

Machine Learning

# Regularization

Regularized linear regression

## Regularized linear regression

termo para regularizar

$$J(\theta) = \frac{1}{2m} \left[ \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)})^2 + \left( \sum_{j=1}^{n} \theta_j^2 \right) \right]$$

$$\min_{\theta} \frac{J(\theta)}{}$$

#### **Gradient descent**

<u></u>

 $\bigcirc$ ,  $\bigcirc$ ,  $\bigcirc$ ,  $\bigcirc$ n

$$m$$
 $(i)$ 



$$\Rightarrow \theta_0 := \theta_0 - \alpha \frac{1}{m} \sum_{i=1}^m (h_\theta(x^{(i)}) - y^{(i)}) x_0^{(i)}$$

derivada parcial?

$$\underbrace{\frac{1}{m} \sum_{i=1}^{m} (h_{\theta}(x^{(i)}) - y^{(i)}) x_{j}^{(i)}}_{(j=\mathbf{X}, 1, 2, 3, \dots, n)}$$



}

$$-\frac{1}{m}\sum_{i=1}^{m}(h_{\theta}(x^{(i)})-y^{(i)})x_{j}^{(i)}$$



 $\frac{\lambda}{h}$  <

, Q .a

0jx0.99

### **Normal equation**

$$X = \begin{bmatrix} (x^{(1)})^T \\ \vdots \\ (x^{(m)})^T \end{bmatrix} \leftarrow y = \begin{bmatrix} y^{(1)} \\ \vdots \\ y^{(m)} \end{bmatrix}$$

$$\Rightarrow \min_{\theta} J(\theta)$$

$$\Rightarrow 0 = (x^T \times + \lambda)$$

## Non-invertibility (optional/advanced).

Suppose 
$$m \leq n$$
,

(#examples) (#features) se tivermos poucos exemplos e variaveis é impossivelinverter matriz

$$\theta = \underbrace{(X^T X)^{-1} X^T y}_{\text{Non-invertible / singular}} \qquad \qquad \underbrace{\text{pinu}}_{\text{R}}$$

If 
$$\frac{\lambda > 0}{\theta} = \left( X^T X + \lambda \begin{bmatrix} 0 & 1 & 1 & 1 \\ & 1 & & \\ & & \ddots & 1 \end{bmatrix} \right)^{-1} X^T y$$