



EDM (Elucidating the Design Space of Diffusion-Based Generative Models)

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Artificial Intelligence
Creating the Future

Dong-A University

Division of Computer Engineering &
Artificial Intelligence

References

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, (nvidia)

"Elucidating the Design Space of Diffusion-Based Generative Models," NeurIPS 2022.

<https://arxiv.org/abs/2206.00364>

<https://github.com/NVlabs/edm>

<https://www.youtube.com/watch?v=T0Qxzf0eaio>

https://research.nvidia.com/publication/2022-11_elucidating-design-space-diffusion-based-generative-models

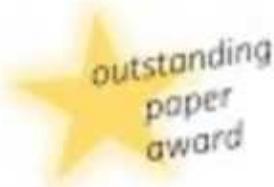
Blog

<https://sang-yun-lee.notion.site/Elucidating-the-Design-Space-of-Diffusion-Based-Generative-Models-a81b14bf297743ec90a72c11f0fbce57>

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Elucidating the Design Space of Diffusion-Based Generative Models

NeurIPS 2022



Tero Karras

Miika Aittala

Timo Aila

Samuli Laine



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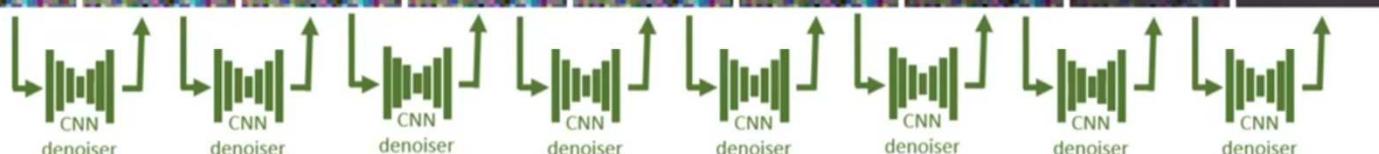
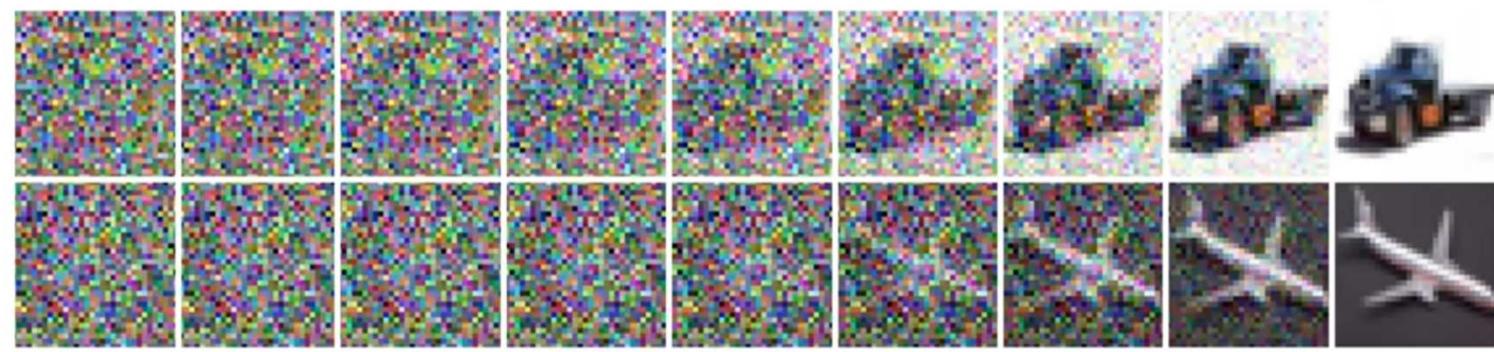
Intuition on denoising diffusion

2) **Quality** of individual images, and variety?

Tradeoff with the quality of the individual generated images and with the distribution as whole

start from random noise

1) **Efficiency:** typically 50 to 2000 network evaluations – slow!



gradually removing noise reveals a random image – a **generative model!**

Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Deterministically
“fade out” noise,
vs. replace it?

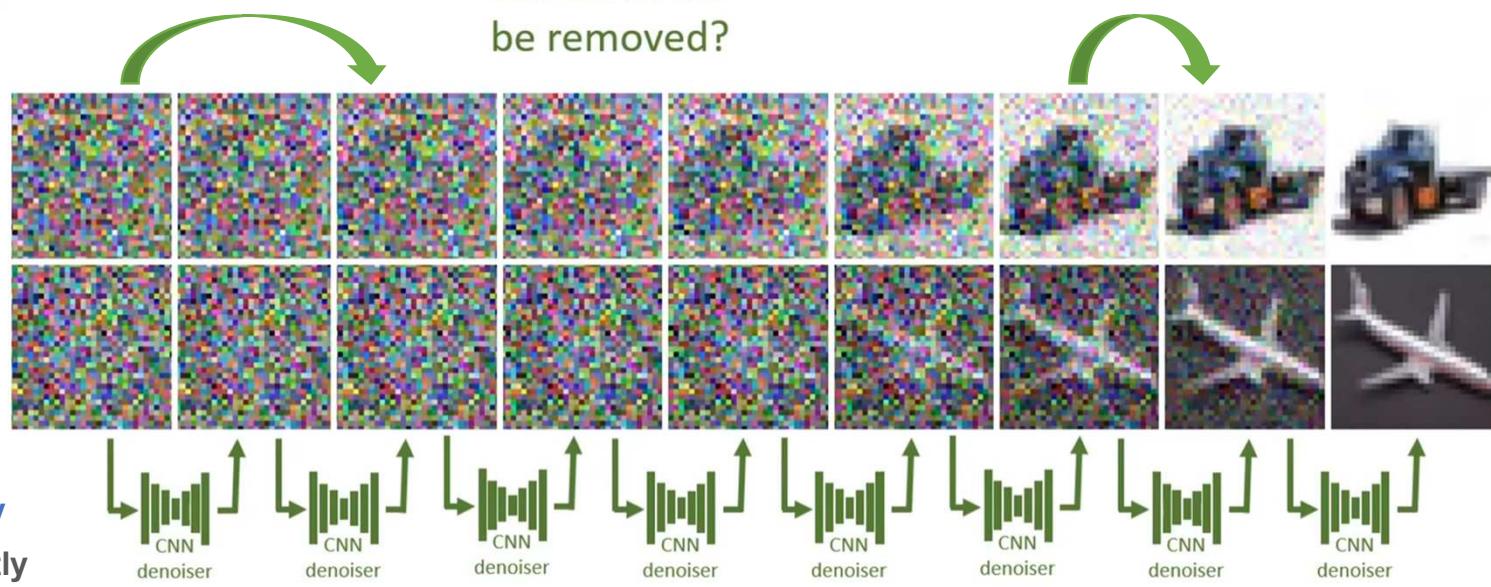
Differ vastly in Practical
design choices like at what
rate do you reduce the noise
level at different stages of
the generation

Deterministically or stastically
How do you deal with the vastly
different signal magnitudes at
different stages of this process
and how do you predict the
signal or the noise

On what
schedule
should noise
be removed?

Large numerical scale of the noise?
Normalization?
Where to implement it?

Predict noise or clean image?
Training effort per noise level?



EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Differential equation formalism

by Y. Song et al. (2021)

- Image evolves according to a **stochastic differential equation (SDE)**
- Also deterministic **ordinary differential equation (ODE)** variant
- Generalizes existing methods, in principle

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Outline

- **Part I: Common framework**
 - Identifying the moving parts in existing work
- **Part II: Deterministic sampling**
 - Solving the ODE efficiently
- **Part III: Stochastic sampling**
 - Why SDE's? How to do stochastic stepping?
- **Part IV: Preconditioning and training**
 - How to train the CNN used in evaluating a step?
- We will **not** study network architectures (what layers to use, etc)!

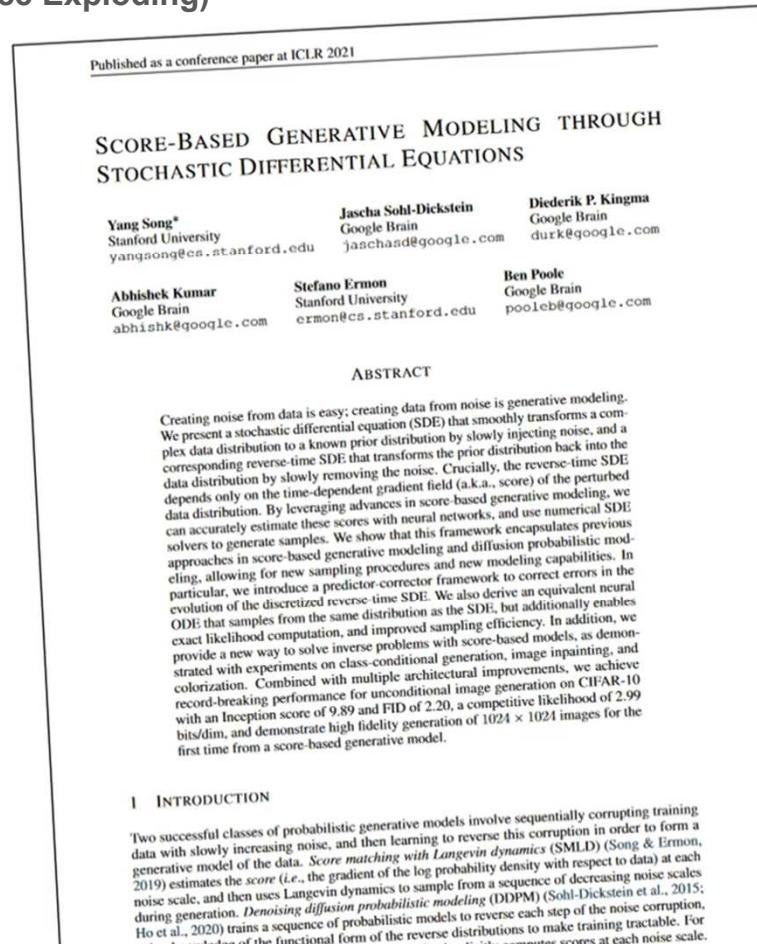
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VP (Variance Preserving)
VE (Variance Exploding)

VP

VE



iDDPM + **DDIM**

Published as a conference paper at ICLR 2021

DENOISING DIFFUSION IMPLICIT MODELS

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ABSTRACT

Denoising diffusion probabilistic models (DDPM) are a family of generative models for image generation without an explicit Markov chain for sampling. They have shown state-of-the-art performance on several benchmarks, including CIFAR-10, LSUN, and ImageNet. However, they are slow and require many sampling steps to produce high-quality samples.

Improved Denoising Diffusion Probabilistic Models

Alex Nichol^{*†} Prafulla Dhariwal^{*†}

Abstract

Denoising diffusion probabilistic models (DDPM) are a class of generative models which have recently been shown to produce excellent samples. We show that with a few simple modifications, DDPMs can also achieve competitive log-likelihoods while maintaining high sample quality. Additionally, we find that learning variances of the reverse diffusion process allows sampling with an order of magnitude fewer forward passes with a negligible difference in sample quality, which is important for the practical deployment of these models. We additionally use precision and recall to compare how well DDPMs and GANs cover the target distribution. Finally, we show that the sample quality and likelihood of these models scale smoothly with model capacity and training compute, making them easily scalable. We release our code and pre-trained models at <https://github.com/openai/ddim>.

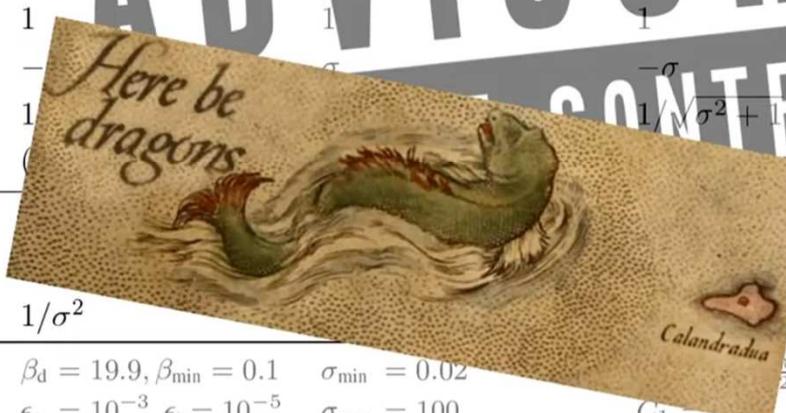
and VAEs (Kingma & Welling, 2013). This raises various questions, such as whether DDPMs are capable of capturing all the modes of a distribution. Furthermore, while Ho et al. (2020) showed extremely good results on the CIFAR-10 (Krizhevsky, 2009) and LSUN (Yu et al., 2015) datasets, it is unclear how well DDPMs scale to datasets with higher diversity such as ImageNet. Finally, while Chen et al. (2020b) found that DDPMs can efficiently generate audio using a small number of sampling steps, it has yet to be shown that the same is true for images.

In this paper, we show that DDPMs can achieve log-likelihoods competitive with other likelihood-based models, even on high-diversity datasets like ImageNet. To more tightly optimise the variational lower-bound (VLB), we learn the reverse process variances using a simple reparameterization and a hybrid learning objective that combines the VLB with the simplified objective from Ho et al. (2020).

We find surprisingly that, with our hybrid objective, our models obtain better log-likelihoods than those obtained by optimizing the log-likelihood directly, and discover that the latter objective has much more gradient noise during

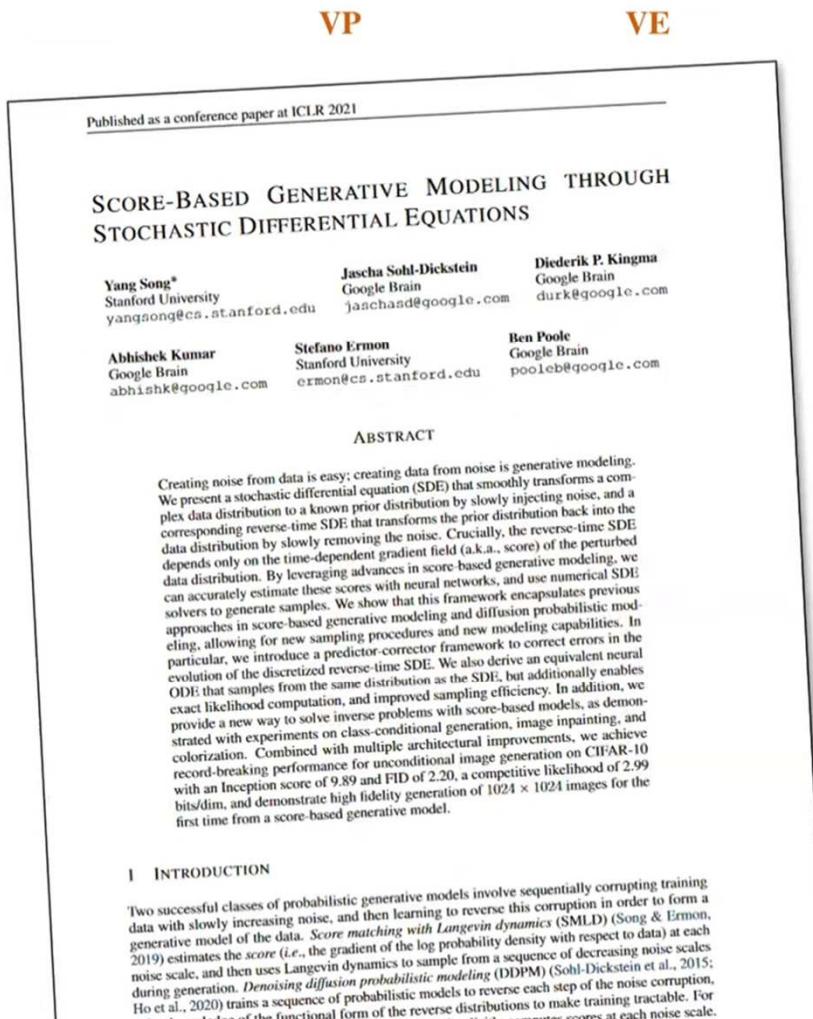
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	VP	VE	iDDPM	+ DDIM	Ours
Sampling					
ODE solver	Euler	Euler	Euler		
Time steps	$t_{i < N}$	$1 + \frac{i}{N-1}(\epsilon_s - 1)$	$\sigma_{\max}^2 (\sigma_{\min}^2 / \sigma_{\max}^2)^{\frac{i}{N-1}}$	$u_{\lfloor j_0 + \frac{M-1-j_0}{N-1} i + \frac{1}{2} \rfloor}, \text{ where } u_M = 0$ $u_{j-1} = \sqrt{\frac{u_j^2 + 1}{\max(\alpha_{j-1}/\bar{\alpha}_j, C_1)}} - 1$	
Schedule	$\sigma(t)$	$\sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t} - 1}$	\sqrt{t}	t	$2^{\text{nd}} \text{ order Heun}$ $(\sigma_{\max}^{\frac{1}{\rho}} + \frac{i}{N-1}(\sigma_{\min}^{\frac{1}{\rho}} - \sigma_{\max}^{\frac{1}{\rho}}))^{\rho}$
Scaling	$s(t)$	$1 / \sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t}}$	1	1	
Network and preconditioning					
Architecture of F_θ	DDPM++	NCSN++	DDPM		
Skip scaling $c_{\text{skip}}(\sigma)$	1	1	1		
Output scaling $c_{\text{out}}(\sigma)$	$-\sigma$	σ	$-\sigma$		
Input scaling $c_{\text{in}}(\sigma)$	$1/\sqrt{\sigma^2 + 1}$	$1/\sqrt{\sigma^2 + 1}$	$1/\sqrt{\sigma^2 + 1}$		
Noise cond. $c_{\text{noise}}(\sigma)$	$(\min_j u_j - \sigma)$	$(\min_j u_j - \sigma)$	$(\min_j u_j - \sigma)$		
Training					
Noise distribution		$\mathcal{U}\{0, M-1\}$	$\mathcal{U}\{0, M-1\}$	$\mathcal{U}\{0, M-1\}$	$\ln(\sigma) \sim \mathcal{N}(P_{\text{mean}}, P_{\text{std}}^2)$
Loss weighting $\lambda(\sigma)$	$1/\sigma^2$				$(\sigma^2 + \sigma_{\text{data}}^2) / (\sigma \cdot \sigma_{\text{data}})^2$
Parameters	$\beta_d = 19.9, \beta_{\min} = 0.1$ $\epsilon_s = 10^{-3}, \epsilon_t = 10^{-5}$ $M = 1000$	$\sigma_{\min} = 0.02$ $\sigma_{\max} = 100$	$C_1 = 0.001, C_2 = 0.008$ $M = 1000, j_0 = 8^\dagger$		$\sigma_{\min} = 0.002, \sigma_{\max} = 80$ $\sigma_{\text{data}} = 0.5, \rho = 7$ $P_{\text{mean}} = -1.2, P_{\text{std}} = 1.2$

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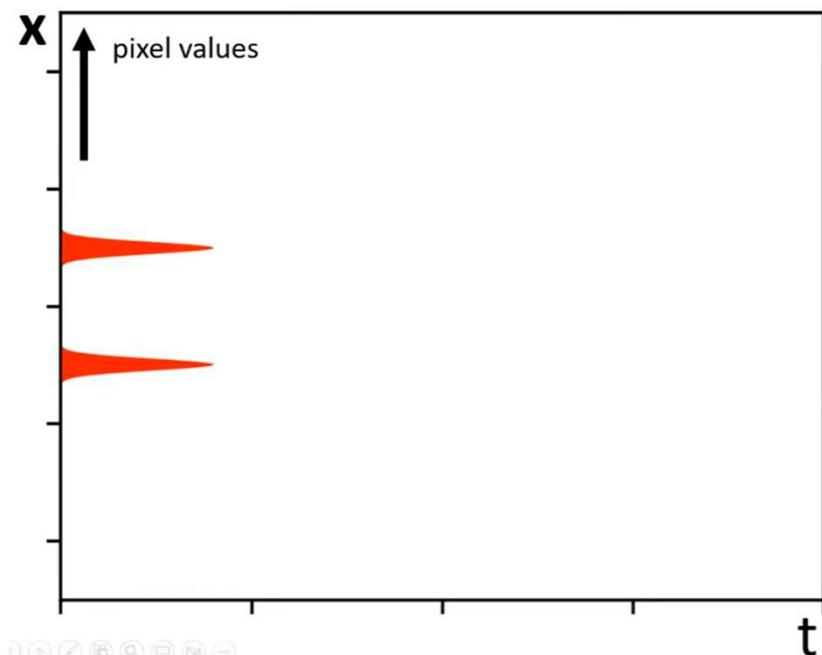
For background, let's review how Song et al. (2021) formulate denoising diffusion SDE/ODE

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Milliondimensional data space

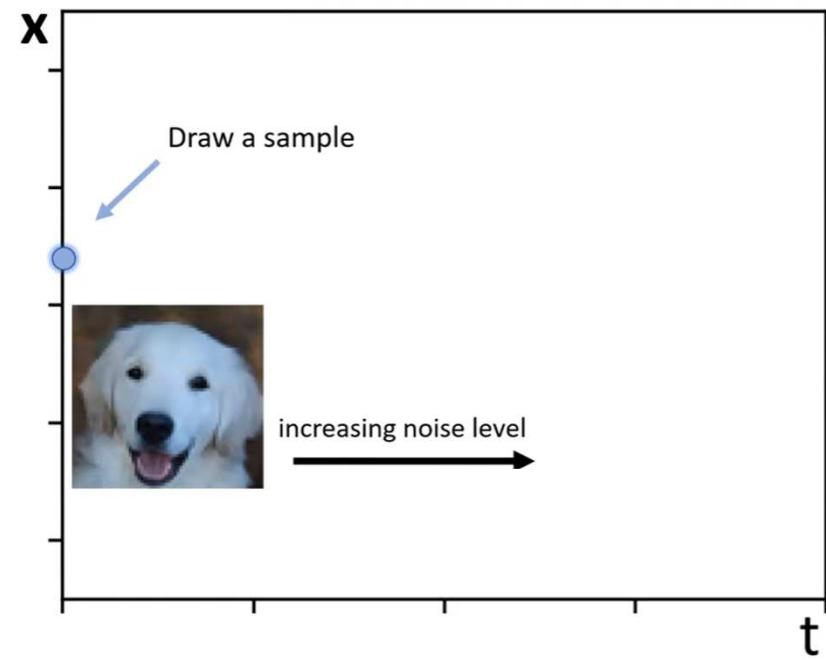
Data distribution from Dataset



Learn to produce novel samples
from this distribution

Data distribution

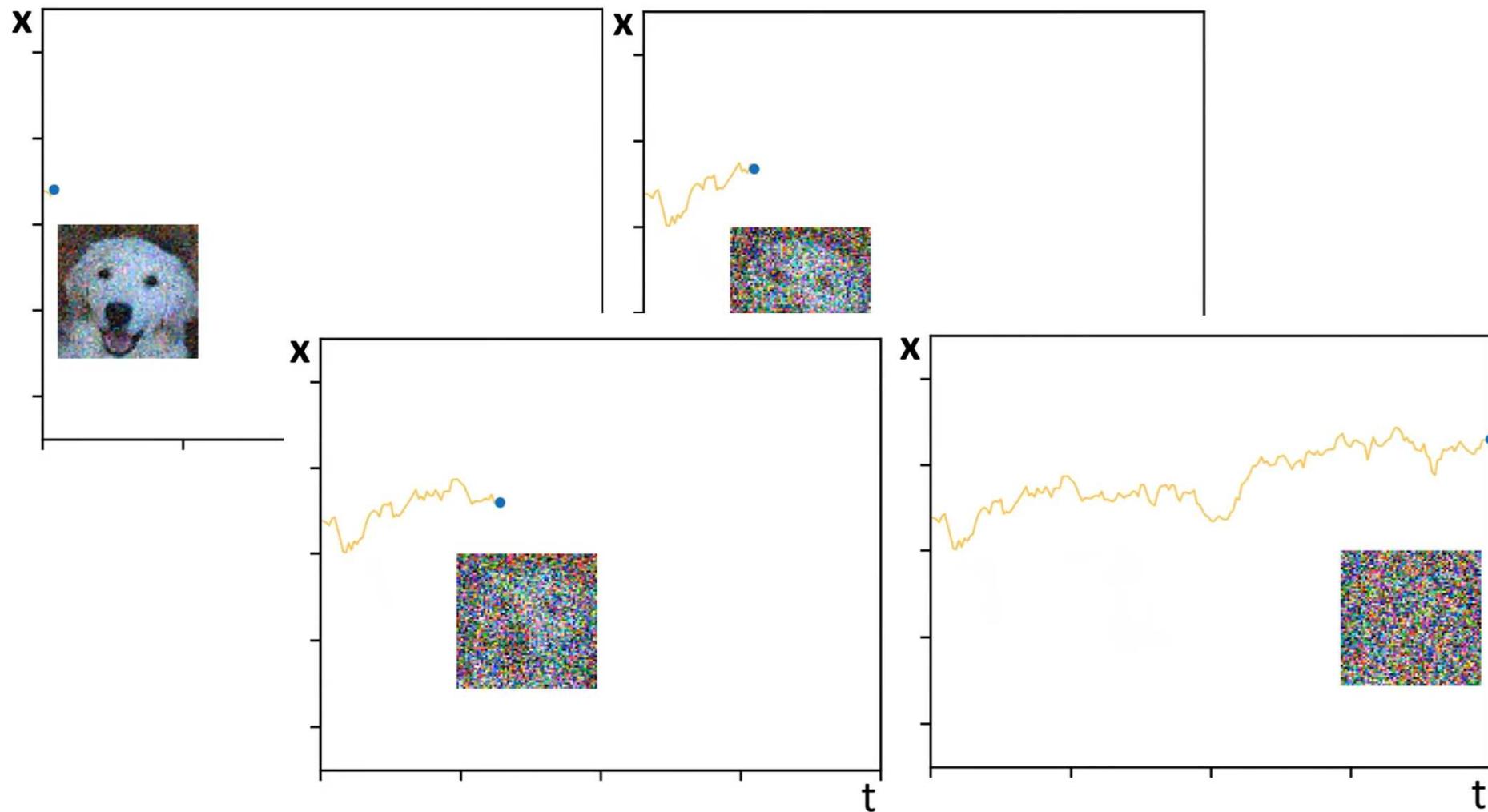
- Data lives in high dimensional space of pixel values
- We'll visualize in 1D



Increasing time which is an essential
increasing noise level

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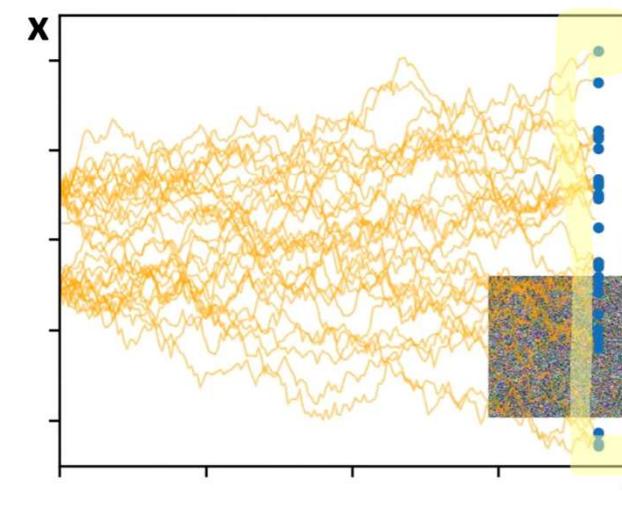
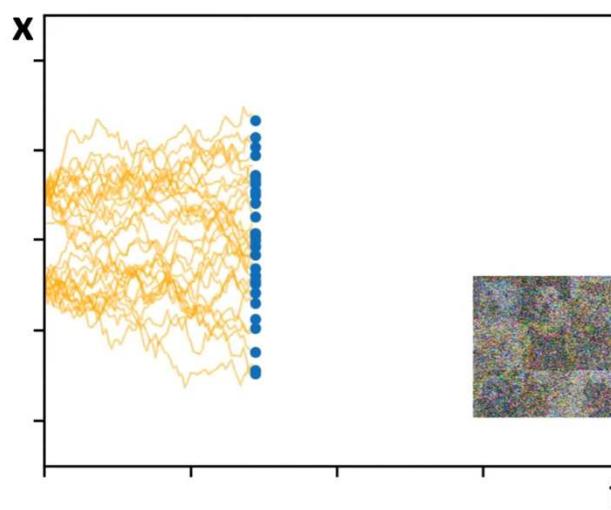
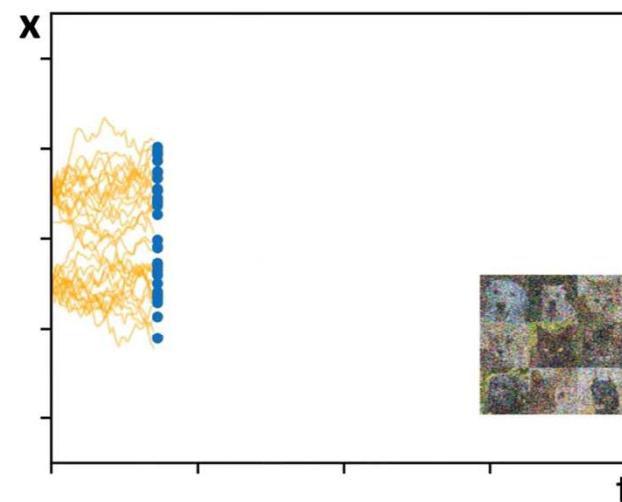
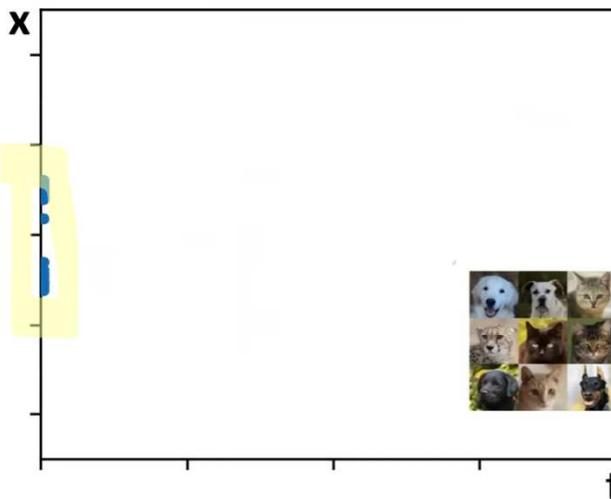
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Gradually add
noise to destroy
the image

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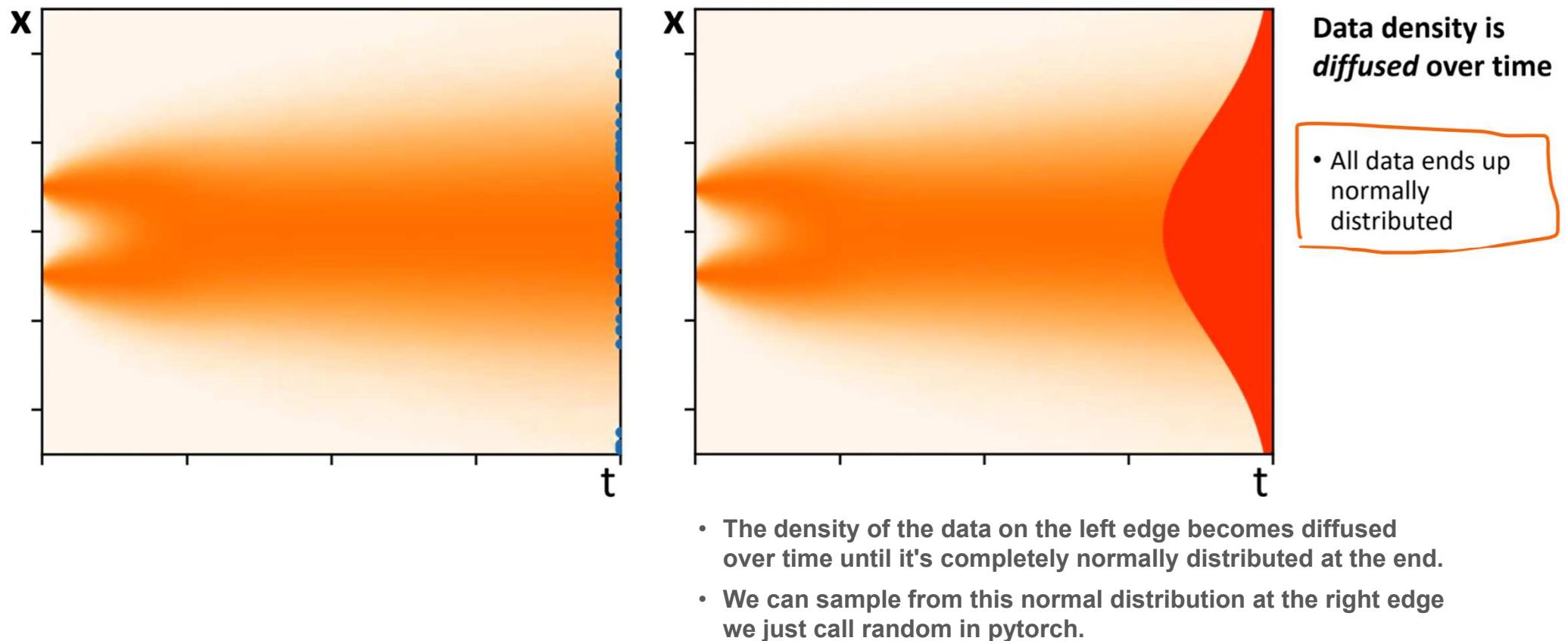
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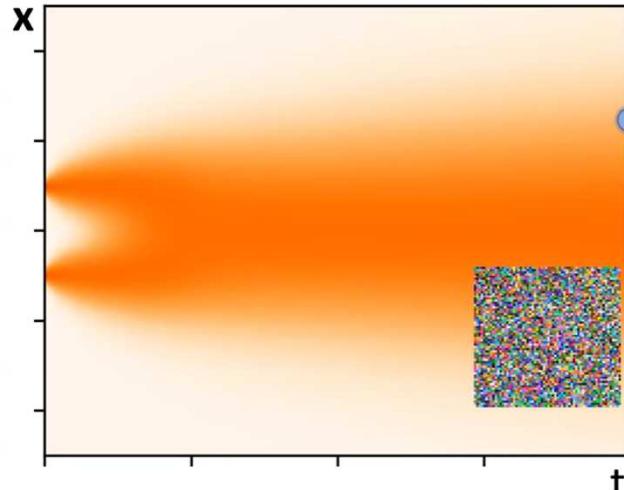
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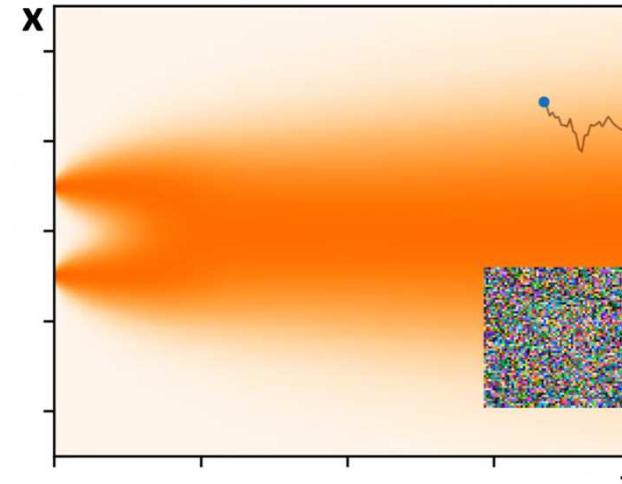
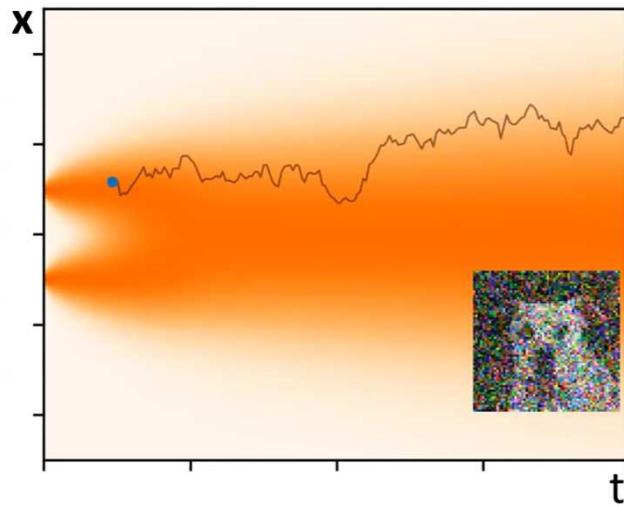
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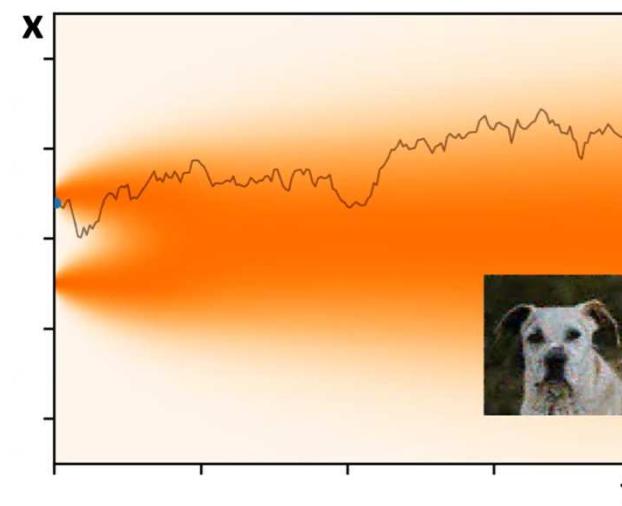


Data density is diffused over time

- All data ends up normally distributed
- Let's draw a sample...



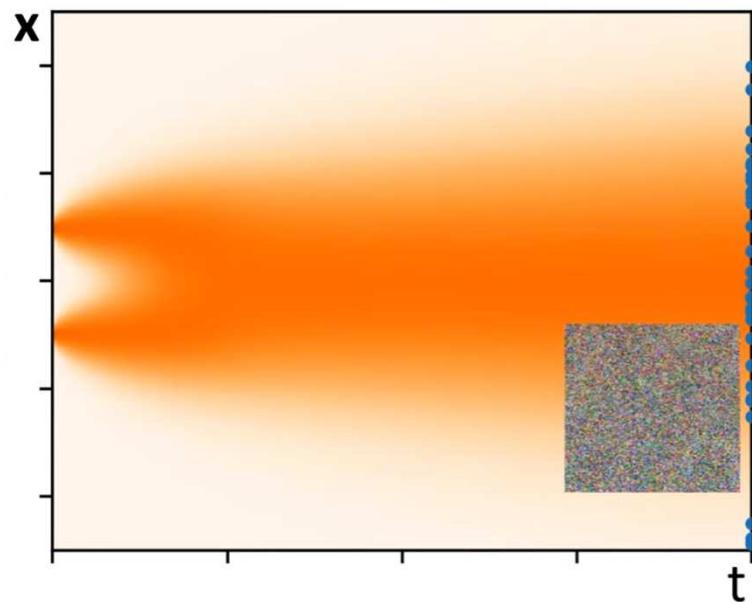
We can reverse the trajectory by gradual denoising



- They'll give us a sample from that edge.
- There exist to sort of reverse this path so go backward in time.
- Land us on the left edge that have the density of the actual data - Generate an image

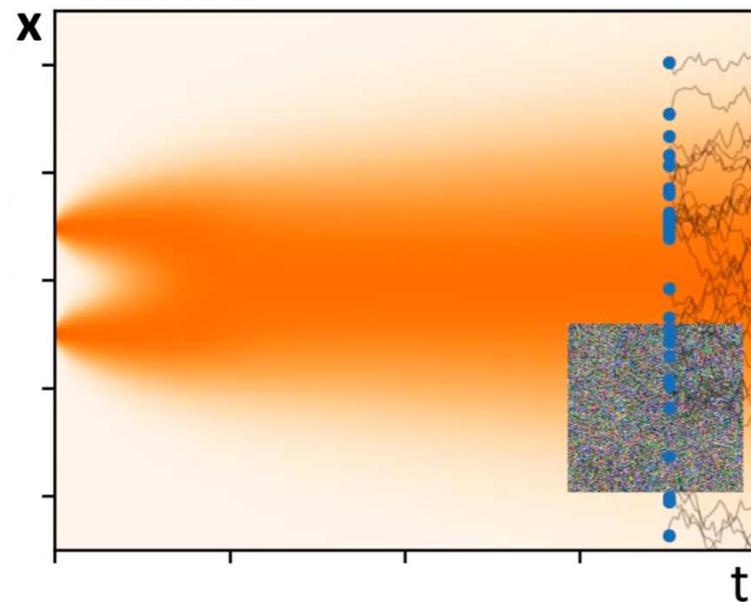
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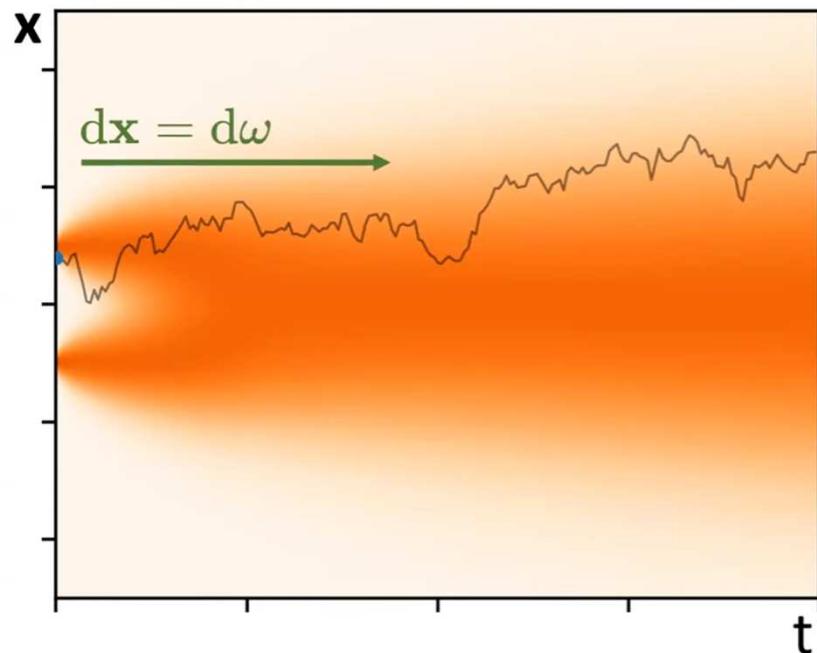
We can *reverse* the trajectory by gradual denoising

- Endpoint is a random sample from data distribution!

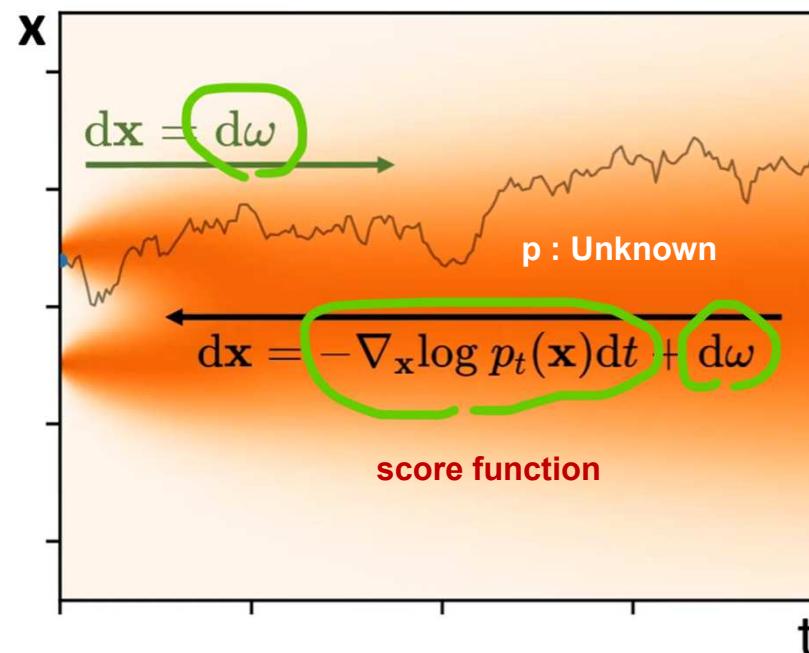


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- The change in image dx , equals $d\omega$ which is a white noise so that's just the mathematical expression of doing cumulative sum of random noise.



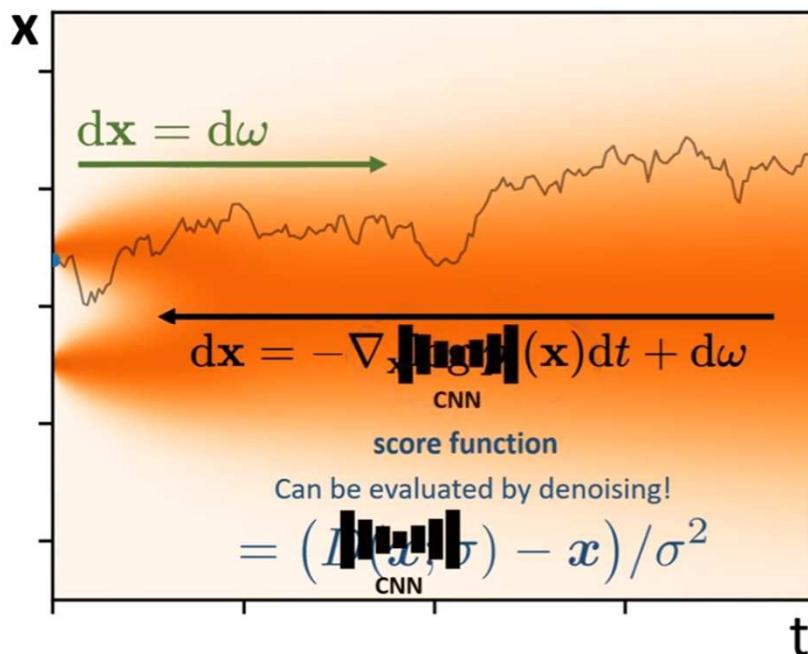
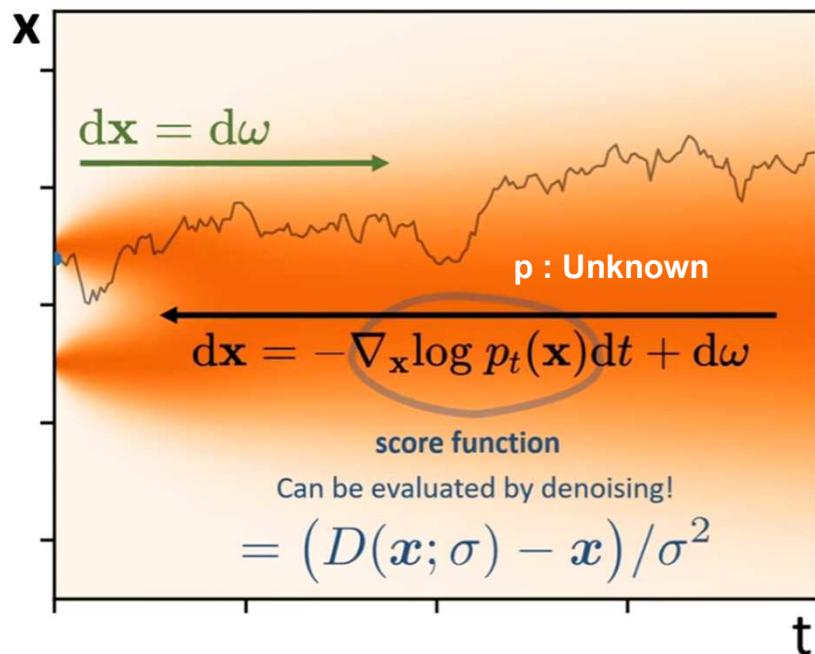
- This forward equation corresponds to a backward version that has this same stochastic component random walk component.
- Score function: Term that kind of attract the samples towards the data density you see some kind of a gradient of log of the data density. p is unknown

Forward and reverse SDE

- Evolution governed by a *stochastic differential equation* (SDE)
- We'll generalize these later!

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Forward and reverse SDE

- Evolution governed by a *stochastic differential equation* (SDE)
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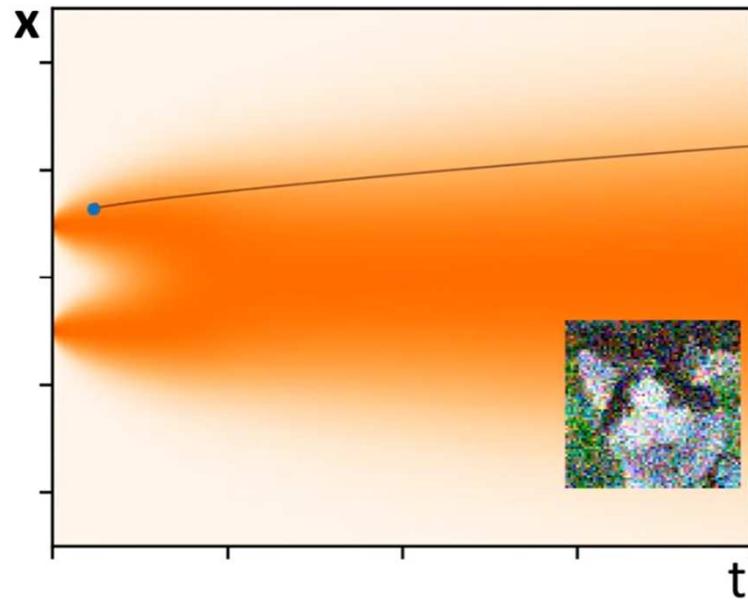
- You do not need to know the P if you have an optimal Denoiser for this data set so you can directly evaluate that formula
- This is an opportunity we train a neural network to be such a denoiser. This means that we can run this kind of backboard equation Evolution using that learn D.

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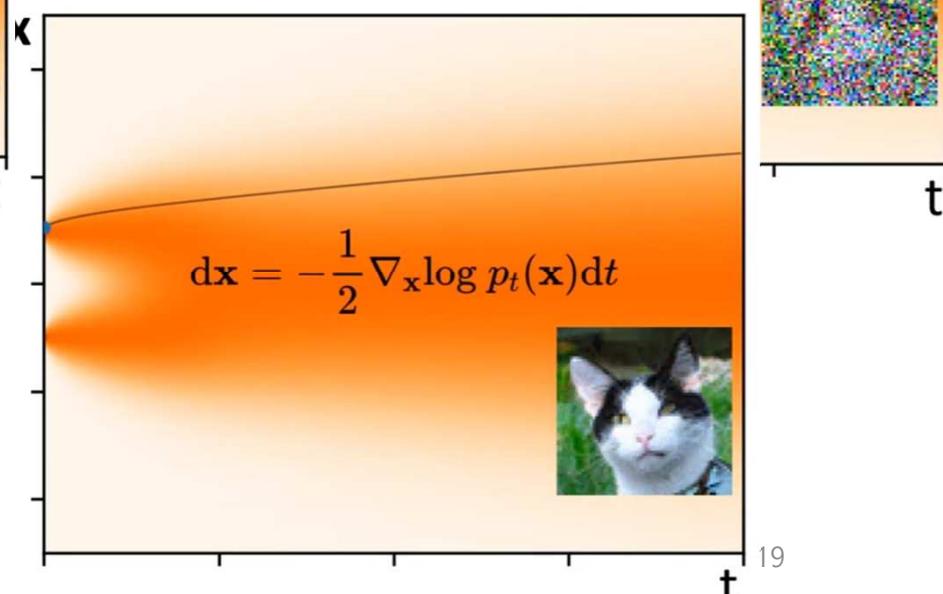
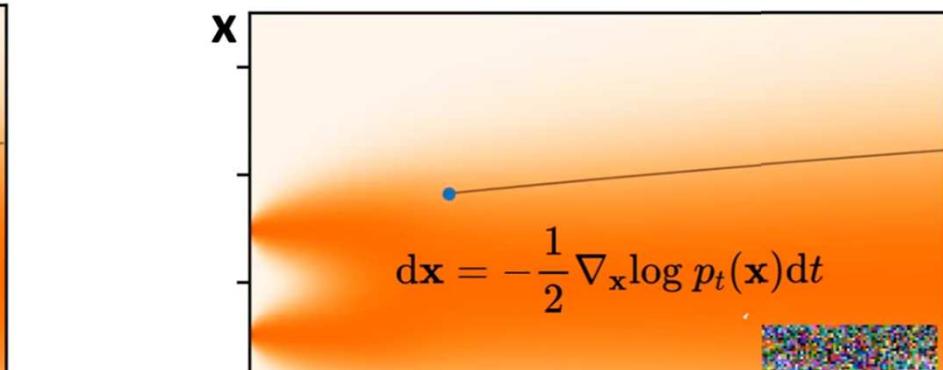
Deterministic ODE

- Song et al. also present a *deterministic* ordinary differential equation



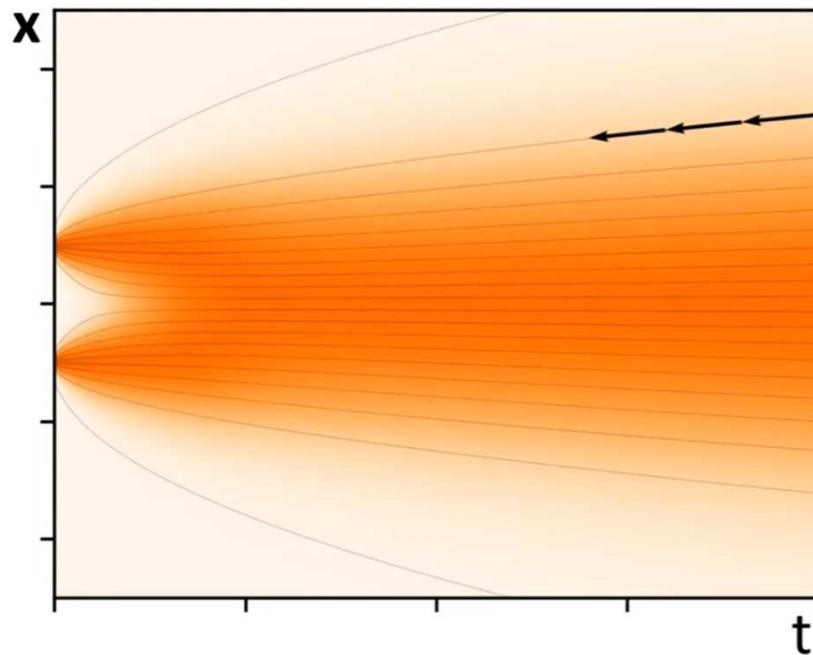
Don't have the stochastic term.

Have the core term scaled in a way.



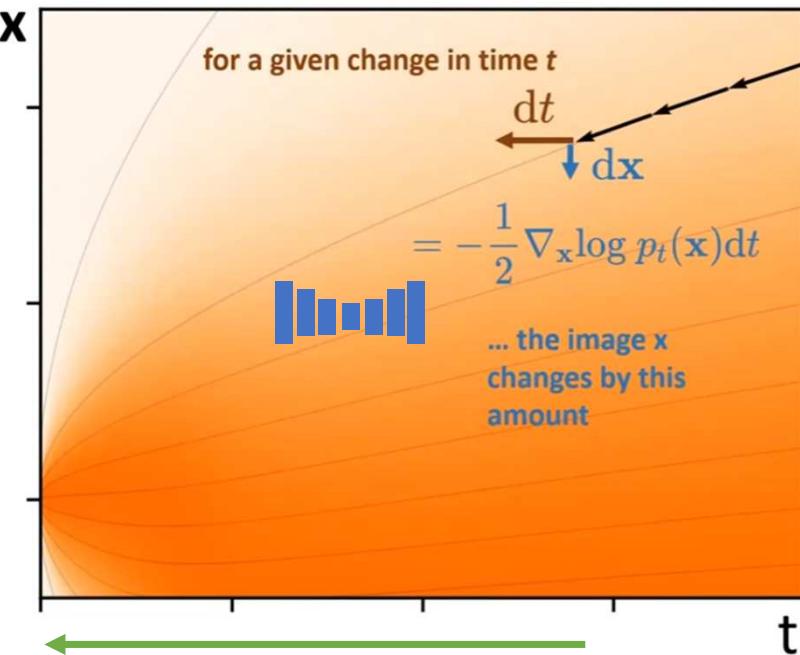
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Solution by discretization

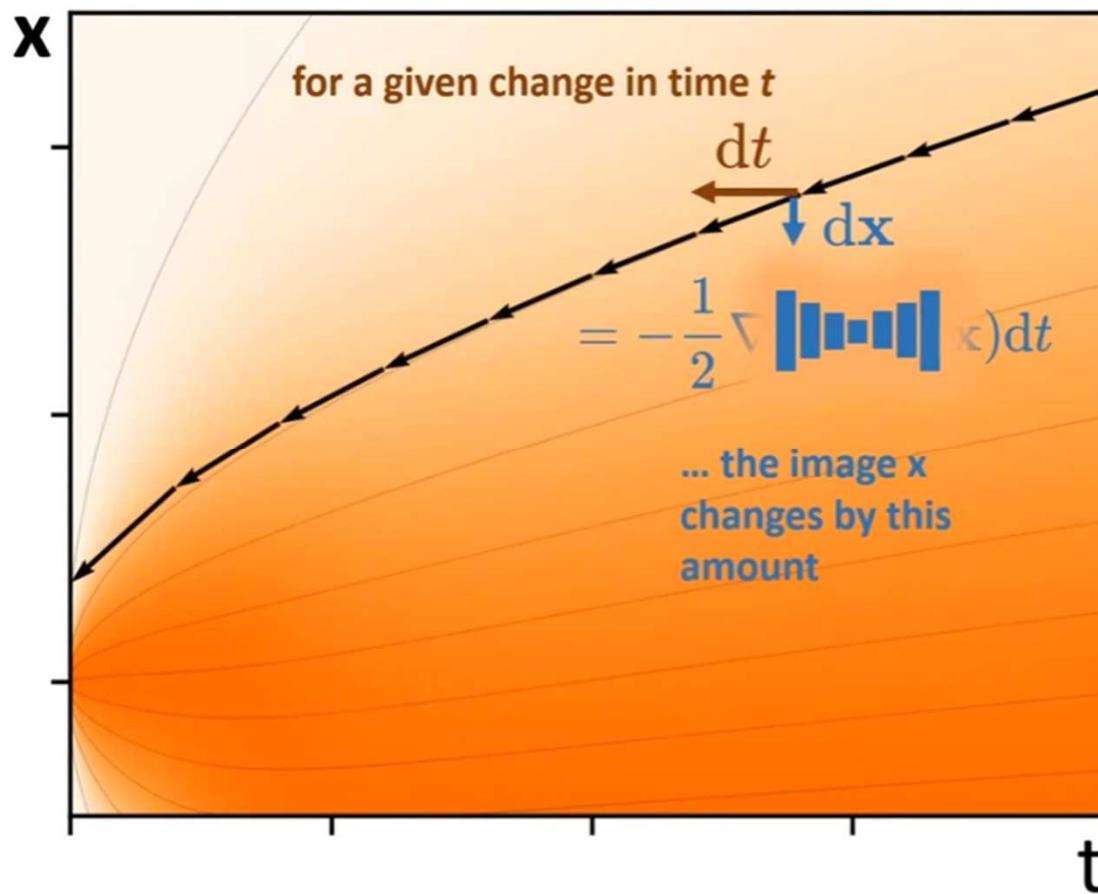
Try to somehow follow flow lines to do the generation and in the way that happens is by discretization.



Time 축 스케일 확대

- For any change in time I want to jump, the ODE formula tells me how much the image changes and again the ODE formula is evaluated this neural network, so the Network tells us where to go on the next step that's the general idea.

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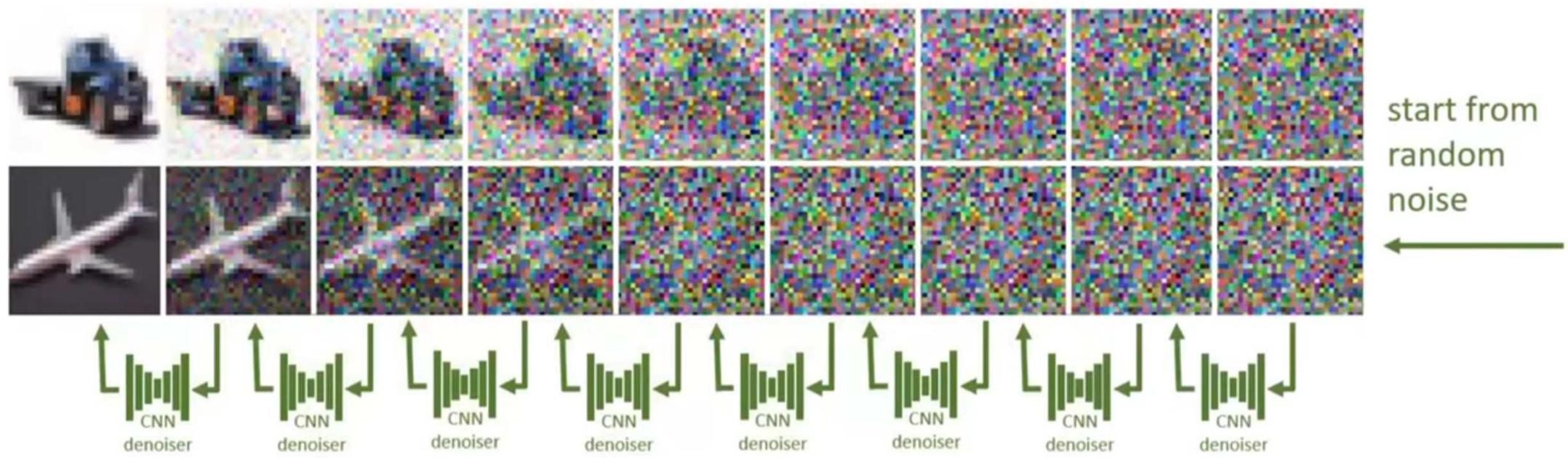


Solution by discretization

- In stochastic sampling (SDE), we would also inject noise at every step.
- We'll leave that for later and focus on the ODE first.

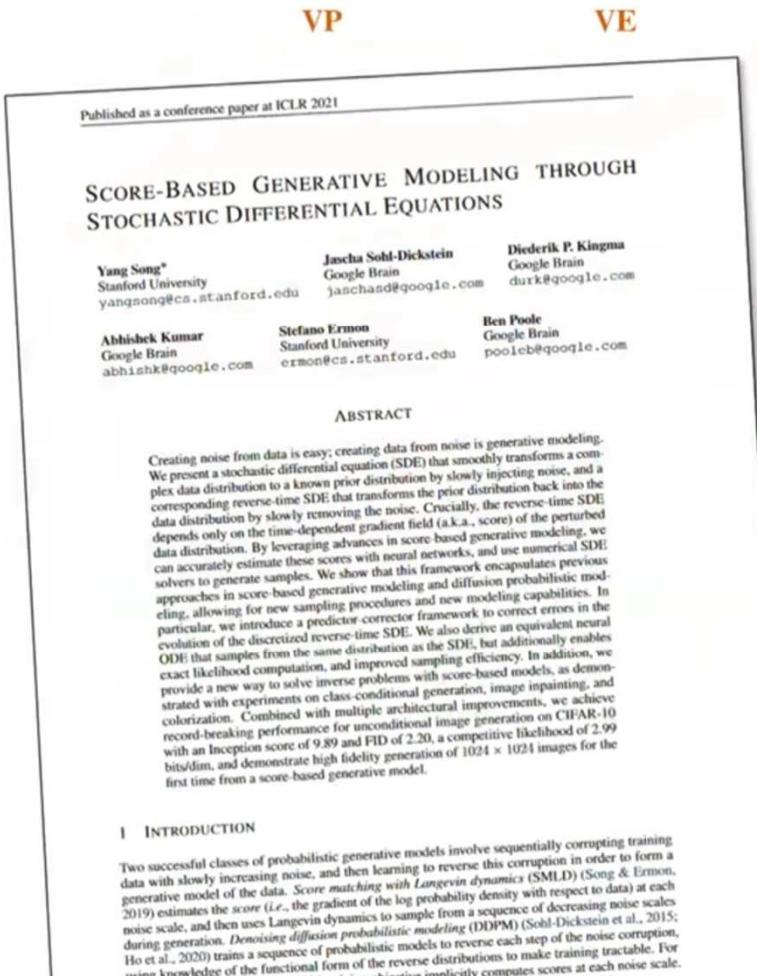
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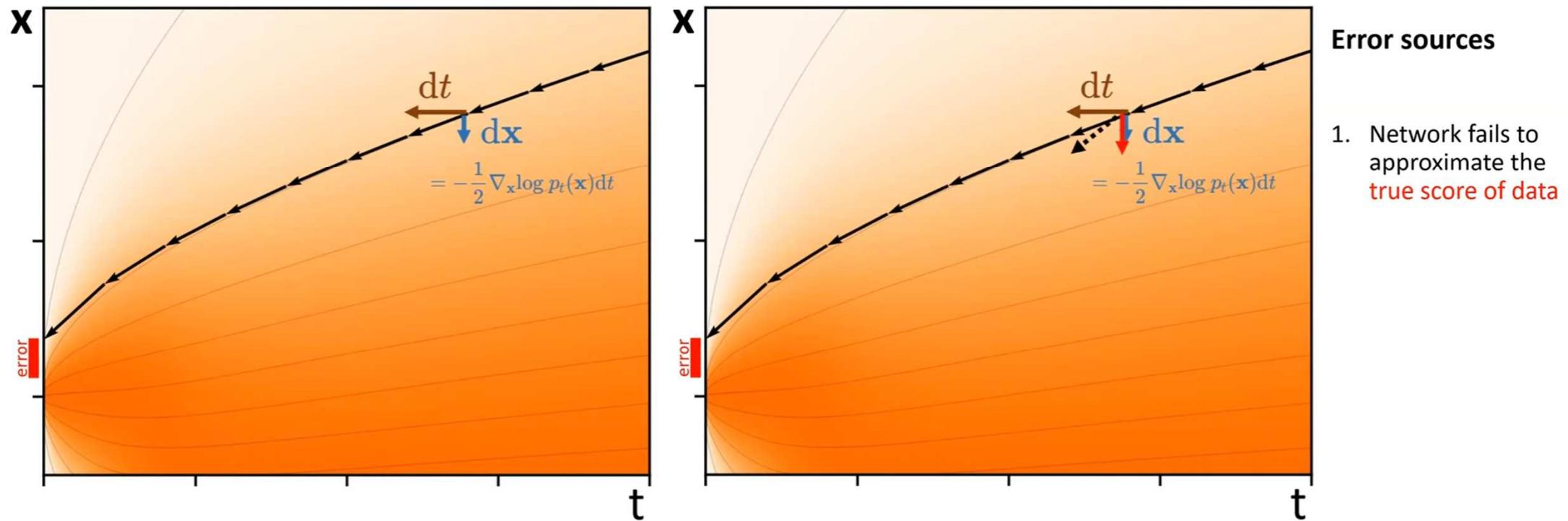


That was
Song et al. (2021)
in a nutshell (for our
purposes)

Next, let's identify some
design choices from
different methods, and
generalize.

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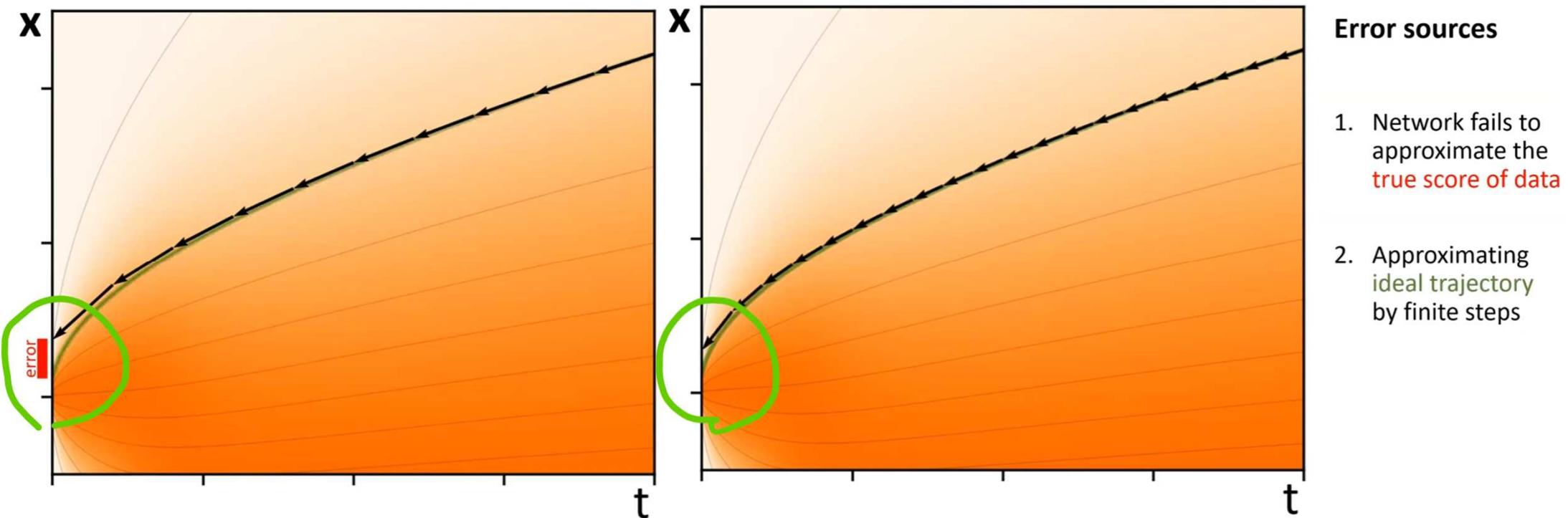
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- When I do this sampling chain, the obvious one is that if the network gives me an incorrect direction and I end up moving in the incorrect direction and in the end I end up somewhat in the wrong place.

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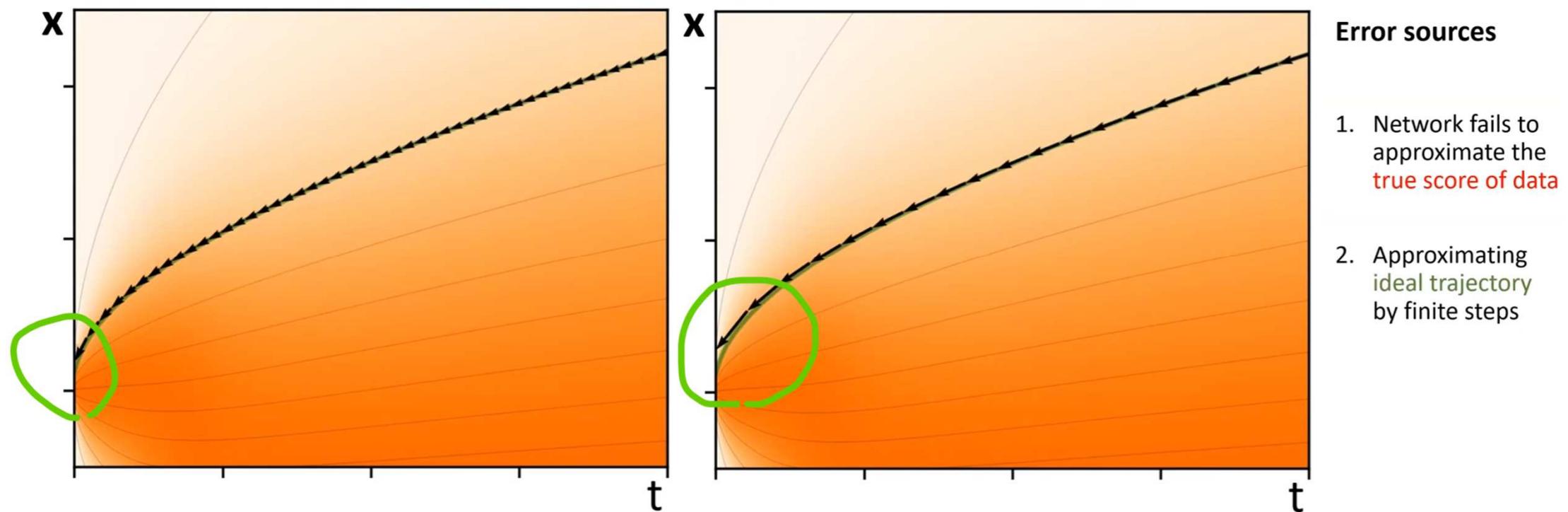
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- Try to approximate this continuous trajectory in green here using these linear segments.
- If try to jump too far at once, the curve will kind of move away from our feet.

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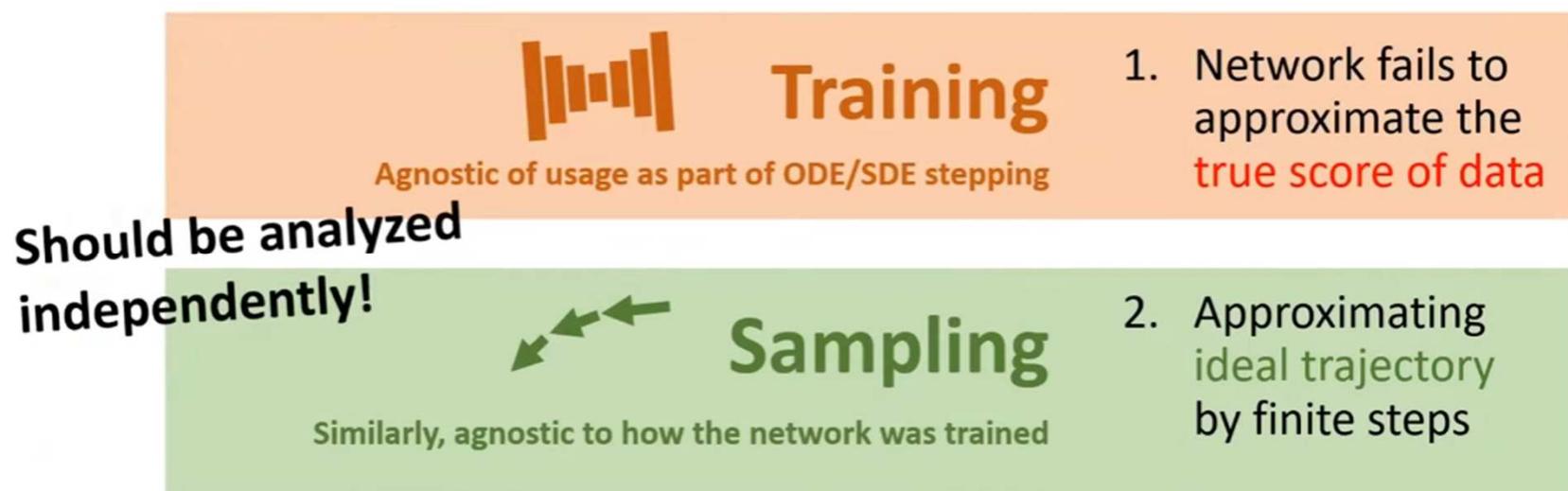
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- Brutal solution is to take more steps but more compute to generate an image.

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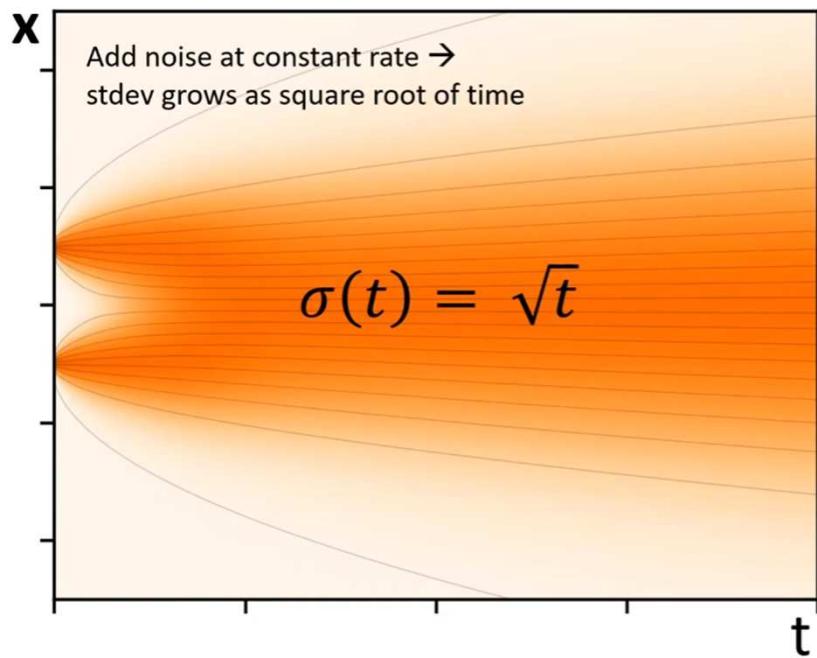
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- You don't have to sample in a certain way just because you train your neural network in a certain way and so on you can decouple this.
- We'll be looking at sampling first and then coming back to the training later.

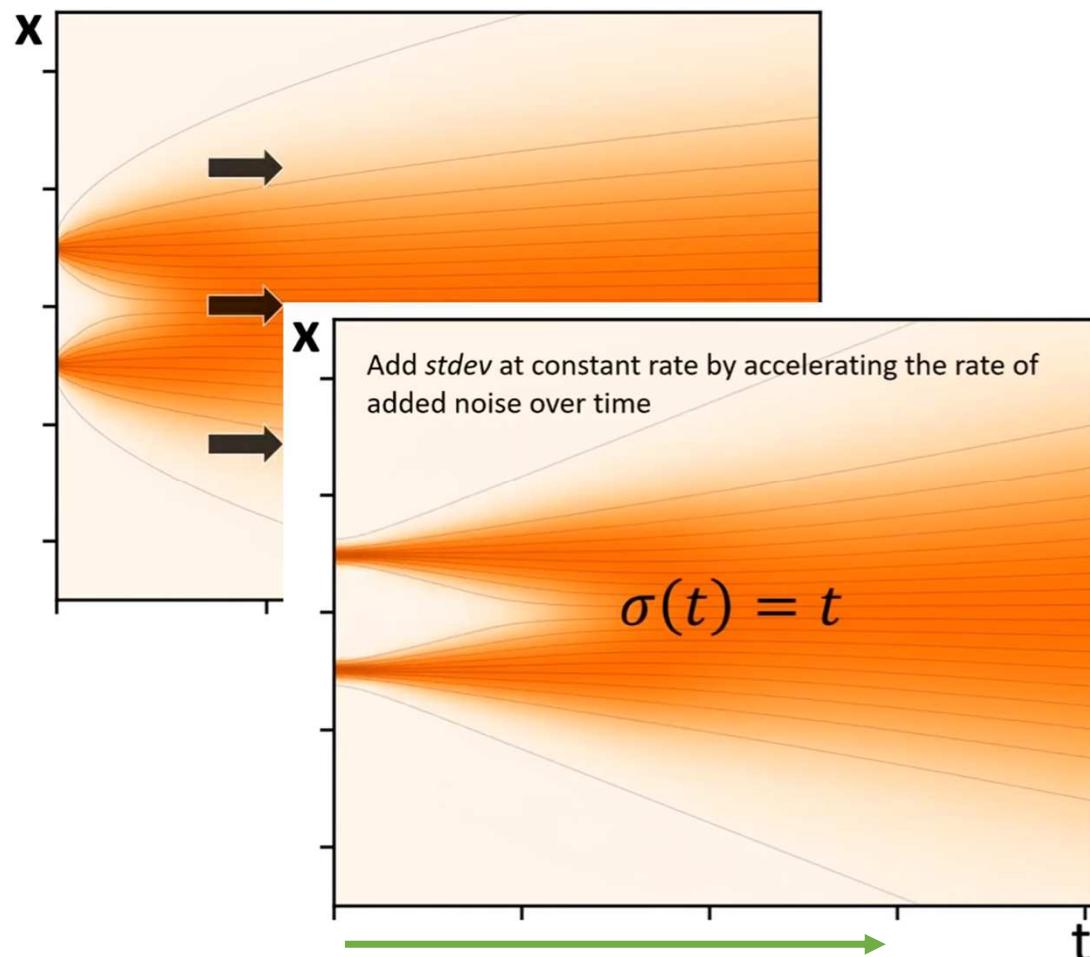
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Noise schedule

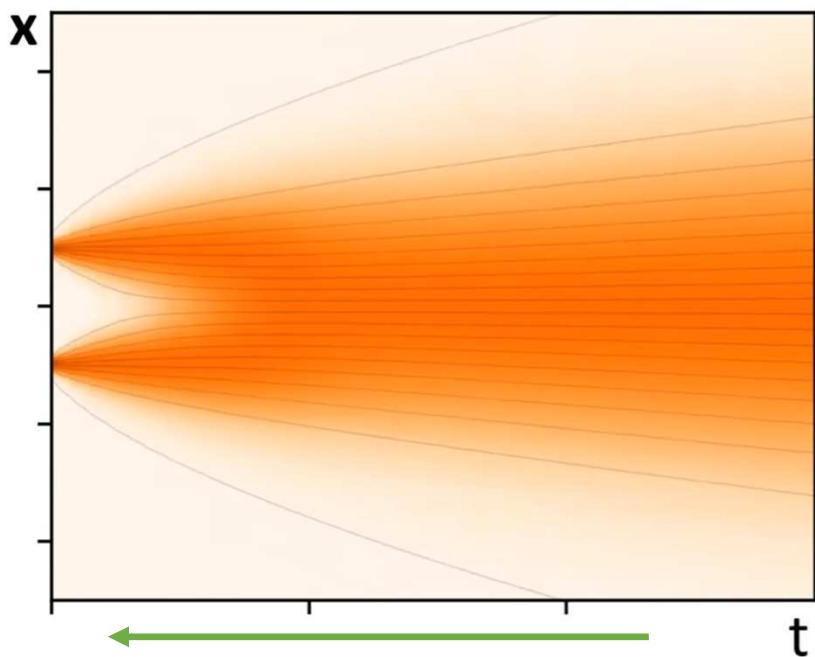
- Add noise at different rate → different ODE
- Many schedules in literature



- Noise schedule where the noise level increase as a square root of time because that's how the variance grows linearly, so the standard deviation grows square root.

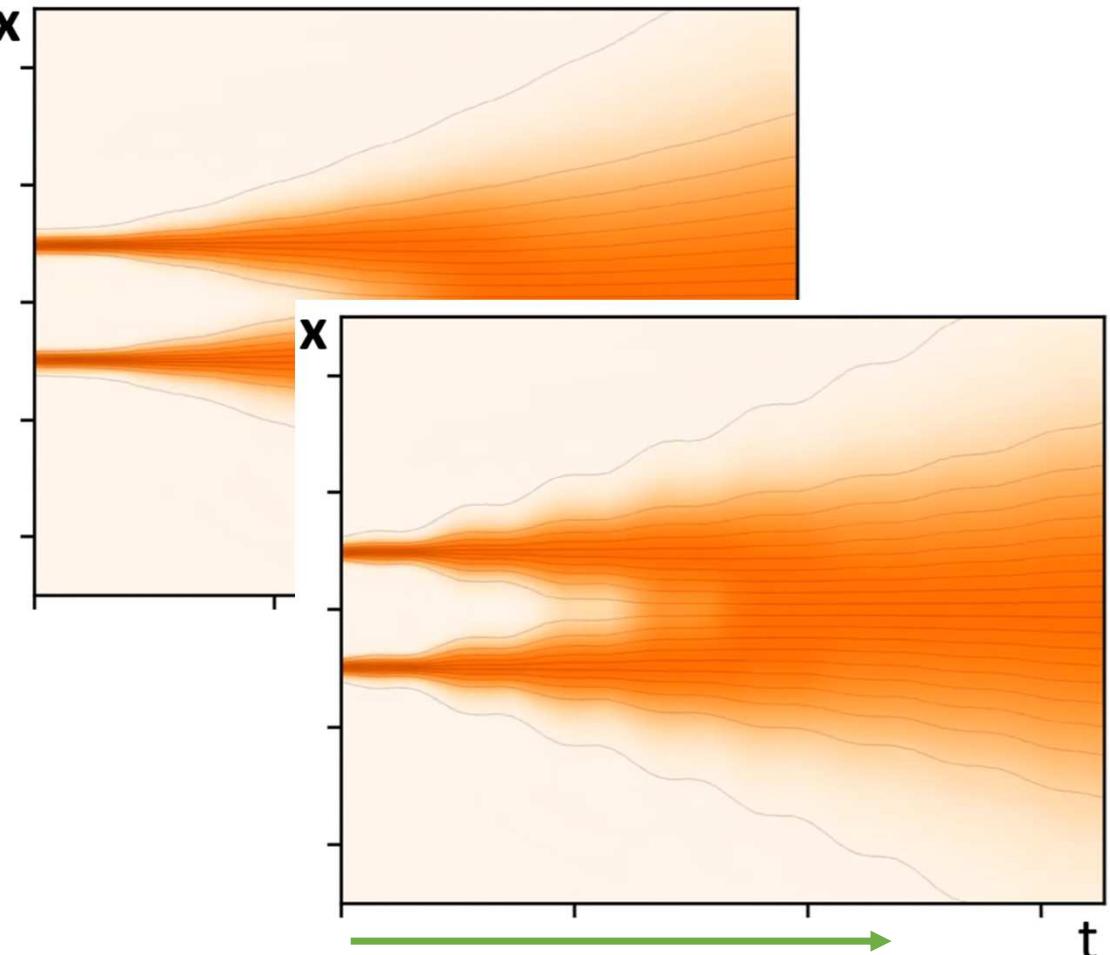
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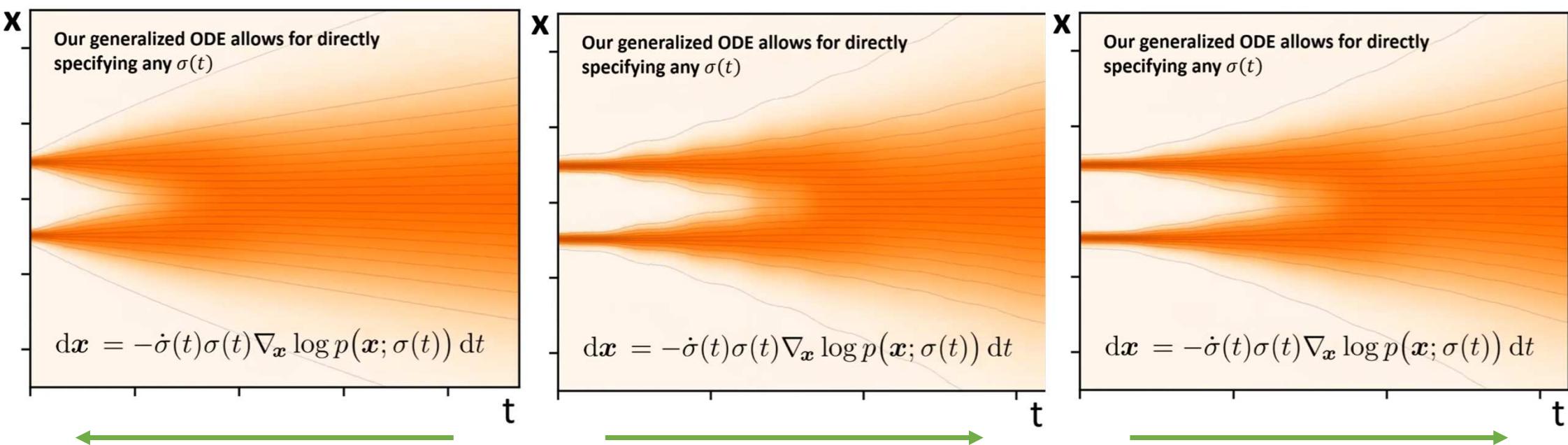
Noise schedule

- Add noise at different rate \rightarrow different ODE
- Many schedules in literature
- All of them simply warp the t -axis



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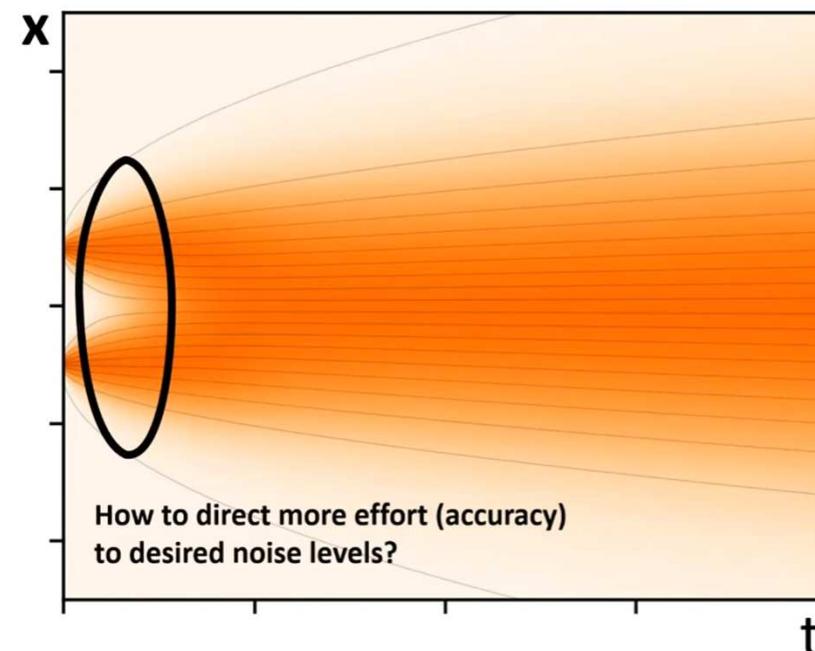
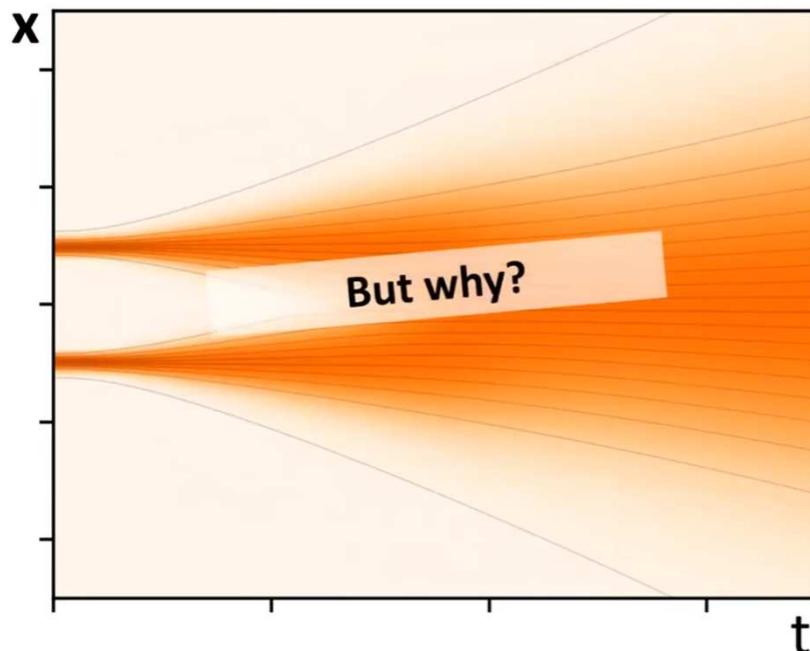
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- Generalize ODE
- We can parameterize the noise level we want to have reached by explicitly by this Sigma function.

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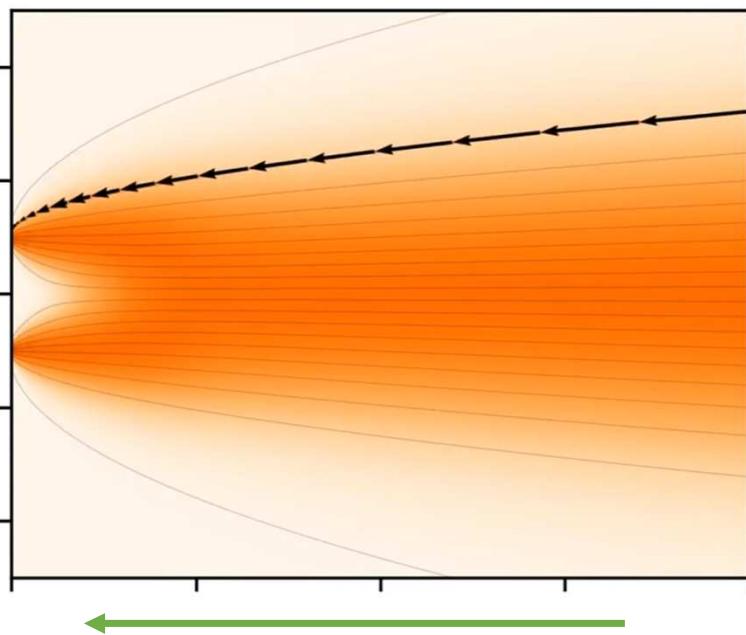


- Almost nothing happens until at almost zero time, noise level suddenly curves rapidly to one of these two basins and there's high curvature.
- Careful in sampling that region and less careful here in the bulk

- There's two ideas of how you might do that.

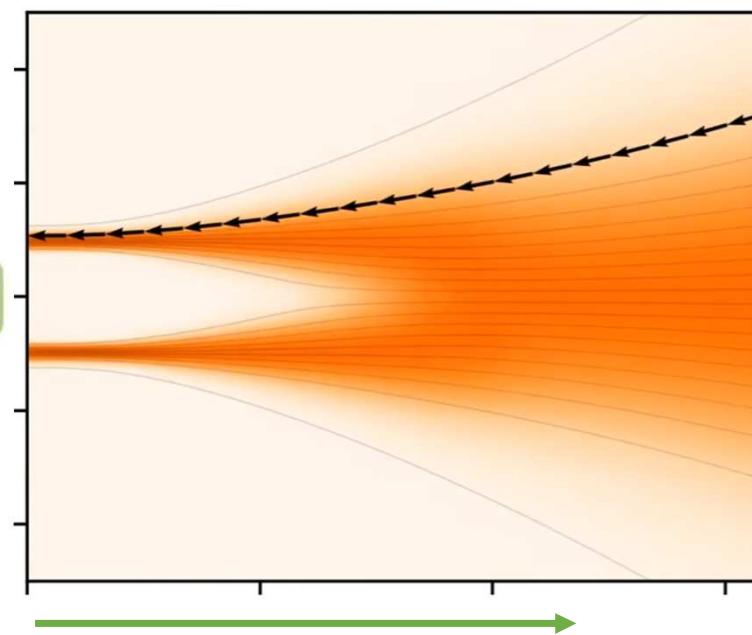
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Noise schedule vs step lengths

- Two options:
 - Take shorter steps at desired levels
 - Warp noise schedule to spend more time at those levels



Noise schedule vs step lengths

- Two options:
 - Take shorter steps at desired levels
 - Warp noise schedule to spend more time at those levels

- Take shorter steps at the more difficult parts usually it's the low noise levels

These two approaches are not equivalent.

The error characteristics can be vastly different between these choices like the error that comes from tracking this continuous curve.

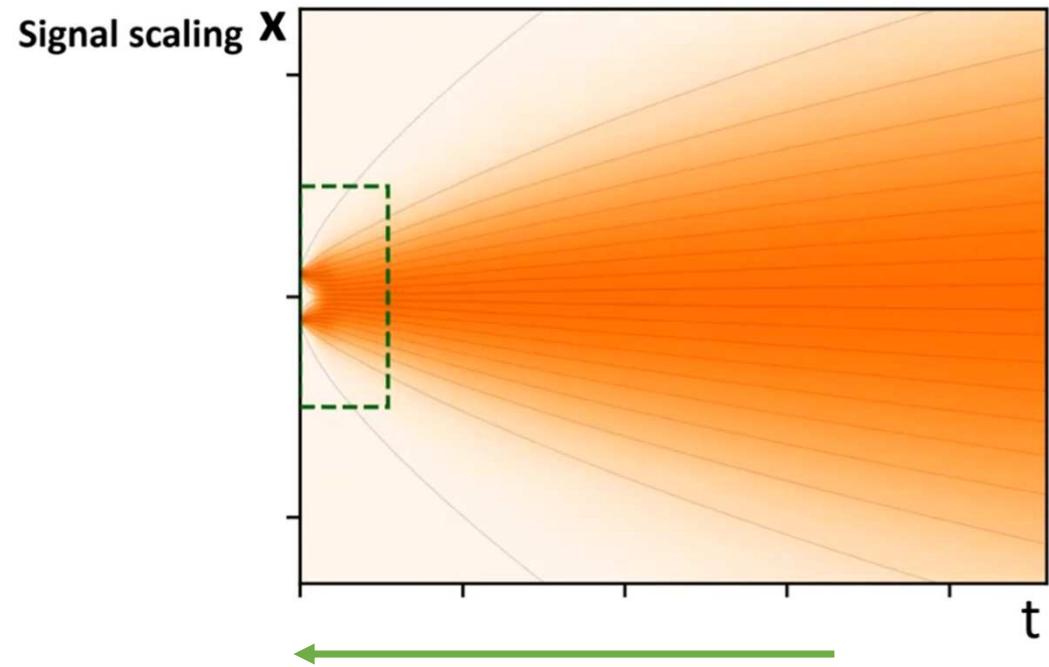
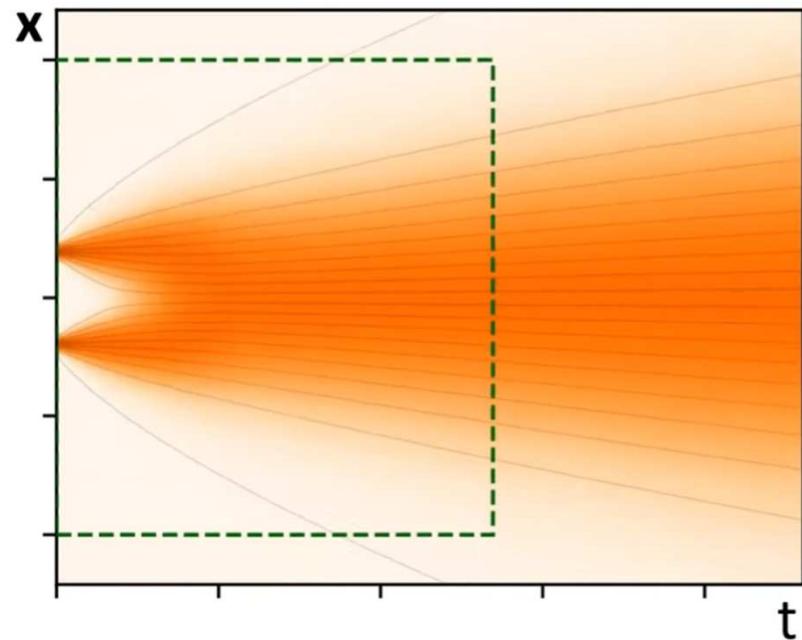
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	VP	VE	iDDPM	+ DDIM	Ours
Sampling					
Time steps	$t_{i < N}$				
Sampling time					
Schedule	$\sigma(t)$				
Noise schedule					

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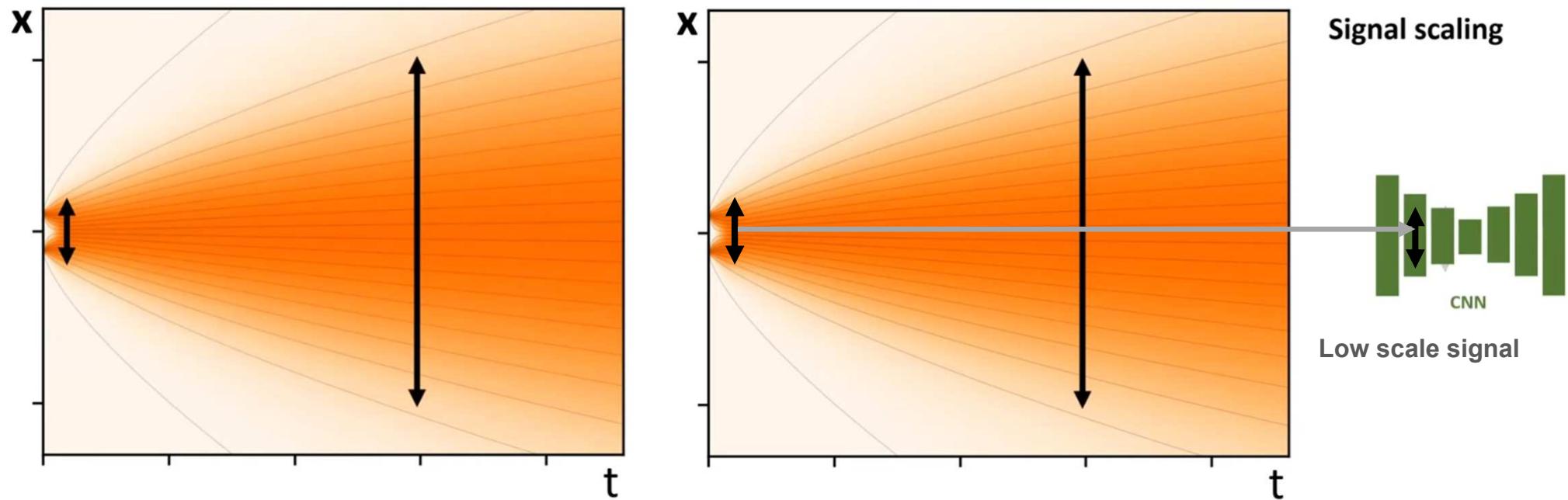
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



- Zoom out a little because in reality we add a ton of noise,
the noise level is very large at the other extreme.

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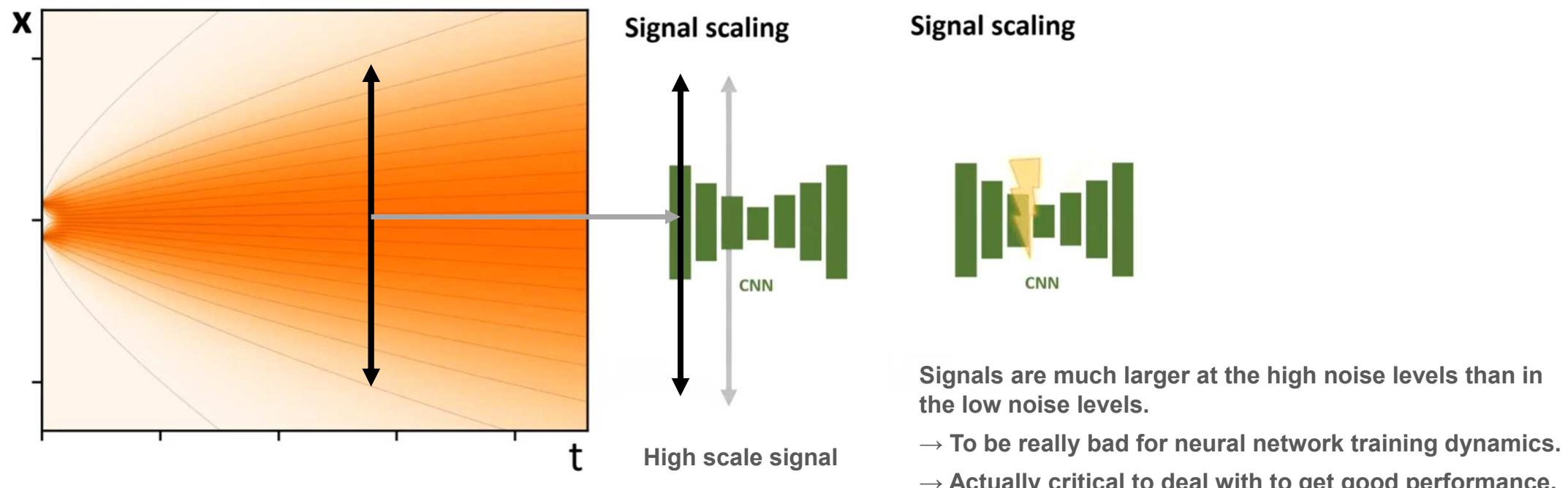
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



- If don't do anything, the signal magnitude grows as the noise level grows -
Keep piling noise
- The signal is quite simply bigger numerically

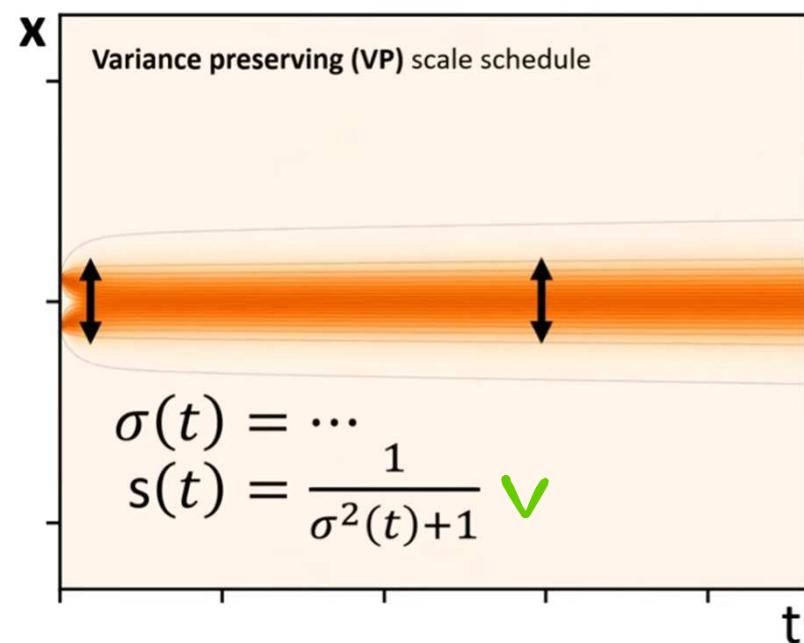
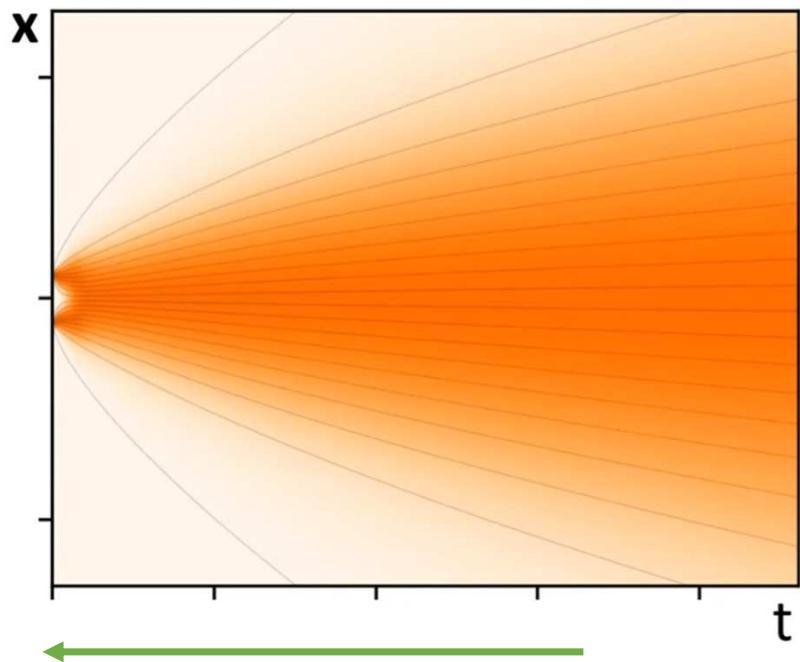
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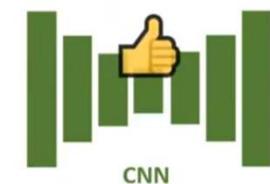


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Signal scaling

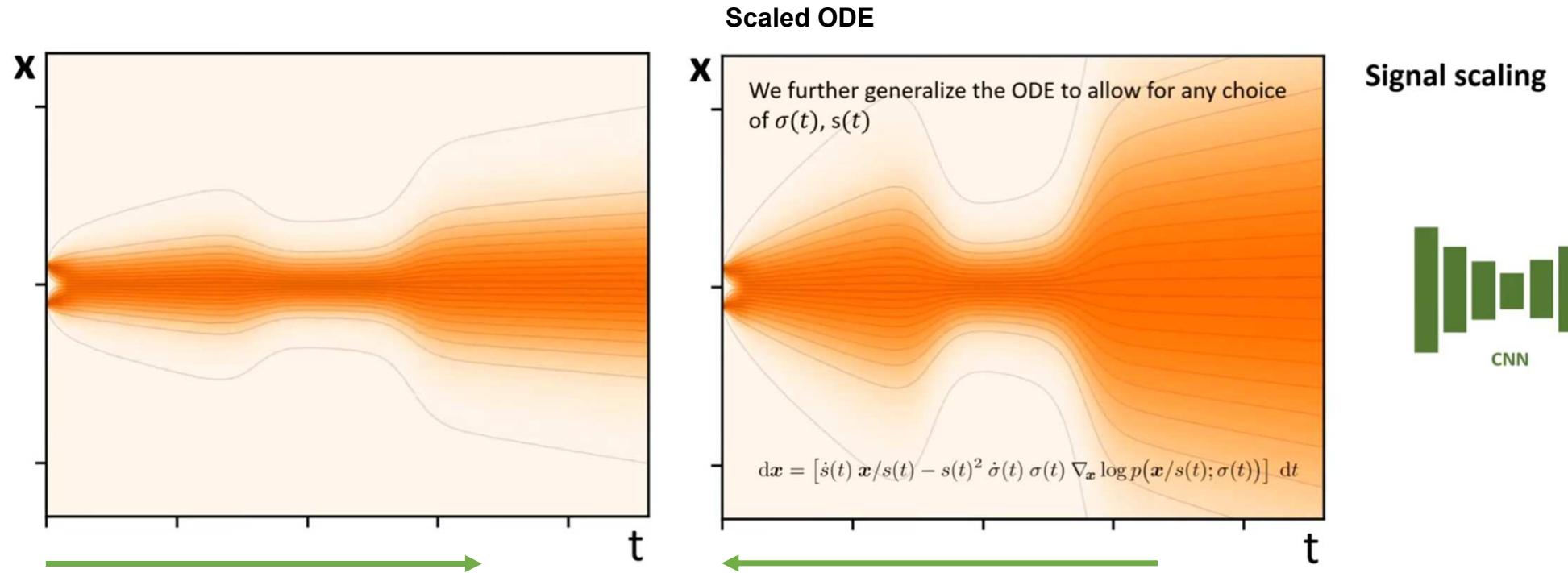


Variance Preserving (VP) Scale Schedule

- Scale schedule : Squeeze the signal magnitude into the constant variance tube so that makes the network happy

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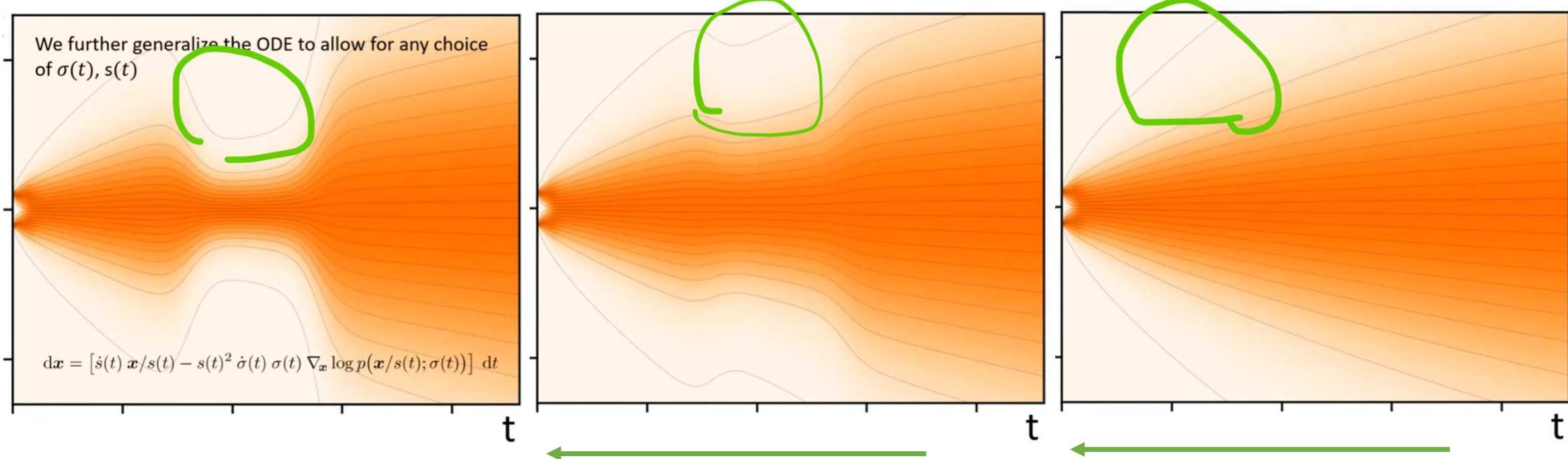
- Formulating an **ODE** that allows you to **directly specify any arbitrary scale schedule**.
- The only thing that **the scale schedule does is distort these flow lines in some way**.



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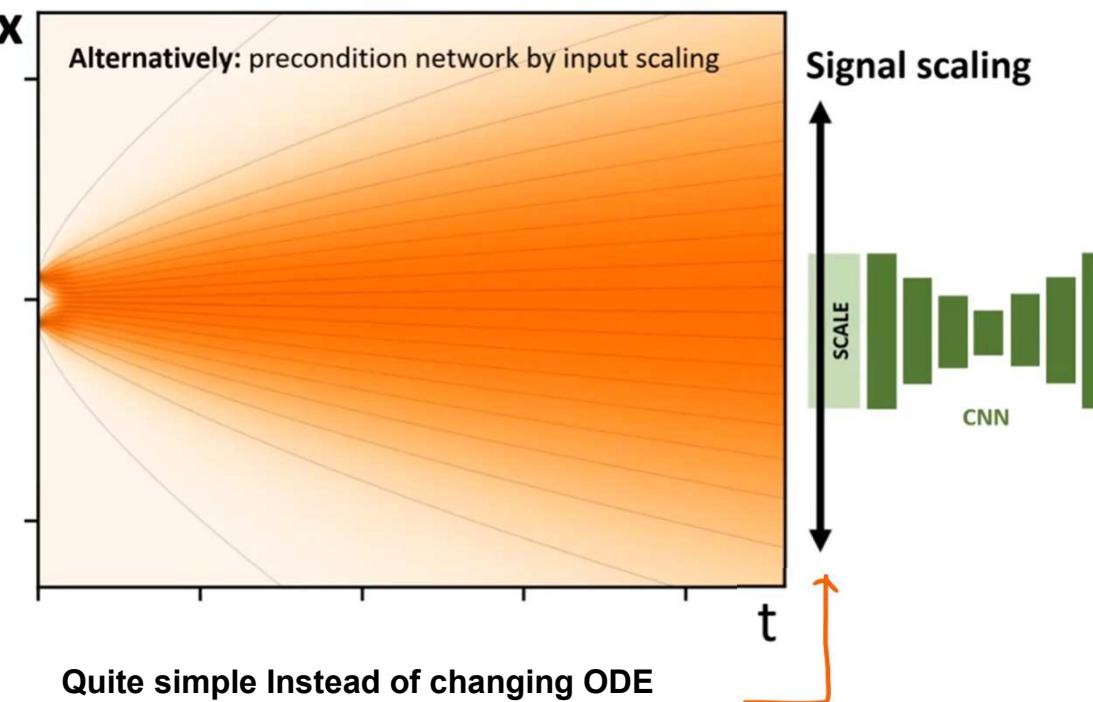
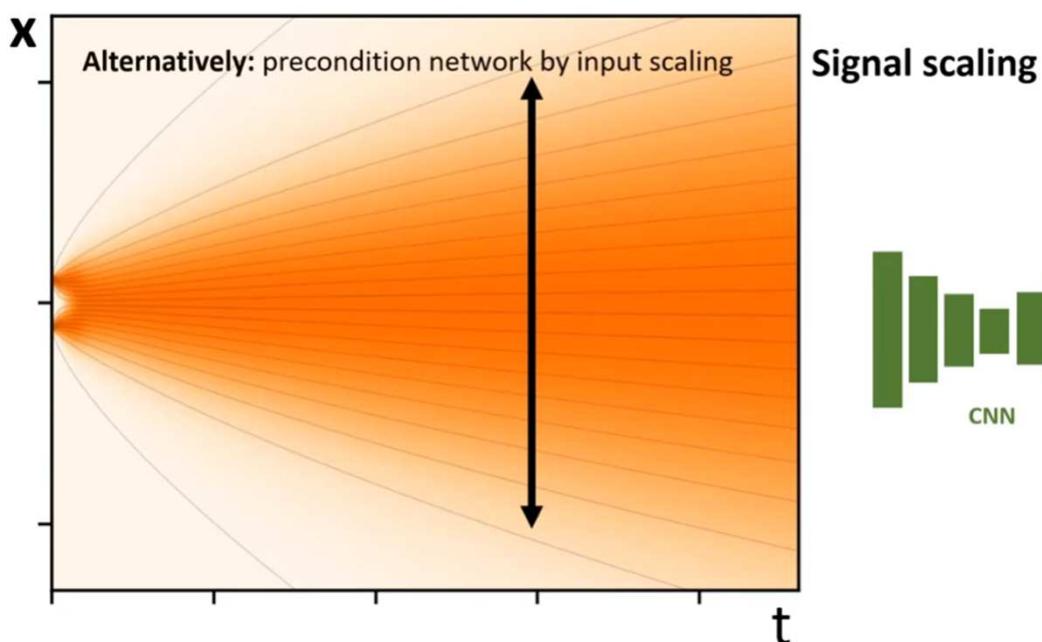
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Scaled ODE



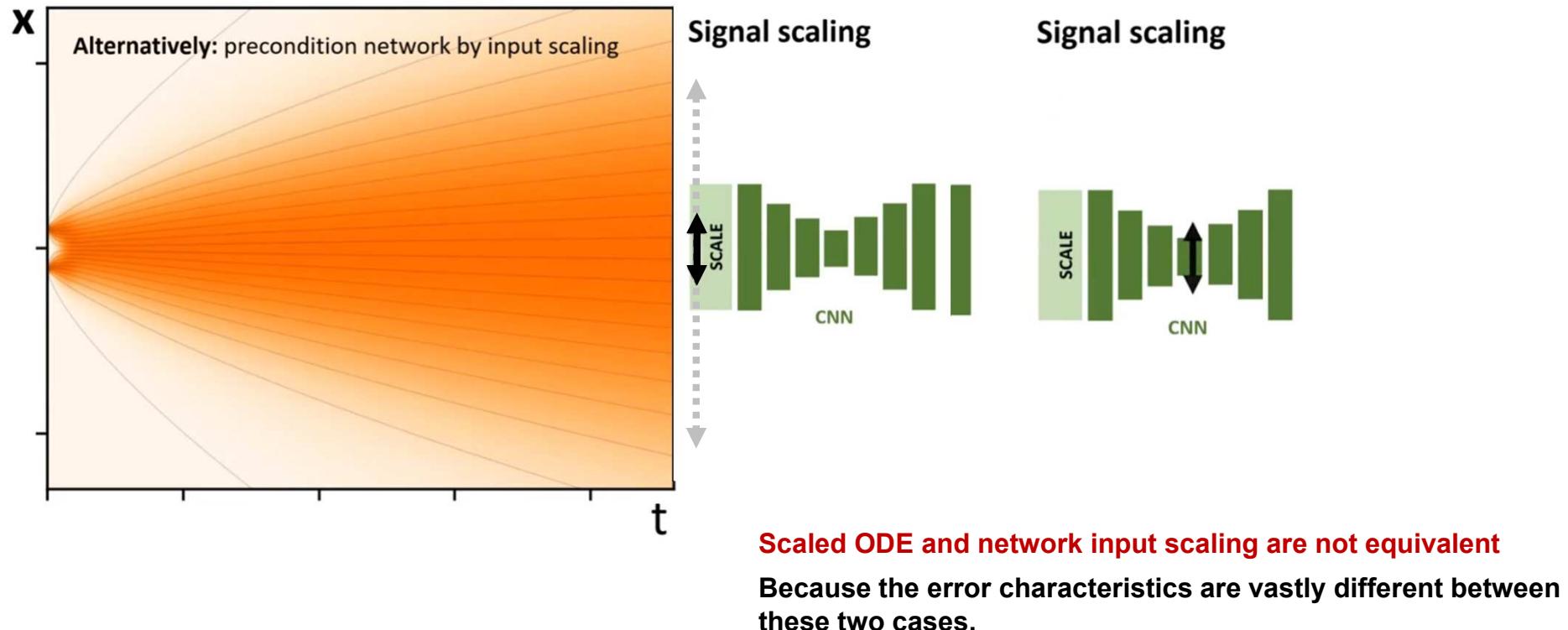
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Alternatively : Initial Scaling layer



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	VP	VE	iDDPM	+ DDIM	Ours
Sampling					
Time steps	$t_{i < N} = 1 + \frac{i}{N-1}(\epsilon_s - 1)$	$\sigma_{\max}^2 (\sigma_{\min}^2 / \sigma_{\max}^2)^{\frac{N-1}{N}}$	$u_{\lfloor j_0 + \frac{M-1-j_0}{N-1} i + \frac{1}{2} \rfloor}$, where $u_M = 0$		
Noise schedule	Schedule	$\sigma(t) = \sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t} - 1}$	\sqrt{t}	t	?
Scaling schedule	Scaling	$s(t) = 1 / \sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t}}$	1	1	
Network and preconditioning					
		Skip scaling	$c_{\text{skip}}(\sigma)$		
		Output scaling	$c_{\text{out}}(\sigma)$		
		Input scaling	$c_{\text{in}}(\sigma)$		
		Noise cond.	$c_{\text{noise}}(\sigma)$		
	Input scaling	$c_{\text{in}}(\sigma) = 1 / \sqrt{\sigma^2 + 1}$	1	$1 / \sqrt{\sigma^2 + 1}$	

Identified the design choices the **scaling & schedule** and
the **scaling that happens inside the neural network itself**
that we count as a so-called **preconditioning of the**
neural network.

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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

	VP	VE	iDDPM	+ DDIM	Ours
Sampling					
Time steps	$t_{i < N} = 1 + \frac{i}{N-1}(\epsilon_s - 1)$	$\sigma_{\max}^2 (\sigma_{\min}^2 / \sigma_{\max}^2)^{\frac{N-i}{N-1}}$	$u_{\lfloor j_0 + \frac{M-1-j_0}{N-1} i + \frac{1}{2} \rfloor}$, where $u_M = 0$ $u_{j-1} = \sqrt{\frac{u_j^2 + 1}{\max(\bar{\alpha}_{j-1}/\bar{\alpha}_j, C_1)} - 1}$?
Noise schedule	Schedule	$\sigma(t) = \sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t} - 1}$	\sqrt{t}	t	
Scaling schedule	Scaling	$s(t) = 1 / \sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t}}$	1	1	
Network and preconditioning					

We'll use pre-trained networks from
previous work for now...

$$\text{Input scaling } c_{\text{in}}(\sigma) = 1 / \sqrt{\sigma^2 + 1}$$

and return to training in Section IV

We'll just try to improve the sampling;
Deterministic & Stochastic sampling.

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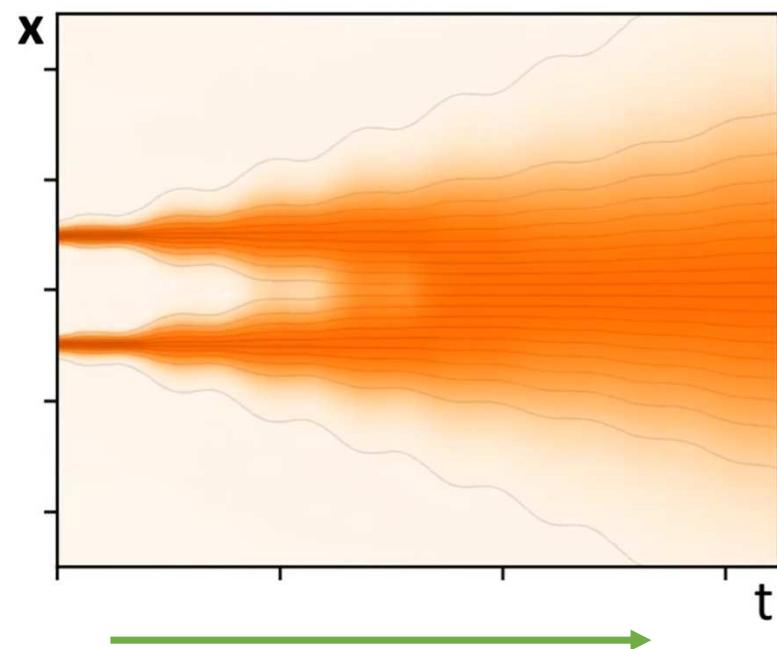
Outline

- Part I: Common framework
 - Identifying the moving parts in existing work
- Part II: Deterministic sampling
 - Solving the ODE efficiently
- Part III: Stochastic sampling
 - Why SDE's? How to do stochastic stepping?
- Part IV: Preconditioning and training
 - How to train the CNN used in evaluating a step?

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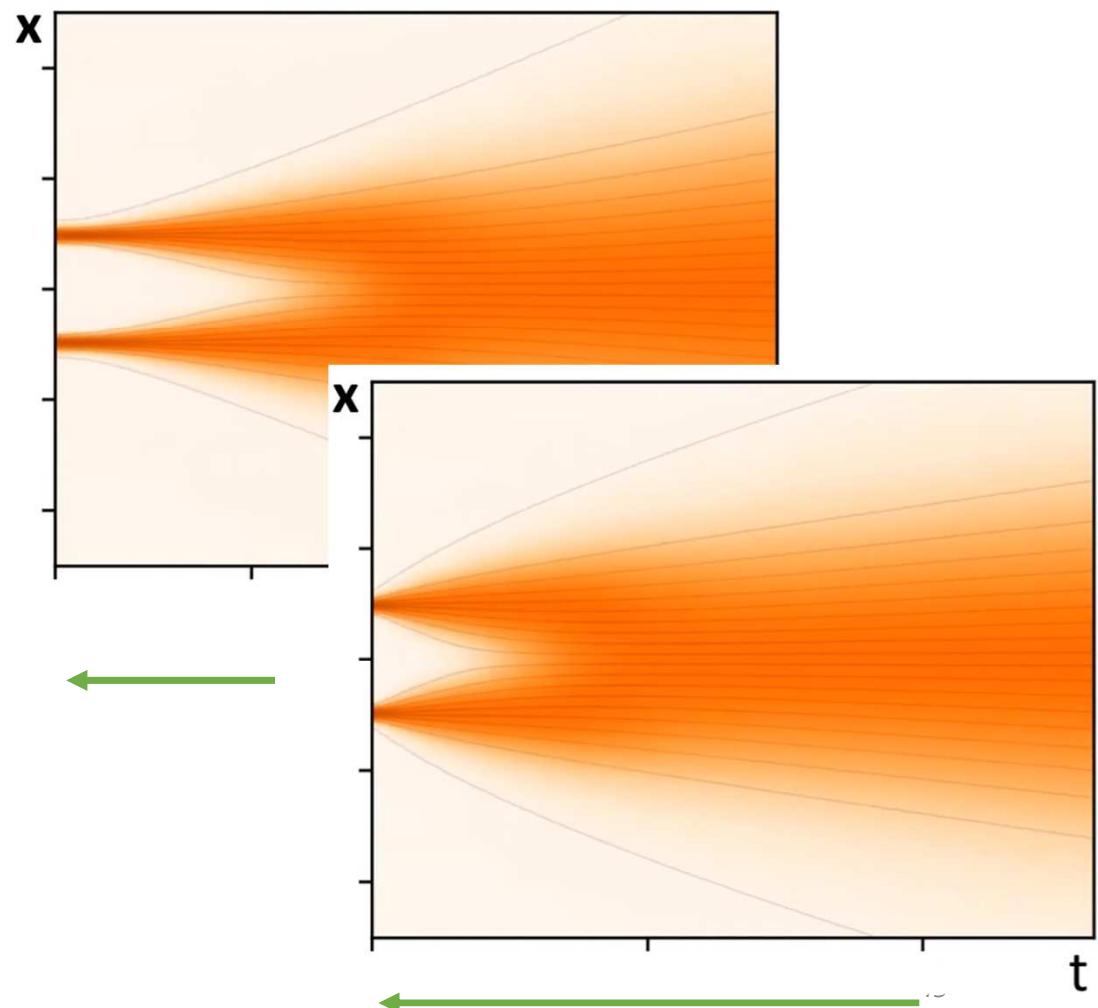
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Noise Schedule $\sigma(t)$



Noise schedule

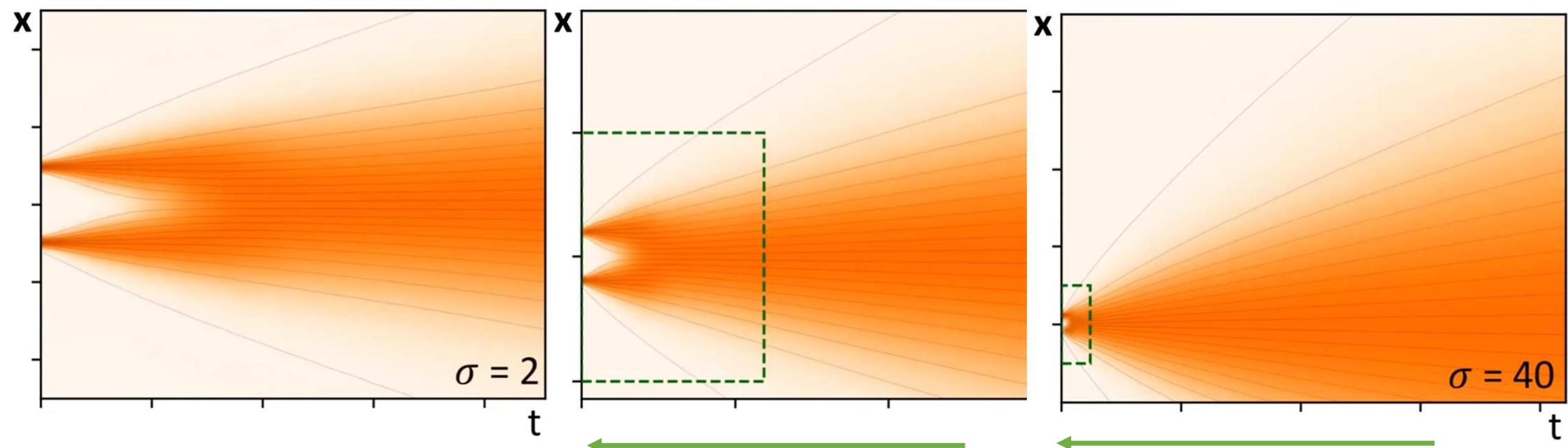
- Why are some better than others?



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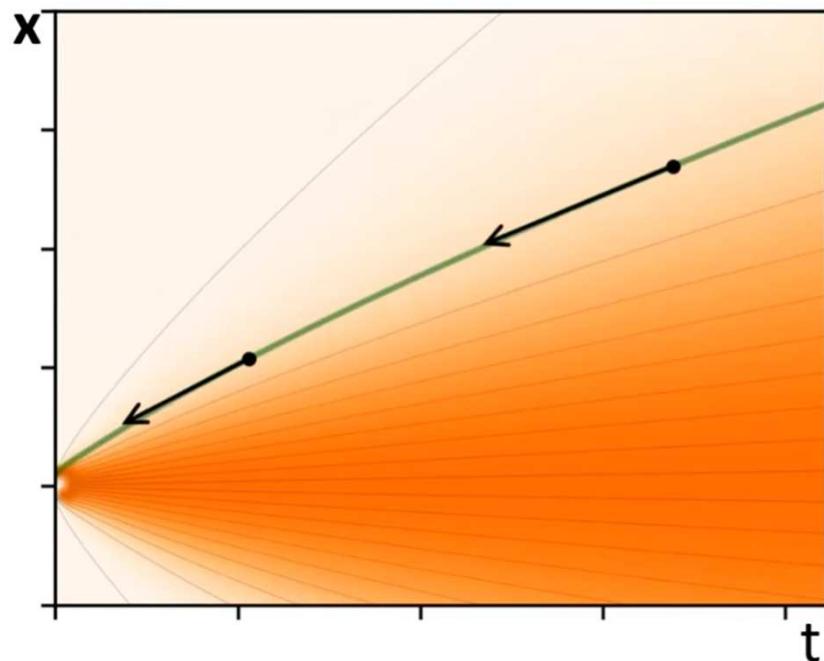
Noise Schedule $\sigma(t)$



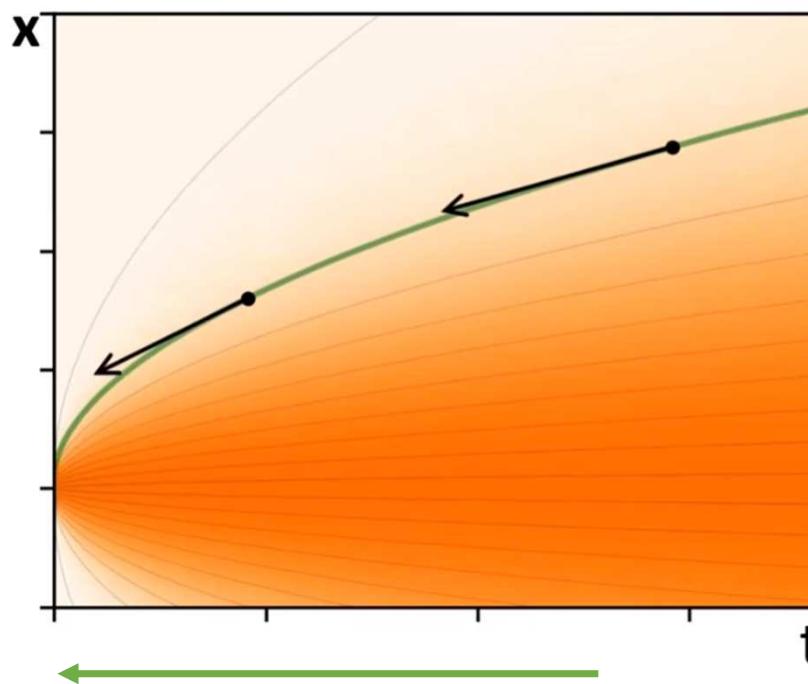
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Noise Schedule $\sigma(t)$



More successful when the tangents happen to coincide with this curve trajectory and so the trajectory is as straight as possible

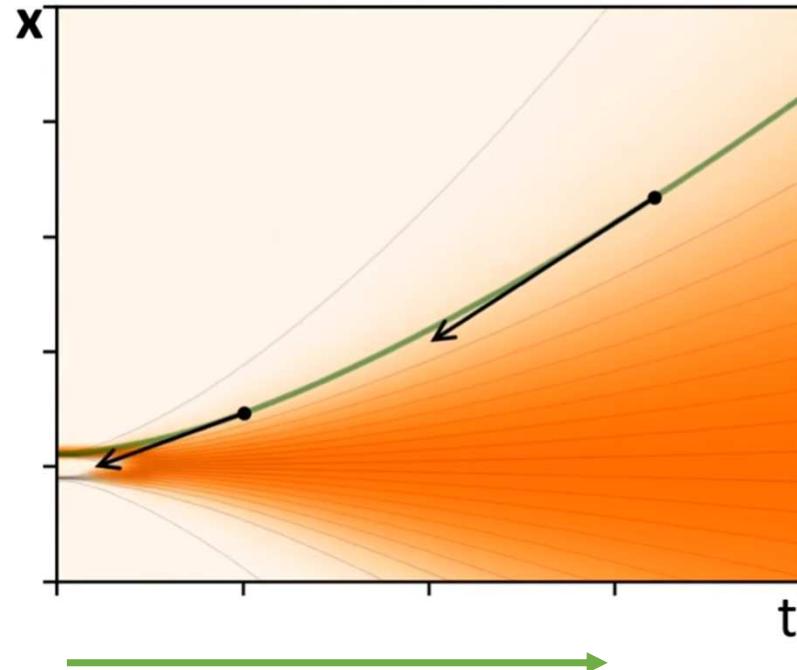
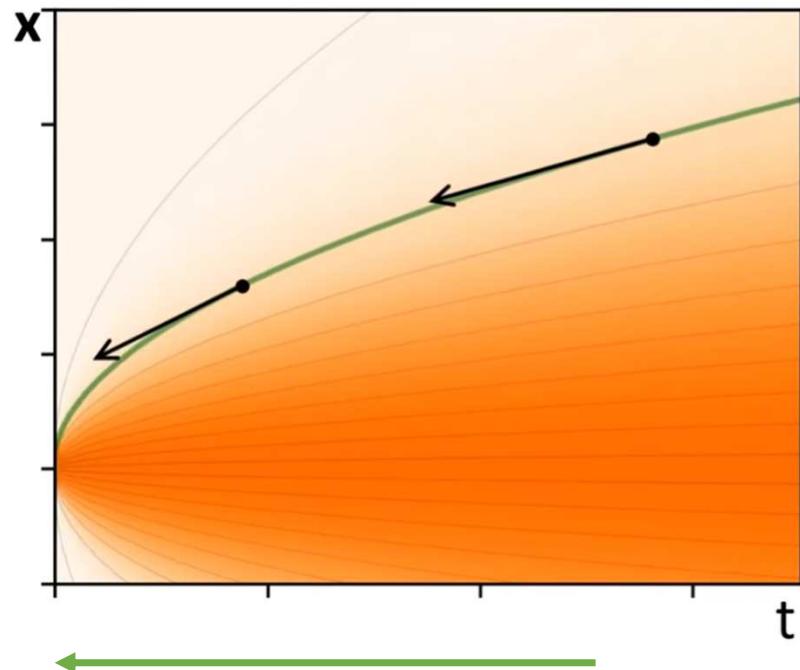


Bad schedule : a visible gap between the tangent and the curve
Easily fall off if you try to step too much.

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Noise Schedule $\sigma(t)$



Random family of different schedules

Noise schedule

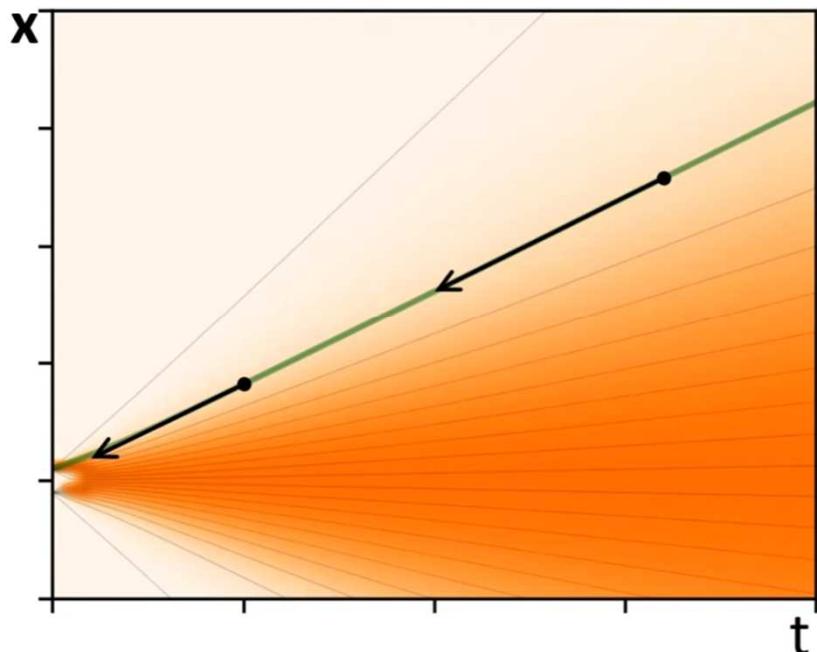
- Why are some better than others?
- Straighter trajectory
 - less need to "correct course" along the way
 - fewer steps suffice

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Noise Schedule $\sigma(t)$

Scaling Schedule $s(t)$



We advocate the
“linear” schedule
(same as DDIM):

$$\begin{aligned}\sigma(t) &= t \\ s(t) &= 1\end{aligned}$$

Note: We'll normalize
signals by
preconditioning rather
than scaling the ODE.
But more on that later.

We advocate the
“linear” schedule
(same as DDIM):

$$\begin{aligned}\sigma(t) &= t \\ s(t) &= 1\end{aligned}$$

$$dx = -t \nabla_x \log p_t(x) dt$$

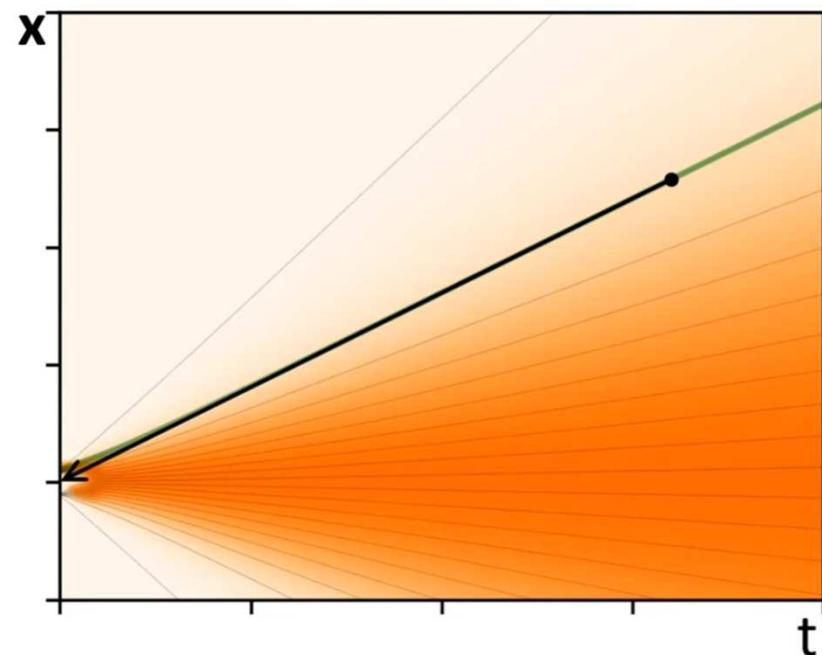
We'll be leaving the scaling for Neural Network parameterization.
The reason for that is that the scaling also introduces unwanted
curvature into these lines.

As a further with this the ODE becomes very simple

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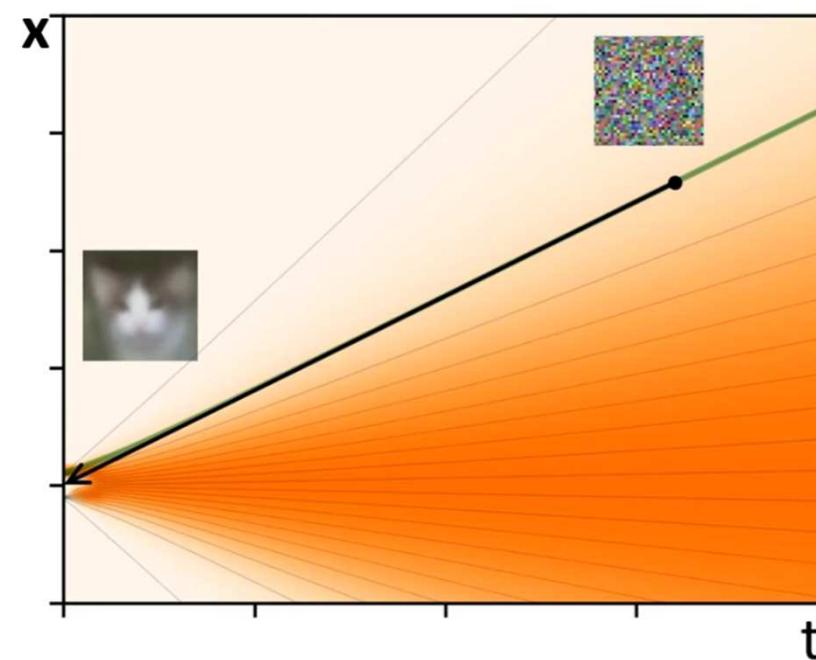
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Noise Schedule $\sigma(t)$



This schedule allows us to take long steps

Scaling Schedule $s(t)$



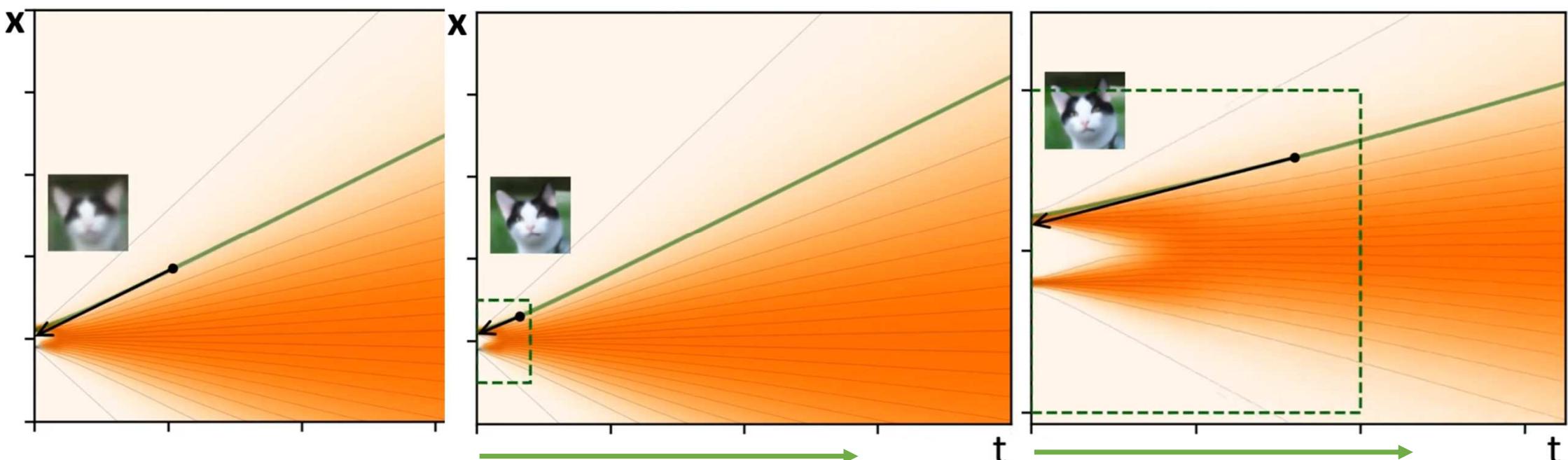
If I take a step directly to time zero, then with only these schedules, the tangent is pointing directly to the denoise output.

We advocate the
“linear” schedule
(same as DDIM):

$$\begin{aligned}\sigma(t) &= t \\ s(t) &= 1\end{aligned}$$

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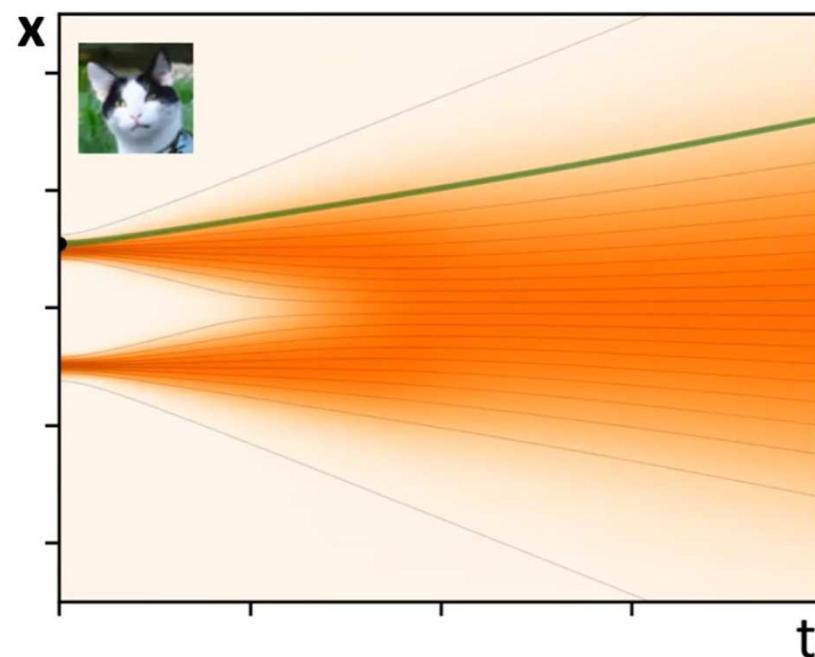
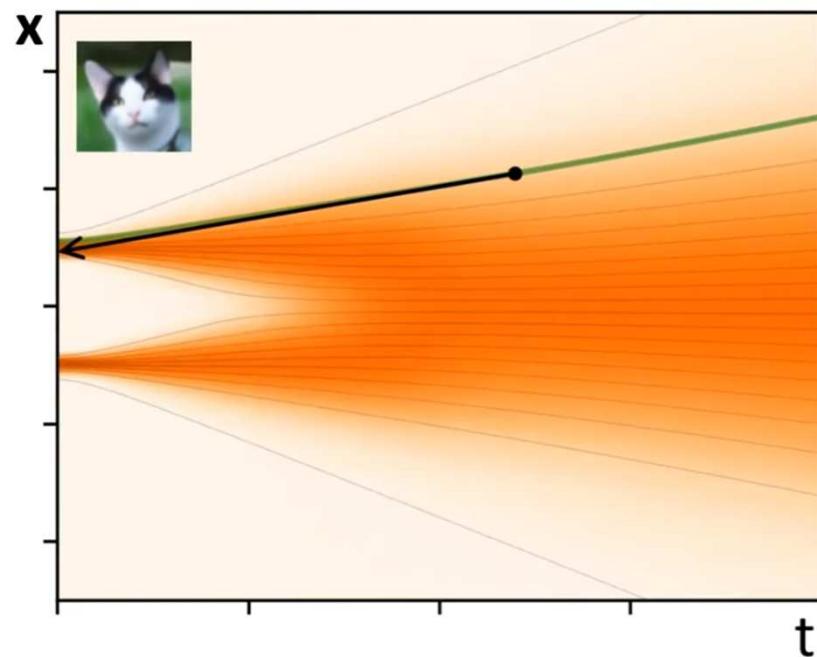


The denoise output changes only very slowly during the sampling process.

Mean that the direction you are going to doesn't change almost at all
So it means you can take long bold steps and you can consequently only take a few steps or many fewer steps than with the alternatives.

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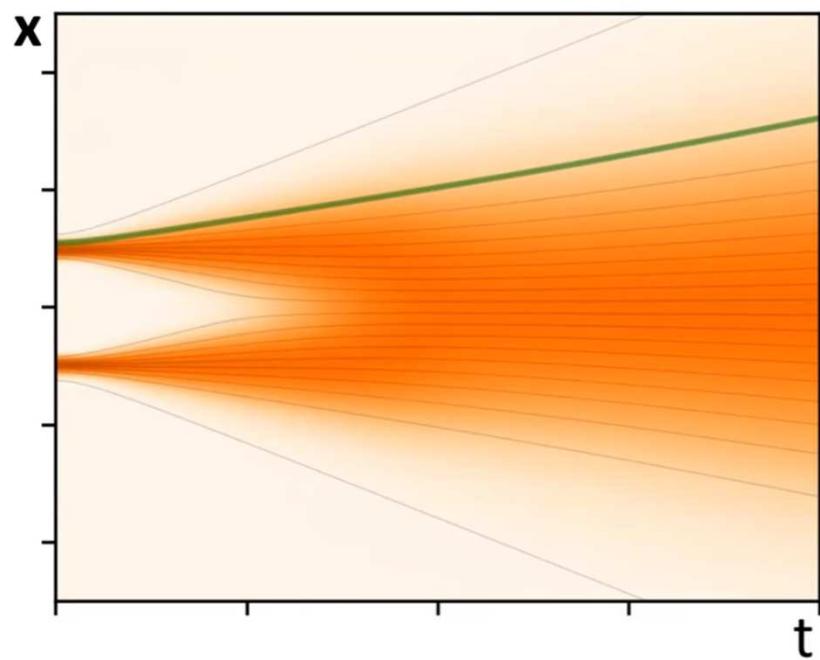
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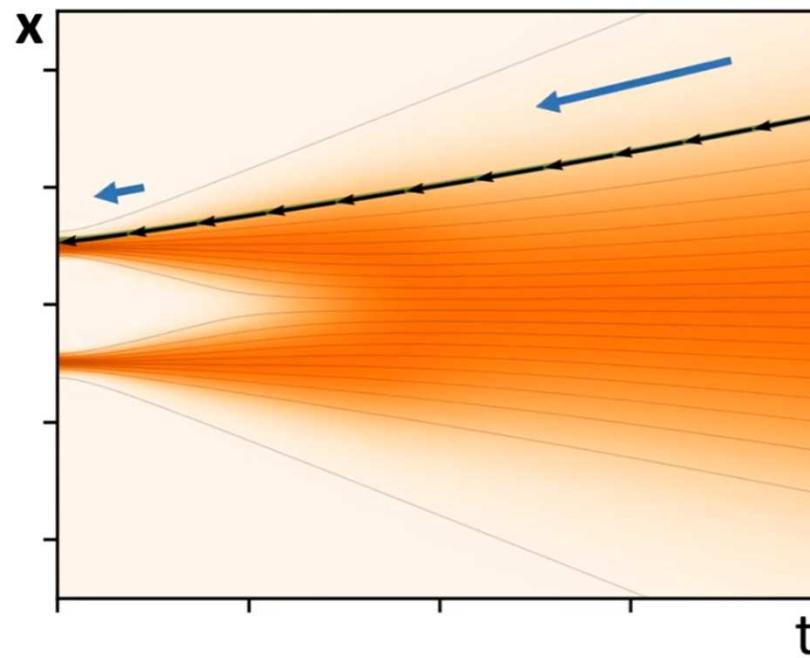
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Varying step length



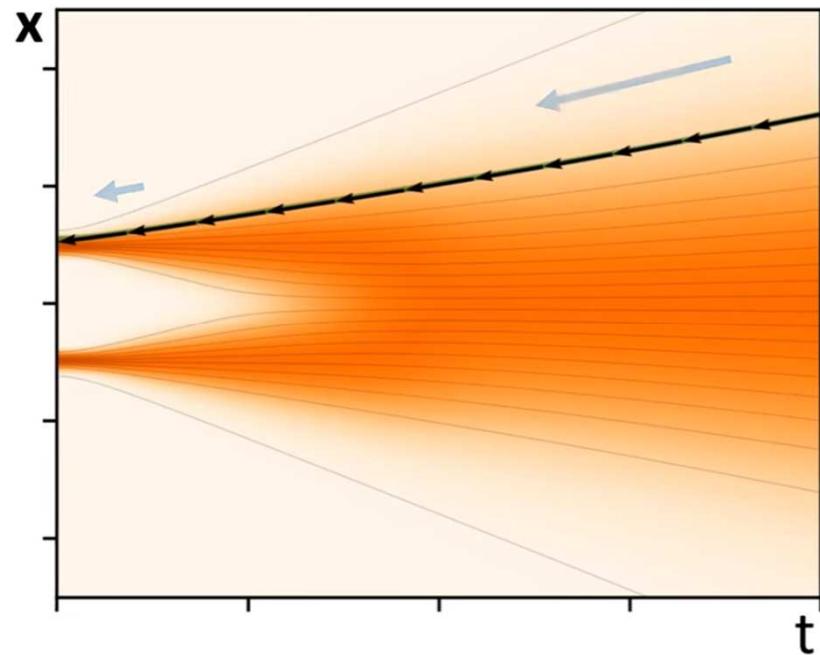
Take different length steps at different stages
of the generation



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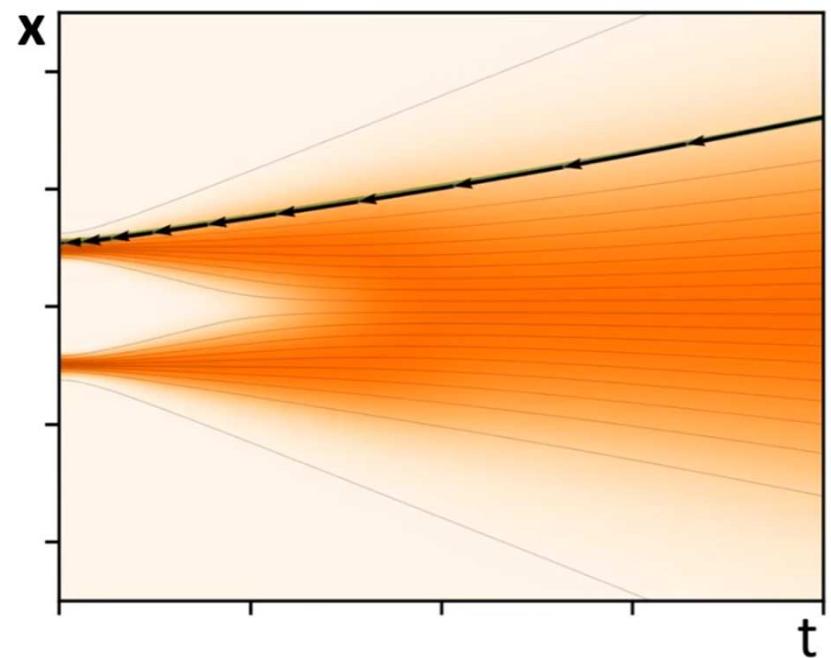
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Varying step length



Varying step length

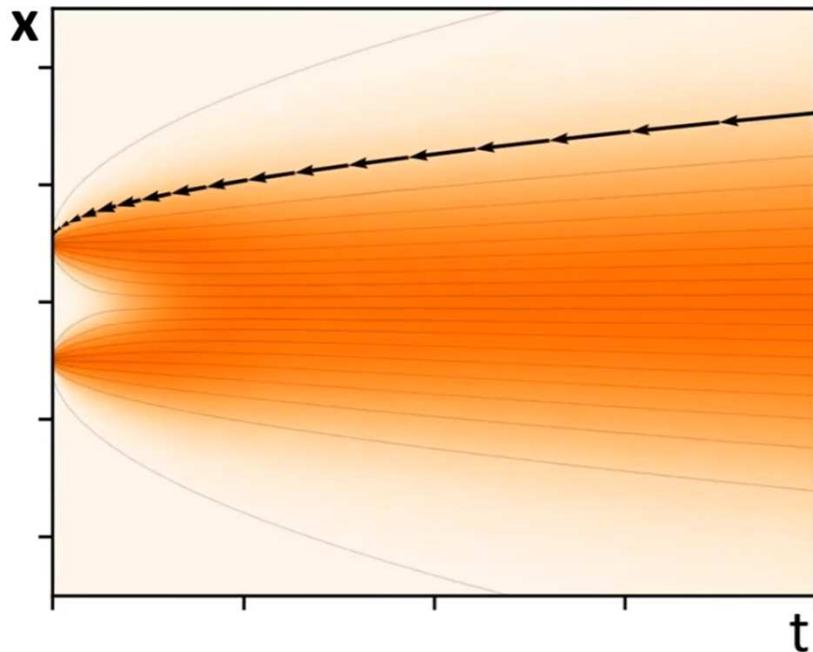
- All previous methods effectively use shorter steps at low noise levels
- A **polynomially growing step length** captures the essence of these schemes. We find the optimal growth rate empirically.



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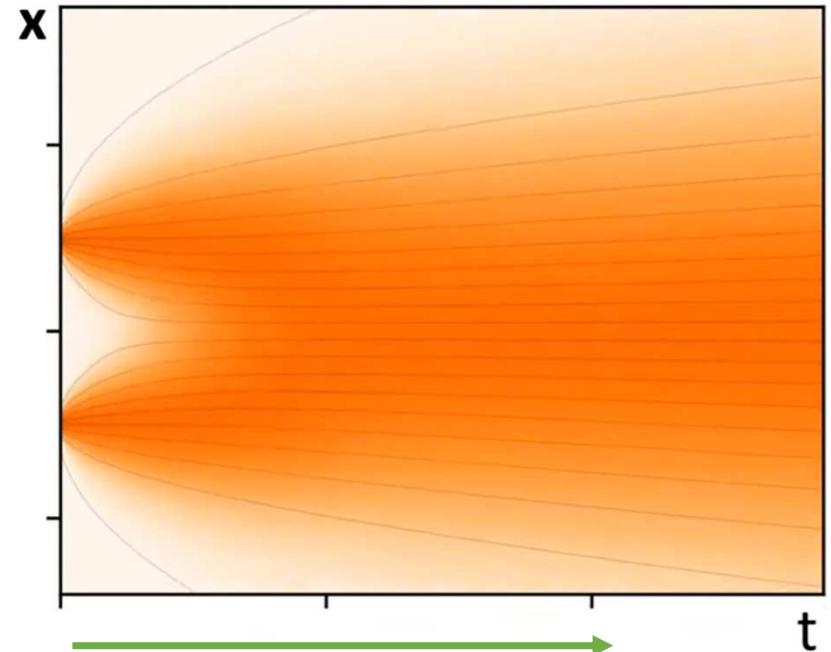
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Higher-order solvers



Higher-order solvers

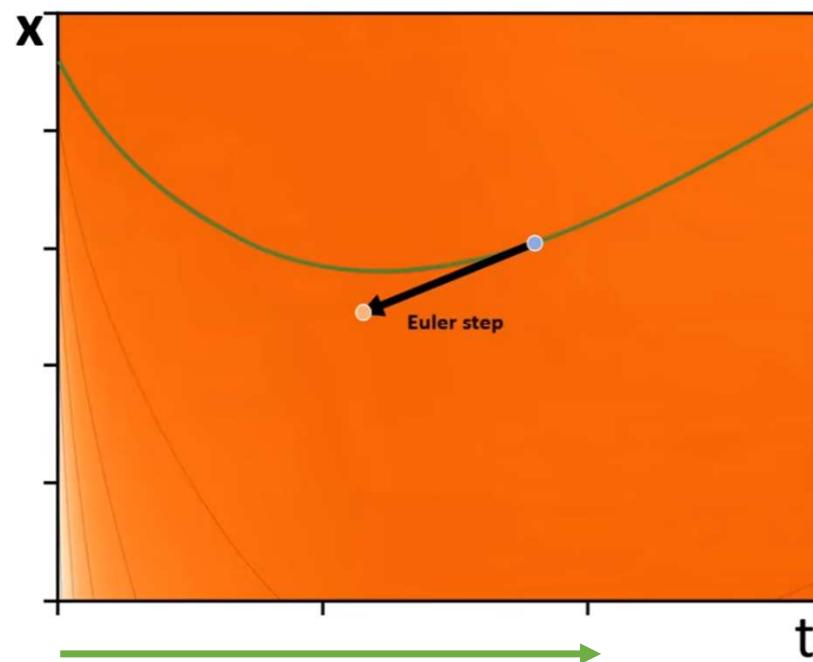
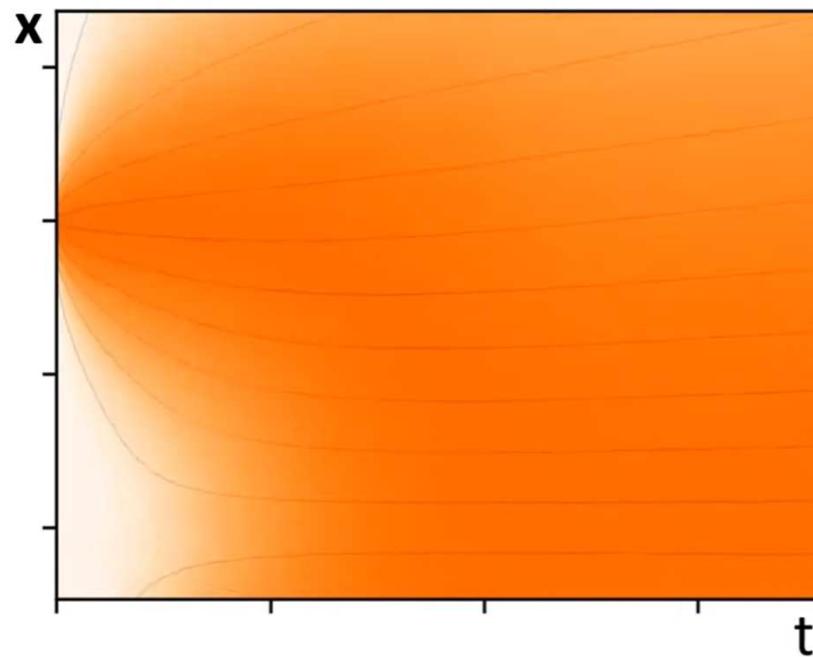
- Clever sub-steps → **higher accuracy**, **higher cost**
- Empirically, 2nd order **Heun method** strikes best balance



ODE framework allows you to do which the Markov chain formulas uses the higher-order solvers, so there is going to be curvature.

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Higher-order solvers

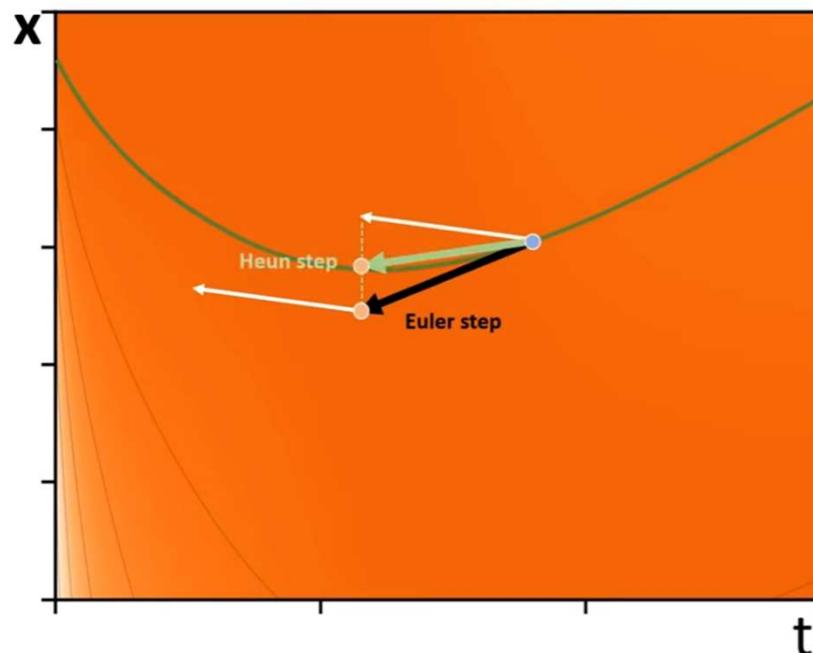
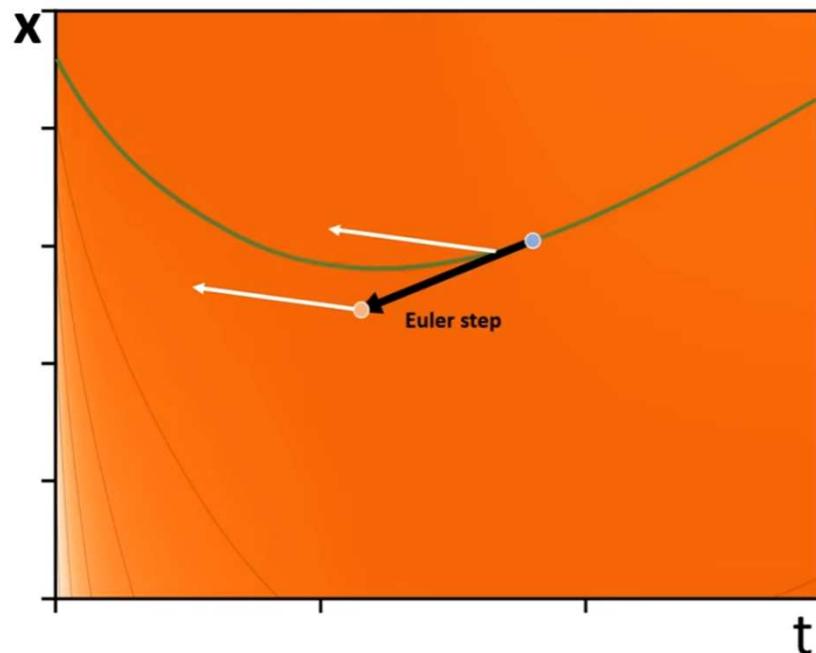
- Clever sub-steps → **higher accuracy, higher cost**
- Empirically, 2nd order **Heun method** strikes best balance

It can be rapid at places, so you can fall off the track if you just follow the tangent by using the Euler step

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2nd order Heun step



Heun's method : 1) Take the second tentative step and move it back to where you started from, 2) Take average of that and the initial one

Strike the best balance between these higher-order methods

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	VP	VE	iDDPM	+ DDIM	Ours
Sampling					
ODE solver	Euler	Euler	Euler		2^{nd} order Heun
Time steps	$t_{i < N}$	$1 + \frac{i}{N-1}(\epsilon_s - 1)$	$\sigma_{\max}^2 (\sigma_{\min}^2 / \sigma_{\max}^2)^{\frac{i}{N-1}}$	$u_{\lfloor j_0 + \frac{M-1-j_0}{N-1} i + \frac{1}{2} \rfloor}, \text{ where } u_M = 0$ $u_{j-1} = \sqrt{\frac{u_j^2 + 1}{\max(\bar{\alpha}_{j-1}/\bar{\alpha}_j, C_1)} - 1}$	$(\sigma_{\max}^{\frac{1}{\rho}} + \frac{i}{N-1}(\sigma_{\min}^{\frac{1}{\rho}} - \sigma_{\max}^{\frac{1}{\rho}}))^{\rho}$
Schedule	$\sigma(t)$	$\sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t} - 1}$	\sqrt{t}	t	t
Scaling	$s(t)$	$1 / \sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t}}$	1	1	1

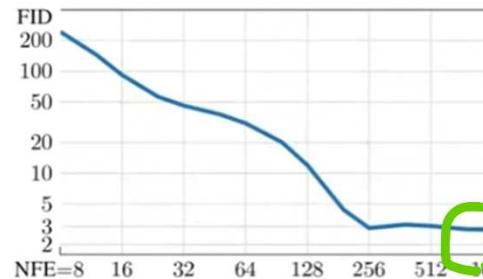
Network and preconditioning

Output scaling $c_{\text{out}}(\sigma)$

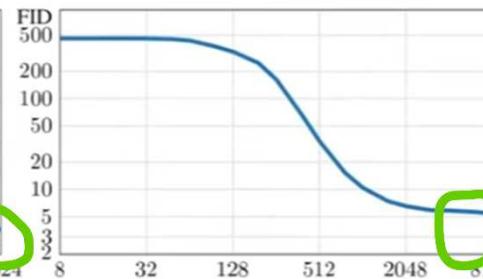
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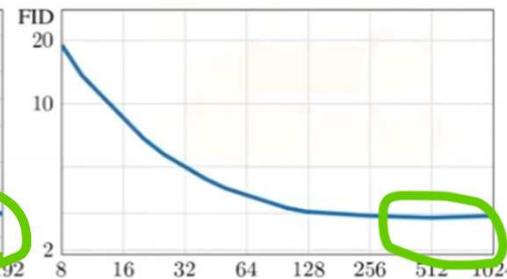
Evaluation of discretization & solver



(a) Uncond. CIFAR-10, VP ODE



(b) Uncond. CIFAR-10, VE ODE



(c) Class-cond. ImageNet-64, DDIM

Need to take something like a hundreds or even thousands of steps to get kind of saturated quality and to get the best quality that model gives you



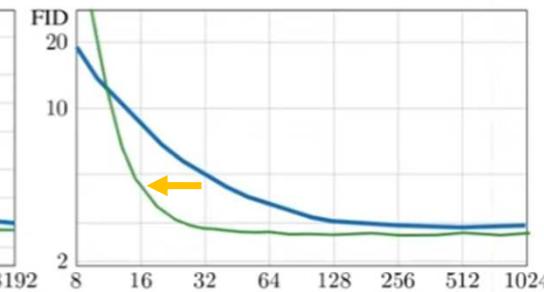
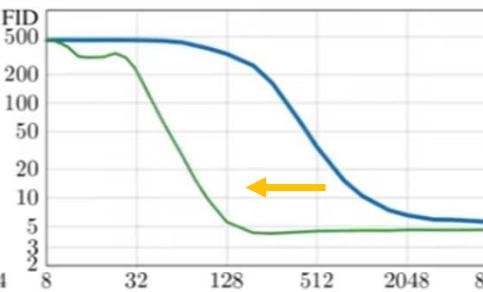
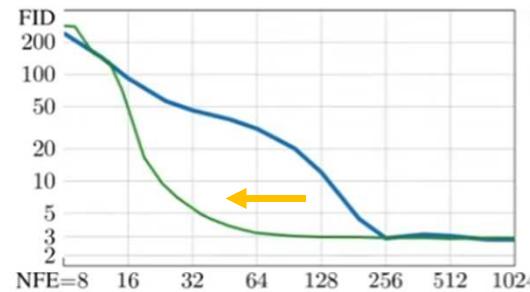
— Original sampler

NFE (the number of neural function evaluations) : Forward pass 중에 전체 모델 파라미터가 몇번이나 계산되었는가를 의미하는 지표

Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Evaluation of discretization & solver



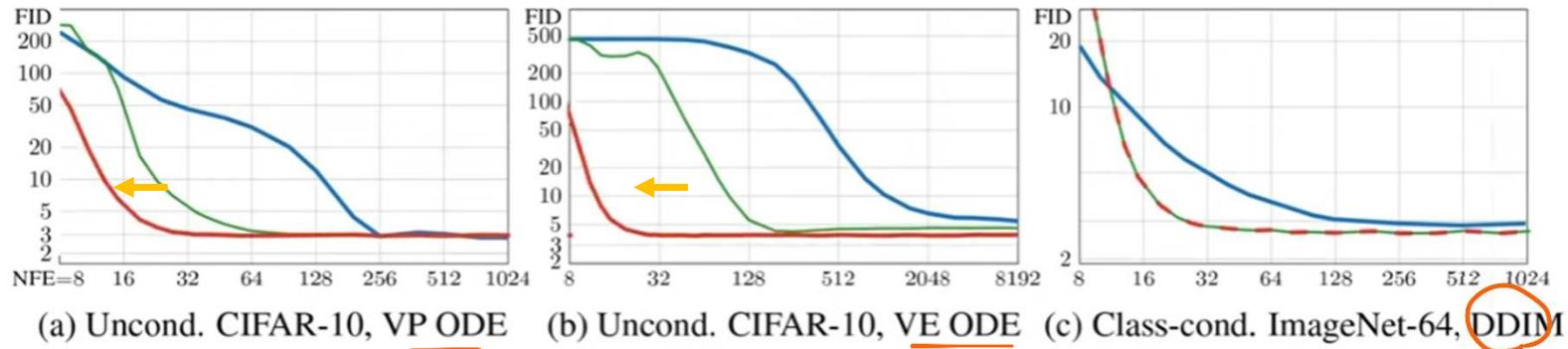
- Original sampler
- + Heun & our $\{t_i\}$

Heun & Our discretization schedule : Go from hundreds to dozens of evaluations

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Evaluation of schedule

Noise schedule and Scaling schedule

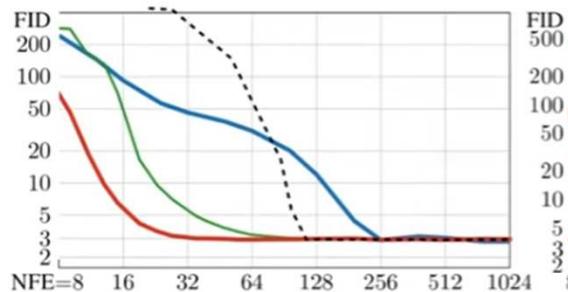


Further improves the results by a large amount except in the DDIM which was already using those schedules

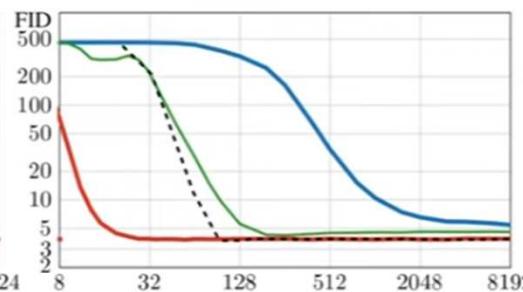
- Original sampler
- + Heun & our $\{t_i\}$
- + Our $\sigma(t)$ & $s(t)$

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

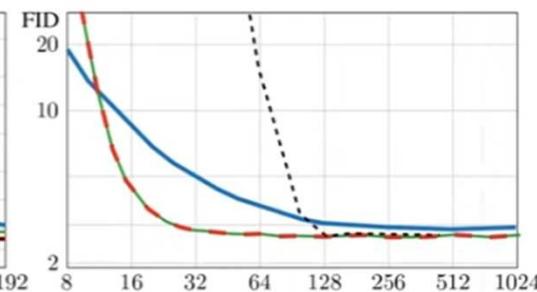
Evaluation of schedule



(a) Uncond. CIFAR-10, VP ODE



(b) Uncond. CIFAR-10, VE ODE



(c) Class-cond. ImageNet-64, DDIM

- Original sampler
- + Heun & our $\{t_i\}$
- + Our $\sigma(t)$ & $s(t)$
- - - Black-box RK45

Youtube Presentaiton

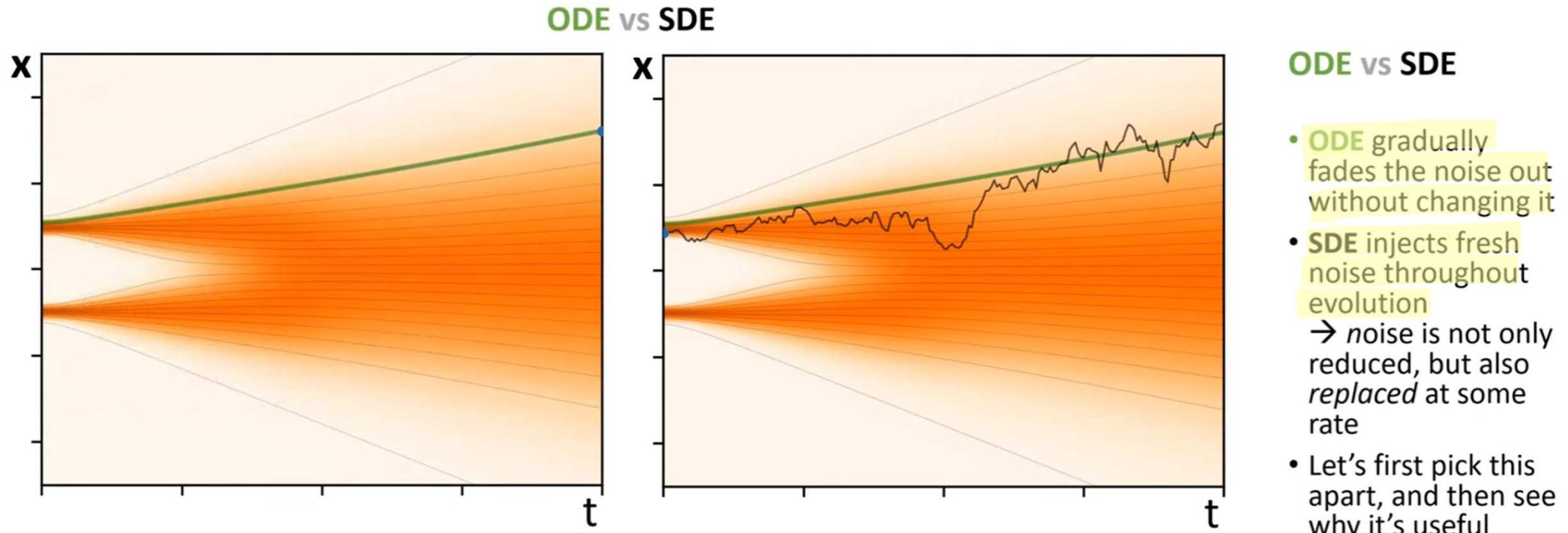
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Outline

- Part I: **Common framework**
 - Identifying the moving parts in existing work
- Part II: **Deterministic sampling**
 - Solving the ODE efficiently
- Part III: **Stochastic sampling**
 - Why SDE's? How to do stochastic stepping?
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 - How to train the CNN used in evaluating a step?

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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



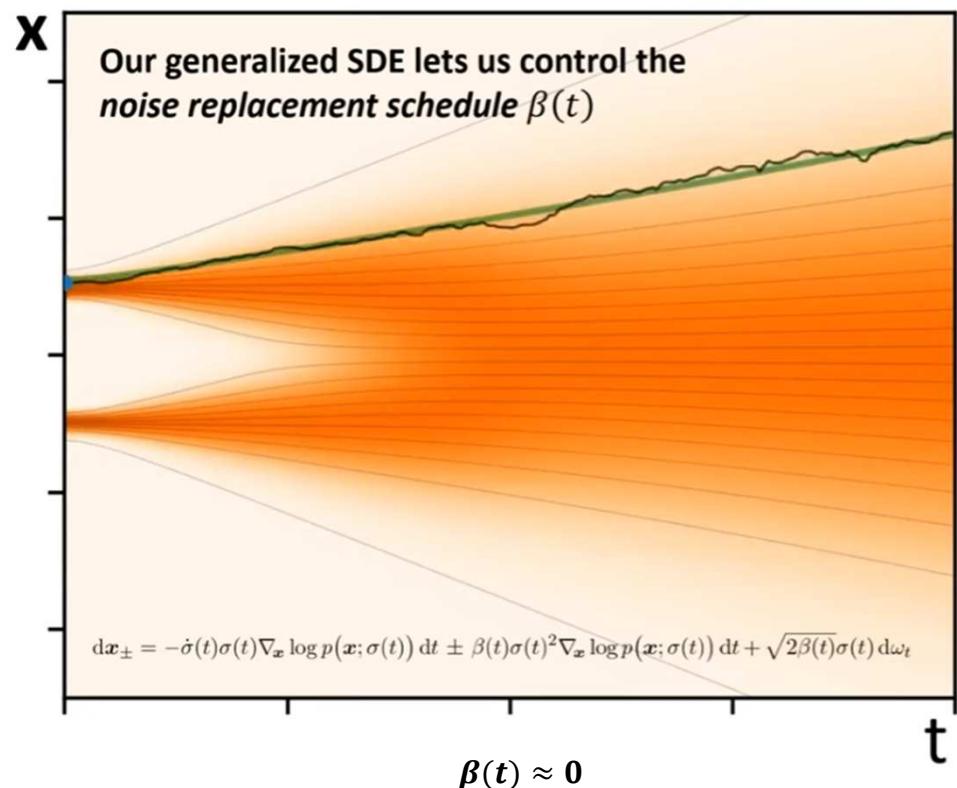
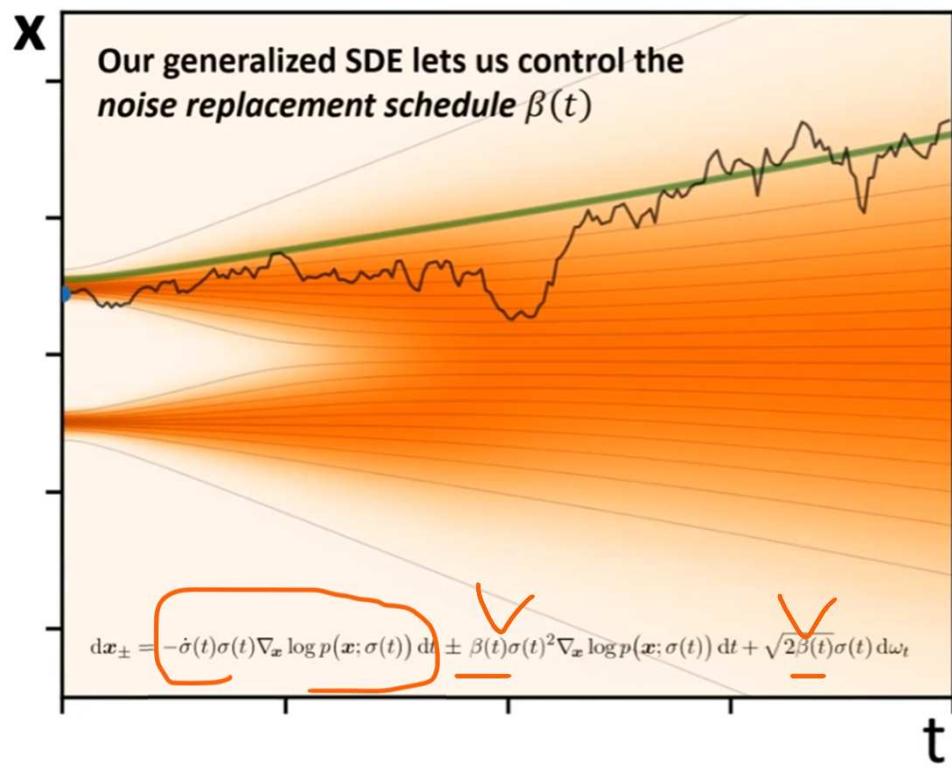
Instead of following these nice smooth flow trajectories, the SDE is sort as some kind of exploration around that baseline so it can be interpreted as replacing the noise and reducing it.

In practice you tend to get better results when you use the SDE instead of the ODE at least in previous works

Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Generalized SDE

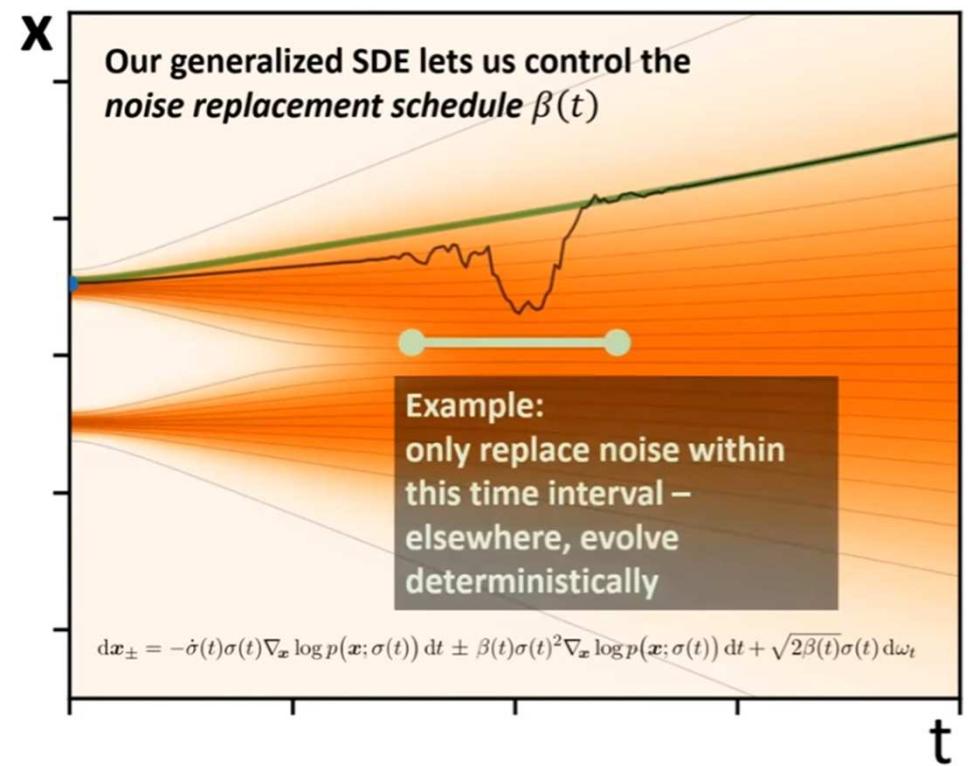
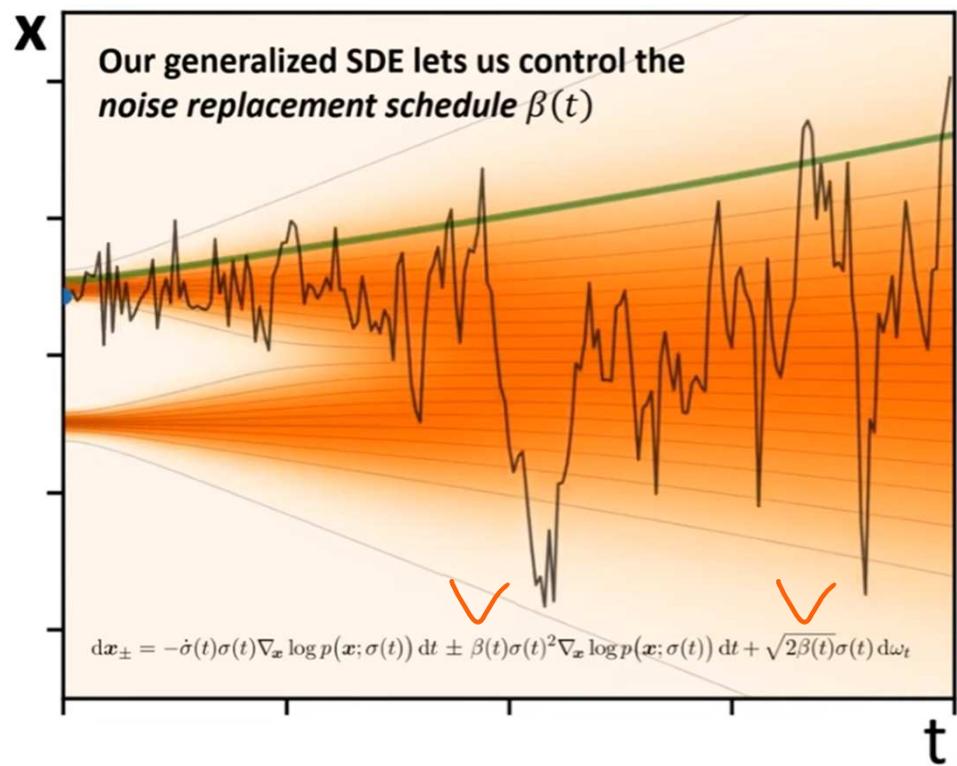


Generalized SDE allows you to specify the strength of this exploration by this
noise replacement schedule $\beta(t)$

Youtube Presentaiton

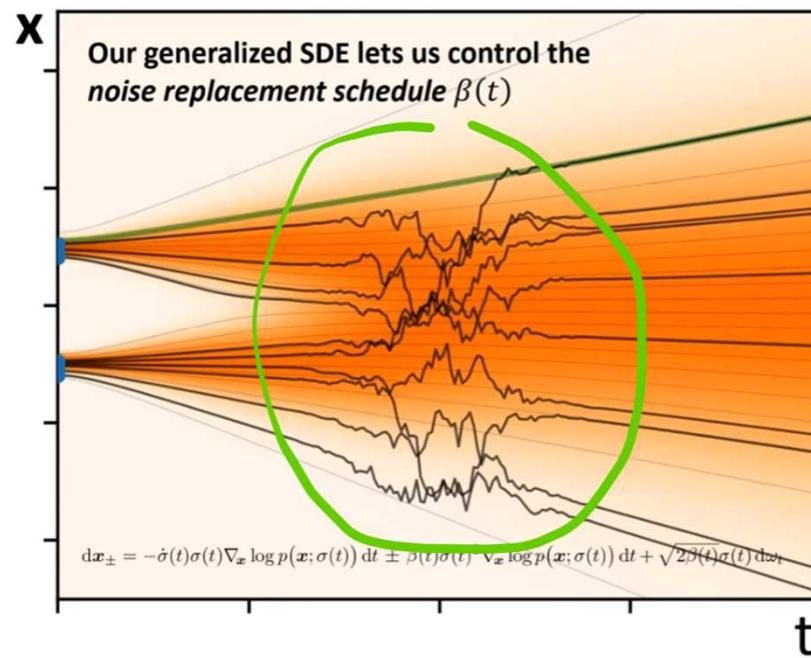
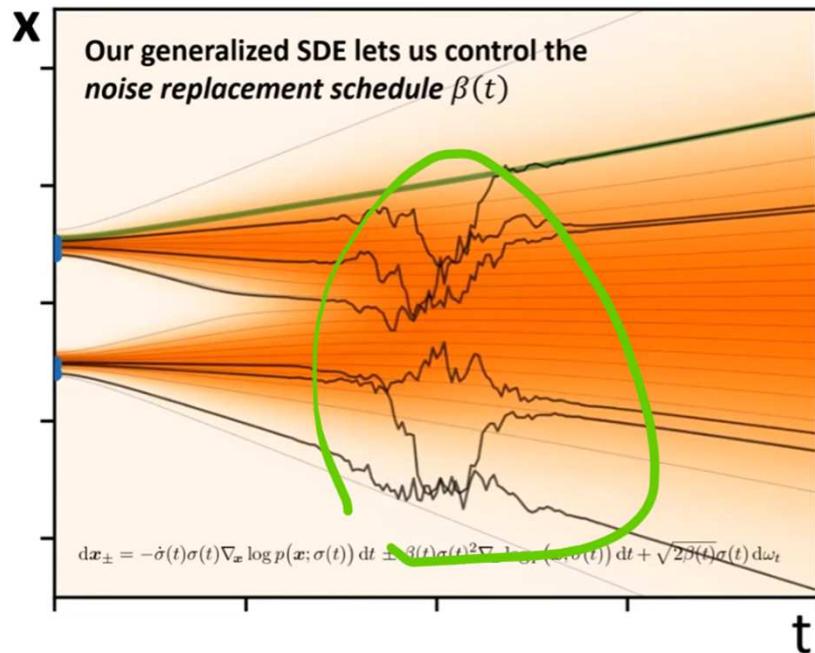
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Generalized SDE



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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



$$dx_{\pm} = \underbrace{-\dot{\sigma}(t)\sigma(t)\nabla_x \log p(x; \sigma(t)) dt}_{\text{probability flow ODE (Eq. I)}} \pm \underbrace{\beta(t)\sigma(t)^2\nabla_x \log p(x; \sigma(t)) dt}_{\text{deterministic noise decay}} + \underbrace{\sqrt{2\beta(t)}\sigma(t) d\omega_t}_{\text{noise injection}}$$

Langevin diffusion SDE

Generalized SDE

- Nice trick, but doesn't it still just go through the same distributions as ODE?
- Empirically, stochasticity does improve results. Why?

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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

$$dx_{\pm} = \underbrace{-\dot{\sigma}(t)\sigma(t)\nabla_x \log p(x; \sigma(t)) dt}_{\text{probability flow ODE}} \pm \underbrace{\beta(t)\sigma(t)^2\nabla_x \log p(x; \sigma(t)) dt}_{\text{deterministic noise decay}} + \underbrace{\sqrt{2\beta(t)}\sigma(t) d\omega_t}_{\text{noise injection}}$$

Langevin diffusion SDE

*Shapes the trajectories,
such that they pass
through the desired
distributions p_t at time t*

Driving towards the distribution and
making it follow the flow lines

*Randomly explores the
distribution p_t at time t , driving
the samples towards it*

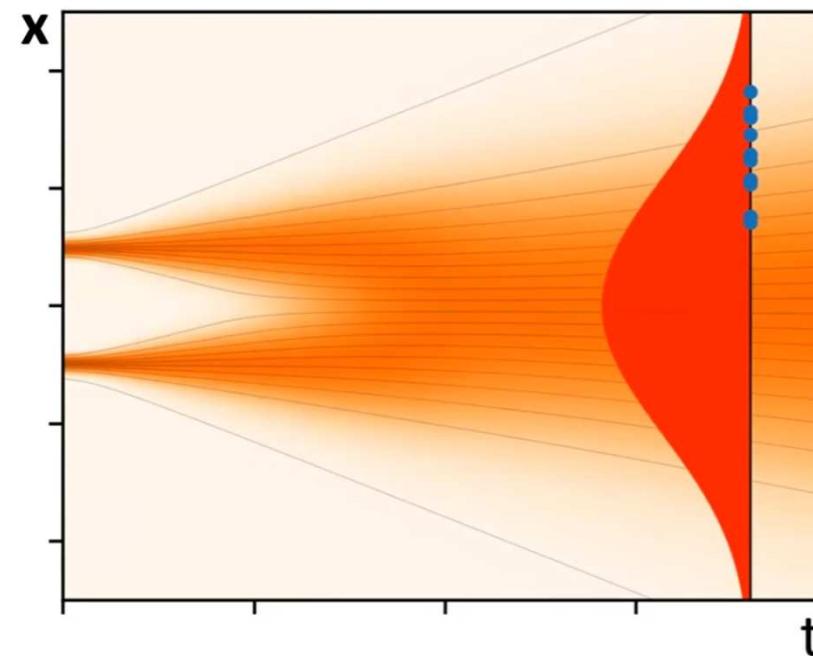
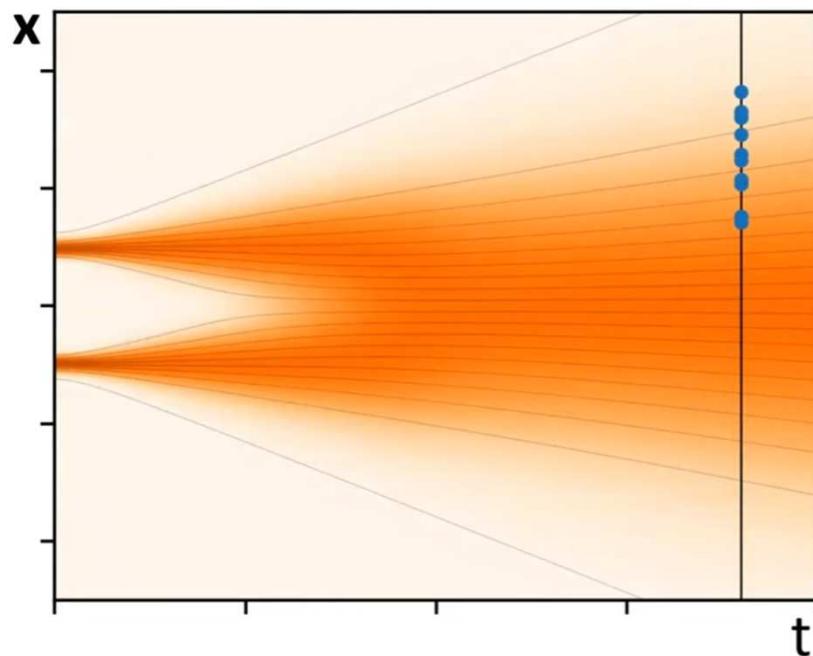
It makes the samples explore the distribution.
**If the samples are not distributed correctly, it will
reduce that error.** Healing property
→ Because we do make errors during the
sampling, it can actively corrects for them

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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

- Why the stochastic is helpful?

Langevin diffusion

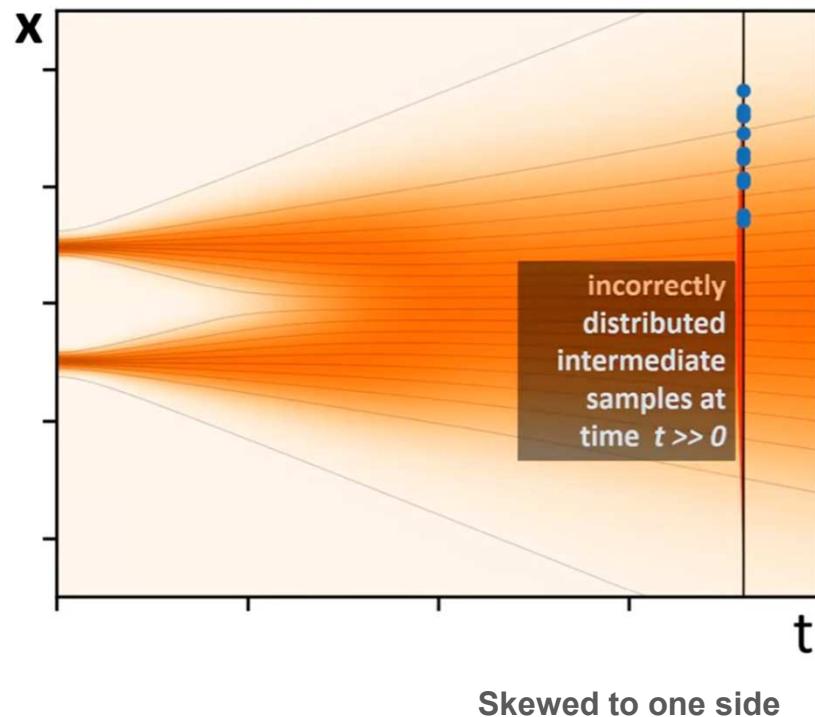


Samples blue dots in **Bad case** (not follow the underlying distribution at all)

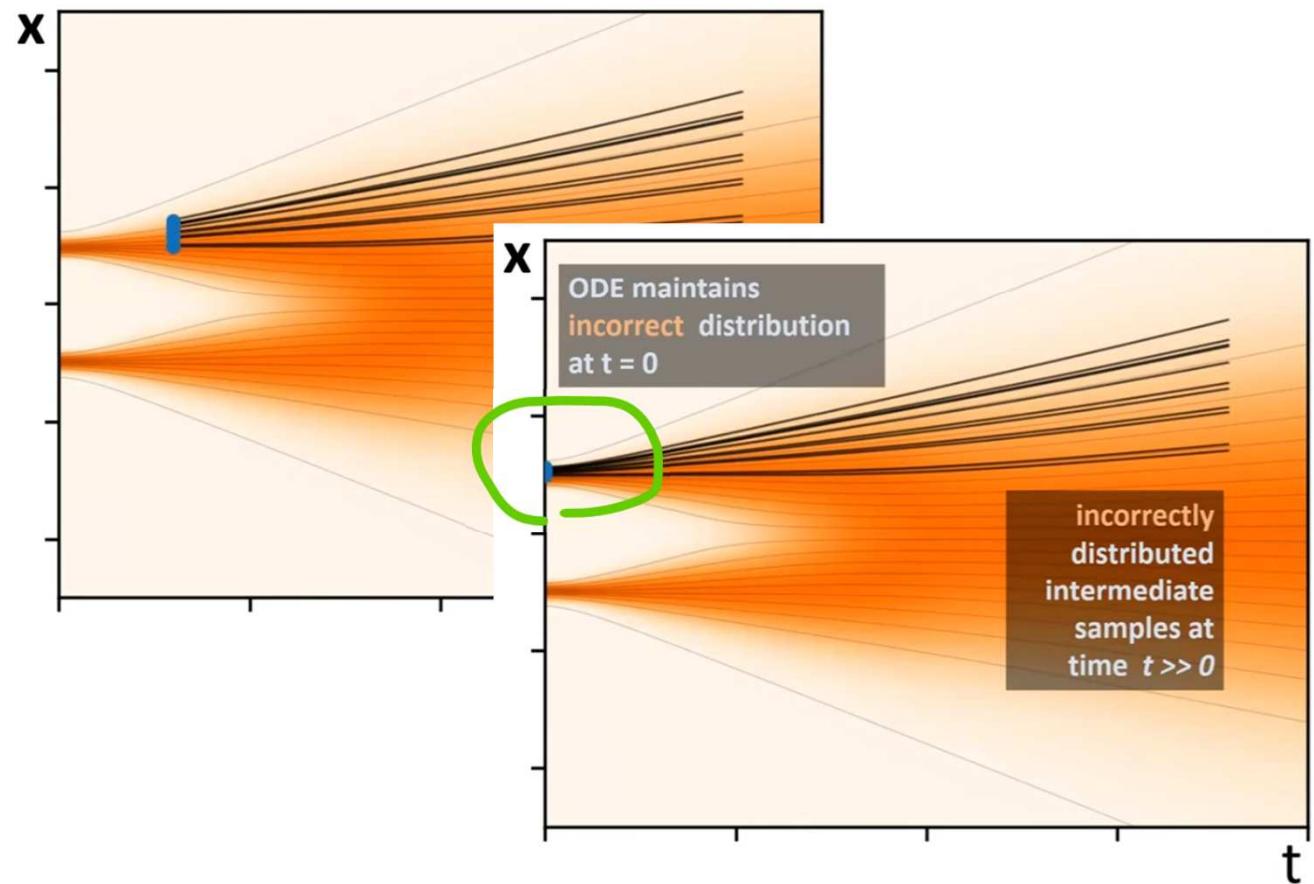
Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

➤ Why the stochastic is helpful?



If keep following ODE, do nothing to correct that skew and completely miss the other base data

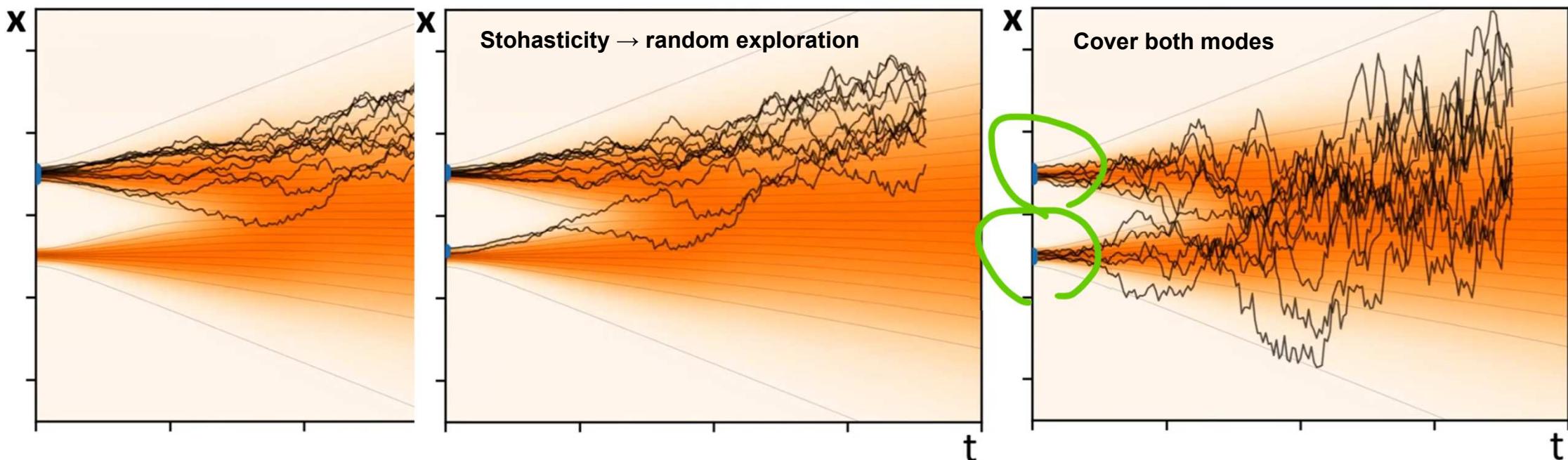


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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

- Why the stochastic is helpful?

Langevin diffusion

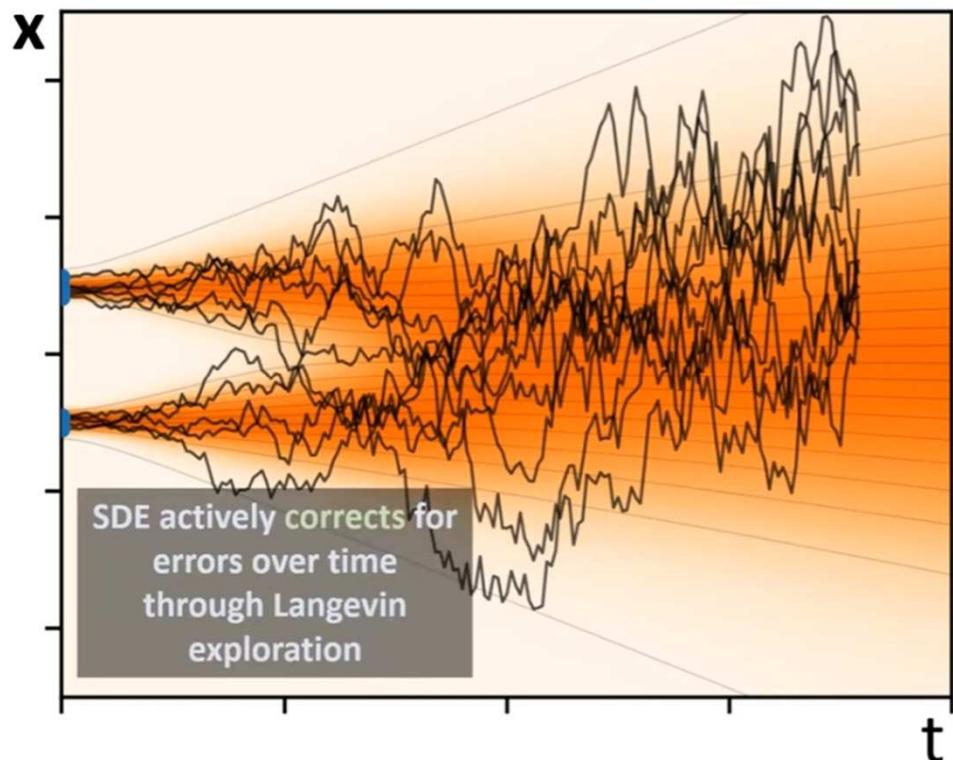


So these samples do this kind of random exploration and gradually forget where they came from and forget the error and initial position.

And now we've covered both modes for example in the generated images on left edge.

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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



Langevin diffusion

- The main benefit of SDE over ODE is the implicit Langevin exploration
- Could we instead simply combine the higher-order ODE solver and Langevin diffusion?

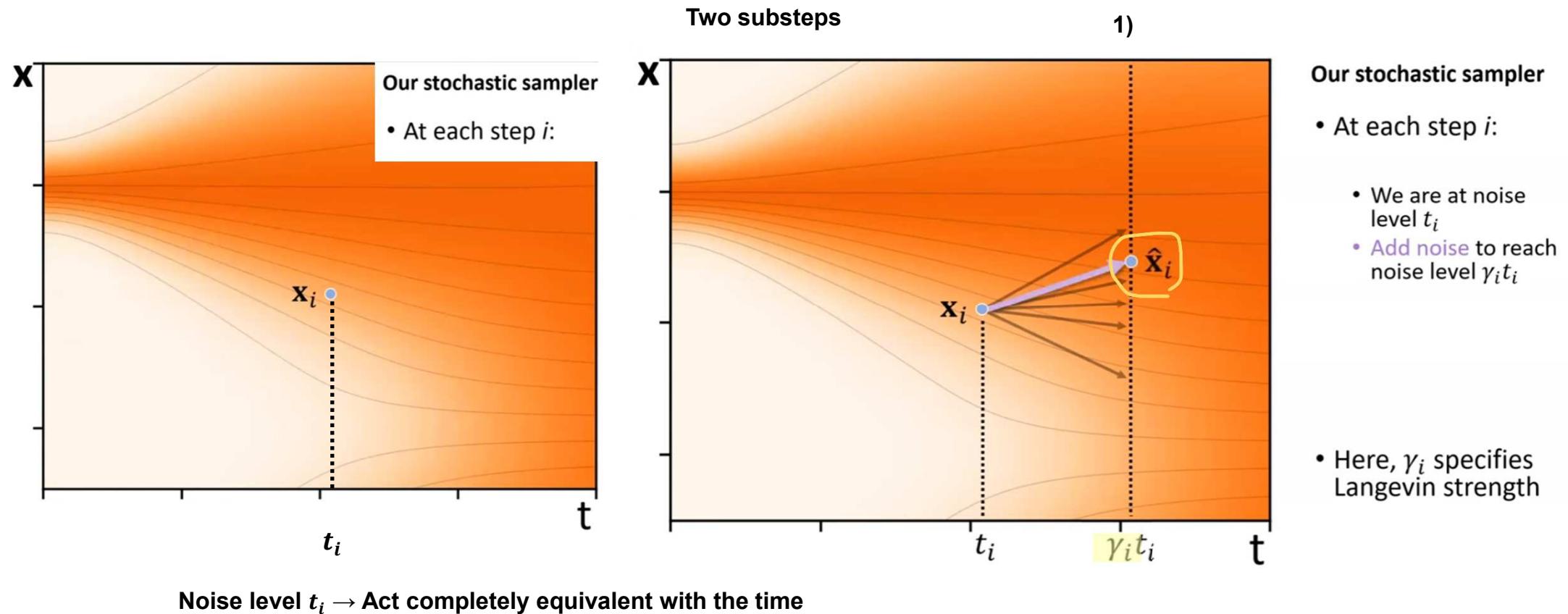
→
Answer

Our stochastic sampler

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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

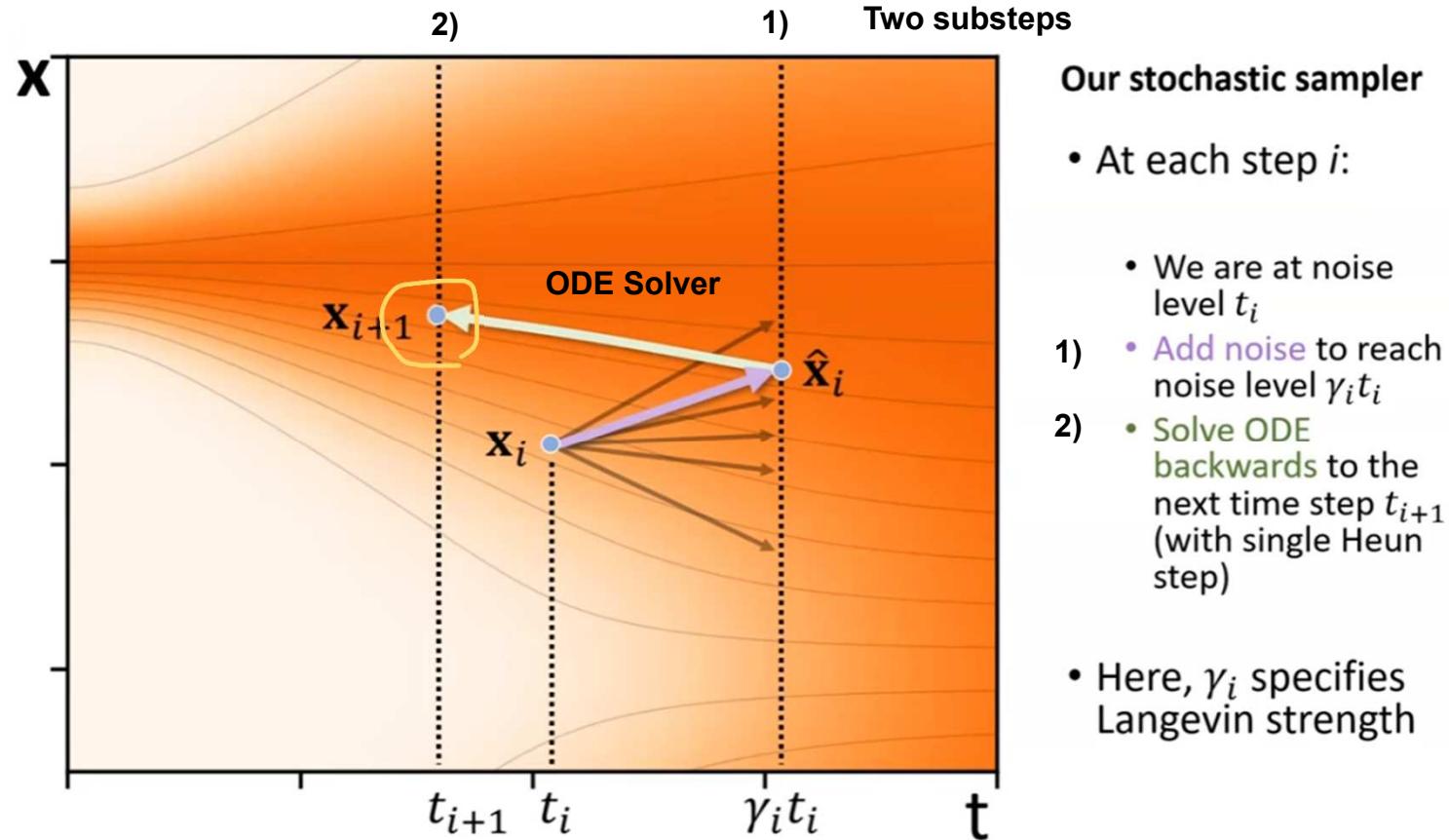
Stochastic Sampler



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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

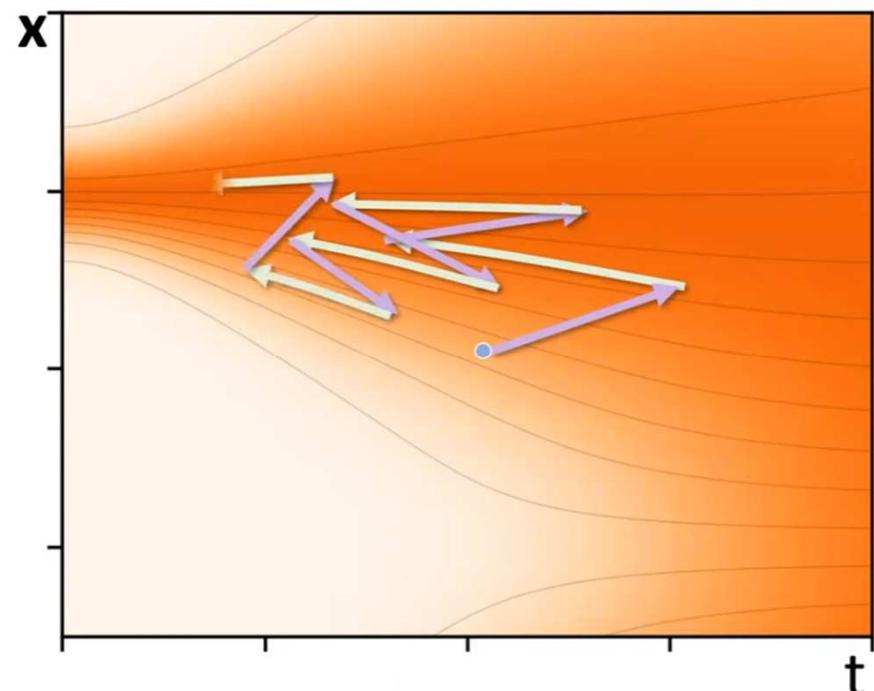
Stochastic Sampler



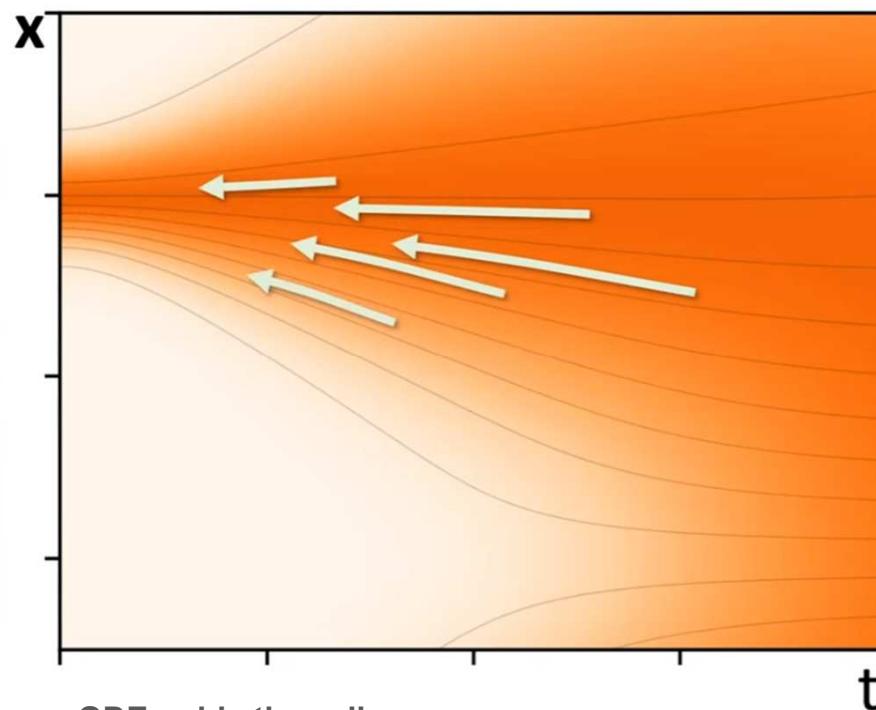
Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Stochastic Sampler



Alternating between the noise addition
and the Heun step as closer to time zero.



ODE guide these lines.
We now have the jittering which corrects errors.

Our stochastic sampler

- At each step i :
 - We are at noise level t_i
 - Add noise to reach noise level $\gamma_i t_i$
 - Solve ODE backwards to the next time step t_{i+1} (with single Heun step)
- Here, γ_i specifies Langevin strength

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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



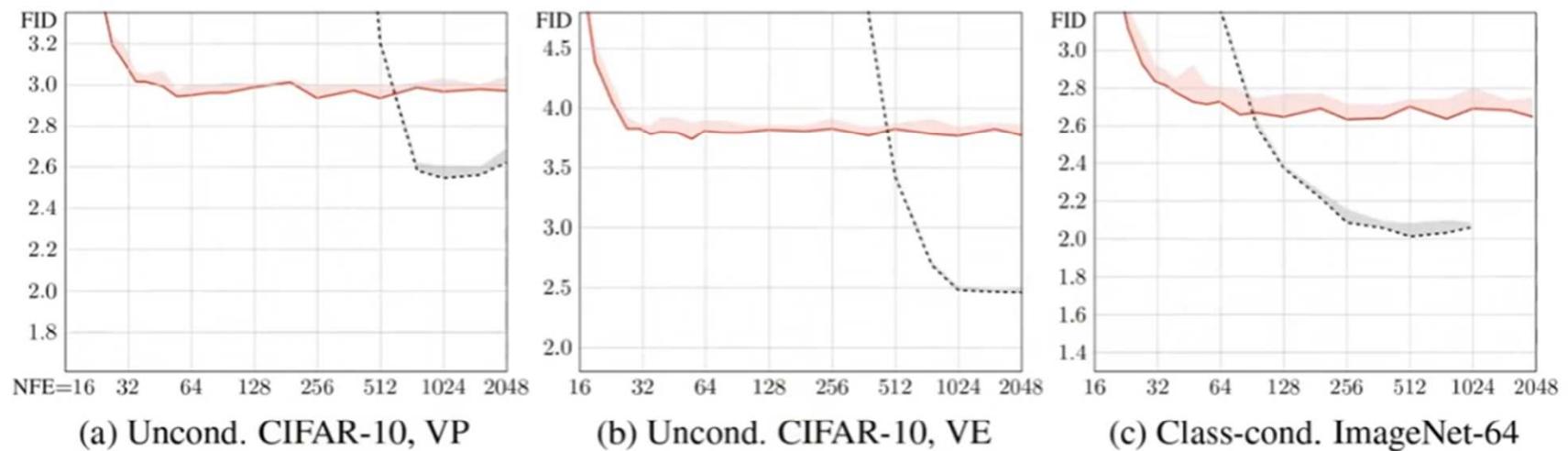
Image: winnifredxoxo at Flickr

Get these errors correct reaction but it's not actually free because the Langevin diffusion is also an approximation of some continuous thing.

Quite delicate balance how much make error
Need to tune the amount of stochasticity on a data set per architectural basis

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Evaluation

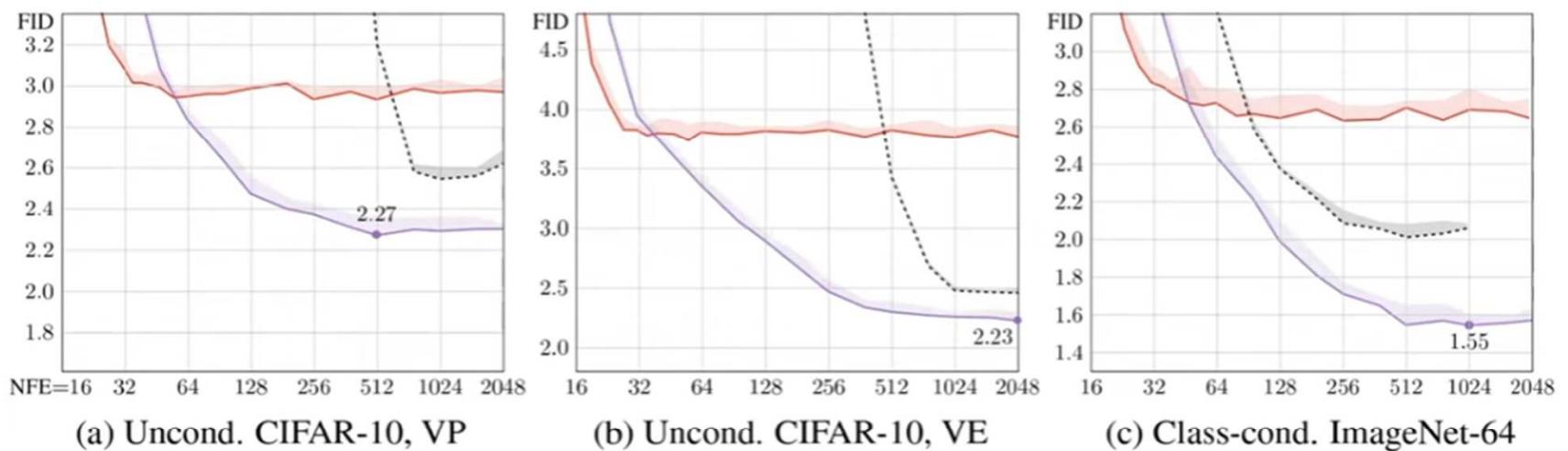


SDE solvers are better but very slow

— Deterministic (ODE)
- - - Original sampler (SDE)

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Evaluation



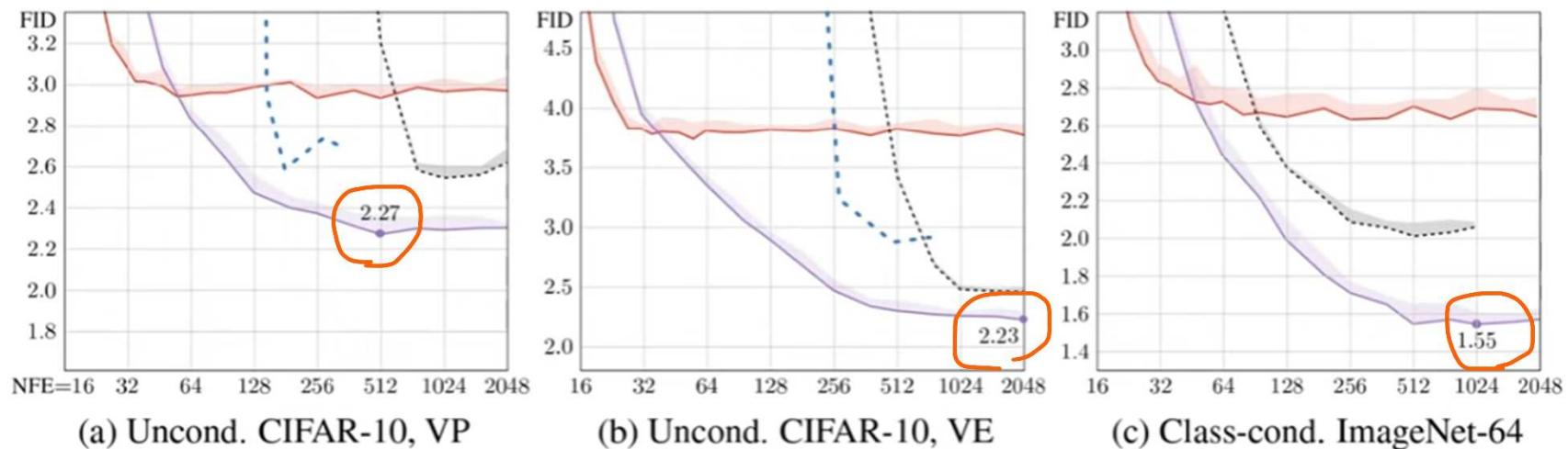
Optimal seetings of SDE solvers : Both much better quality and much faster

- Deterministic
- Original sampler
- Optimal settings

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Evaluation

5.27
from 2.07 to 1.55
(SOTA at the time)



- Deterministic
- ... Original sampler
- Optimal settings
- - - Jolicoeur-Martineau et al. [23]

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Outline

- Part I: Common framework
 - Identifying the moving parts in existing work
- Part II: Deterministic sampling
 - Solving the ODE efficiently
- Part III: Stochastic sampling Summary (정리)
 - Why SDE's? How to do stochastic stepping?
- Part IV: Preconditioning and training
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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Recall two sources of error



- Discretized steps in sampling
 - We studied this with pre-trained networks



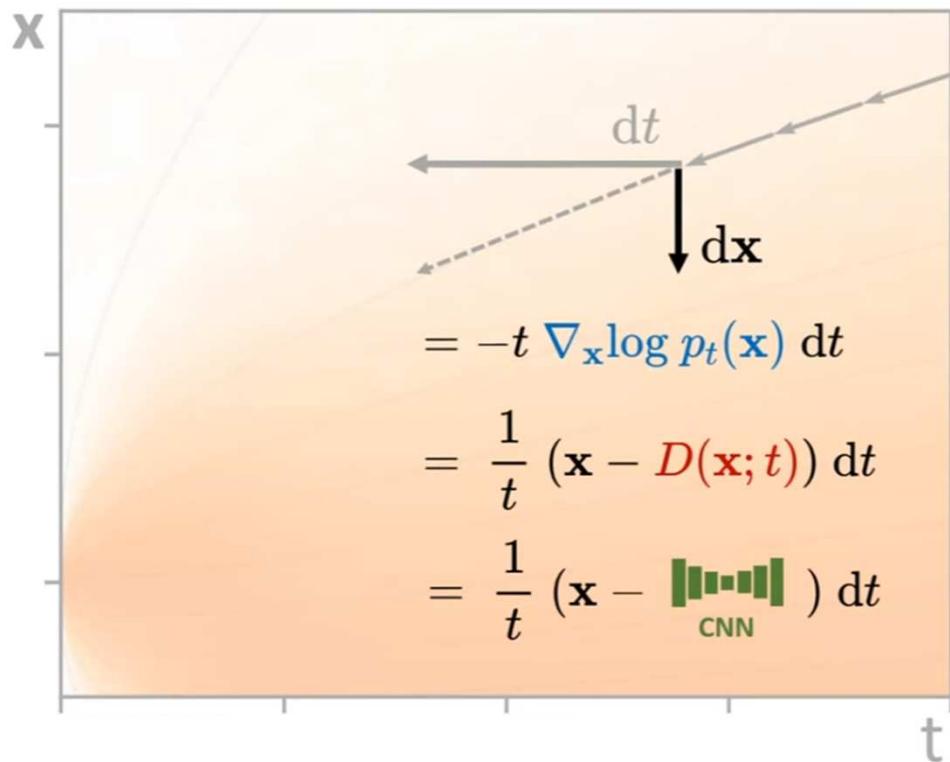
- Inaccurate neural denoiser, a.k.a. score function

Next up:

- Improved network preconditioning (e.g., input and output scales)
- Improved training (loss scaling, and what noise levels to train at?)

- We will not change the layer architecture, etc. (much)

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



Recall...

- ODE step uses the *score function*
- ... which can be computed using a *denoiser*
- ... which we approximate with a neural network

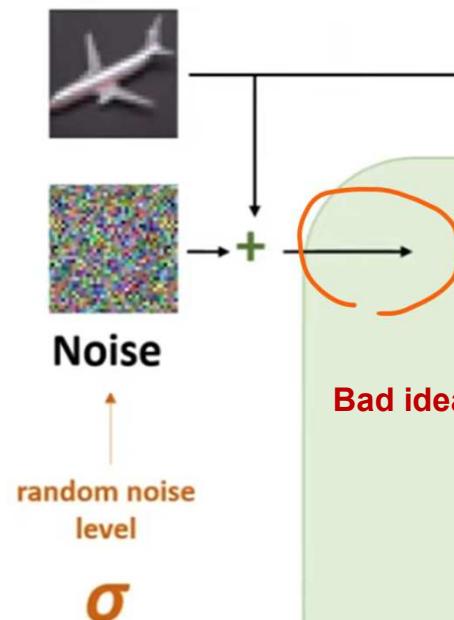
ODE Role Give us the step direction by the **score function**, evaluated using a **Denoiser** which can be approximated using **neural network**

The role of neural networks tells where to go in a single step or what direction you need to go to

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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Training data image



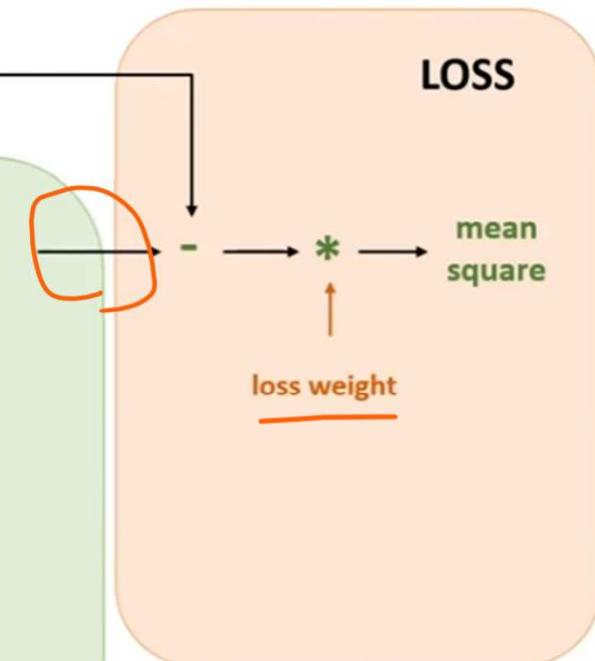
Let's look at Denoiser itself
before we go to the loss weight

Bad idea



DENOISER

Actually a **bad idea** to directly connect the noisy image to the input of the network or to read the denoised image from its output layer.



Denoiser do someting that minimizes the L2 denoising loss

You can do this separately at every noise level,
so can weight this loss according to the noise level

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Preconditioning

- To make things easy for the CNN:
 - (A) Always feed **unit stdev inputs** to networks
 - (B) .. and train with **unit stdev targets**
- Networks make errors. We should
 - (C) **minimize network's contribution** to output of the denoiser
- Our noise levels vary wildly, so this is critical!
 - Should copy just what we know and only fix the remainder we're going to come to that soon.

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Training data image



Noise

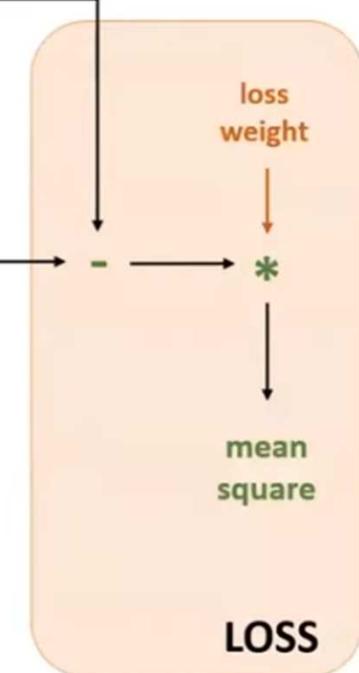
random noise level
 σ

- VE method implement the denoiser
- Learning to predict the noise instead of the signal using CNN layers

Noise prediction

raw
CNN
layers

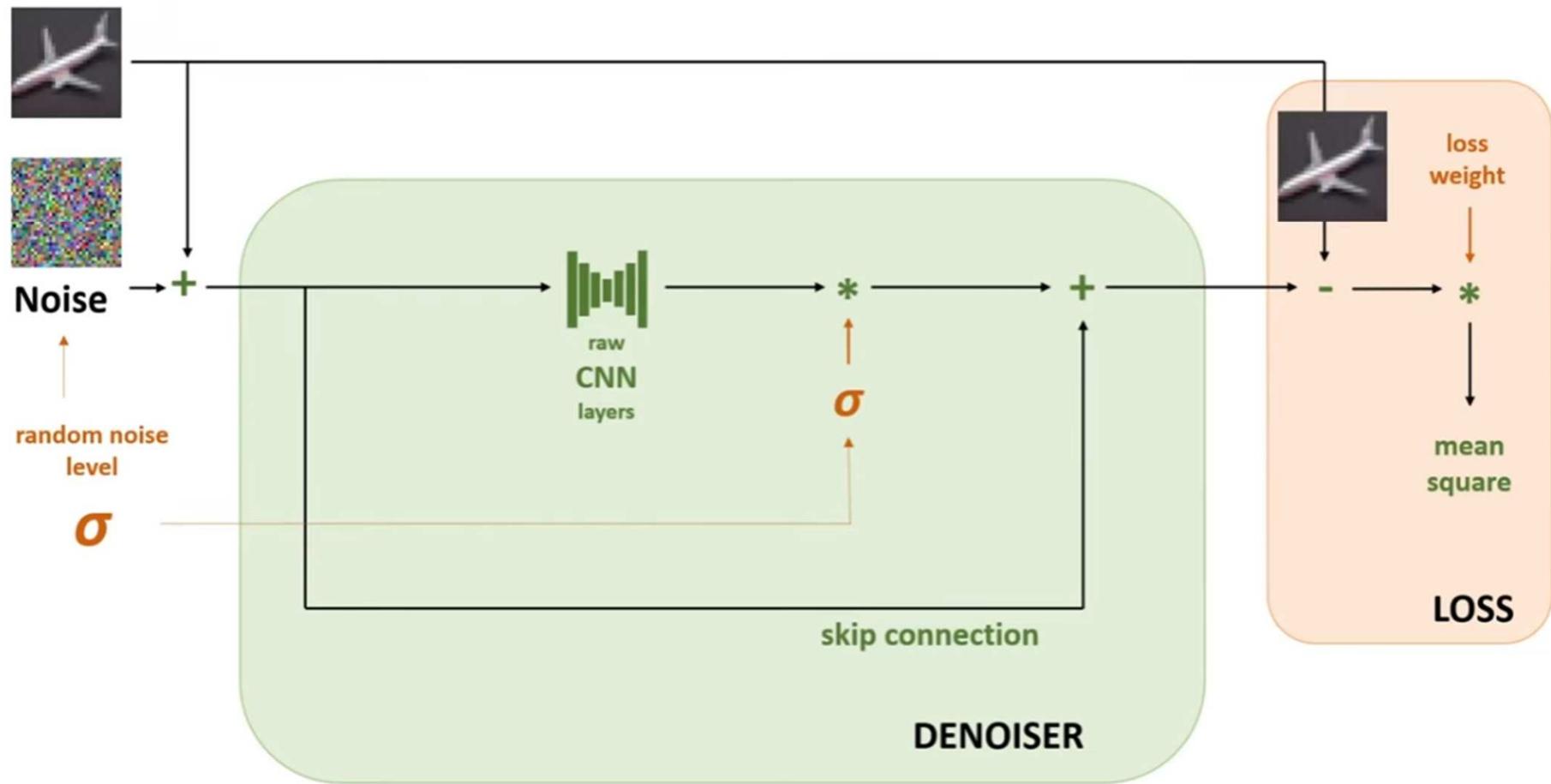
skip connection
DENOISER



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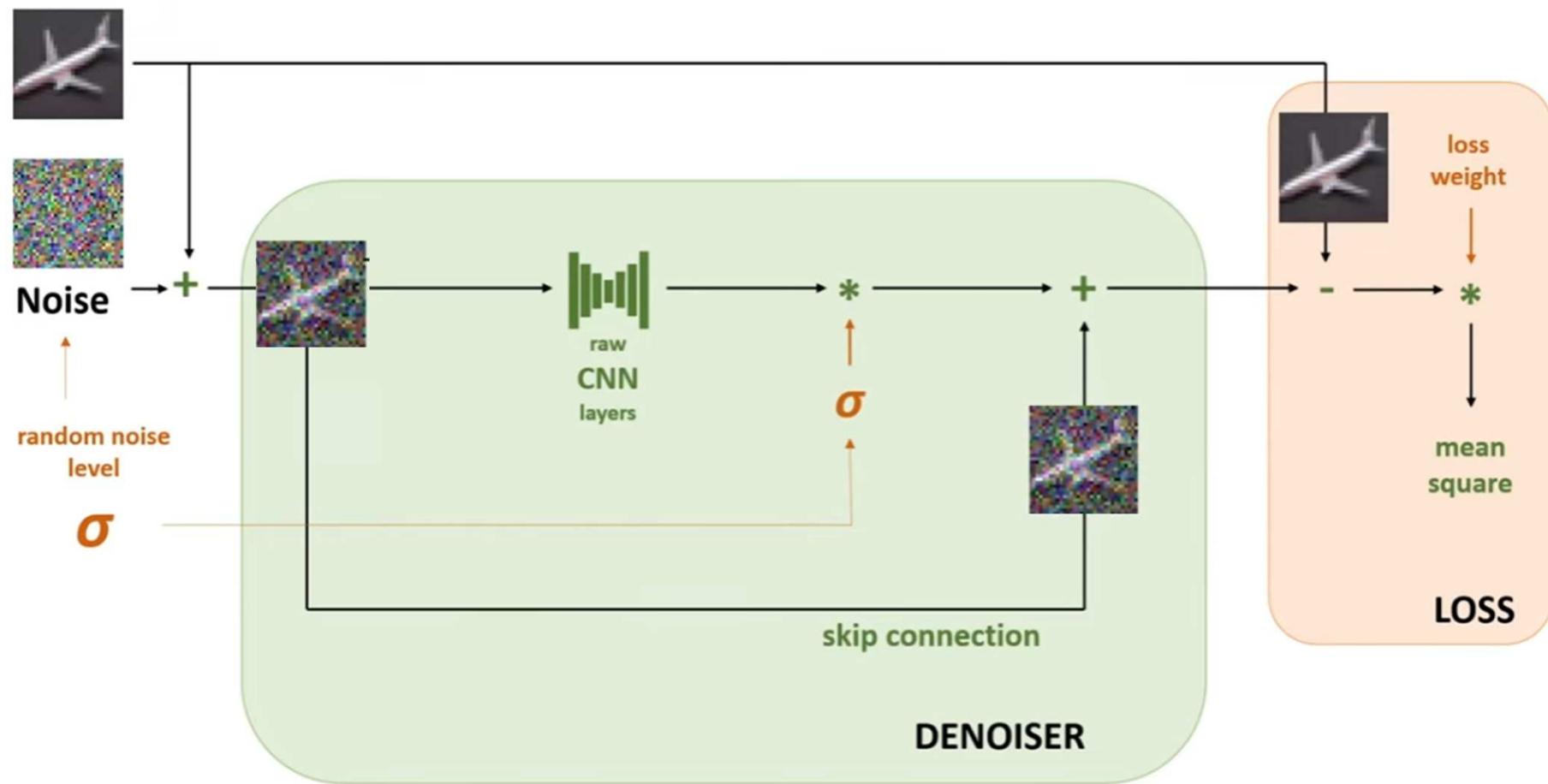
Training data image



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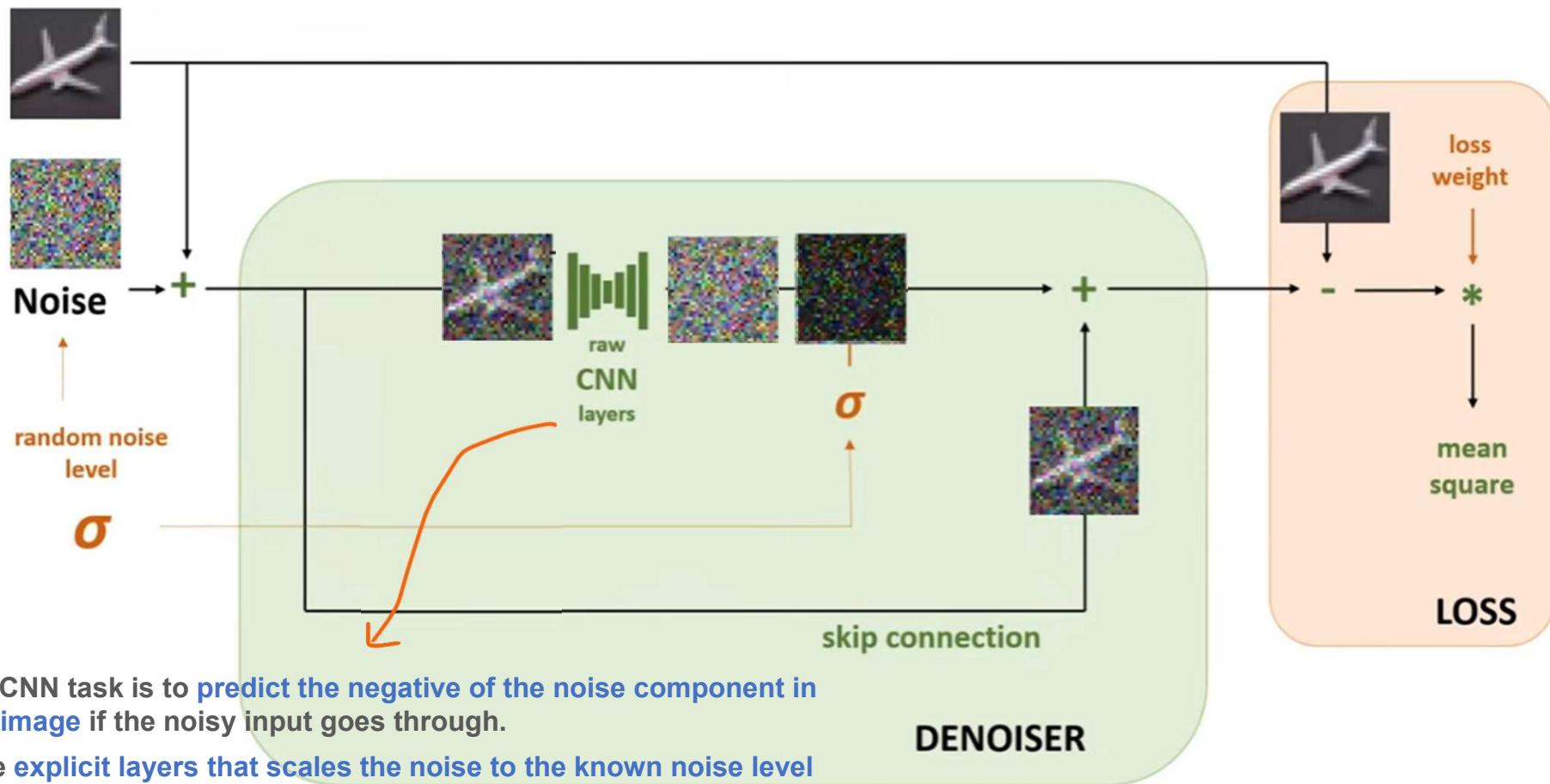
Training data image



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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

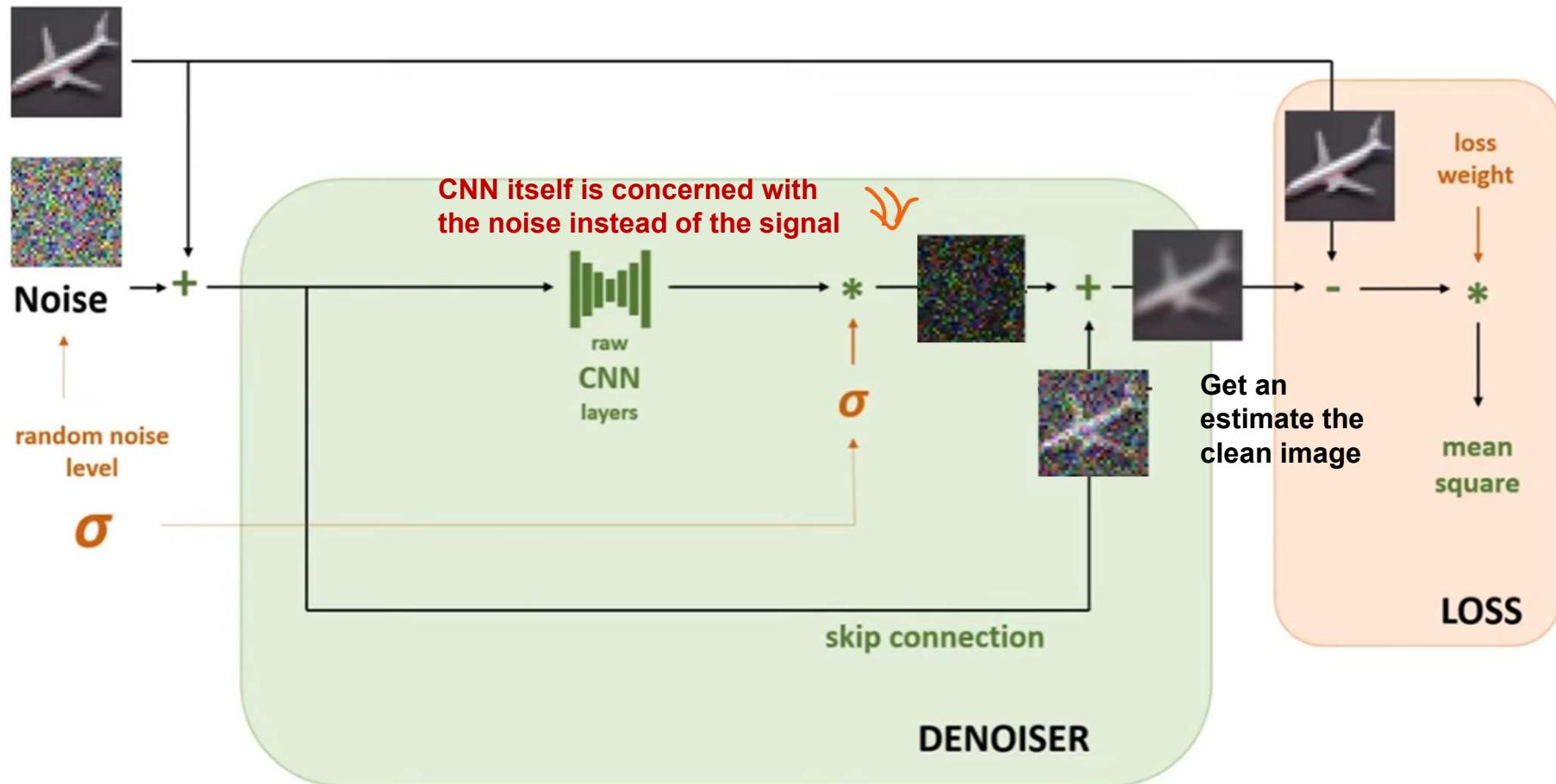
Training data image



Youtube Presentaiton

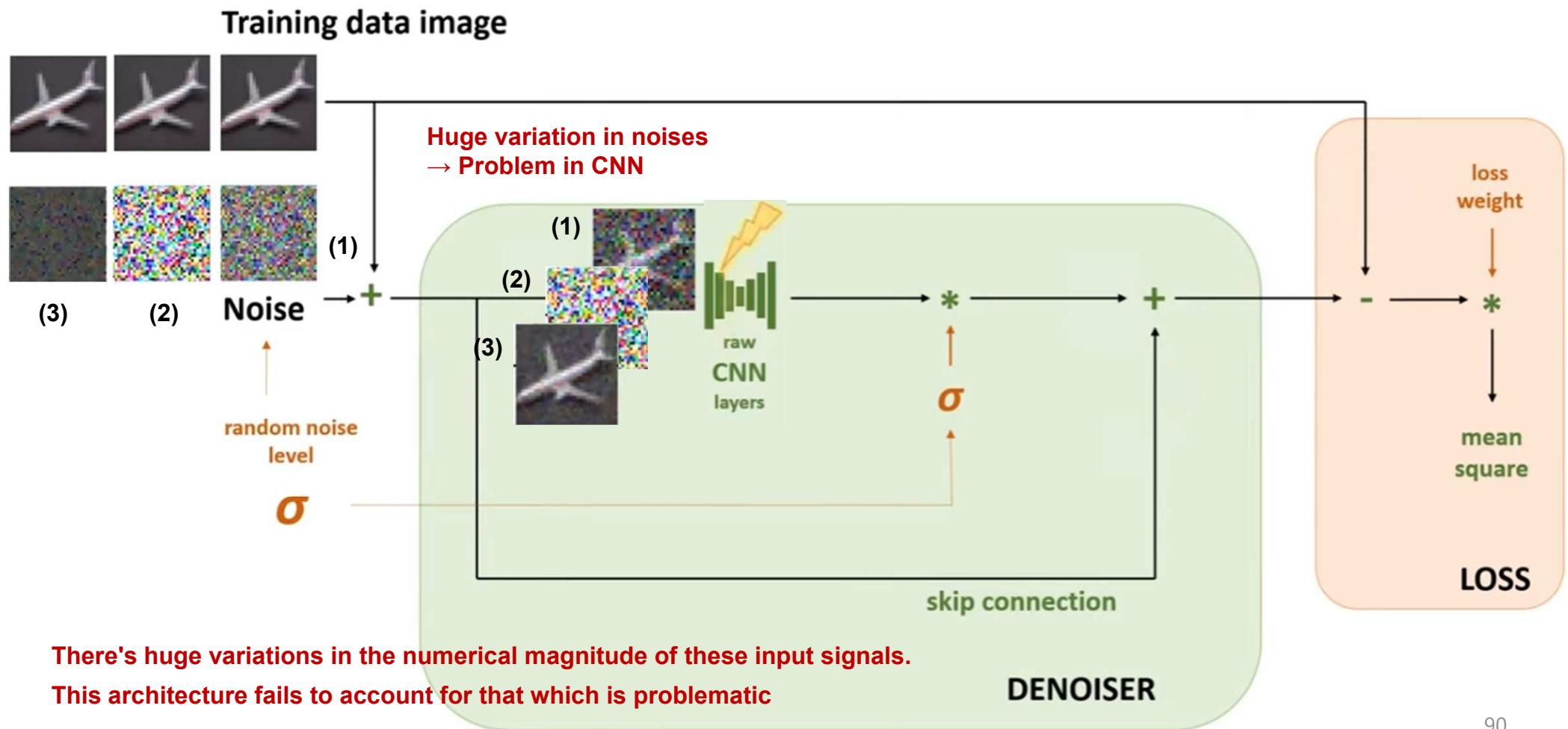
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Training data image



Youtube Presentaiton

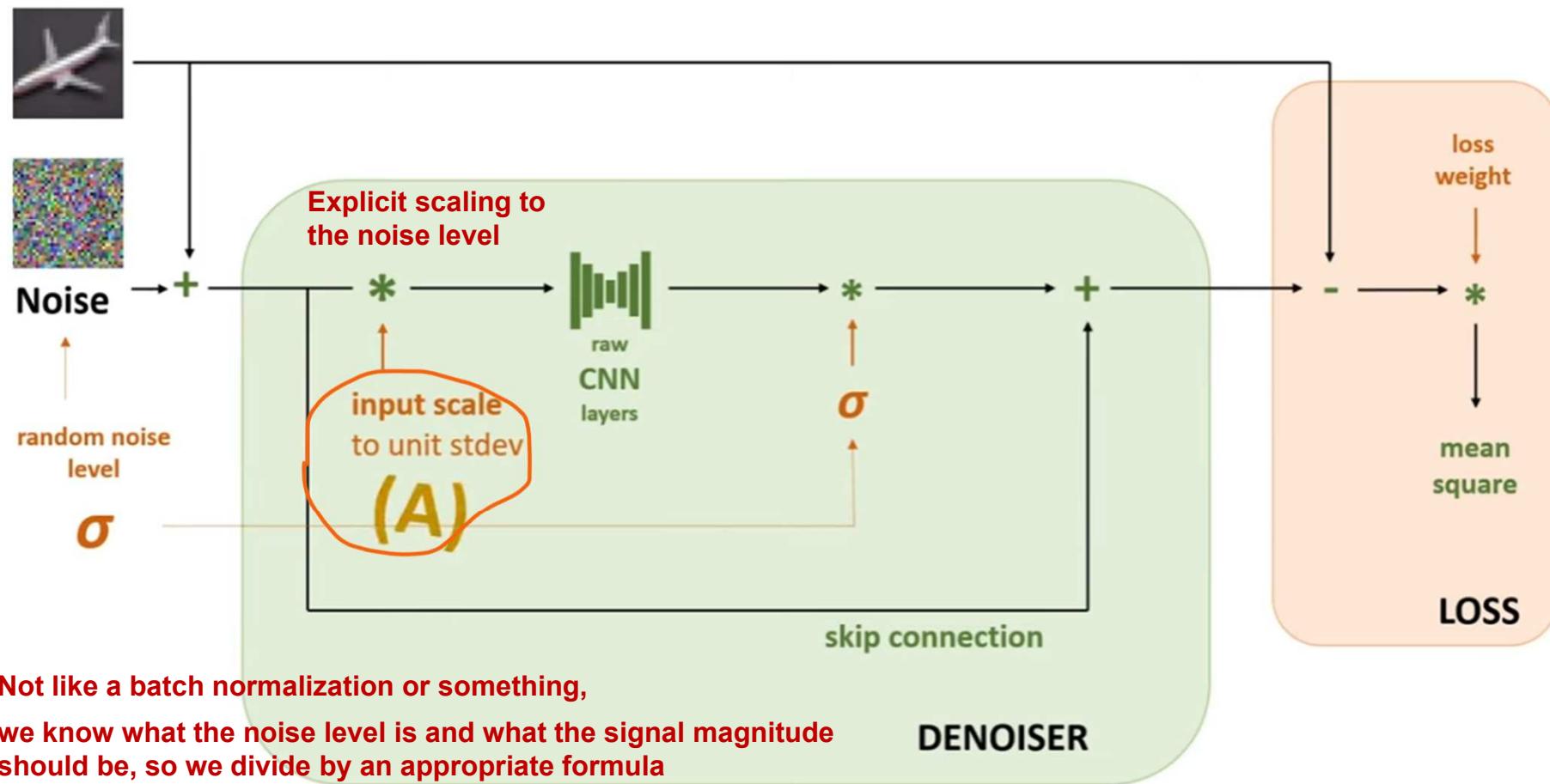
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



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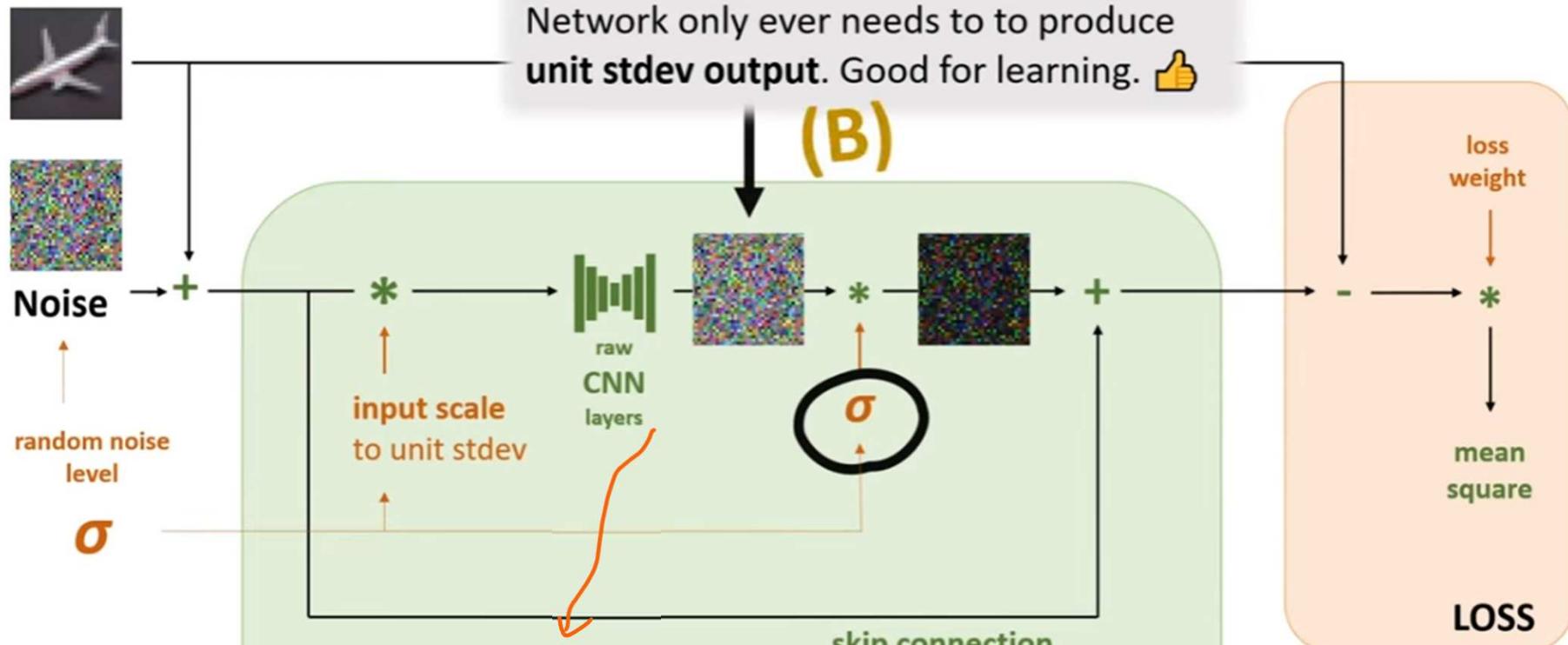
Training data image



Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Training data image



Now the network only needs to produce a unit standard deviation output.

This explicit scaling to the noise level make much easier for the network it can always work with these unit standard signals

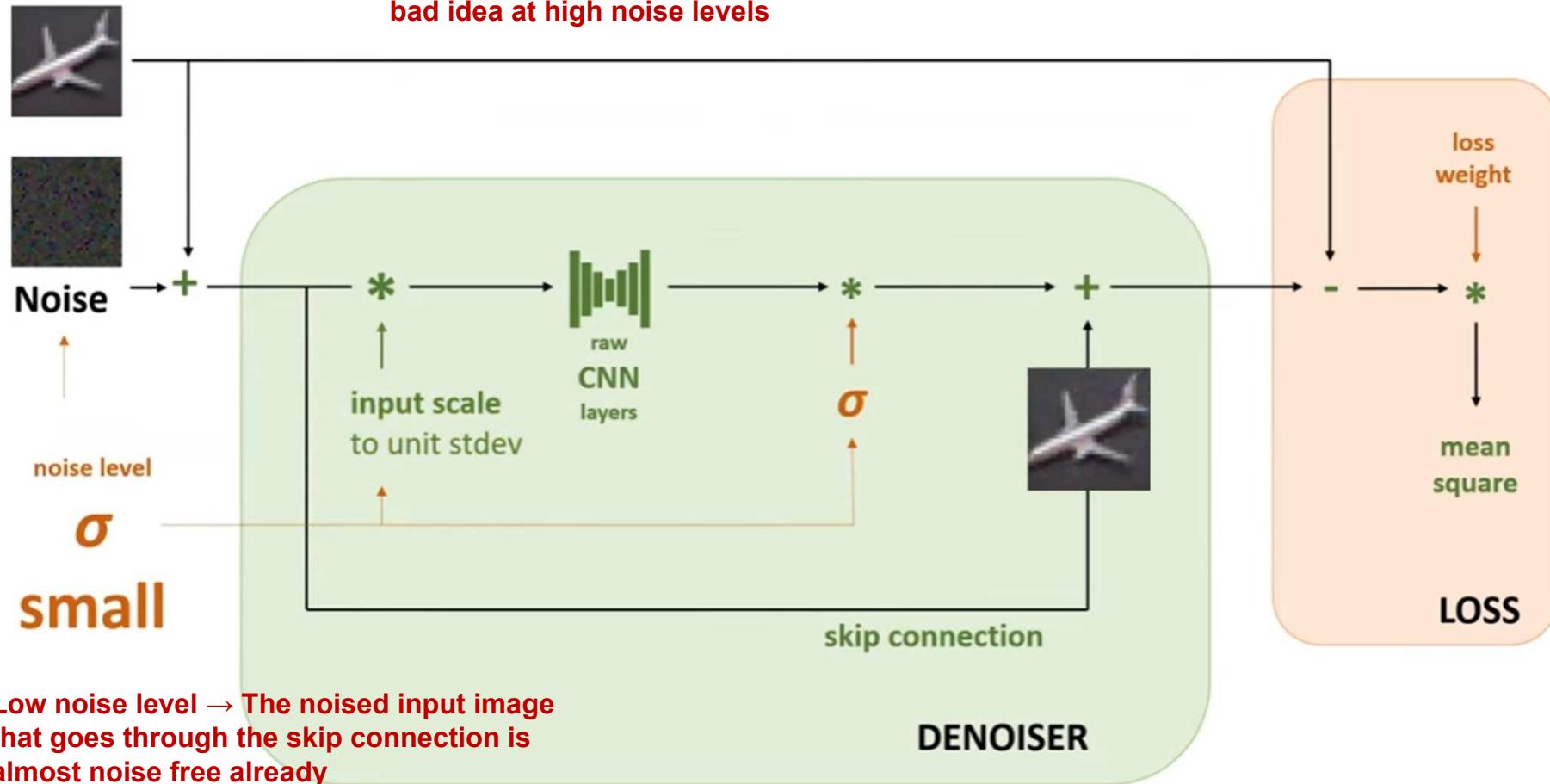
DENOISER

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Training data image

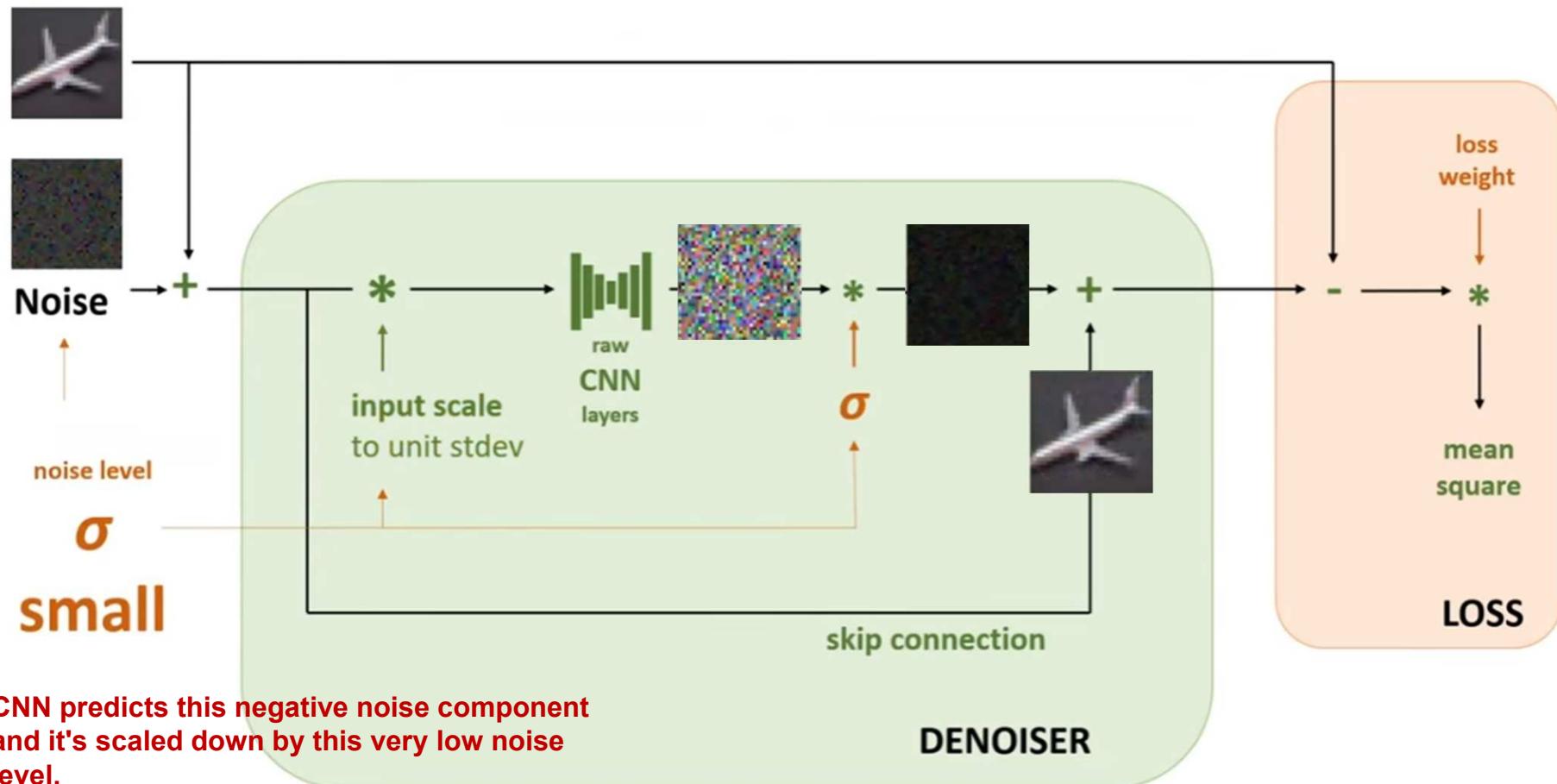
This is actually a good idea at a small noise levels but a bad idea at high noise levels



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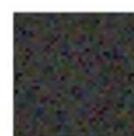
Training data image



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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Training data image



Noise

noise level
 σ

small

Clean image from input is recycled,
network output (and its error) is downweighted 

(C)*

loss weight

mean square

LOSS

raw
CNN
layers

σ

skip connection

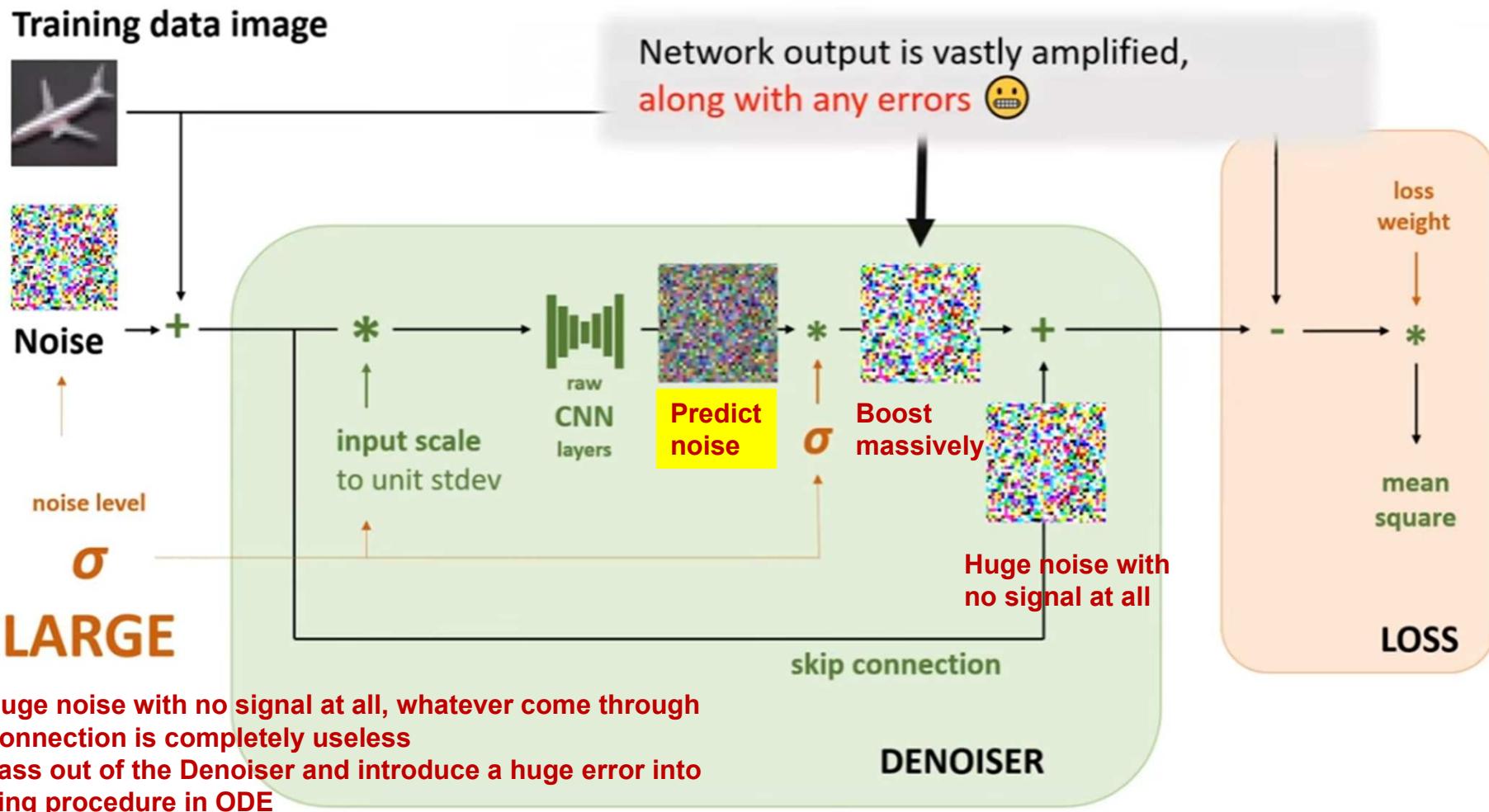
DENOISER

The network is actually the only source error in this process.
If the network made errors, we've down scaled them.

Recycling what we already knew instead of trying to learn the identity function with the network

Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "Elucidating the Design Space of Diffusion-Based Generative Models," NeurIPS 2022.



Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Training data image



Noise



noise level

σ

LARGE

Network output is vastly amplified,
along with any errors 😬

Absurd Task!!



raw
CNN
layers

σ

skip connection

DENOISER



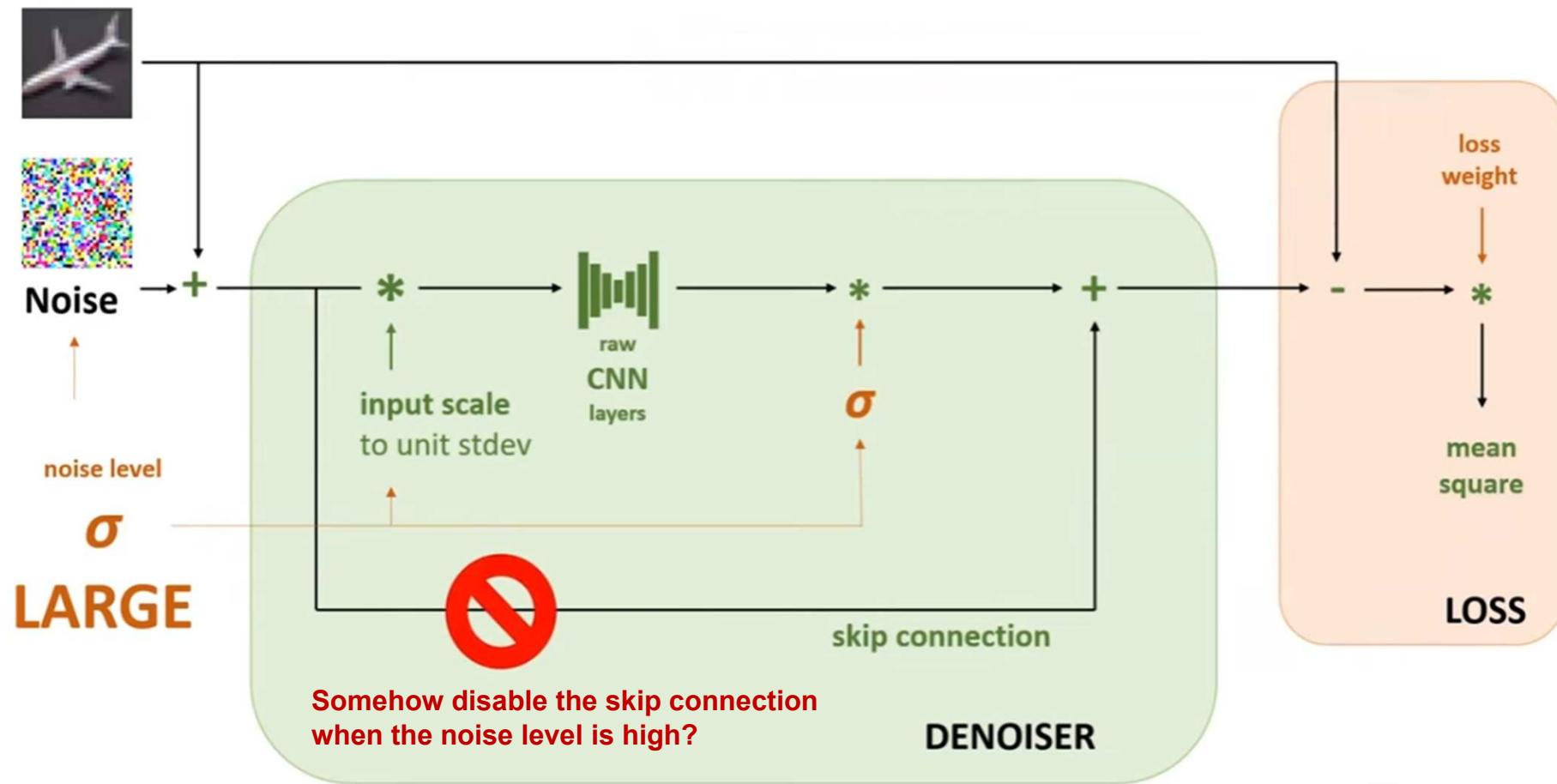
loss
weight



Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

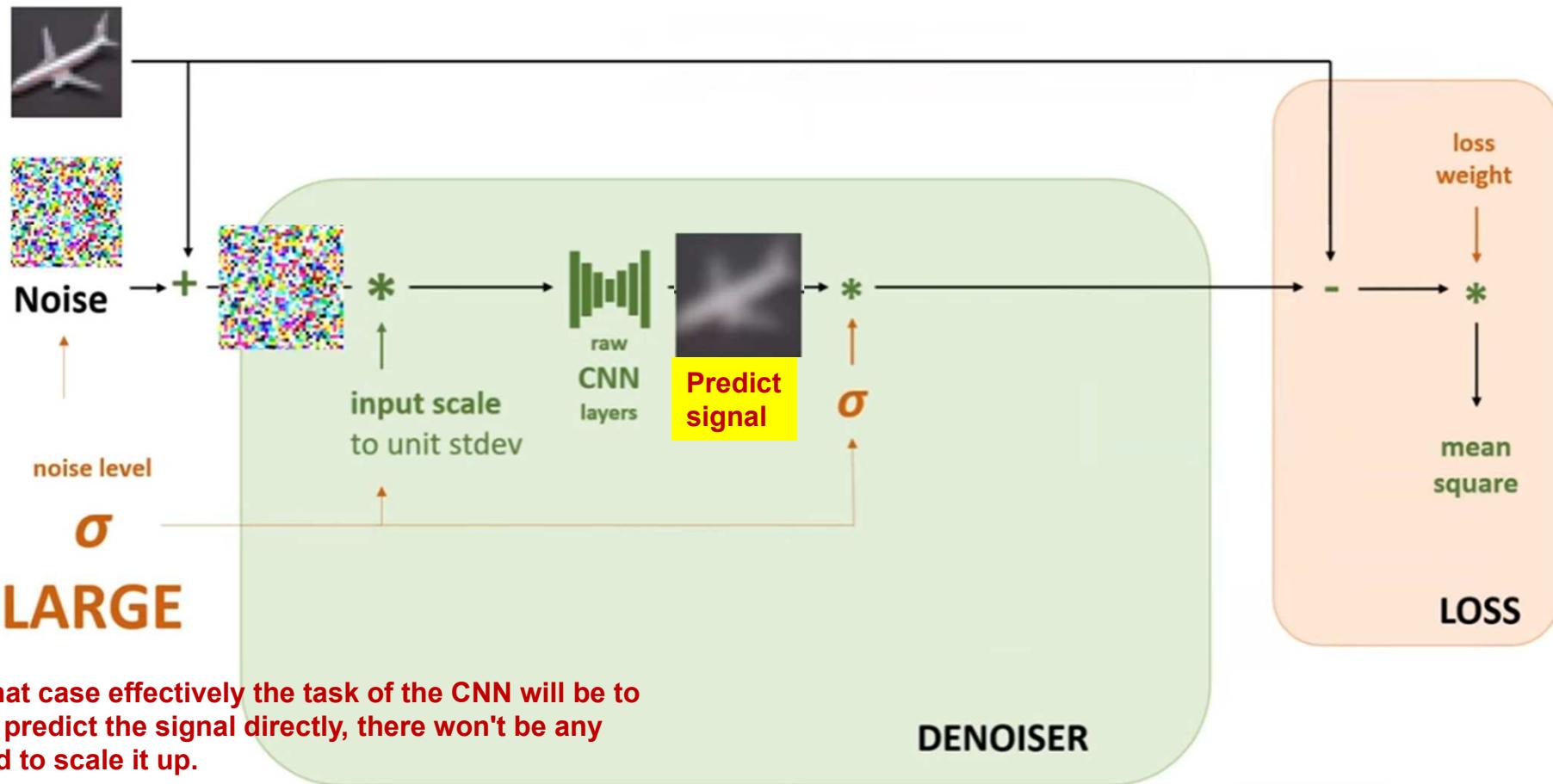
Training data image



Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

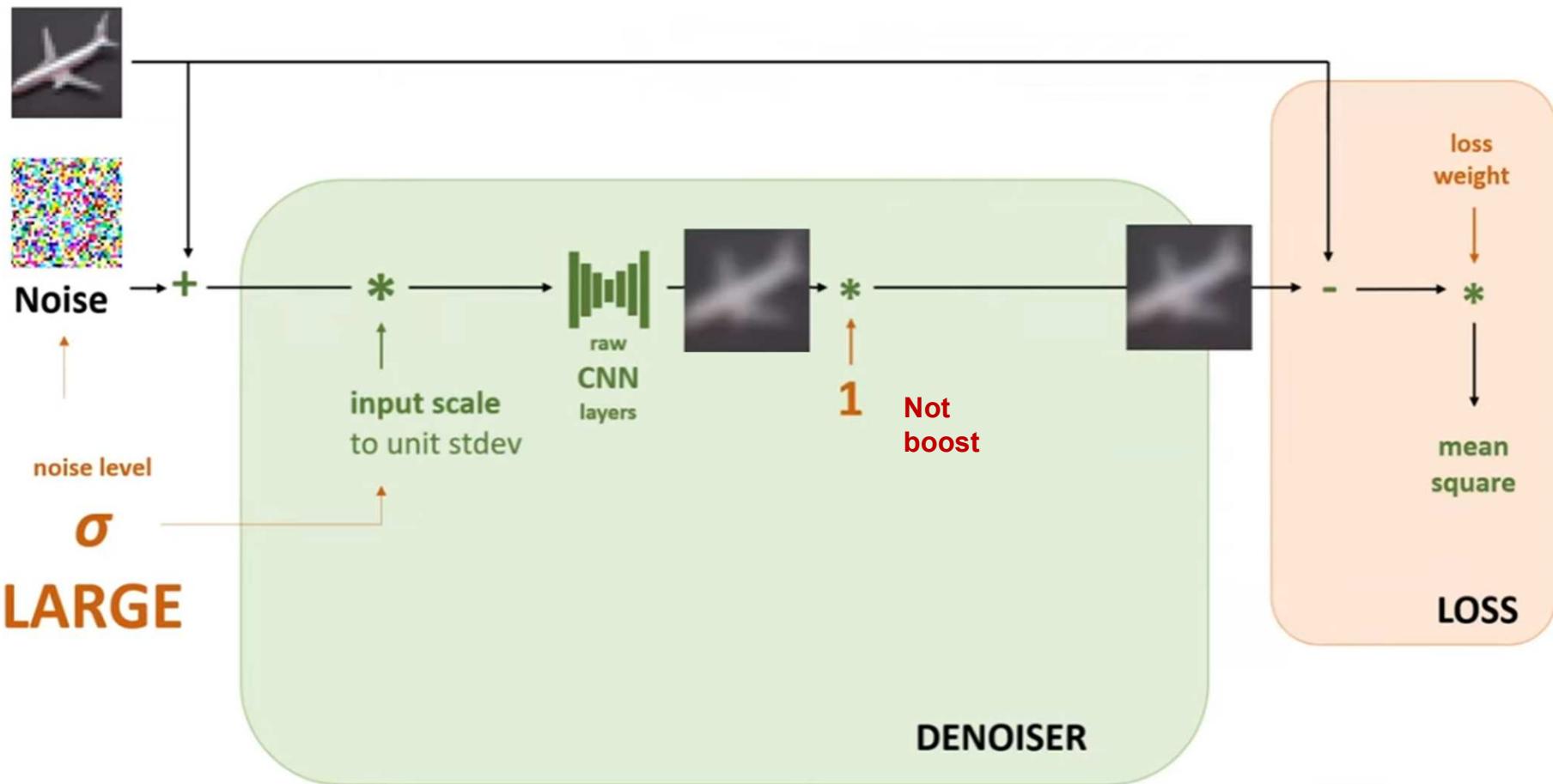
Training data image



Youtube Presentaiton

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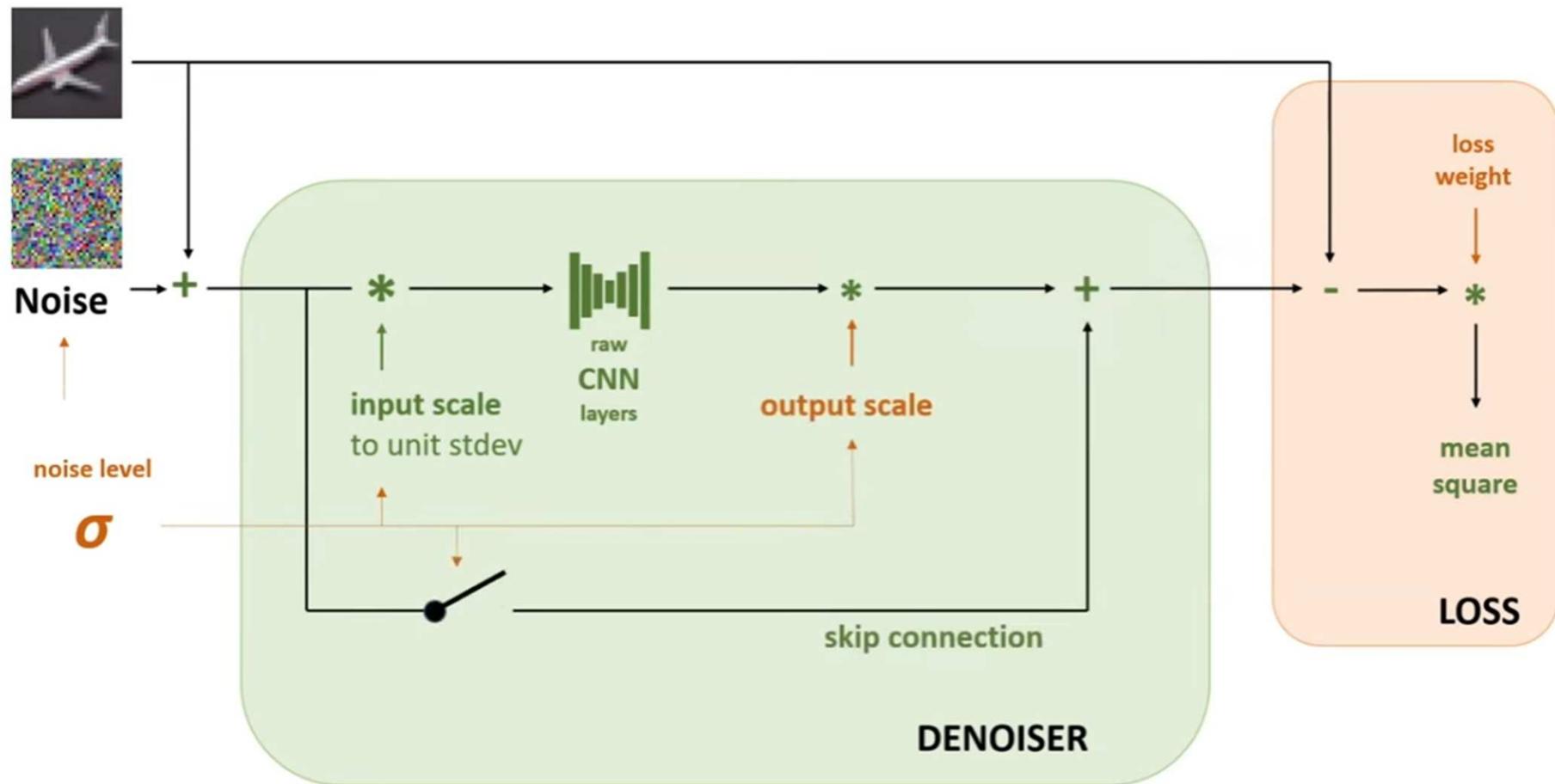
Training data image



Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Training data image



Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based](#)

Training data image



Noise

noise level
 σ

$$D_\theta(x; \sigma) = c_{\text{skip}}(\sigma)x + c_{\text{out}}(\sigma)F_\theta(c_{\text{in}}(\sigma)x; c_{\text{noise}}(\sigma))$$

input scale
to unit stdev



output scale

skip connection

skip scale

1 to predict noise, 0 to predict signal

DENOISER

Architecture of F_θ (any)

Skip scaling $c_{\text{skip}}(\sigma) \frac{\sigma_{\text{data}}^2}{(\sigma^2 + \sigma_{\text{data}}^2)}$

Output scaling $c_{\text{out}}(\sigma) \sigma \cdot \sigma_{\text{data}} / \sqrt{\sigma_{\text{data}}^2 + \sigma^2}$

Input scaling $c_{\text{in}}(\sigma) 1 / \sqrt{\sigma^2 + \sigma_{\text{data}}^2}$

Noise cond. $c_{\text{noise}}(\sigma) \frac{1}{4} \ln(\sigma)$

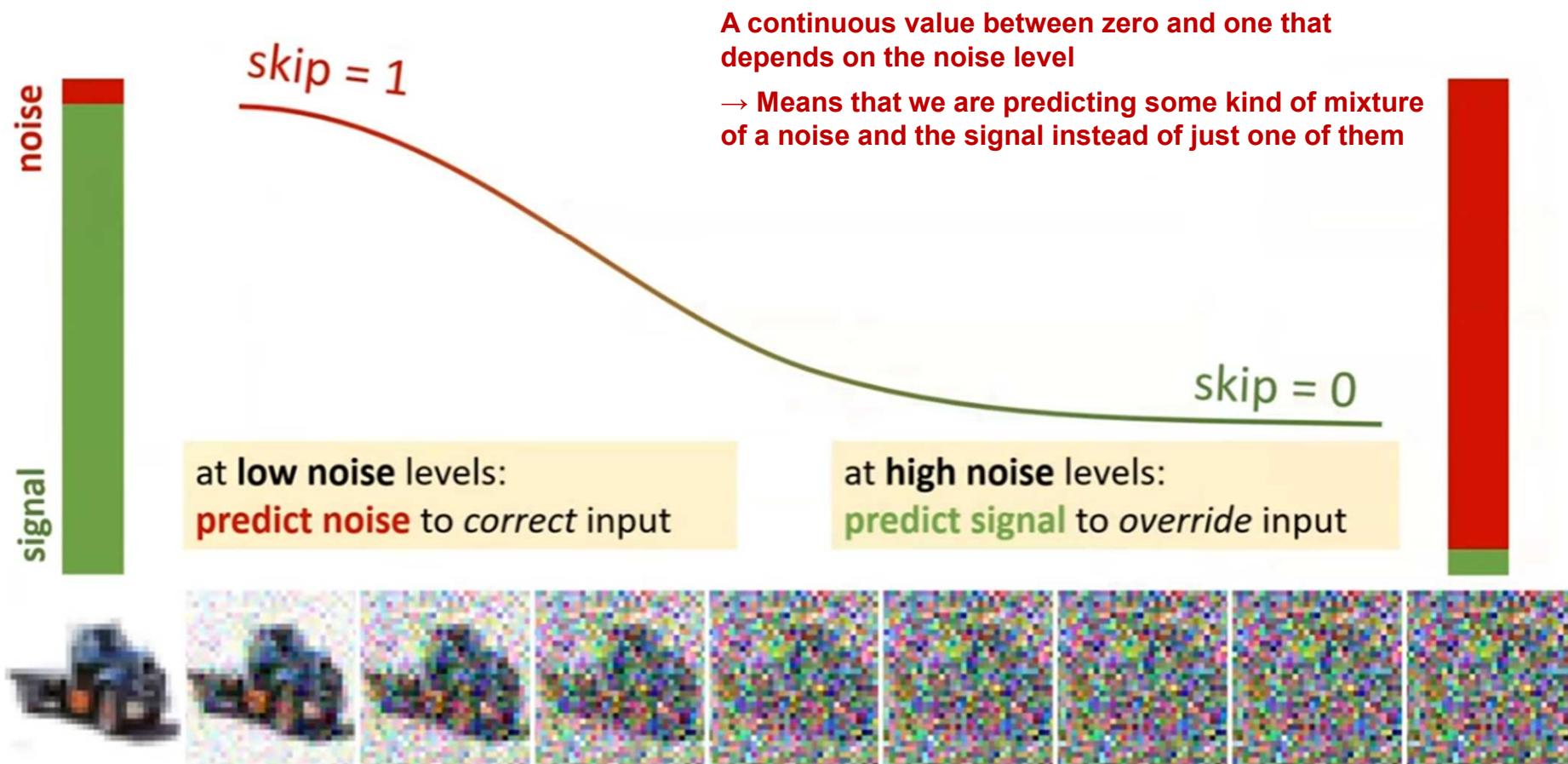
loss weight

mean square

LOSS

Youtube Presentaiton

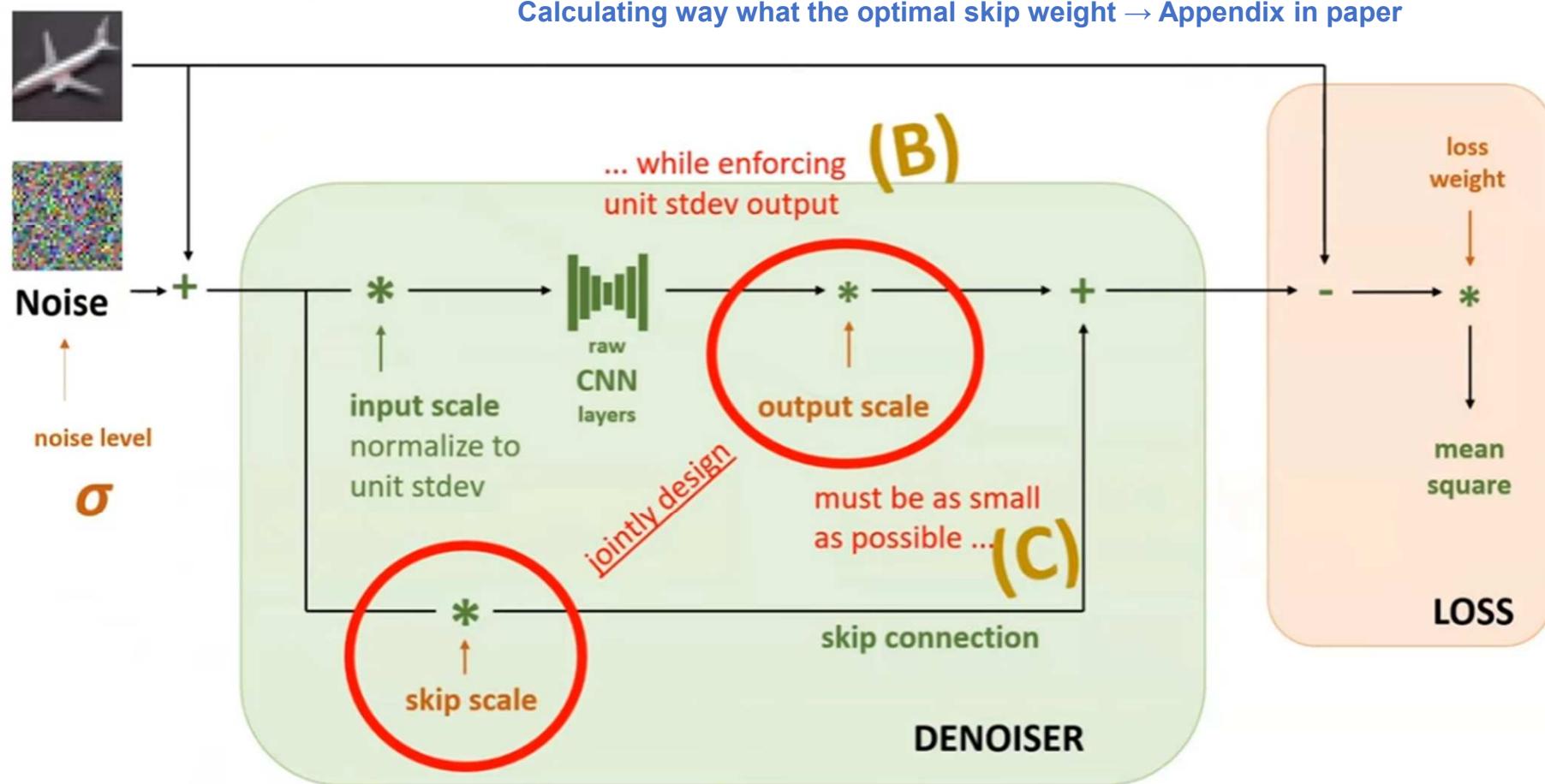
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



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Training data image



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	VP	VE	iDDPM	+ DDIM	Ours
Sampling					
ODE solver	Euler	Euler	Euler		2^{nd} order Heun
Time steps	$t_{i < N}$	$1 + \frac{i}{N-1}(\epsilon_s - 1)$	$\sigma_{\max}^2 (\sigma_{\min}^2 / \sigma_{\max}^2)^{\frac{i}{N-1}}$	$u_{\lfloor j_0 + \frac{M-1-j_0}{N-1} i + \frac{1}{2} \rfloor}$, where $u_M = 0$ $u_{j-1} = \sqrt{\frac{u_j^2 + 1}{\max(\bar{\alpha}_{j-1}/\bar{\alpha}_j, C_1)} - 1}$	$(\sigma_{\max}^{\frac{1}{\rho}} + \frac{i}{N-1}(\sigma_{\min}^{\frac{1}{\rho}} - \sigma_{\max}^{\frac{1}{\rho}}))^{\rho}$
Schedule	$\sigma(t)$	$\sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t} - 1}$	\sqrt{t}	t	t
Scaling	$s(t)$	$1/\sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t}}$	1	1	1

Network and preconditioning

Skip scaling	$c_{\text{skip}}(\sigma)$	1	1	1	$\sigma_{\text{data}}^2 / (\sigma^2 + \sigma_{\text{data}}^2)$
Output scaling	$c_{\text{out}}(\sigma)$	$-\sigma$	σ	$-\sigma$	$\sigma \cdot \sigma_{\text{data}} / \sqrt{\sigma_{\text{data}}^2 + \sigma^2}$
Input scaling	$c_{\text{in}}(\sigma)$	$1/\sqrt{\sigma^2 + 1}$	1	$1/\sqrt{\sigma^2 + 1}$	$1/\sqrt{\sigma^2 + \sigma_{\text{data}}^2}$
Noise cond.	$c_{\text{noise}}(\sigma)$	$(M-1) \sigma^{-1}(\sigma)$	$\ln(\frac{1}{2}\sigma)$	$M-1 - \arg \min_j u_j - \sigma $	$\frac{1}{4} \ln(\sigma)$

Training

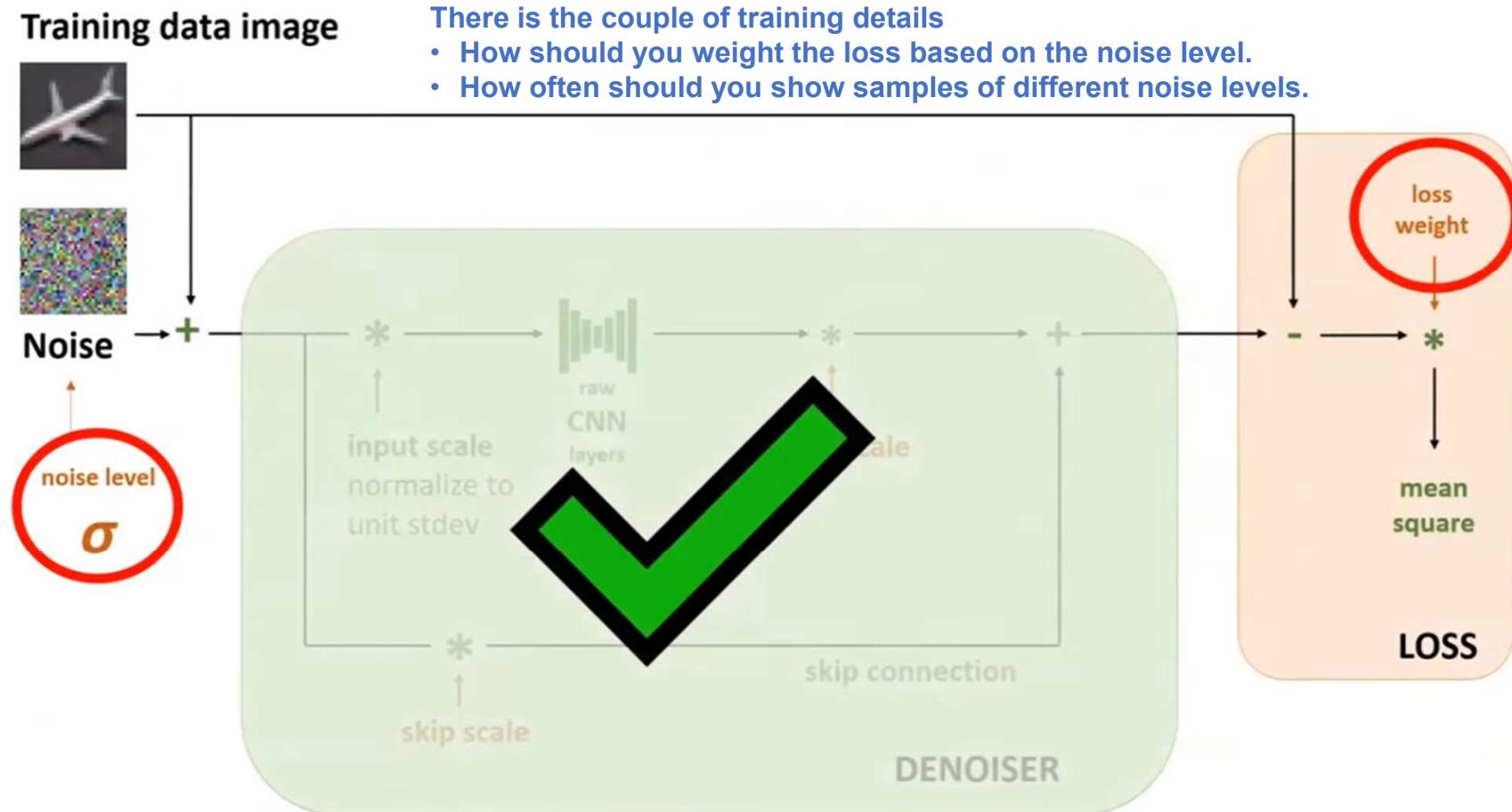
Noise distribution

Loss weighting $\lambda(\sigma)$



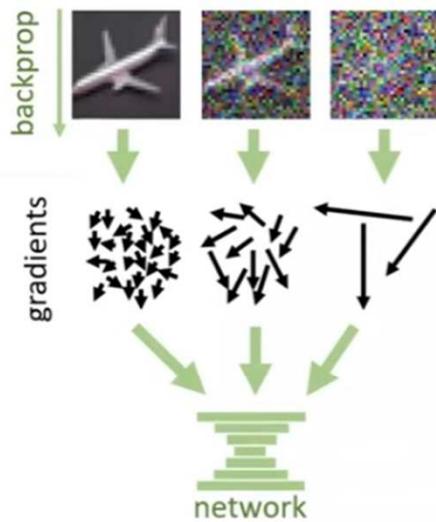
Youtube Presentaiton

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Loss weighting and noise level distribution



1. Baseline: frequent small updates on some noise levels, infrequent large updates on others. **Unhealthy training dynamics.**

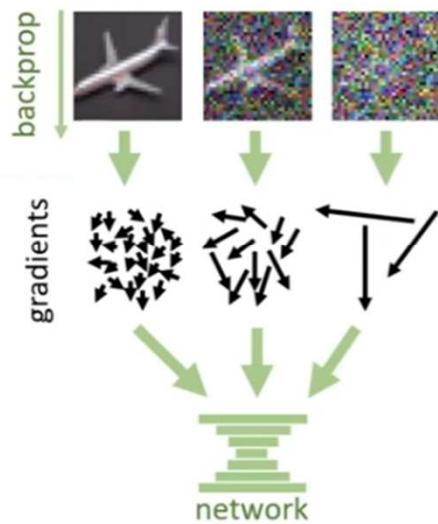
General problem

- Might have a highly lopsided distribution of like gradient feedback.
- If not careful on most iteration, provide the weights gently to one direction or the other and have the massive gradient smash on the weights every few iterations.

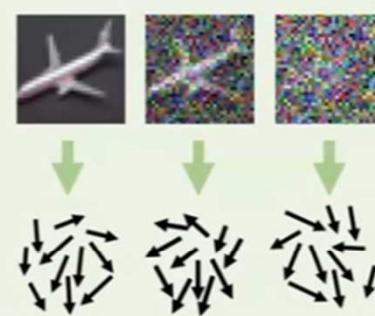
That's probably very bad for your training dynamics.

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

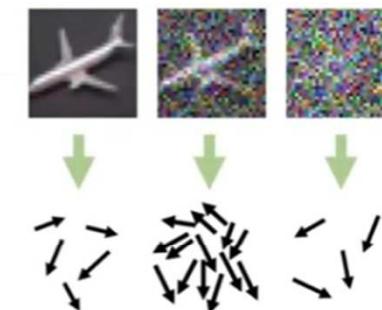
Loss weighting and noise level distribution



1. Baseline: frequent small updates on some noise levels, infrequent large updates on others. **Unhealthy training dynamics.**



2. Loss weighting equalizes gradient magnitudes.



3. Use noise level distribution to train the network more often at noise levels where training has impact.

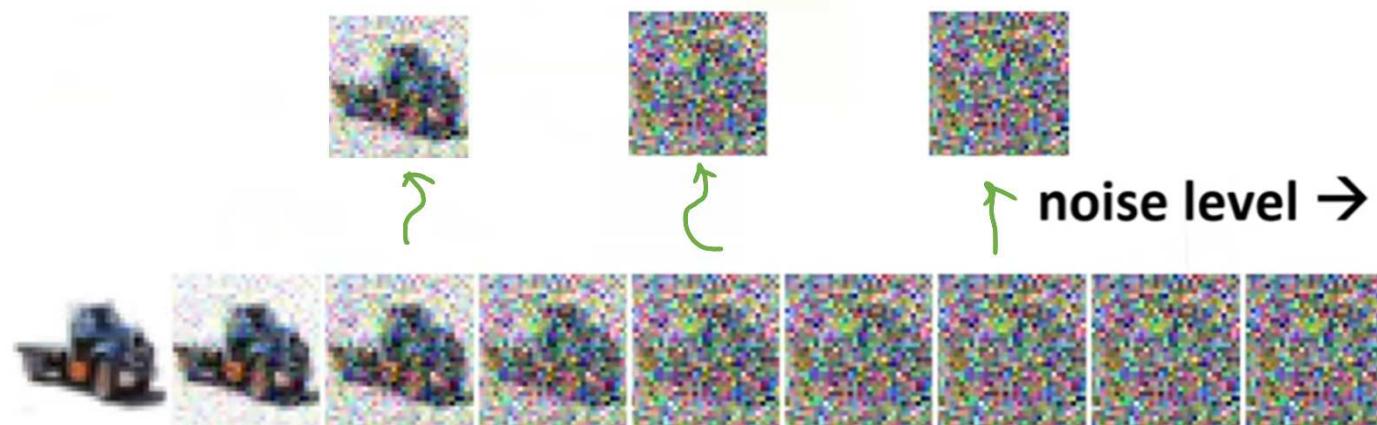
The **noise level distribution** may how often you show images of any given noise level.

The role of the **loss weighting** or the **scaling**, the numerical scale in front of the loss term, should be to just equalize the magnitude of the loss or equivalently equalize the magnitude of the gradient feedback it gives.

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

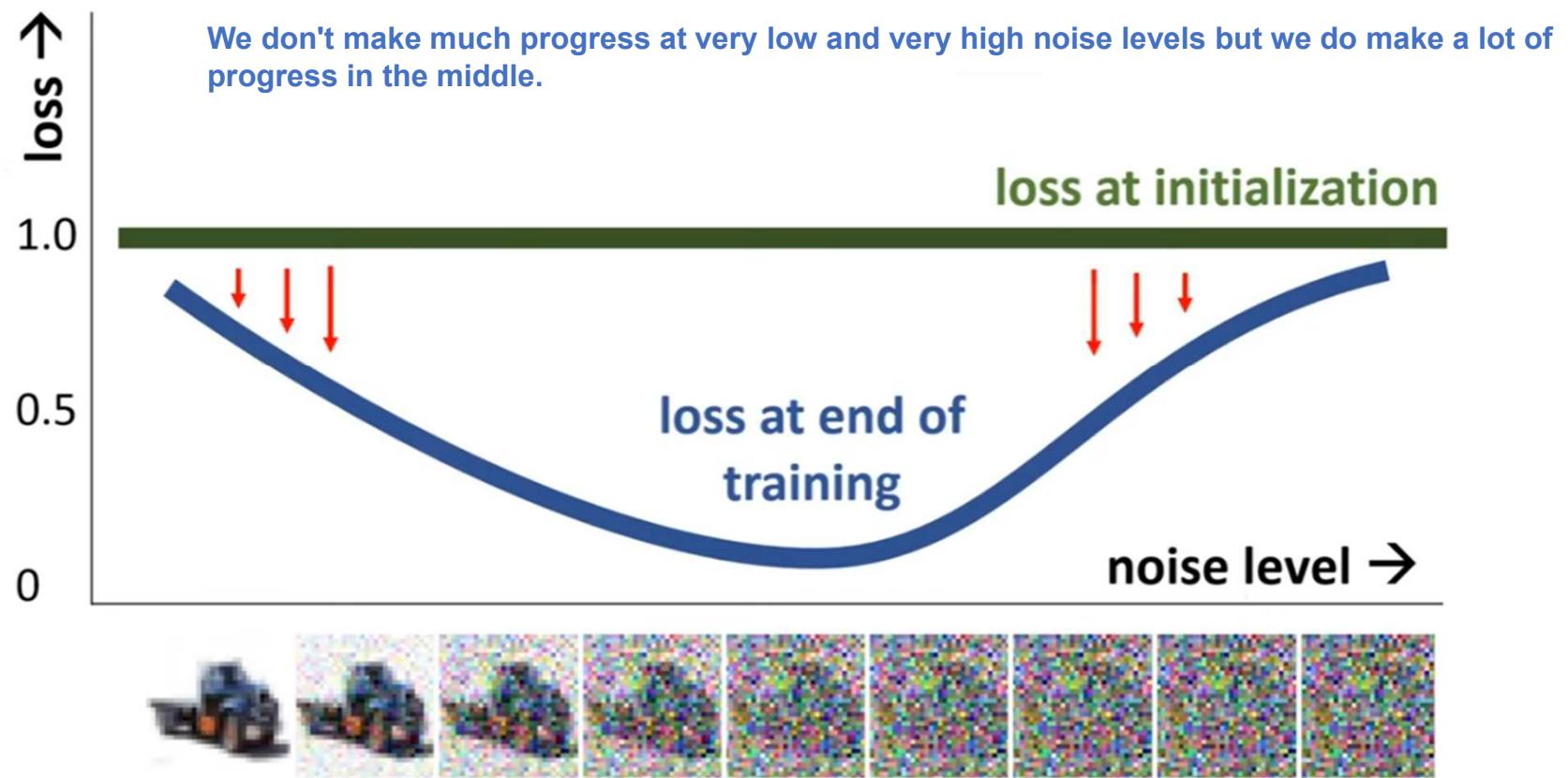
Loss weighting and noise level distribution

The role of noise level distribution is to direct your training efforts to the levels where you know it's relevant where you know you can make an impact.



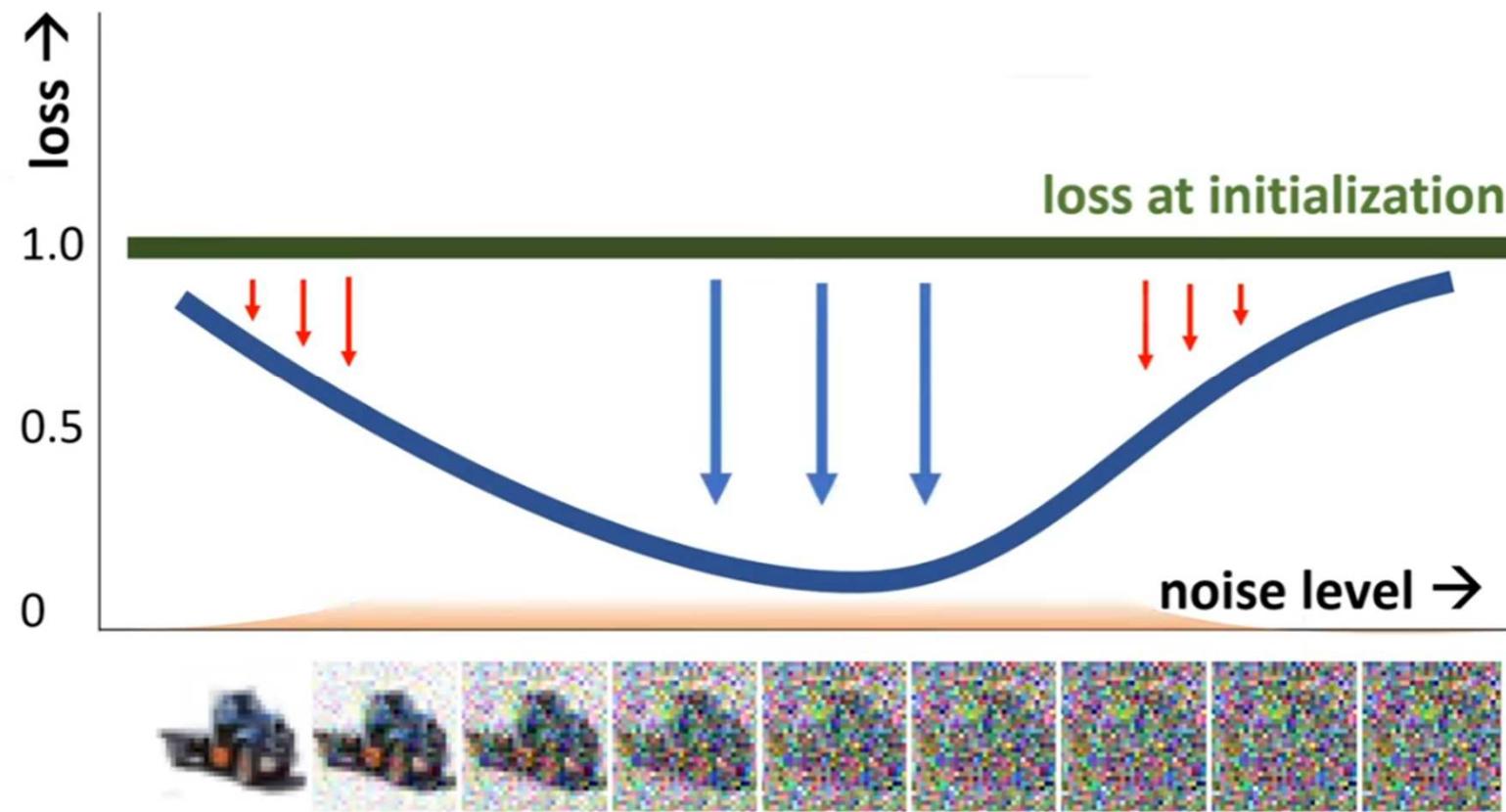
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Loss weighting and noise level distribution



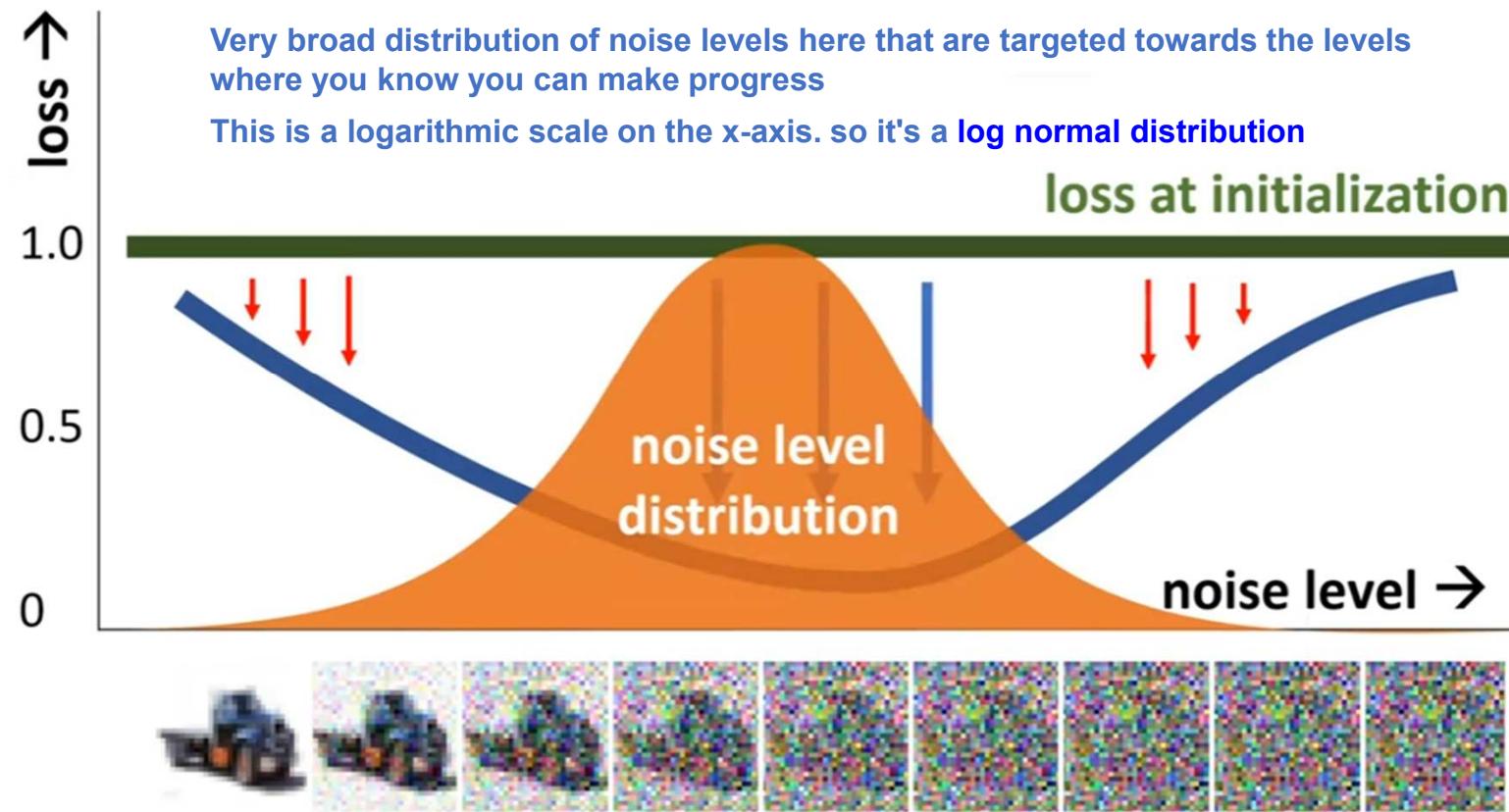
EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Loss weighting and noise level distribution



EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Loss weighting and noise level distribution



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	VP	VE	iDDPM	+ DDIM	Ours
Sampling					
ODE solver	Euler	Euler	Euler		2nd order Heun
Time steps	$t_{i < N}$	$1 + \frac{i}{N-1}(\epsilon_s - 1)$	$\sigma_{\max}^2 (\sigma_{\min}^2 / \sigma_{\max}^2)^{\frac{i}{N-1}}$	$u_{\lfloor j_0 + \frac{M-1-j_0}{N-1} i + \frac{1}{2} \rfloor}$, where $u_M = 0$ $u_{j-1} = \sqrt{\frac{u_j^2 + 1}{\max(\bar{\alpha}_{j-1}/\bar{\alpha}_j, C_1)} - 1}$	$(\sigma_{\max}^{\frac{1}{\rho}} + \frac{i}{N-1}(\sigma_{\min}^{\frac{1}{\rho}} - \sigma_{\max}^{\frac{1}{\rho}}))^{\rho}$
Schedule	$\sigma(t)$	$\sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t} - 1}$	\sqrt{t}	t	t
Scaling	$s(t)$	$1/\sqrt{e^{\frac{1}{2}\beta_d t^2 + \beta_{\min} t}}$	1	1	1
Network and preconditioning					
Skip scaling	$c_{\text{skip}}(\sigma)$	1	1	1	$\sigma_{\text{data}}^2 / (\sigma^2 + \sigma_{\text{data}}^2)$
Output scaling	$c_{\text{out}}(\sigma)$	$-\sigma$	σ	$-\sigma$	$\sigma \cdot \sigma_{\text{data}} / \sqrt{\sigma_{\text{data}}^2 + \sigma^2}$
Input scaling	$c_{\text{in}}(\sigma)$	$1/\sqrt{\sigma^2 + 1}$	1	$1/\sqrt{\sigma^2 + 1}$	$1/\sqrt{\sigma^2 + \sigma_{\text{data}}^2}$
Noise cond.	$c_{\text{noise}}(\sigma)$	$(M-1) \sigma^{-1}(\sigma)$	$\ln(\frac{1}{2}\sigma)$	$M-1 - \arg \min_j u_j - \sigma $	$\frac{1}{4} \ln(\sigma)$
Training					
Noise distribution		$\sigma^{-1}(\sigma) \sim \mathcal{U}(\epsilon_t, 1)$	$\ln(\sigma) \sim \mathcal{U}(\ln(\sigma_{\min}), \ln(\sigma_{\max}))$	$\sigma = u_j, \quad j \sim \mathcal{U}\{0, M-1\}$	$\ln(\sigma) \sim \mathcal{N}(P_{\text{mean}}, P_{\text{std}}^2)$
Loss weighting	$\lambda(\sigma)$	$1/\sigma^2$	$1/\sigma^2$	$1/\sigma^2$ (note: *)	$(\sigma^2 + \sigma_{\text{data}}^2) / (\sigma \cdot \sigma_{\text{data}})^2$

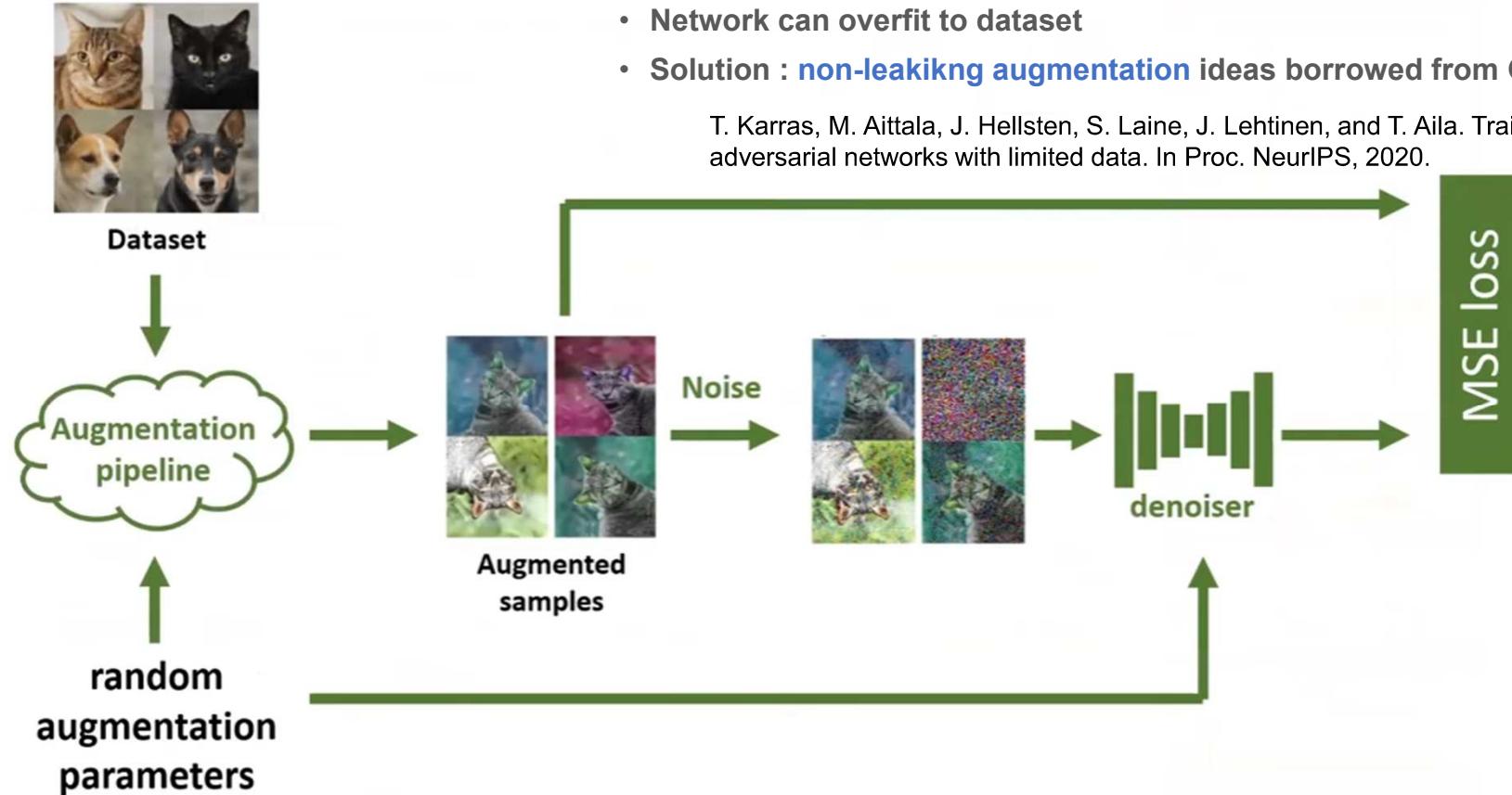
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EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Overfitting and Augmentations

- Network can overfit to dataset
- Solution : **non-leakikng augmentation ideas borrowed from GAN literature**

T. Karras, M. Aittala, J. Hellsten, S. Laine, J. Lehtinen, and T. Aila. Training generative adversarial networks with limited data. In Proc. NeurIPS, 2020.



Youtube Presentaiton

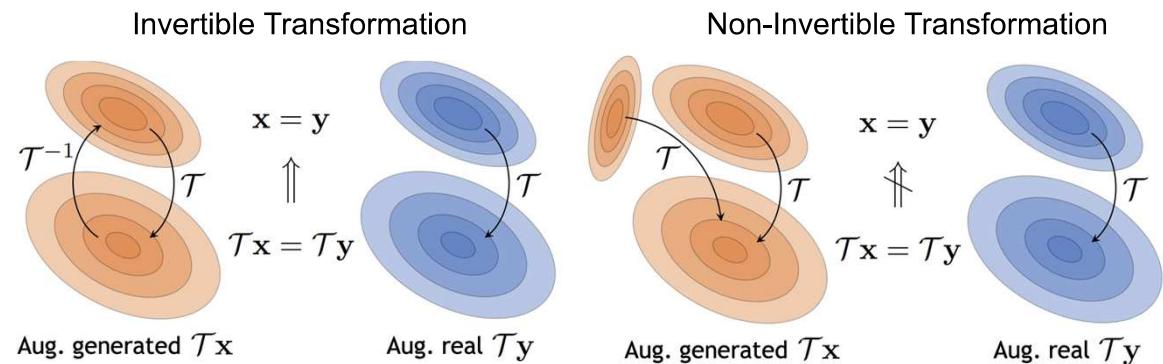
Training GANs With Limited Data, StyleGAN2 with Adaptive Discriminator Augmentation (ADA)

<https://medium.com/swlh/training-gans-with-limited-data-22a7c8ffce78>

<https://yun905.tistory.com/56>

Non-leakikng augmentation & ADA(Adaptive Discriminator Augmentation)

- 만약 training data에 90도 회전이라는 augmentation을 주면, generator는 90도 돌아간 이미지를 생성한다. 이것을 **leaking**이라고 한다. Discriminator가 augmentation된 이미지와 그렇지 않은 이미지를 구분하지 못하게 되는 것이다.
- Non-leaking augmentation**을 위해서는 이미지에 transformation을 가하되, 그 transformation이 확률 분포의 관점에서 *invertible*해야 한다. Invertible한 augmentation을 가했을 경우 training 과정에서 모델이 corruption을 걸러내고 원래의 분포를 잘 학습하게 된다고 한다.
- 가령 전체 이미지의 90%를 0으로 만드는 변환을 한다고 하자. 그러면 90%의 검은 이미지를 제외하고 10%의 진짜 이미지를 찾을 수 있고, 그 augmentation을 undo 할 수 있다. 이것은 확률 분포의 관점에서 invertible한 변환의 예이다. 이번에는 {0, 90, 180, 270}도 중 무작위로 골라 이미지를 회전하는 augmentation을 생각해보자. 그러면 원래의 방향을 가늠할 수 없으므로 undo할 수 없고, 따라서 invertible하지 않다. 이런 augmentation에서는 leaking이 발생하게 된다.
- 여기서, augmentation을 p의 확률로 적용한다고 하자. 그러면 회전되지 않은 이미지의 개수가 늘어나므로 진짜 이미지를 구분할 수 있고, invertible하게 된다. 다시 말해, 어떤 augmentation이 p 값에 따라 leaking 할 수도 있고 non-leaking 할 수도 있다는 뜻이다



- The generator is forced to match the fake distribution x to the real distribution y in order to match the transformed distributions Tx and Ty .
- If we apply an invertible transformation T to the generated and real distributions x and y , then it is sufficient to match augmented distributions Tx and Ty in order to match the original distributions x and y .
- Theoretically, if the augmentation operator T is “invertible”, there exists one and only one x for the augmented distribution Tx , and there should be no “leaks” in x . However, in practice, due to limitations of finite sampling, finite representational power of the networks, inductive bias and training dynamics, very high values of p leads to leaking of augmentations in the generated images.

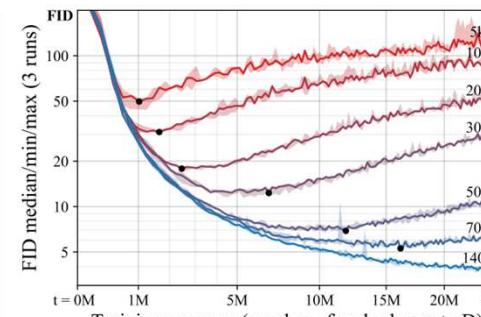
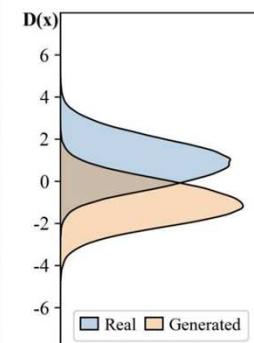
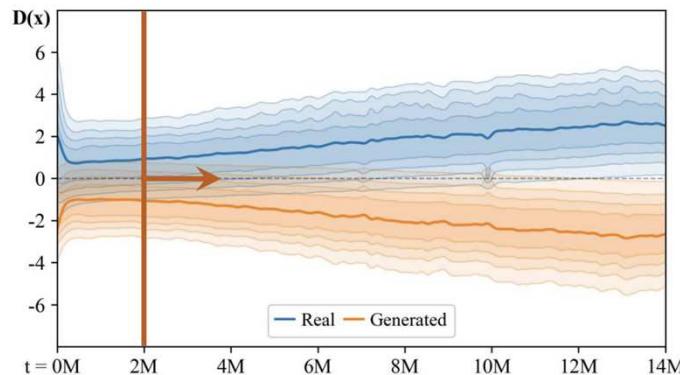
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Training GANs With Limited Data, StyleGAN2 with Adaptive Discriminator Augmentation (ADA)

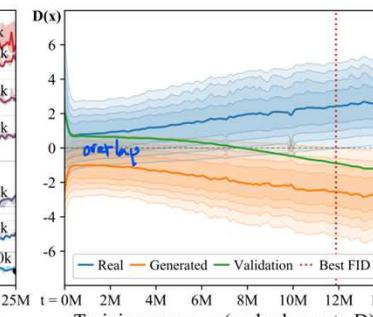
<https://medium.com/swlh/training-gans-with-limited-data-22a7c8ffce78>

<https://yun905.tistory.com/56>

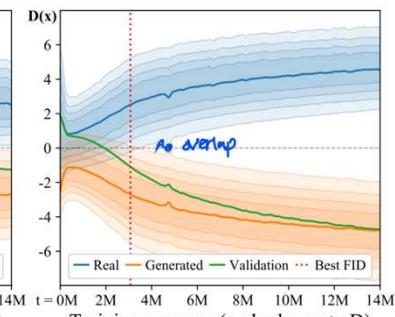
Non-leakng augmentation & ADA(Adaptive Discriminator Augmentation)



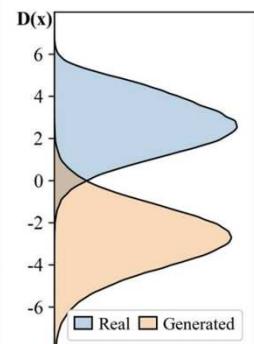
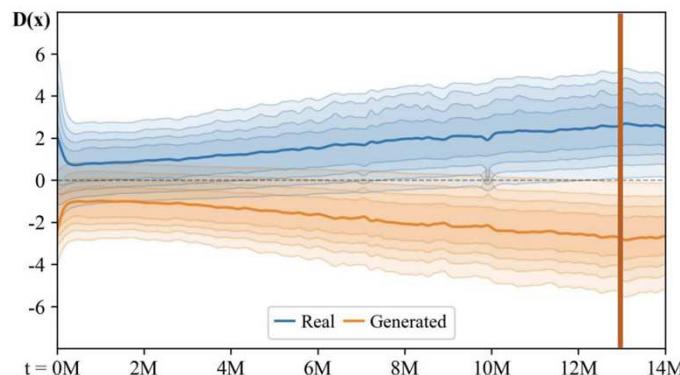
(a) Convergence of FFHQ (256 × 256)



(b) Discriminator outputs, 50k



(c) Discriminator outputs, 20k



- The standard way of quantifying overfitting is to use a separate validation set and observe its behavior relative to the training set. When overfitting kicks in, the validation set starts to behave increasingly like the generated images, and the discriminator outputs for real and generated samples begin to diverge.
- Figure (a) : 데이터 수와 성능은 매우 밀접한 관계를 가지고 있음. 적은 데이터에서는 training이 diverge함.
- Figure (b)와 (c) : Discriminator output으로 discriminator overfitting이 일어나는 것을 확인 할 수 있음. Discriminator가 적은 수의 training data에 overfit되어서 overlap이 없어지면 FID 도 하락함을 알 수 있음.

Figure. As the training progresses, the overlap between discriminator output distributions for real and generated images decreases

Youtube Presentaiton

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Non-leakikng augmentation & ADA(Adaptive Discriminator Augmentation)

Two plausible overfitting heuristics to measure overfitting

$$r_v = \frac{\mathbb{E}[D_{\text{train}}] - \mathbb{E}[D_{\text{validation}}]}{\mathbb{E}[D_{\text{train}}] - \mathbb{E}[D_{\text{generated}}]} \quad r_t = \mathbb{E}[\text{sign}(D_{\text{train}})]$$

- The first heuristic r_v , expresses the output for a validation set relative to the training set and generated images. The numerator is 0 when the training and validation set behave exactly the same, hence $r=0$ means no overfitting. The numerator and denominator are the same when the generated and validation set behave exactly the same, hence $r=1$ indicates complete overfitting.
- Since it assumes the existence of a separate validation set in an already small dataset, it is not feasible to calculate the r_v heuristic. Hence, the authors turn to r_t - which estimates the portion of the training set that gets positive discriminator outputs - to identify overfitting and dynamically adapt the augmentation probability p as the training progresses:
 - r_t too high → augment more (increase p)
 - r_t too low → augment less (decrease p)

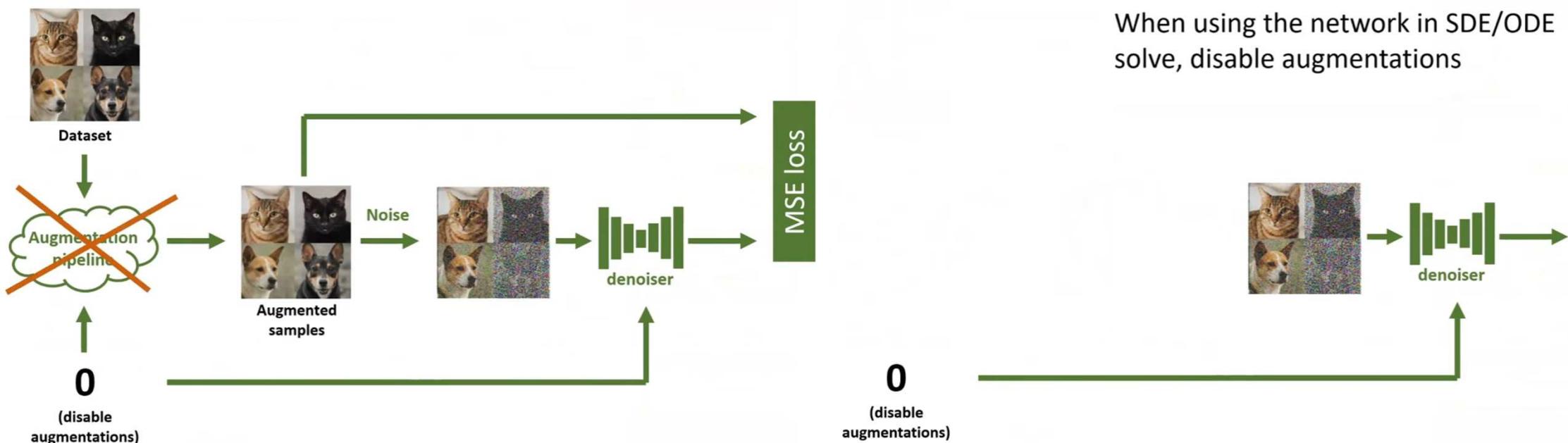
왼쪽은 단지 비교를 위한 수식이고, 실제로 대부분의 실험에서 오른쪽을 사용하였다.
왼쪽의 수식은 validation set을 필요로 하기 때문에 limited dataset에서 적용하기 힘든 부분이 있다.

둘 다 0~1의 범위에서 1이면 discriminator overfitting이 매우 심한 것이고 0이면 전혀 없는 것이다. Overfitting이 심해질수록 discriminator가 validation set을 generated image라고 판단한다는 것을 위에서 확인했다. 이 경우 r_v 는 1이 된다. r_t 에서 sign이 붙은 이유는 단지 그렇게 하면 여러 세팅에서 덜 sensitive하기 때문이다.

이러한 heuristic의 target value를 0~1 사이의 임의의 값으로 정하고, 그 값을 기준으로 p 값을 adaptive하게 조절하는 것을 ADA라고 한다.

Youtube Presentaiton

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.



EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Evaluation of training (deterministic sampling)

Training configuration	CIFAR-10 [28] at 32×32				FFHQ [26] 64×64		AFHQv2 [7] 64×64	
	Conditional		Unconditional		Unconditional		Unconditional	
	VP	VE	VP	VE	VP	VE	VP	VE
A Baseline [42] (*pre-trained)	2.48	3.11	3.01*	3.77*	3.39	25.95	2.58	18.52
B + Adjust hyperparameters	2.18	2.48	2.51	2.94	3.13	22.53	2.43	23.12
C + Redistribute capacity	2.08	2.52	2.31	2.83	2.78	41.62	2.54	15.04
D + Our preconditioning	2.09	2.64	2.29	3.10	2.94	3.39	2.79	3.81
E + Our loss function	1.88	1.86	2.05	1.99	2.60	2.81	2.29	2.28
F + Non-leaky augmentation	1.79	1.79	1.97	1.98	2.39	2.53	1.96	2.16
NFE	35	35	35	35	79	79	79	79

Imagenet 64 × 64 (stochastic sampling)

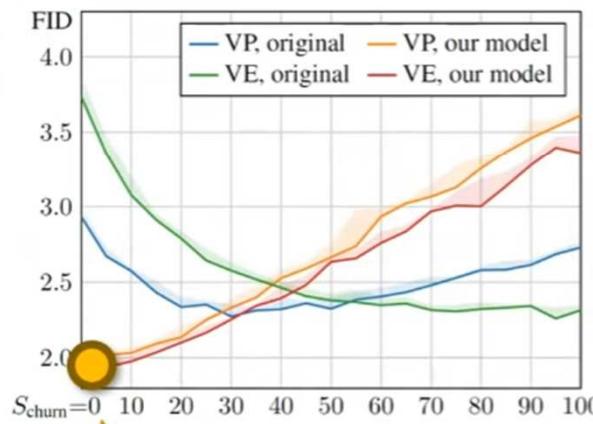
FID 1.36  state of the art FID

With deterministic sampling when we enabled the stochastic sampling and tailor it for these architectures for ImageNet and use this retrained these networks we trained ourselves using these principles, We get a FID of 1.36.

EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

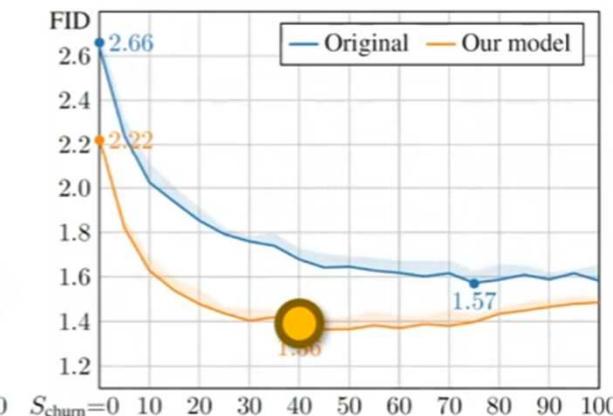
Is stochasticity still helpful?

CIFAR-10: no



best FID at zero stochasticity

Imagenet: yes



EDM : Tero Karras, Miika Aittala, Timo Aila, Samuli Laine, "[Elucidating the Design Space of Diffusion-Based Generative Models](#)," NeurIPS 2022.

Conclusions

- Modular design of diffusion models
 - Training, and sampling and network architectures are not tightly coupled
- Careful design of each “module” yields considerable improvements
- Stochasticity is a double-edged sword
- Higher resolutions, network architectures, conditioning/guidance, large scale datasets, ... ?
 - Ripe for principled analysis of foundations