



Machine Learning

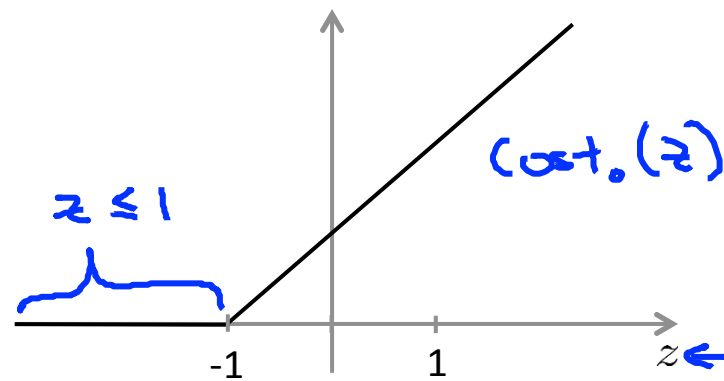
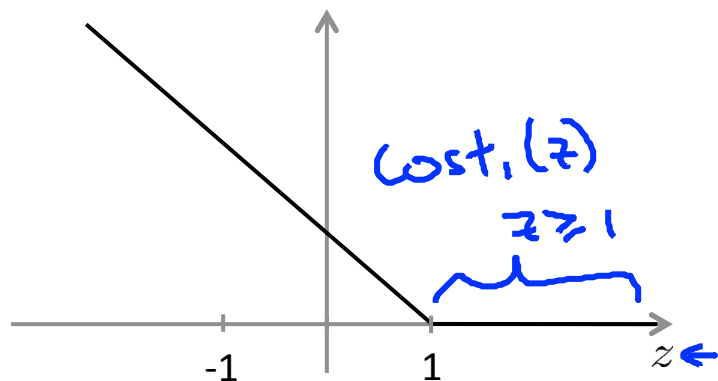
# Support Vector Machines

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## Large Margin Intuition

# Support Vector Machine

$$\rightarrow \min_{\theta} C \sum_{i=1}^m \left[ y^{(i)} \underline{\text{cost}_1(\theta^T x^{(i)})} + (1 - y^{(i)}) \underline{\text{cost}_0(\theta^T x^{(i)})} \right] + \frac{1}{2} \sum_{j=1}^n \theta_j^2$$



$\rightarrow$  If  $y = 1$ , we want  $\theta^T x \geq 1$  (not just  $\geq 0$ )

$$\theta^T x \geq 1$$

$\rightarrow$  If  $y = 0$ , we want  $\theta^T x \leq -1$  (not just  $< 0$ )

$$\theta^T x \leq -1$$

$$C = 100,000$$

# SVM Decision Boundary

$$\min_{\theta} C \sum_{i=1}^m \left[ y^{(i)} \text{cost}_1(\theta^T x^{(i)}) + (1 - y^{(i)}) \text{cost}_0(\theta^T x^{(i)}) \right] + \frac{1}{2} \sum_{j=1}^n \theta_j^2$$

minimization objective

este 1.º termo = 0

$= 0$

Whenever  $y^{(i)} = 1$ :

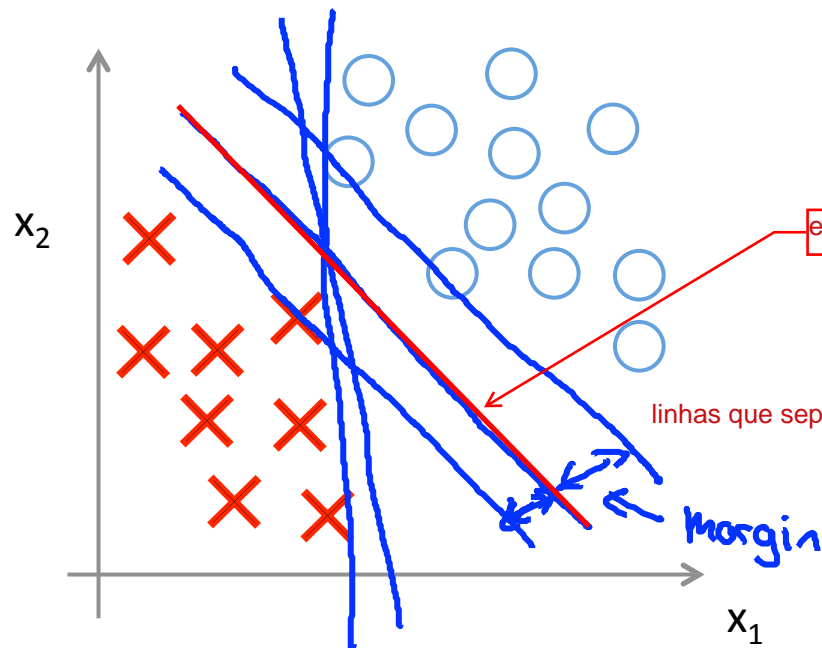
$$\theta^T x^{(i)} \geq 1$$

Whenever  $y^{(i)} = 0$ :

$$\theta^T x^{(i)} \leq -1$$

$$\begin{aligned} \min_{\theta} & C \sum_{i=1}^m \theta_j + \frac{1}{2} \sum_{j=1}^n \theta_j^2 \\ \text{s.t. } & \theta^T x^{(i)} \geq 1 \quad \text{if } y^{(i)} = 1 \\ & \theta^T x^{(i)} \leq -1 \quad \text{if } y^{(i)} = 0 \end{aligned}$$

# SVM Decision Boundary: Linearly separable case



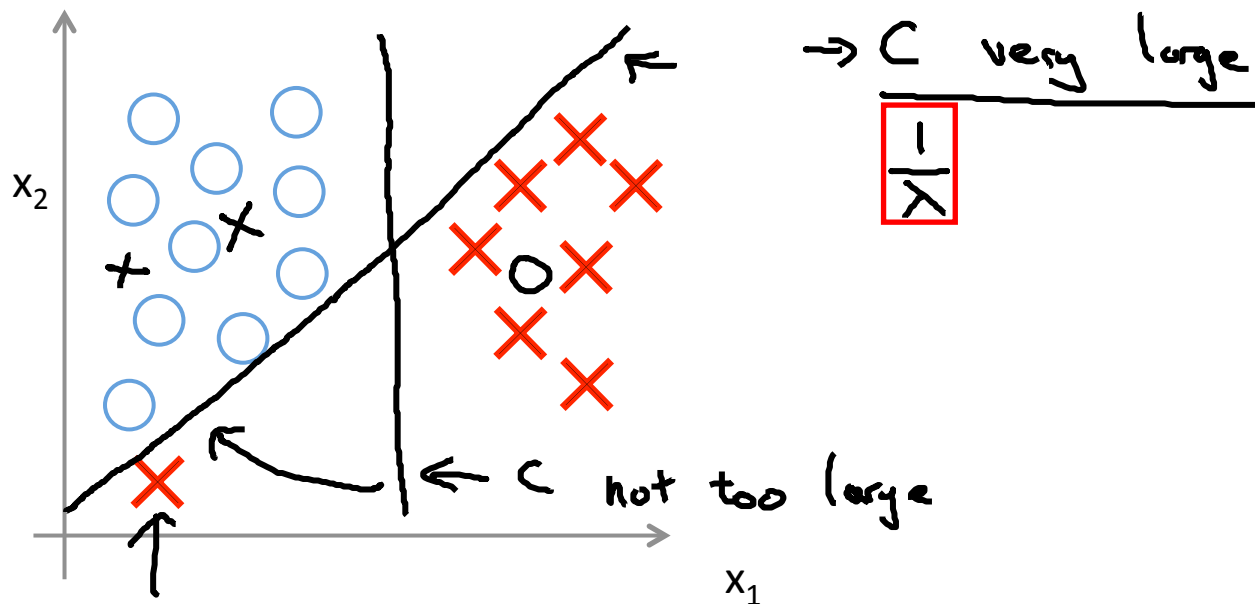
este linha tem distancia chamada margin

linhas que separam + dos -

a linha da ao SVM uma robustez pois tenta separar os dados com maior margem possivel

Large margin classifier

# Large margin classifier in presence of outliers



se  $C$  for grande mudamos linha decision boundary