



Latent Consistency Models - Synthesizing High-Resolution Images with Few-Step Inference

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References

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<https://latent-consistency-models.github.io/>
<https://github.com/luosiallen/latent-consistency-model>

huggingface
https://huggingface.co/docs/diffusers/api/pipelines/latent_consistency_models
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[Paper Review blog]
<https://kimjy99.github.io/논문리뷰/latent-consistency-model/>
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Accelerating Diffusion Models: Consistency Models and Hybrid Approach
<https://www.youtube.com/watch?v=OT3JWNz0ll8&t=235s>

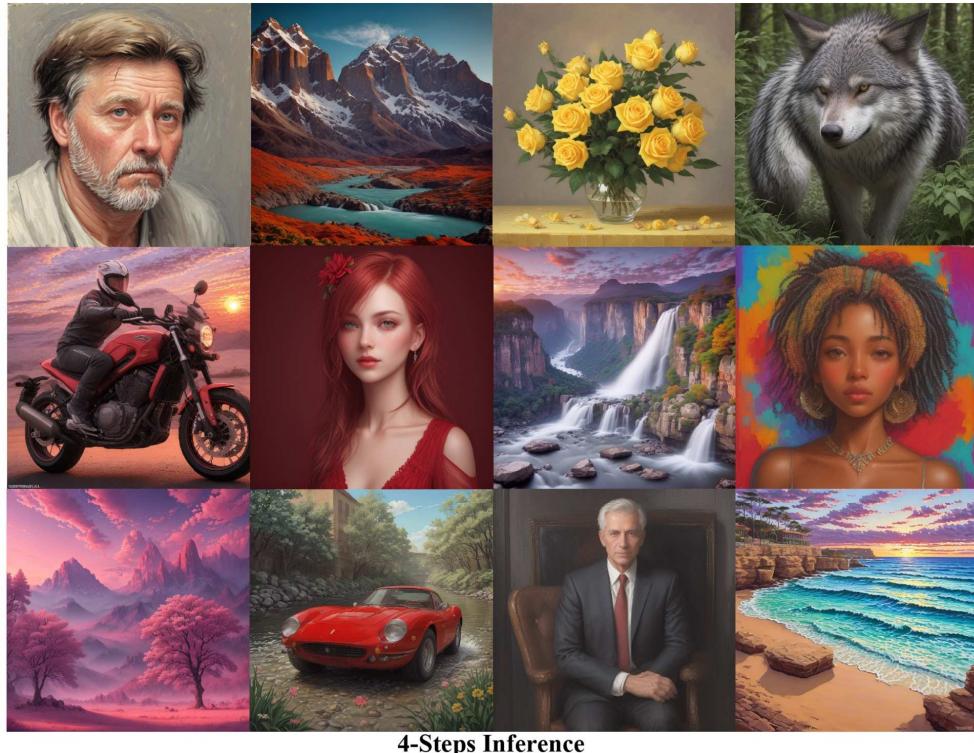
Latent Consistency Models

Abstract (Paper)

- **Latent Diffusion models (LDMs)**
 - ✓ Remarkable results in **synthesizing high-resolution images**.
 - ✓ However, **Iterative sampling process** - Computationally intensive and leads to slow generation.
- Inspired by **Consistency Models** (song et al.),
- Propose **Latent Consistency Models (LCMs)**,
 - ✓ Enabling **swift Inference** with minimal steps on any **pre-trained LDMs**, including **Stable Diffusion** (rombach et al).
- Viewing **the guided reverse diffusion process** as **solving an augmented probability flow ODE (PF-ODE)**,
- LCMs are designed to directly predict the solution of such ODE in latent space, mitigating the need for numerous iterations and allowing rapid, high-fidelity sampling.
- Efficiently distilled from pre-trained classifier-free guided diffusion models, a high-quality **768 x 768 2~4-step LCM** takes only **32 A100 GPU hours for training**.
- Furthermore, introduce **Latent Consistency Fine-tuning (LCF)**, a novel method that is tailored for fine-tuning LCMs on customized image datasets.
- Evaluation on the LAION-5B-Aesthetics dataset demonstrates that LCMs achieve **state-of-the-art text-to-image generation** performance with **few-step inference**.
- Project Page: <https://latent-consistency-models.github.io/>

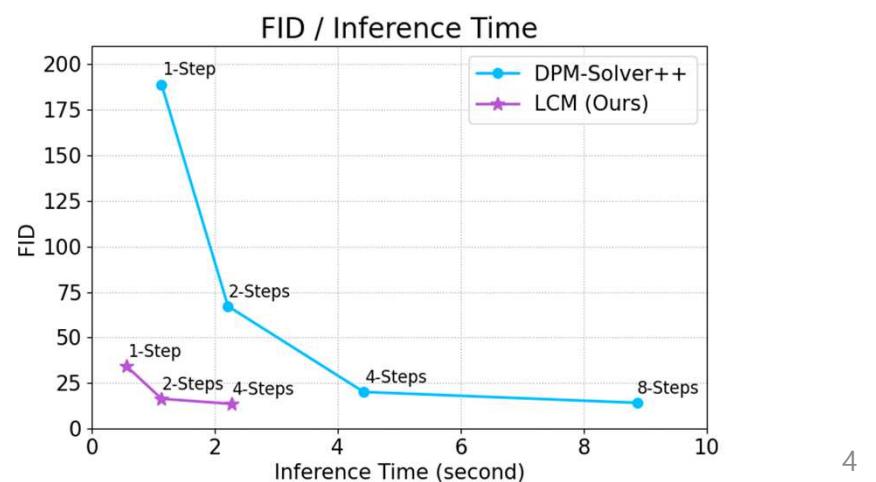
Latent Consistency Models

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Few-Step Generated Images :

LCMs can be distilled from any pre-trained Stable Diffusion (SD) in only 4,000 training steps (~32 A100 GPU Hours) for generating high quality 768 x 768 resolution images in 2~4 steps or even one step, significantly accelerating text-to-image generation. We employ LCM to distill the Dreamshaper-V7 version of SD in just 4,000 training iterations.



1 Introduction & 2. Related Works

➤ Diffusion Models

- Compared to VAEs and GANs, diffusion models enjoy the benefit of **training stability** and **better likelihood estimation**.
 - Be trained to **denoise the noise-corrupted data to estimate the score of data distribution**.
 - During inference, draw samples by running the reverse diffusion process to gradually denoise the data point.
 - Bottlenecked by their **slow generation speed**
-
- Ho et al., 2020, **DDPM**, Denoising Diffusion Probabilistic Models
 - Song et al., 2020a, **DPIM**, Denoising Diffusion Implicit Models
 - Nichol & Dhariwal, 2021, **iDDPM**, Improved Denoising Diffusion Probabilistic Models
 - Ramesh et al., 2022, **DALL-E2**, Hierarchical Text-Conditional Image Generation with Clip Latents
 - Rombach et al., 2022, **Stable Diffusion**, High-Resolution Image Synthesis with Latent Diffusion Models
 - Song & Ermon, 2019. Generative Modeling by Estimating Gradients of the Data Distribution

➤ Accelerating DMs

- Training-free methods such as
 - **ODE solvers** : Song et al., 2020a, **DPIM**; Lu et al., 2022a;b, DPM-Solver, **DPM-Solver++**
 - **Adaptive step size solvers** : Jolicoeur-Martineau et al., 2021, Gotta go fast when generating data with score-based models.
 - **Predictor-corrector methods** : Song et al., 2020b, Score-based generative modeling through stochastic differential equations
- Training-based approaches include
 - **Optimized discretization** : Watson et al., 2021, Learning to efficiently sample from diffusion probabilistic models
 - **Truncated diffusion** : Lyu et al., 2022; Zheng et al., 2022,
 - **Neural operator** : Zheng et al., 2023, Fast sampling of diffusion models via operator learning
 - **Distillation** : Salimans & Ho, 2022, Progressive distillation for fast sampling of diffusion models; Meng et al., 2023, **On distillation of guided diffusion models**
- More recently, new generative models for faster sampling have also been proposed (Liu et al., 2022; 2023).

1 Introduction & 2. Related Works

➤ Latent Diffusion Models (LDMs)

- Synthesizing high-resolution text-to-images.
- Ex) Stable Diffusion (SD) performs forward and reverse diffusion processes in the data latent space, resulting in more efficient computation.
- Rombach et al., 2022, **Stable Diffusion**, High-Resolution Image Synthesis with Latent Diffusion Models

➤ Consistency Models (CMs)

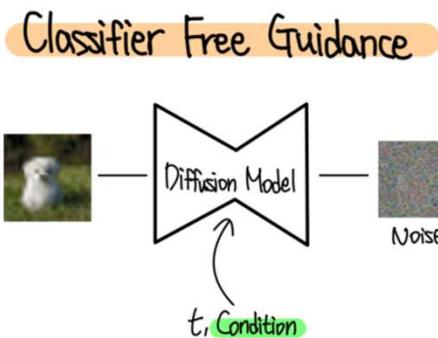
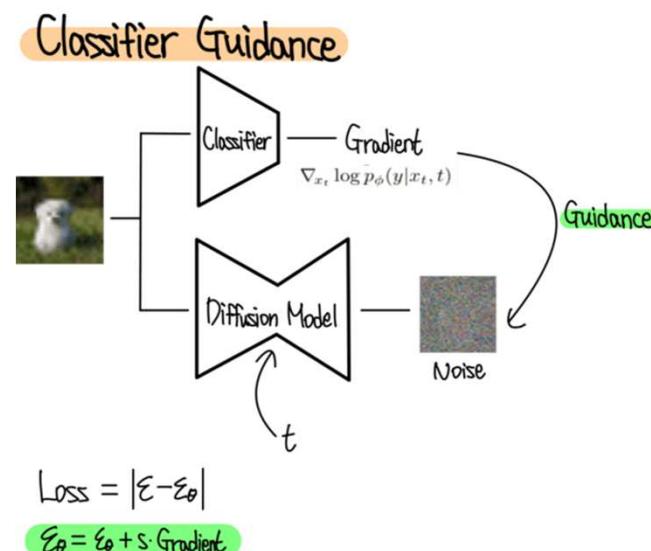
- A new type of generative model for **faster sampling while preserving generation quality**.
- CMs adopt **consistency mapping** to **directly map any point in ODE trajectory** to its origin, **enabling fast one-step generation**.
- CMs can be **trained by distilling pre-trained diffusion models** or as standalone **generative models**.
- Song et al., 2023, Consistency Models
- CMs **constrained to pixel space image generation tasks**, making it **unsuitable for synthesizing high-resolution images**.
- Moreover, the applications to the **conditional diffusion model** and the incorporation **of classifier-free guidance** have **not been explored**, rendering their methods unsuitable for text-to-image generation synthesis.

Latent Consistency Models

1 Introduction & 2. Related Works

❖ Classifier Free Guidance : Classifier-free diffusion guidance

- Jonathan Ho, Tim Salimans, Classifier-Free Diffusion Guidance, NIPS2021, Google Research, Brain team
- Diffusion Models Beat GANs on Image Synthesis 논문 :
 - ✓ 추가 classifier를 학습하여 샘플의 품질을 향상시키는 classifier guidance가 제안됨. **Classifier guidance**는 **diffusion model**의 **score** 추정치와 **classifier**의 로그 확률의 입력 기울기를 혼합함.
 - ✓ Classifier gradient의 강도를 변경하여 Inception Score (IS)와 FID (또는 precision과 recall)를 절충할 수 있음
- 어떠한 classifier도 사용하지 않는 classifier-free guidance를 제안함
- **Classifier-free guidance**는 이미지 classifier의 기울기 방향으로 샘플링하는 대신 **conditional diffusion model**과 함께 학습된 **unconditional diffusion model**의 **score** 추정치를 혼합함.
- 혼합 가중치를 사용하여 classifier guidance에서 얻은 것과 유사한 FID/IS tradeoff를 얻는다. 또한 pure generative diffusion model과 다른 유형의 생성 모델과 함께 매우 높은 fidelity의 샘플을 합성하는 것이 가능함



$$\text{Loss} = |\epsilon - \epsilon_\theta|$$
$$\epsilon_\theta = \text{Interpolation}[\epsilon_0(\pi, t), \epsilon_0(\pi, t, 0)]$$

[Source] <https://ffighting.net/deep-learning-paper-review/diffusion-model/classifier-free-guidance/>

Latent Consistency Models

Main Contributions

- **Latent Consistency Models (LCMs)** for fast, high-resolution image generation.
 - LCMs employ **consistency models** in the **image latent space**, enabling **fast few-step or even one-step high-fidelity sampling on pre-trained latent diffusion models** (e.g., Stable Diffusion (SD)).
- Provide a simple and efficient **one-stage guided consistency distillation method**
 - to distill SD for few-step (2~4) or even 1-step sampling
 - to efficiently convert a **pre-trained guided diffusion model** into a **latent consistency model** by solving an **augmented PF-ODE**.
- Propose the **SKIPPING-STEP** technique to further accelerate the convergence.
- For 2- and 4-step inference, our method costs only 32 A100 GPU hours for training and achieves state-of-the-art performance
- Propose **Latent Consistency Finetuning**, which allows fine-tuning a pre-trained LCM to support few-step inference on customized image datasets while preserving the ability of fast inference.

3. PRELIMINARIES

❖ Diffusion Models

- Diffusion models, or score-based generative models
 - Progressively inject Gaussian noises into the data, and then generate samples from noise via a reverse denoising process
 - Define a **forward process** transitioning the origin data distribution $p_{data}(\mathbf{x})$ to marginal distribution $q_t(\mathbf{x}_t)$, via transition kernel:
- $$q_{0t}(\mathbf{x}_t | \mathbf{x}_0) = N(\mathbf{x}_t | \alpha(t)\mathbf{x}_0, \sigma^2(t)\mathbf{I}),$$
- $\alpha(t)$, $\sigma(t)$ specify the noise schedule.

- In continuous time perspective, the forward process can be described by a **stochastic differential equation (SDE)** for $t \in [0, T]$: (☞ Song et al. (2020b); Lu et al. (2022a); Karras et al. (2022))

$$d\mathbf{x}_t = f(t)\mathbf{x}_t dt + g(t)d\mathbf{w}_t, \quad \mathbf{x}_0 \sim p_{data}(\mathbf{x}_0)$$
 - $w(t)$ is the standard Brownian motion

$$f(t) = \frac{d \log \alpha(t)}{dt}, \quad g^2(t) = \frac{d \sigma^2(t)}{dt} - 2 \frac{d \log \alpha(t)}{dt} \sigma^2(t). \quad (1)$$

- By considering the reverse time SDE,
 - the marginal distribution $q_t(\mathbf{x})$ satisfies the following ordinary differential equation, called the **Probability Flow ODE (PF-ODE)** (☞ Song et al., 2020b; Lu et al., 2022a):

$$\frac{d\mathbf{x}_t}{dt} = f(t)\mathbf{x}_t - \frac{1}{2}g^2(t)\nabla_{\mathbf{x}} \log q_t(\mathbf{x}_t), \quad \mathbf{x}_T \sim q_T(\mathbf{x}_T). \quad (2)$$

- In diffusion models, we train the noise prediction model $\epsilon_\theta(\mathbf{x}_t, t)$ to fit $-\nabla \log q_t(\mathbf{x}_t)$ (called the **score function**).
 - Approximating the score function by the noise prediction model in 21, one can obtain the following **empirical PF-ODE** for sampling:

$$\frac{d\mathbf{x}_t}{dt} = f(t)\mathbf{x}_t + \frac{g^2(t)}{2\sigma_t}\epsilon_\theta(\mathbf{x}_t, t), \quad \mathbf{x}_T \sim \mathcal{N}(\mathbf{0}, \tilde{\sigma}^2 \mathbf{I}). \quad (3)$$

3. PRELIMINARIES

❖ Diffusion Models

- For **class-conditioned diffusion models**,
 - **Classifier-Free Guidance (CFG)** (Ho & Salimans, 2022) :
 - ✓ An effective technique to significantly improve the quality of generated samples
 - ✓ Has been widely used in several large-scale diffusion models including **GLIDE** Nichol et al. (2021), **Stable Diffusion** (Rombach et al., 2022), **DALL·E 2** (Ramesh et al., 2022) and **Imagen** (Saharia et al., 2022).
 - Given a CFG scale ω , the original noise prediction is replaced by a linear combination of conditional and unconditional noise prediction:

$$\tilde{\epsilon}_{\theta}(z_t, \omega, c, t) = (1 + \omega)\epsilon_{\theta}(z_t, c, t) - \omega\epsilon_{\theta}(z, \emptyset, t)$$

3. PRELIMINARIES

❖ Consistency Models

- A new family of generative models
 - Enables one-step or few-step generation.
 - Core idea : **Learn the consistency function that maps any points on a trajectory of the PF-ODE to that trajectory's origin** (i.e., the solution of the PF-ODE)

$$\mathbf{f} : (\mathbf{x}_t, t) \longmapsto \mathbf{x}_\epsilon$$

ϵ is a fixed small positive number.

- The consistency function should satisfy the ***self-consistency property***:

$$\mathbf{f}(\mathbf{x}_t, t) = \mathbf{f}(\mathbf{x}_{t'}, t'), \forall t, t' \in [\epsilon, T]. \quad (4)$$

- (Song et al., 2023) Key idea for learning a consistency model \mathbf{f}_θ : To learn a consistency function from data by effectively enforcing the self-consistency property
- Ensure that $\mathbf{f}_\theta(\mathbf{x}, \epsilon) = \mathbf{x}$, the consistency model \mathbf{f}_θ is parameterized as:

$$\mathbf{f}_\theta(\mathbf{x}, t) = c_{\text{skip}}(t)\mathbf{x} + c_{\text{out}}(t)\mathbf{F}_\theta(\mathbf{x}, t), \quad (5)$$

$c_{\text{skip}}(t)$ and $c_{\text{out}}(t)$: Differentiable functions with $c_{\text{skip}}(t, \epsilon) = 1$ and $c_{\text{out}}(\epsilon) = 0$

$\mathbf{F}_\theta(\mathbf{x}, t)$: a deep neural network

- A CM can be either distilled from a pre-trained diffusion model (known as *Consistency Distillation*) or trained from scratch

3. PRELIMINARIES

❖ Consistency Models

- To enforce the self-consistency property, we maintain a target model θ^- , updated with exponential moving average (EMA) of the parameter θ , we intend to learn; $\theta^- \leftarrow \mu\theta^- + (1 - \mu)\theta$
- Define the consistency loss

$$\mathcal{L}(\theta, \theta^-; \Phi) = \mathbb{E}_{x,t} \left[d \left(f_\theta(x_{t_{n+1}}, t_{n+1}), f_{\theta^-}(\hat{x}_{t_n}^\phi, t_n) \right) \right], \quad (6)$$

$d(\cdot)$: a chosen metric function for measuring the distance between two samples; $d(x, y) = \|x - y\|^2$

$\hat{x}_{t_n}^\phi$: a one-step estimation of x_{t_n} from $x_{t_{n+1}}$

$$\hat{x}_{t_n}^\phi \leftarrow x_{t_{n+1}} + (t_n - t_{n+1})\Phi(x_{t_{n+1}}, t_{n+1}; \phi). \quad (7)$$

- Φ denotes the one-step ODE solver applied to PF-ODE in Eq. 24. (Song et al., 2023) used Euler (Song et al., 2020b) or Heun solver (Karras et al., 2022) as the numerical ODE solver

- Pseudo-code for consistency distillation

Algorithm 2 Consistency Distillation (CD) (Song et al., 2023)

Input: dataset \mathcal{D} , initial model parameter θ , learning rate η , ODE solver $\Phi(\cdot, \cdot, \cdot)$, distance metric $d(\cdot, \cdot)$, and EMA rate μ

$$\theta^- \leftarrow \theta$$

repeat

 Sample $x \sim \mathcal{D}$ and $n \sim \mathcal{U}[1, N - 1]$

 Sample $x_{t_{n+1}} \sim \mathcal{N}(x; t_{n+1}^2 \mathbf{I})$

$\hat{x}_{t_n}^\phi \leftarrow x_{t_{n+1}} + (t_n - t_{n+1})\Phi(x_{t_{n+1}}, t_{n+1}, \phi)$

$\mathcal{L}(\theta, \theta^-; \Phi) \leftarrow d(f_\theta(x_{t_{n+1}}, t_{n+1}), f_{\theta^-}(\hat{x}_{t_n}^\phi, t_n))$

$\theta \leftarrow \theta - \eta \nabla_\theta \mathcal{L}(\theta, \theta^-; \Phi)$

$\theta^- \leftarrow \text{stopgrad}(\mu\theta^- + (1 - \mu)\theta)$

until convergence

Latent Consistency Models

4. LATENT CONSISTENCY MODELS

❖ Summary

Consistency Models (CMs) (Song et al., 2023)

- Only focused on image generation tasks on ImageNet 64×64 (Deng et al., 2009) and LSUN 256×256 (Yu et al., 2015).
- Unexplore to generate higher-resolution text-to-image tasks

Latent Consistency Models (LCMs)

- Adopt a **consistency model in the image latent space**, similar to LDMs
- Choose the **Stable Diffusion (SD)** as the underlying diffusion model to **distill** from.
- Aim to achieve **few-step (2~4) and even one-step inference on SD without compromising image quality**.
- The **classifier-free guidance (CFG)** (Ho & Salimans, 2022) is an effective technique to further **improve sample quality** and is widely used in SD.

- Propose a **simple one-stage guided distillation method** in Sec 4.2 that solves an **augmented PF-ODE**, **integrating CFG into LCM** effectively.
- Propose **SKIPPING-STEP** technique to **accelerate the convergence of LCMs** in Sec. 4.3.
- Finally, propose **Latent Consistency Fine-tuning** to finetune a pre-trained LCM for few-step inference on a customized dataset in Sec 4.4.

Latent Consistency Models

4.1 LCM : Consistency Distillation in the Latent Space

- **LDM** : Stable Diffusion (SD) - Image Latent Space (Rombach et al., 2022)
 - Utilizing **image latent space** in large-scale diffusion models has effectively **enhanced image generation quality** and **reduced computational load**.
 - SD
 - An autoencoder (E, D) is first trained to compress high-dim image data into low-dim latent vector $z = E(x)$, which is then decoded to reconstruct the image as $x = D(z)$.
 - **Training diffusion models in the latent space** greatly reduces the computation costs compared to pixel-based models and speeds up the inference process;
 - LDMs make it possible to generate high-resolution images on laptop GPUs.
- For **LCMs**, we leverage the advantage of **the latent space for consistency distillation**, contrasting with the pixel space used in **CMs** (Song et al., 2023).
 - Termed **Latent Consistency Distillation (LCD)** is applied to **pre-trained SD**, allowing the synthesis of high-resolution (e.g., 768×768) images in 1~4 steps.
 - We focus on **conditional generation**.

Latent Consistency Models

4.1 LCM : Consistency Distillation in the Latent Space

- Recall that the **PF-ODE** of the reverse diffusion process (Song et al., 2020b; Lu et al., 2022a)

$$\frac{dz_t}{dt} = f(t)z_t + \frac{g^2(t)}{2\sigma_t} \epsilon_\theta(z_t, c, t), \quad z_T \sim \mathcal{N}(0, \tilde{\sigma}^2 I), \quad (8)$$

- z_t are image latents
- $\epsilon_\theta(z_t, c, t)$ is the noise prediction model
- c is the given condition (e.g text)
- Samples can be drawn by solving the PF-ODE from T to 0.

- To perform **LCD**, introduce the **consistency function** $f_\theta: (z_t, c, t) \mapsto z_0$ to directly predict the solution of PF-ODE (Eq. 8) for $t = 0$.

- We parameterize f_θ by the noise prediction model $\hat{\epsilon}_\theta$,

$$f_\theta(z, c, t) = c_{\text{skip}}(t)z + c_{\text{out}}(t) \left(\frac{z - \sigma_t \hat{\epsilon}_\theta(z, c, t)}{\alpha_t} \right), \quad (\epsilon\text{-Prediction}) \quad (9)$$

- $c_{\text{skip}}(0) = 1$ and $c_{\text{out}}(0) = 0$
- $\hat{\epsilon}_\theta(z_t, c, t)$: a noise prediction model that initializes with the same parameters as the teacher diffusion model
- f_θ can be parameterized in various ways, depending on the teacher diffusion model parameterizations of predictions ↗ Appendix D.

Latent Consistency Models

4.1 LCM : Consistency Distillation in the Latent Space

➤ Recall that the **PF-ODE** of the reverse diffusion process

$$\frac{dz_t}{dt} = f(t)z_t + \frac{g^2(t)}{2\sigma_t} \epsilon_\theta(z_t, c, t), \quad z_T \sim \mathcal{N}(0, \tilde{\sigma}^2 I), \quad (8)$$

- Assume that an efficient **ODE solver** $\Psi(z_t, t, s, c)$ is available for approximating the integration of the right-hand side of Eq (8) from time t to s .
- In practice, we can use DDIM (Song et al., 2020a), DPM-Solver (Lu et al., 2022a) or DPM-Solver++ (Lu et al., 2022b) as $\Psi(\cdot, \cdot, \cdot, \cdot)$.
- Note that we only use these solvers in training/distillation, not in inference
- ❖ Discuss these solvers further when we introduce the **SKIPPING-STEP** technique in Sec. 4.3

➤ **LCM** aims to **predict the solution of the PF-ODE by minimizing the consistency distillation loss** (Song et al., 2023):

$$\mathcal{L}_{CD}(\theta, \theta^-; \Psi) = \mathbb{E}_{z, c, n} \left[d \left(f_\theta(z_{t_{n+1}}, c, t_{n+1}), f_{\theta^-}(\hat{z}_{t_n}^\Psi, c, t_n) \right) \right] \quad (10)$$


- $\hat{z}_{t_n}^\Psi$: an estimation of the evolution of the PF-ODE from $t_{n+1} \rightarrow t_n$ using ODE solver Ψ :

$$\begin{aligned} \hat{z}_{t_n}^\Psi - z_{t_{n+1}} &= \int_{t_{n+1}}^{t_n} \left(f(t)z_t + \frac{g^2(t)}{2\sigma_t} \epsilon_\theta(z_t, c, t) \right) dt \\ &\approx \Psi(z_{t_{n+1}}, t_{n+1}, t_n, c), \end{aligned} \quad (11)$$

- The solver $\Psi(\cdot, \cdot, \cdot, \cdot)$ is used to approximate the integration from $t_{n+1} \rightarrow t_n$.

4.2 One-Stage Guided Distillation by Solving Augmented PF-ODE

➤ **Classifier-free guidance (CFG)** (Ho & Salimans, 2022)

- Crucial for **synthesizing high-quality textaligned images in SD**, typically needing a **CFG scale ω over 6**. Thus, **integrating CFG into a distillation method becomes indispensable**.
- Previous method **Guided-Distill** (Meng et al., 2023) introduces a **two-stage distillation** to support few-step sampling from a guided diffusion model. However, it is computationally intensive (e.g. at least **45 A100 GPUs Days for 2-step inference**, estimated in (Liu et al., 2023)).
- An **LCM** demands merely **32 A100 GPUs Hours training for 2-step inference**, as depicted in Figure 1.
- Furthermore, the **two-stage guided distillation** might result in **accumulated error**, leading to suboptimal performance.
- **LCMs** adopt efficient **one-stage guided distillation** by **solving an augmented PF-ODE**.

➤ **CFG used in reverse diffusion process**

$$\tilde{\epsilon}_\theta(z_t, \omega, c, t) := (1 + \omega)\epsilon_\theta(z_t, c, t) - \omega\epsilon_\theta(z_t, \emptyset, t), \quad (12)$$

- The original noise prediction is replaced by the linear combination of conditional and unconditional noise
- ω is called the *guidance scale*

➤ **Augmented PF-ODE**

- To sample from the guided reverse process, we need to solve the following augmented PF-ODE: (i.e., augmented with the terms related to ω)

$$\frac{dz_t}{dt} = f(t)z_t + \frac{g^2(t)}{2\sigma_t}\tilde{\epsilon}_\theta(z_t, \omega, c, t), \quad z_T \sim \mathcal{N}(\mathbf{0}, \tilde{\sigma}^2 I). \quad (13)$$

4.2 One-Stage Guided Distillation by Solving Augmented PF-ODE

➤ Augmented consistency function f_θ

- To efficiently perform **one-stage guided distillation**, we introduce an augmented consistency function

$$f_\theta : (z_t, \omega, c, t) \mapsto z_0$$

to directly predict the solution of augmented PF-ODE (Eq. 13) for $t = 0$.

- We parameterize the f_θ in the same way as in Eq. 9, except that $\hat{\epsilon}_\theta(z_t, c, t)$ is replaced by $\hat{\epsilon}_\theta(z_t, \omega, c, t)$, which is a **noise prediction model initializing with the same parameters as the teacher diffusion model**, but also contains additional trainable parameters for conditioning on ω .

- The **consistency loss** is the same as Eq. 10 except that we use augmented consistency function $f_\theta(z_t, \omega, c, t)$.

$$\mathcal{L}_{CD}(\theta, \theta^-; \Psi) = \mathbb{E}_{z, c, \omega, n} \left[d \left(f_\theta(z_{t_{n+1}}, \omega, c, t_{n+1}), f_{\theta^-}(\hat{z}_{t_n}^{\Psi, \omega}, \omega, c, t_n) \right) \right] \quad (14)$$

4.2 One-Stage Guided Distillation by Solving Augmented PF-ODE

➤ Consistency Loss

- The **consistency loss** is the same as Eq. 10 except that we use augmented consistency function $f_\theta(z_t, \omega, c, t)$.

$$\mathcal{L}_{CD}(\theta, \theta^-; \Psi) = \mathbb{E}_{z, c, \omega, n} \left[d \left(f_\theta(z_{t_{n+1}}, \omega, c, t_{n+1}), f_\theta(\hat{z}_{t_n}^{\Psi, \omega}, \omega, c, t_n) \right) \right] \quad (14)$$

- ω and n are uniformly sampled from interval $[\omega_{\min}, \omega_{\max}]$ and $\{1, \dots, N-1\}$ respectively.
- $\hat{z}_{t_n}^{\Psi, \omega}$ is estimated using the new noise model $\hat{\epsilon}_\theta(z_t, \omega, c, t)$

$$\begin{aligned} \hat{z}_{t_n}^{\Psi, \omega} - z_{t_{n+1}} &= \int_{t_{n+1}}^{t_n} \left(f(t) z_t + \frac{g^2(t)}{2\sigma_t} \tilde{\epsilon}_\theta(z_t, \omega, c, t) \right) dt \\ &= (1 + \omega) \int_{t_{n+1}}^{t_n} \left(f(t) z_t + \frac{g^2(t)}{2\sigma_t} \epsilon_\theta(z_t, c, t) \right) dt - \omega \int_{t_{n+1}}^{t_n} \left(f(t) z_t + \frac{g^2(t)}{2\sigma_t} \epsilon_\theta(z_t, \emptyset, t) \right) dt \quad (15) \\ &\approx (1 + \omega) \Psi(z_{t_{n+1}}, t_{n+1}, t_n, c) - \omega \Psi(z_{t_{n+1}}, t_{n+1}, t_n, \emptyset). \end{aligned}$$

- We can use **DDIM** (Song et al., 2020a), **DPM-Solver** (Lu et al., 2022a) or **DPM-Solver++** (Lu et al., 2022b) as the **PF-ODE solver** $\Psi(\cdot, \cdot, \cdot, \cdot)$.

4.3 Accelerating Distillation with Skipping Time Steps

➤ Discretization Schedule (or Time Schedule)

- Discrete diffusion models (Ho et al., 2020; Song & Ermon, 2019) typically train noise prediction models with a **long time-step schedule** $\{t_i\}_i$ (also called discretization schedule or time schedule) to achieve **high quality generation results**.

✓ Stable Diffusion (SD) has a time schedule of length **1,000**.

- Directly applying Latent Consistency Distillation (LCD) to SD with such **an extended schedule** can be problematic.
 - ✓ The model needs to **sample across all 1,000 time steps**.
 - ✓ The **consistency loss** attempts to **aligns the prediction of LCM model** $f_\theta(z_{t_{n+1}}, c, t_{n+1})$ with the prediction $f_\theta(z_{t_n}, c, t_n)$ at the **subsequent step along the same trajectory**.
 - ✓ Since $t_n - t_{n+1}$ is tiny, z_{t_n} and $z_{t_{n+1}}$ (and thus $f_\theta(z_{t_{n+1}}, c, t_{n+1})$ and $f_\theta(z_{t_n}, c, t_n)$) are **already close to each other**, incurring **small consistency loss** and hence leading to **slow convergence**.

➤ Skipping-Step

- To address this issues, we introduce the **SKIPPING-STEP** method to considerably **shorten the length of time schedule (from thousands to dozens)** to achieve **fast convergence** while **preserving generation quality**
- Consistency Models (CMs) (Song et al., 2023)
 - ✓ Use the **EDM** (Karras et al., 2022) **continuous time schedule**, and the **Euler, or Heun Solver** as the numerical **continuous PF-ODE solver**.
 - For **LCMs**, in order to adapt to the **discrete-time schedule** in **SD**,
 - ✓ We utilize **DDIM** (Song et al., 2020a), **DPM-Solver** (Lu et al., 2022a), or **DPM-Solver++** (Lu et al., 2022b) as the **ODE solver**. (Lu et al., 2022a) shows that these advanced solvers can solve the PF-ODE efficiently in Eq. 8.

4.3 Accelerating Distillation with Skipping Time Steps

➤ Skipping-Step Method in Latent Consistency Distillation (LCD)

- Instead of ensuring consistency between adjacent time steps $\mathbf{t}_{n+1} \rightarrow \mathbf{t}_n$, LCMs aim to ensure consistency between the current time step and k -step away, $\mathbf{t}_{n+k} \rightarrow \mathbf{t}_n$. →
- SKIPPING-STEP method is crucial in accelerating the LCD process.
- Consistency distillation loss in Eq. 14 is modified to ensure consistency from \mathbf{t}_{n+k} to \mathbf{t}_n :

$$\mathcal{L}_{CD}(\theta, \theta^-; \Psi) = \mathbb{E}_{z, c, \omega, n} \left[d \left(\mathbf{f}_\theta(z_{t_{n+k}}, \omega, \mathbf{c}, t_{n+k}), \mathbf{f}_{\theta^-}(\hat{z}_{t_n}^{\Psi, \omega}, \omega, \mathbf{c}, t_n) \right) \right] \quad (16)$$

$\hat{z}_{t_n}^{\Psi, \omega}$ being an estimate of z_{t_n} using numerical **augmented PF-ODE** solver Ψ

$$\hat{z}_{t_n}^{\Psi, \omega} \leftarrow z_{t_{n+k}} + (1 + \omega)\Psi(z_{t_{n+k}}, t_{n+k}, t_n, \mathbf{c}) - \omega\Psi(z_{t_{n+k}}, t_{n+k}, t_n, \emptyset) \quad (17)$$

Latent Consistency Models

4.3 Accelerating Distillation with Skipping Time Steps

➤ Skipping-Step Method in Latent Consistency Distillation (LCD)

- Consistency distillation loss in Eq. 14 is modified to ensure consistency from \mathbf{t}_{n+k} to \mathbf{t}_n :

$$\mathcal{L}_{CD}(\theta, \theta^-; \Psi) = \mathbb{E}_{z, c, \omega, n} \left[d\left(f_\theta(z_{t_{n+k}}, \omega, c, t_{n+k}), f_{\theta^-}(\hat{z}_{t_n}^{\Psi, \omega}, \omega, c, t_n)\right) \right] \quad (16)$$

$\hat{z}_{t_n}^{\Psi, \omega}$ being an estimate of z_{t_n} using numerical **augmented PF-ODE** solver Ψ

$$\hat{z}_{t_n}^{\Psi, \omega} \leftarrow z_{t_{n+k}} + (1 + \omega)\Psi(z_{t_{n+k}}, t_{n+k}, t_n, c) - \omega\Psi(z_{t_{n+k}}, t_{n+k}, t_n, \emptyset) \quad (17)$$

- For LCM, we use three possible ODE solvers here: DDIM (Song et al., 2020a), DPM-Solver (Lu et al., 2022a), DPM-Solver++ (Lu et al., 2022b), and we compare their performance in Sec 5.2.
- In fact, DDIM (Song et al., 2020a) is the first-order discretization approximation of the DPM-Solver (Proven in (Lu et al., 2022a)). Here we provide the detailed formula of the DDIM PF-ODE solver Ψ_{DDIM} from \mathbf{t}_{n+k} to \mathbf{t}_n .

$$\Psi_{DDIM}(z_{t_{n+k}}, t_{n+k}, t_n, c) = \underbrace{\frac{\alpha_{t_n}}{\alpha_{t_{n+k}}} z_{t_{n+k}} - \sigma_{t_n} \left(\frac{\sigma_{t_{n+k}} \cdot \alpha_{t_n}}{\alpha_{t_{n+k}} \cdot \sigma_{t_n}} - 1 \right) \hat{\epsilon}_\theta(z_{t_{n+k}}, c, t_{n+k}) - z_{t_{n+k}}}_{\text{DDIM Estimated } z_{t_n}} \quad (18)$$

Latent Consistency Models

4.3 Accelerating Distillation with Skipping Time Steps

➤ Pseudo-code for LCD with CFG and Skipping-Step techniques

- The modifications from the original Consistency Distillation (CD) algorithm in Song et al. (2023) are highlighted in blue.
- LCM sampling algorithm 3 is provided in Appendix B.

Algorithm 1 Latent Consistency Distillation (LCD)

Input: dataset \mathcal{D} , initial model parameter θ , learning rate η , ODE solver $\Psi(\cdot, \cdot, \cdot, \cdot)$, distance metric $d(\cdot, \cdot)$, EMA rate μ , noise schedule $\alpha(t), \sigma(t)$, guidance scale $[w_{\min}, w_{\max}]$, skipping interval k , and encoder $E(\cdot)$
Encoding training data into latent space: $\mathcal{D}_z = \{(\mathbf{z}, \mathbf{c}) | \mathbf{z} = E(\mathbf{x}), (\mathbf{x}, \mathbf{c}) \in \mathcal{D}\}$

$\theta^- \leftarrow \theta$

repeat

 Sample $(\mathbf{z}, \mathbf{c}) \sim \mathcal{D}_z, n \sim \mathcal{U}[1, N - k]$ and $\omega \sim [\omega_{\min}, \omega_{\max}]$

 Sample $\mathbf{z}_{t_{n+k}} \sim \mathcal{N}(\alpha(t_{n+k})\mathbf{z}; \sigma^2(t_{n+k})\mathbf{I})$

$\hat{\mathbf{z}}_{t_n}^{\Psi, \omega} \leftarrow \mathbf{z}_{t_{n+k}} + (1 + \omega)\Psi(\mathbf{z}_{t_{n+k}}, t_{n+k}, t_n, \mathbf{c}) - \omega\Psi(\mathbf{z}_{t_{n+k}}, t_{n+k}, t_n, \emptyset)$

$\mathcal{L}(\theta, \theta^-; \Psi) \leftarrow d(\mathbf{f}_\theta(\mathbf{z}_{t_{n+k}}, \omega, \mathbf{c}, t_{n+k}), \mathbf{f}_{\theta^-}(\hat{\mathbf{z}}_{t_n}^{\Psi, \omega}, \omega, \mathbf{c}, t_n))$

$\theta \leftarrow \theta - \eta \nabla_\theta \mathcal{L}(\theta, \theta^-)$

$\theta^- \leftarrow \text{stopgrad}(\mu\theta^- + (1 - \mu)\theta)$

until convergence

Latent Consistency Models

4.4 Latent Consistency Fine-Tuning For Customized Dataset

☞ Appendix C

- **Stable Diffusion** excel in diverse text-to-image generation tasks but often **require fine-tuning on customized datasets** to meet the requirements of downstream tasks.

➤ Propose **Latent Consistency Fine-tuning (LCF)**, a **fine-tuning method for pretrained LCM**.

- Inspired by **Consistency Training (CT)** (Song et al., 2023), LCF enables **efficient few-step inference on customized datasets without relying on a teacher diffusion model trained on such data**.

Note that

- This method can also utilize the skipping-step technique to speedup the convergence.
- LCF is independent of the pre-trained teacher model, facilitating direct fine-tuning of a pre-trained LCM model without reliance on the teacher diffusion model

- Randomly select two time steps t_n and t_{n+k} that are k time steps apart and apply the same Gaussian noise ϵ to obtain the noised data $z_{t_n}, z_{t_{n+k}}$ as follows
$$z_{t_{n+k}} = \alpha(t_{n+k})z + \sigma(t_{n+k})\epsilon \quad , \quad z_{t_n} = \alpha(t_n)z + \sigma(t_n)\epsilon.$$
- Directly calculate the consistency loss for these two time steps to enforce self-consistency property in Eq.4.

Algorithm 4 Latent Consistency Fine-tuning (LCF)

Input: customized dataset $\mathcal{D}^{(s)}$, pre-trained LCM parameter θ , learning rate η , distance metric $d(\cdot, \cdot)$, EMA rate μ , noise schedule $\alpha(t), \sigma(t)$, guidance scale $[w_{\min}, w_{\max}]$, skipping interval k , and encoder $E(\cdot)$

Encode training data into the latent space: $\mathcal{D}_z^{(s)} = \{(z, c) | z = E(x), (x, c) \in \mathcal{D}^{(s)}\}$

$\theta^- \leftarrow \theta$

repeat

 Sample $(z, c) \sim \mathcal{D}_z^{(s)}$, $n \sim \mathcal{U}[1, N - k]$ and $w \sim [w_{\min}, w_{\max}]$

 Sample $\epsilon \sim \mathcal{N}(\mathbf{0}, I)$

$z_{t_{n+k}} \leftarrow \alpha(t_{n+k})z + \sigma(t_{n+k})\epsilon \quad , \quad z_{t_n} \leftarrow \alpha(t_n)z + \sigma(t_n)\epsilon$

$\mathcal{L}(\theta, \theta^-) \leftarrow d(f_\theta(z_{t_{n+k}}, t_{n+k}, c, w), f_{\theta^-}(z_{t_n}, t_n, c, w))$

$\theta \leftarrow \theta - \eta \nabla_\theta \mathcal{L}(\theta, \theta^-)$

$\theta^- \leftarrow \text{stopgrad}(\mu \theta^- + (1 - \mu) \theta)$

until convergence

5. EXPERIMENT

- Employ **latency consistency distillation** to train LCM on two subsets of LAION-5B.

5.1 Text-to-Image Generation

➤ Datasets

- LAION-5B (Schuhmann et al., 2022): LAION-Aesthetics-6+ (12M) and LAION-Aesthetics-6.5+ (650K) for text-to-image generation
- Consider two resolutions
- 512x512 resolution : Use LAION-Aesthetics-6+, which comprises 12M text-image pairs with predicted aesthetics scores higher than 6.
- 768x768 resolution : Use LAION-Aesthetics-6.5+, with 650K text-image pairs with aesthetics score higher than 6.5.

➤ Model Configuration

- 512x512 resolution : Use the **pre-trained Stable Diffusion-V2.1-Base** (Rombach et al., 2022) as the **teacher model**, which was originally trained on resolution 512×512 with ϵ -Prediction (Ho et al., 2020).
- 768x768 resolution : Use the widely used **pre-trained Stable Diffusion-V2.1**, originally trained on resolution 768×768 with v-Prediction (Salimans & Ho, 2022).
- Train LCM with 100K iterations and a batch size of 72 for (512×512) setting, and 16 for (768×768) setting, the same learning rate $8e-6$ and EMA rate $\mu = 0.999943$ as used in (Song et al., 2023).
- For *augmented PF-ODE solver* Ψ and skipping step k in Eq. 17,
 - Use DDIM-Solver (Song et al., 2020a) with skipping step $k = 20$.
 - Set the guidance scale range $[\omega_{\min}, \omega_{\max}] = [2, 14]$, consistent with (Meng et al., 2023)

5.1 Text-to-Image Generation

➤ Baselines

- Baselines : DDIM (Song et al., 2020a), DPM (Lu et al., 2022a), DPM++ (Lu et al., 2022b), Guided-Distill (Meng et al., 2023)
- **DDIM, DPM, DPM++** : Training-free samplers requiring **more peak memory** per step with **classifier-free guidance**.
- **Guided-Distill** : Requires **two stages of guided distillation**. Due to the limited resource (Meng et al. (2023) used a large batch size of 512, requiring at least 32 A100 GPUs), reduce the batch size to 72 and trained for the same 100K iterations.
- LCM achieves faster convergence and superior results under the same computation cost.

➤ Evaluation

- Generate **30K images** from **10K text prompts** in the test set (3 images per prompt)
- Adopt **FID** and **CLIP** scores to evaluate the diversity and quality of the generated images.
- Use ViT-g/14 for evaluating CLIP scores

Latent Consistency Models

5.1 Text-to-Image Generation

➤ Results

MODEL (512 × 512) RESO	FID ↓				CLIP SCORE ↑			
	1 STEP	2 STEPS	4 STEPS	8 STEPS	1 STEPS	2 STEPS	4 STEPS	8 STEPS
DDIM (Song et al., 2020a)	183.29	81.05	22.38	13.83	6.03	14.13	25.89	29.29
DPM (Lu et al., 2022a)	185.78	72.81	18.53	12.24	6.35	15.10	26.64	29.54
DPM++ (Lu et al., 2022b)	185.78	72.81	18.43	12.20	6.35	15.10	26.64	29.55
Guided-Distill (Meng et al., 2023)	108.21	33.25	15.12	13.89	12.08	22.71	27.25	28.17
LCM (Ours)	35.36	13.31	11.10	11.84	24.14	27.83	28.69	28.84

Table 1: Quantitative results with $\omega = 8$ at 512×512 resolution. LCM significantly surpasses baselines in the 1-4 step region on LAION-Aesthetic-6+ dataset. For LCM, DDIM-Solver is used with a skipping step of $k = 20$.

MODEL (768 × 768) RESO	FID ↓				CLIP SCORE ↑			
	1 STEP	2 STEPS	4 STEPS	8 STEPS	1 STEPS	2 STEPS	4 STEPS	8 STEPS
DDIM (Song et al., 2020a)	186.83	77.26	24.28	15.66	6.93	16.32	26.48	29.49
DPM (Lu et al., 2022a)	188.92	67.14	20.11	14.08	7.40	17.11	27.25	29.80
DPM++ (Lu et al., 2022b)	188.91	67.14	20.08	14.11	7.41	17.11	27.26	29.84
Guided-Distill (Meng et al., 2023)	120.28	30.70	16.70	14.12	12.88	24.88	28.45	29.16
LCM (Ours)	34.22	16.32	13.53	14.97	25.32	27.92	28.60	28.49

Table 2: Quantitative results with $\omega = 8$ at 768×768 resolution. LCM significantly surpasses the baselines in the 1-4 step region on LAION-Aesthetic-6.5+ dataset. For LCM, DDIM-Solver is used with a skipping step of $k = 20$.

- DDIM, DPM, DPM++ require more peak memory per sampling step with CFG
- LCM requires only one forward pass per sampling step, saving both time and memory.
- Guided-Distill : two-stage distillation procedure
- LCM : one-stage guided distillation, which is much simpler and more practical.

Latent Consistency Models

5.1 Text-to-Image Generation

➤ Results

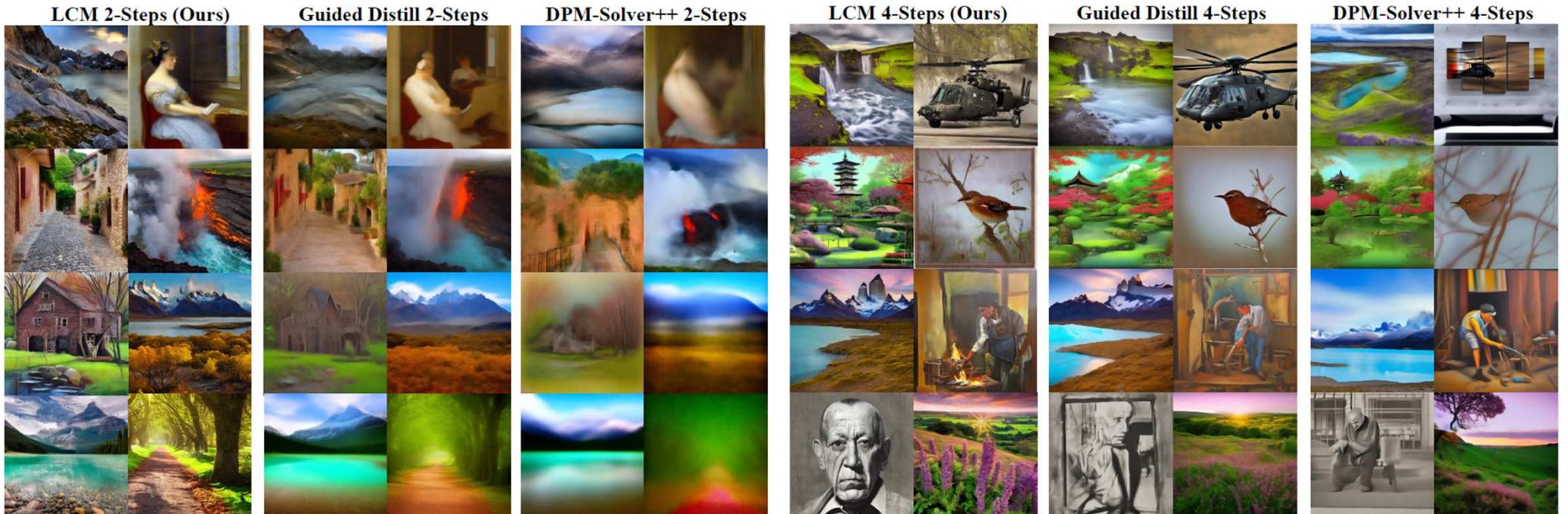


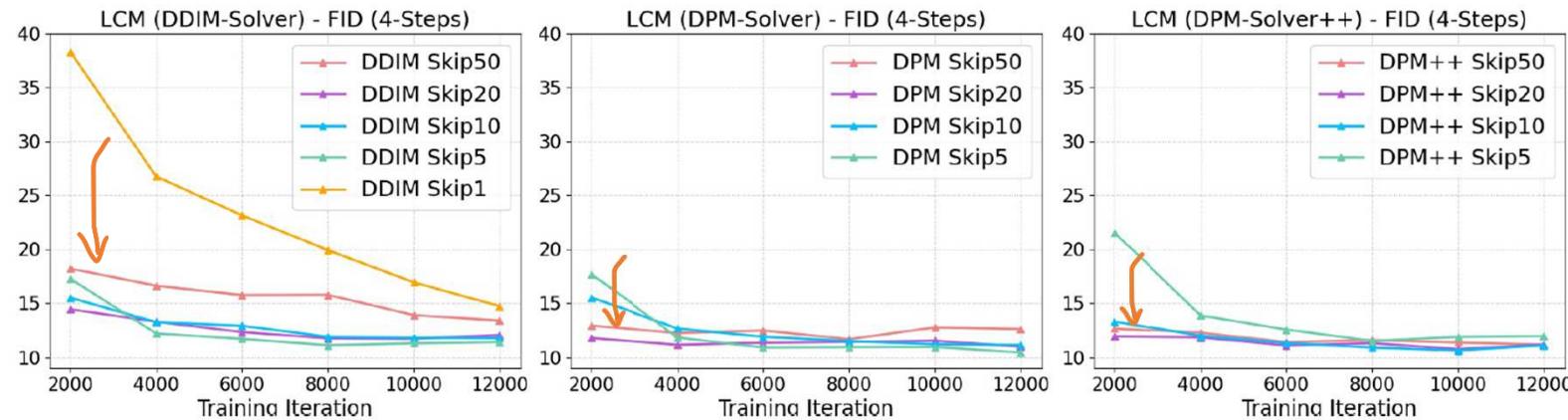
Figure 2: Text-to-Image generation results on LAION-Aesthetic-6.5+ with 2-, 4-step inference. Images generated by LCM exhibit superior detail and quality, outperforming other baselines by a large margin.

5.2 Ablation Study

➤ ODE Solvers & Skipping-Step Schedule

- Compare various solvers Ψ (DDIM, DPM, DPM++) for solving the **augmented PF-ODE** specified in Eq 17, and explore different skipping step schedules with different k .

- 1) Using **SKIPPING-STEP** techniques (see Sec 4.3), LCM achieves fast convergence within **2,000 iterations** in the **4-step** inference setting.
- 2) **DPM** and **DPM++** solvers perform **better at a larger skipping step** ($k = 50$) compared to the **DDIM solver** which suffers from **increased ODE approximation error with larger k**.
- 3) Very small k values (1 or 5) result in slow convergence and very large ones (e.g., 50 for DDIM) may lead to inferior results



- We choose $k = 20$, which provides competitive performance for all three solvers.

Figure 3: Ablation study on different ODE solvers and skipping step k . Appropriate skipping step k can significantly accelerate convergence and lead to better FID within the same number of training steps.

5.2 Ablation Study

➤ The Effect of Guidance Scale ω

- Examine the effect of using different **CFG scales** ω in LCM.
- ω balances sample **quality** and **diversity**
 - ✓ A larger ω generally tends to **improve sample quality** (indicated by **CLIP**), but may **compromise diversity** (measured by **FID**).
 - ✓ An increased ω yields better CLIP scores at the expense of FID.

- 1) Using large ω enhances sample quality (CLIP Scores) but results in relatively inferior FID.
- 2) The performance gaps across 2, 4, and 8 inference steps are negligible, highlighting LCM's efficacy in 2~8 step regions. However, a noticeable gap exists in one-step inference.

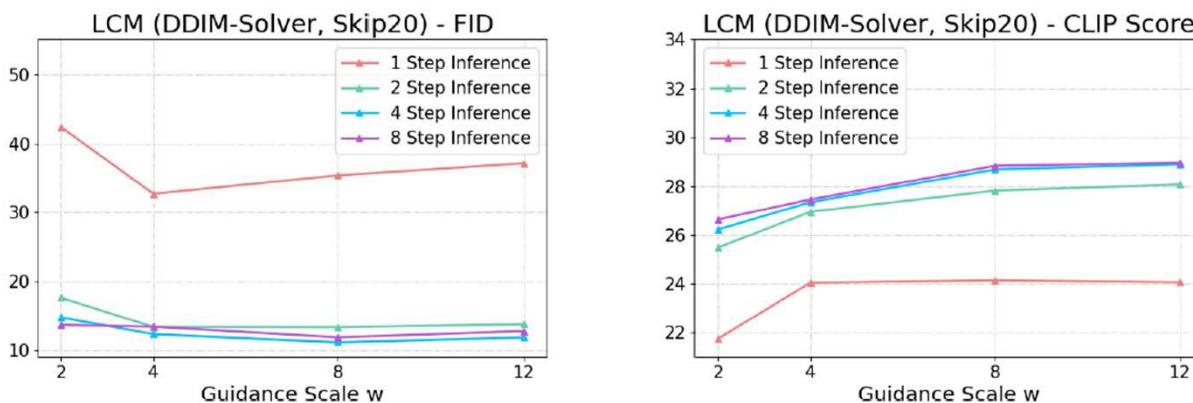


Figure 4: Ablation study on different classifier-free guidance scales ω . Larger ω leads to better sample quality (CLIP Scores). The performance gaps across 2, 4, and 8 steps are minimal, showing the efficacy of LCM.

5.2 Ablation Study

➤ The Effect of Guidance Scale ω

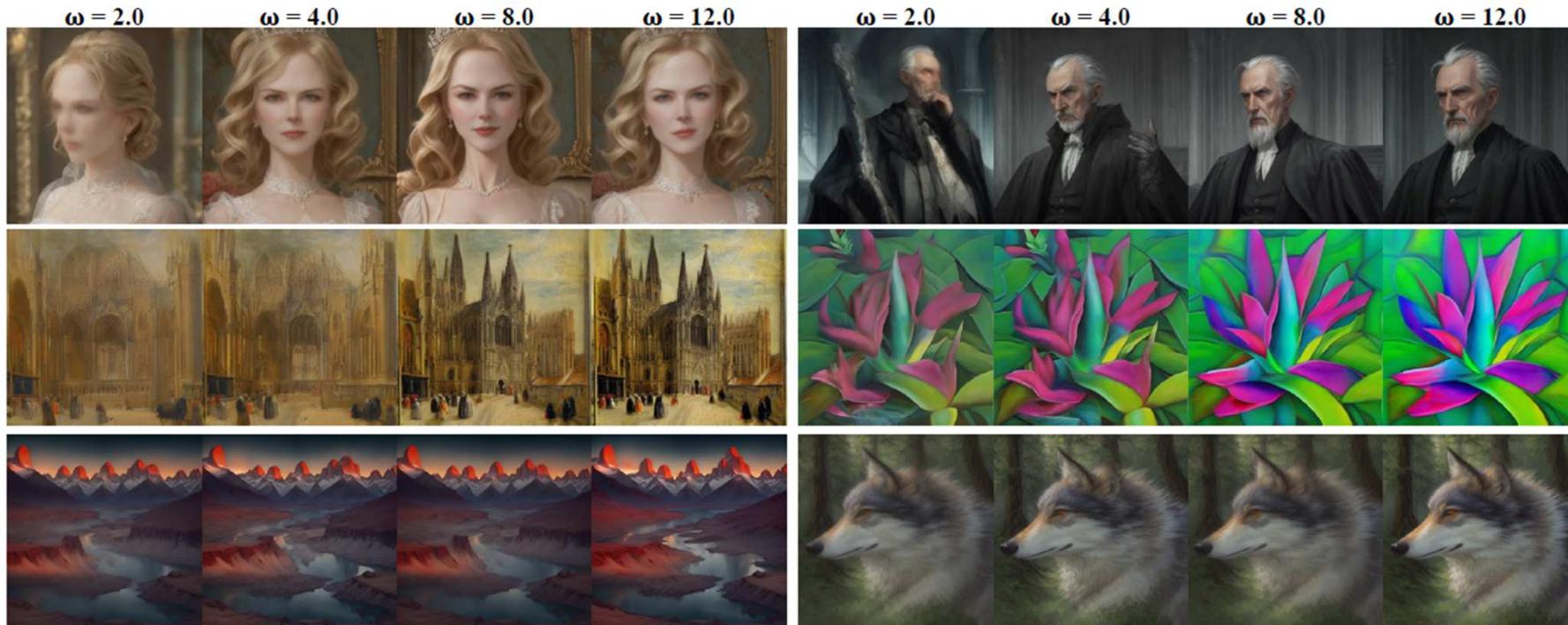


Figure 5: 4-step LCMs using different CFG scales ω . LCMs utilize one-stage guided distillation to directly incorporate CFG scales ω . Larger ω enhances image quality.

A larger ω enhances sample quality, verifying the effectiveness of our one-stage guided distillation method.

5.3 Downstream Consistency Fine-tuning Results

- 2 customized image datasets, Pokemon dataset (Pinkney, 2022) and Simpsons dataset (Norod78, 2022), that **90%** is used for **fine-tuning** and the rest **10%** for **testing**.
- For **LCF**, we utilize **pretrained LCM** that was originally trained at the resolution of 768×768 used in Table 2. We fine-tune the pre-trained LCM for **30K iterations** with a learning rate $8e-6$.

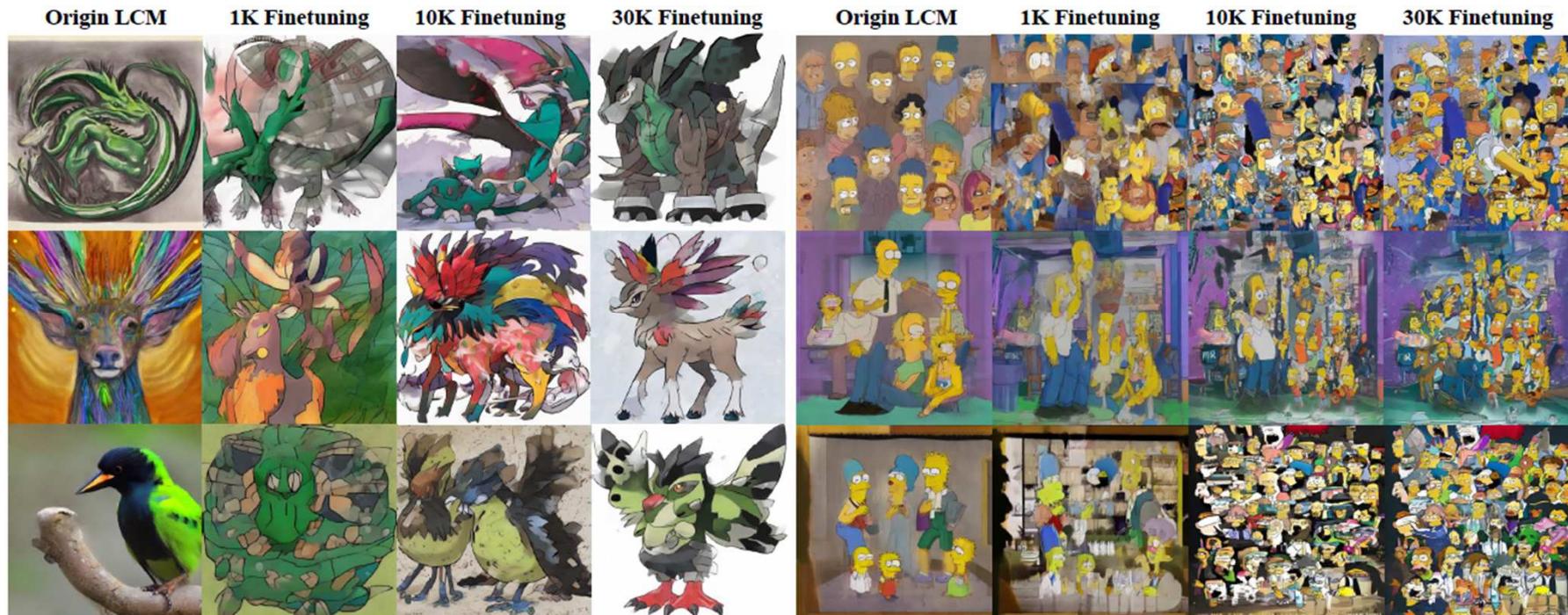


Figure 6: 4-step LCMs using Latent Consistency Fine-tuning (LCF) on two customized datasets: Pokemon Dataset (left), Simpsons Dataset (right). Through LCF, LCM produces images with customized styles.