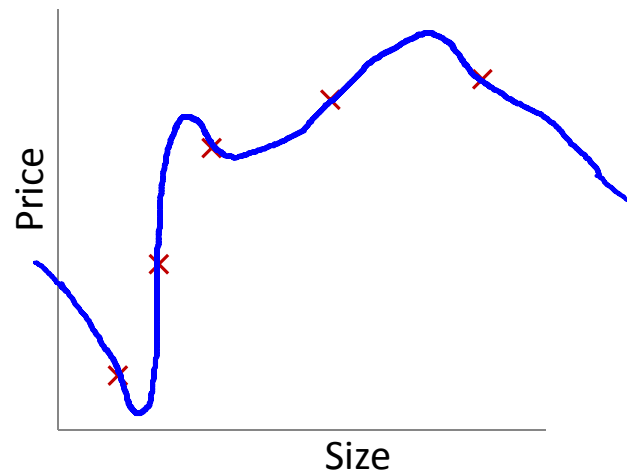
$x_5$  = average income in neighborhood

$x_6$  = kitchen size

⋮

$x_{100}$

quanto + features  
tveremos + difícil vai  
ser fazer plot  
dados com função



# Addressing overfitting:

temos 2 opções  
para simplificar  
função no plot  
dados

## Options:

1. Reduce number of features.
  - — Manually select which features to keep.
  - — Model selection algorithm (later in course).
2. Regularization.
  - — Keep all the features, but reduce magnitude/values of parameters  $\theta_j$ .
  - Works well when we have a lot of features, each of which contributes a bit to predicting  $y$ .

