



Machine Learning

# Logistic Regression

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## Hypothesis Representation

queremos hipótese  
entre 0 e 1

## Logistic Regression Model

Want  $0 \leq h_{\theta}(x) \leq 1$

$$h_{\theta}(x) = g(\theta^T x)$$

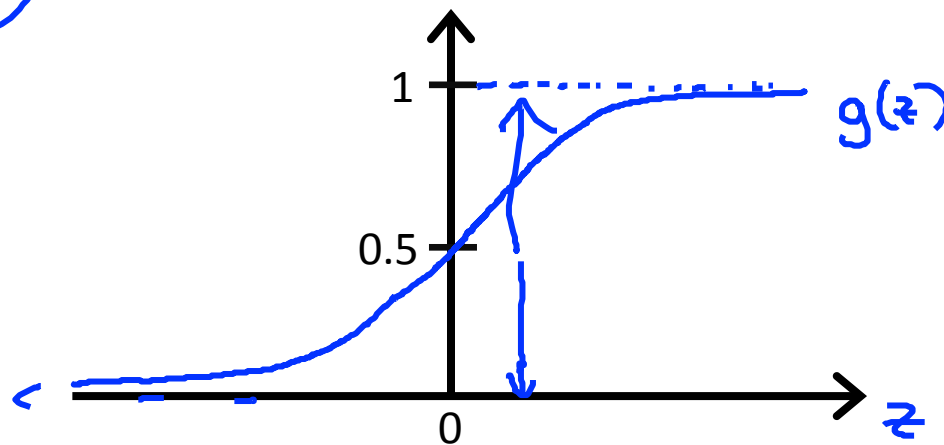
$$\rightarrow g(z) = \frac{1}{1 + e^{-z}}$$

$\theta^T x$

Sigmoid function

Logistic function

$$h_{\theta}(x) = \frac{1}{1 + e^{-\theta^T x}}$$



Parameters  $\theta$ .

## Interpretation of Hypothesis Output

$$h_{\theta}(x)$$

$h_{\theta}(x)$  = estimated probability that  $y = 1$  on input  $x$  ←

Example: If  $\underline{x} = \begin{bmatrix} x_0 \\ x_1 \end{bmatrix} = \begin{bmatrix} 1 \leftarrow \\ \text{tumorSize} \leftarrow \end{bmatrix}$

$h_{\theta}(x)$  = 0.7

$y = 1$

Tell patient that 70% chance of tumor being malignant

$$\underline{h_{\theta}(x)} = \underline{P(y=1|x;\theta)}$$

$y = 0 \text{ or } 1$

“probability that  $y = 1$ , given  $x$ ,  
parameterized by  $\theta$ ”

→  $P(y = 0 | \text{~~scribble~~}) + \boxed{P(y = 1 | \text{~~scribble~~})} = 1$

→  $P(y = 0 | x; \theta) = 1 - \boxed{P(y = 1 | x; \theta)}$