

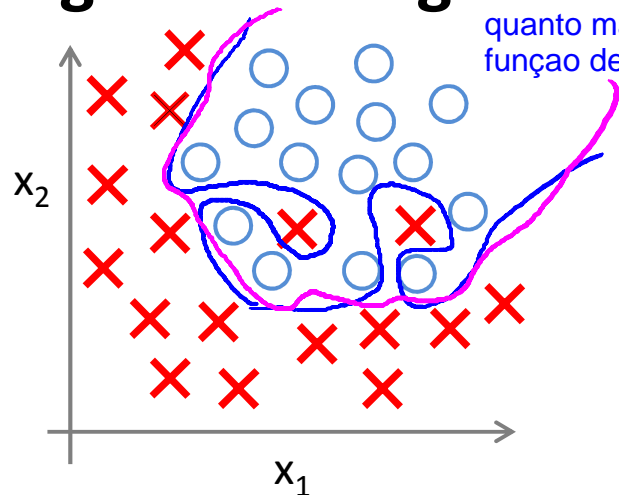


Machine Learning

Regularization

Regularized
logistic regression

Regularized logistic regression.



quanto mais variáveis pior o overfitting

função demasiado complexa e apesar de acertar no training set FALHA previsões

$$h_{\theta}(x) = g(\theta_0 + \theta_1 x_1 + \theta_2 x_1^2 + \theta_3 x_1^2 x_2 + \theta_4 x_1^2 x_2^2 + \theta_5 x_1^2 x_2^3 + \dots)$$

Cost function:

$$\rightarrow J(\theta) = - \left[\frac{1}{m} \sum_{i=1}^m y^{(i)} \log h_{\theta}(x^{(i)}) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)})) \right]$$

regularizar ajuda
o overfitting
problem

$$+ \frac{\lambda}{2m} \sum_{j=1}^n \theta_j^2$$

$$\theta_1, \theta_2, \dots, \theta_n$$

Gradient descent

Repeat {

$$\rightarrow \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_0^{(i)}$$

$$\rightarrow \theta_j := \theta_j - \alpha \left[\underbrace{\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_j^{(i)}}_{\substack{(j = \cancel{0}, 1, 2, 3, \dots, n) \\ \theta_1, \dots, \theta_n}} - \frac{1}{n} \theta_j \right] \leftarrow$$

}

$$\frac{\partial}{\partial \theta_j} J(\theta)$$

$$\underline{h_{\theta}(x)} = \frac{1}{1 + e^{-\theta^T x}}$$

Advanced optimization

→ `function [jVal, gradient] = costFunction(theta)`

`jVal = [code to compute $J(\theta)$];`

$$\rightarrow J(\theta) = \left[-\frac{1}{m} \sum_{i=1}^m y^{(i)} \log(h_{\theta}(x^{(i)})) + (1 - y^{(i)}) \log(1 - h_{\theta}(x^{(i)})) \right] + \left[\frac{\lambda}{2m} \sum_{j=1}^n \theta_j^2 \right]$$

→ `gradient(1) = [code to compute $\frac{\partial}{\partial \theta_0} J(\theta)$];`

$$\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_0^{(i)} \leftarrow$$

→ `gradient(2) = [code to compute $\frac{\partial}{\partial \theta_1} J(\theta)$];`

$$\left(\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_1^{(i)} \right) - \frac{\lambda}{m} \theta_1 \leftarrow$$

→ `gradient(3) = [code to compute $\frac{\partial}{\partial \theta_2} J(\theta)$];`

$$\vdots \left(\frac{1}{m} \sum_{i=1}^m (h_{\theta}(x^{(i)}) - y^{(i)}) x_2^{(i)} \right) - \frac{\lambda}{m} \theta_2$$

`gradient(n+1) = [code to compute $\frac{\partial}{\partial \theta_n} J(\theta)$];`

f_{minunc} (a cost function) $\theta = \begin{bmatrix} \theta_0 \\ \theta_1 \\ \vdots \\ \theta_n \end{bmatrix}$ $\theta_0 \leftarrow \text{theta}(1)$
 $\theta_1 \leftarrow \text{theta}(2)$
 $\theta_n \leftarrow \text{theta}(n+1)$

$J(\theta)$

