

Figure 2: Schematic overview of our two time-line models: C-TLM (solid edges), exploiting entity context, and the simpler S-TLM (dotted edges), which is context independent. The models predict a starting point (s) and duration (d) for each given temporal entity $(t_1, e_1, and t_2)$ in the input.

In contrast, DCT duration $d_{\rm DCT}$ is modeled as a single variable that is learned (initialized with 1). Since multiple entities may be included in the DCT, and entities have a minimum duration d_{min} , a constant $d_{\rm DCT}$ could possibly prevent the model from fitting all entities in the DCT. Modeling $d_{\rm DCT}$ as a variable allows growth of $d_{\rm DCT}$ and averts this issue.³

Training Losses

We propose three loss functions to train time-line models from TimeML-style annotations: a regular time-line loss L_{τ} , and two slightly expanded discriminative time-line losses, $L_{\tau ce}$ and $L_{\tau h}$.

Regular Time-line Loss (L_{τ})

Ground-truth TLinks can be seen as constraints on correct positions of entities on a time-line. The regular time-line loss L_{τ} expresses the degree to which these constraints are met for a predicted time-line. If all TLinks are satisfied in the time-line for a certain text, L_{τ} will be 0 for that text.

As TLinks relate entities (intervals), we first convert the TLinks to expressions that relate the start and end points of entities. How each TLink is translated to its corresponding point-algebraic constraints is given in Table 1, following Allen (1990).

As can be seen in the last column there are only two point-wise operations in the point-algebraic constraints: an order operation (<), and an equality operation (=). To model to what degree each point-wise constraint is met, we employ hinge losses, with a margin m_{τ} , as shown in Eq. 2.

Table 1: Point algebraic interpretation (I_{PA}) of temporal links used to construct the loss function. The start and end points of event X are indicated by s_x and e_x respectively.

Allen Algebra	Temporal Links	Point Algebra
X precedes Y Y preceded by X	X before Y Y after X	$e_x < s_y$
X starts Y Y started by X	X begins Y Y begun by X	$s_x = s_y$ $e_x < e_y$
X finishes Y Y finished by X	X ends Y Y ended by X	$e_x = e_y$ $s_y < s_x$
X during Y Y includes X	X is included Y Y includes X	$s_y < s_x \\ e_x < e_y$
X meets Y Y met by X	X immediately before Y Y immediately after X	$e_x = s_y$
X overlaps Y Y overlapped by X	absent ⁴ absent ⁴	$s_x < s_y$ $s_y < e_x$ $e_x < e_y$
X equals Y	X simultaneous Y X identity Y	$s_x = s_y$ $e_x = e_y$

To explain the intuition and notation: If we have a point-wise expression ξ of the form x < y (first case of Eq. 2), then the predicted point \hat{x} should be at least a distance m_{τ} smaller (or earlier on the time-line) than predicted point \hat{y} in order for the loss to be 0. Otherwise, the loss represents the distance \hat{x} or \hat{y} still has to move to make \hat{x} smaller than \hat{y} (and satisfy the constraint). For the second case, if ξ is of the form x = y, then point \hat{x} and \hat{y} should lie very close to each other, i.e. at most a distance m_{τ} away from each other. Any distance further than the margin m_{τ} is counted as loss. Notice that if we set margin m_{τ} to 0, the second case becomes an L1 loss $|\hat{x} - \hat{y}|$. However, we use a small margin m_{τ} to promote some distance between ordered points and prevent con-

 $^{^3}$ Other combinations of modeling $s_{
m DCT}$ and $d_{
m DCT}$ as variable or constant decreased performance.

⁴No TLink for Allen's overlap relation is present in TimeML, also concluded by UzZaman and Allen (2011).