

Figure 6: The rock-sample problem has $|S| = 257$, $|A| = 9$ and $|Z| = 2$. The maximum time we ran each algorithm was 50 sec. The graphs show the results for different dimensions and compression algorithms. The LPNMF approach allows for deeper compression than both the NMF and ONMF algorithms.

Table 2: PBVI versus LPNMF.

	Time (sec)	$\frac{\sum \gamma^t r}{N}$
tag-avoid $ S = 870, A = 5, Z = 17$		
Perseus-PBVI	2300	-6.5
	500	-13.0
LPNMF ($ S = 150$)	500	-9.0

dimensionality reduction methods need to be investigated as well.

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References

- Belkin, M., and Niyogi, P. 2003. Laplacian Eigenmaps for dimensionality reduction and data representation. *Neural Computation* 6(15):1373–1396.
- Cai, D.; Xiaofei He, X. W.; Bao, H.; and Han, J. 2009. Locality preserving nonnegative matrix factorization. In *IJCAI*.
- Cassandra, A. R.; Littman, M. L.; and Zhang, N. L. 1997. Incremental pruning: A simple, fast, exact method for partially observable Markov decision processes. In *Uncertainty in Artificial Intelligence (UAI)*.
- Cassandra, A. 1998. *Exact and Approximate Algorithms for Partially Observable Markov Decision Processes*. Ph.D. Dissertation, Brown University.
- Chung, F. R. K. 1997. *Spectral Graph Theory (CBMS Regional Conference Series in Mathematics, No. 92) (Cbms Regional Conference Series in Mathematics)*. American Mathematical Society.

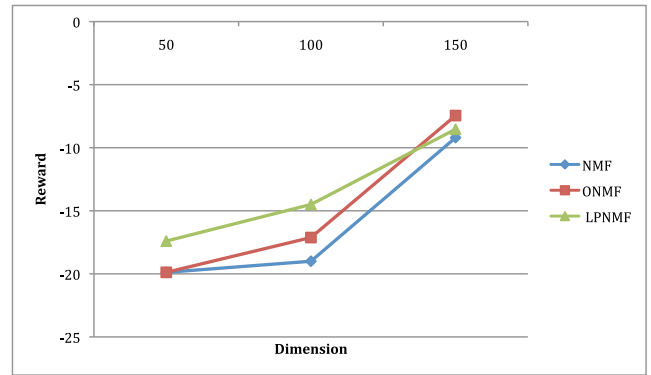


Figure 7: The tag-avoid problem has $|S| = 870$, $|A| = 5$ and $|Z| = 2$. The maximum time we ran each algorithm was 2200 sec. The graphs show the results for different dimensions and compression algorithms. The LPNMF approach allows for deeper compression than both the NMF and LPNMF algorithms.

Hsu, D.; Lee, W.; and Rong, N. 2007. What makes some POMDP problems easy to approximate. In *NIPS*.

Kaelbling, L. P.; Littman, M. L.; and Cassandra, A. R. 1998. Planning and acting in partially observable stochastic domains. *Artificial Intelligence* 101:99–134.

Lee, D. D., and Seung, H. S. 1999. Learning the parts of objects by non-negative matrix factorization. *Nature* 401(6755):788–791.

Lee, D. D., and Seung, H. S. 2001. Algorithms for non-negative matrix factorization. In *NIPS*, 556–562.

Li, X.; Cheung, W. K. W.; Liu, J.; and Wu, Z. 2007. A novel orthogonal nmf-based belief compression for POMDPs. In *ICML '07: Proceedings of the 24th international conference on Machine learning*, 537–544. New York, NY, USA: ACM.

Lusena, C.; Goldsmith, J.; and Mundhenk, M. 2001. Non-approximability results for Partially Observable Markov Decision Processes. *J. Artif. Intell. Res. (JAIR)* 14:83–103.

Pineau, J.; Gordon, G. J.; and Thrun, S. 2006. Anytime point-based approximations for large POMDPs. *Journal of Artificial Intelligence Research* 27:335–380.

Poupart, P., and Boutilier, C. 2002. Value-directed compression of POMDPs. In *In NIPS 15*, 1547–1554. MIT Press.

Smallwood, R. D., and Sondik, E. J. 1973. The optimal control of Partially Observable Markov Processes over a finite horizon. *Operations Research* 21(5):1071–1088.

Smallwood, R. D., and Sondik, E. J. 1978. The optimal control of Partially Observable Markov Processes over the finite horizon: Discounted costs. *Operations Research* 26(2):282–304.

Spaan, M. T. J., and Vlassis, N. 2005. Randomized point-based value iteration for POMDPs. *Journal of Artificial Intelligence Research* 24:195–220.