

| # sent. | MLE      |        | MRE      |        |
|---------|----------|--------|----------|--------|
|         | accuracy | VI     | accuracy | VI     |
| 10,000  | 0.5087   | 3.3471 | 0.5825   | 2.9018 |
| 20,000  | 0.5390   | 3.2387 | 0.5874   | 2.9217 |
| 30,000  | 0.5556   | 3.0764 | 0.6000   | 2.7904 |
| 40,000  | 0.5800   | 3.0117 | 0.6112   | 2.7403 |

Table 2: Effect of training corpus size.

| MLE    | MRE    |
|--------|--------|
| 0.2077 | 0.4632 |
| 0.1514 | 0.0773 |
| 0.0371 | 0.0326 |
| 0.0312 | 0.0198 |
| 0.0307 | 0.0195 |
| 0.0237 | 0.0158 |
| 0.0203 | 0.0119 |
| 0.0169 | 0.0106 |
| 0.0129 | 0.0102 |
| 0.0129 | 0.0101 |

Table 3: Example emission probabilities for the POS tag “VBD” (verb past tense).

| # state | CRF Autoencoders |        | MRE      |        |
|---------|------------------|--------|----------|--------|
|         | accuracy         | VI     | accuracy | VI     |
| 10      | 0.4059           | 2.7145 | 0.3881   | 2.9322 |
| 20      | 0.4657           | 2.7462 | 0.5203   | 2.8879 |
| 30      | 0.5479           | 2.9585 | 0.5653   | 2.8199 |
| 40      | 0.5377           | 3.1048 | 0.6191   | 2.9255 |
| 50      | 0.5662           | 2.8450 | 0.6739   | 2.7522 |

Table 4: Comparison between CRF Autoencoders and MRE on unsupervised part-of-speech induction.

training corpus size for both MLE and MRE. The case for VI is similar. We find that our approach outperforms MLE consistently.

Table 3 shows example emission probabilities (e.g.,  $p(x|z)$ ) for the POS tag “VBD” (verb past tense). We follow Johnson (2007) to deterministically map hidden states to POS tags based on co-occurrence. As shown in Table 3, we find that MLE is prone to learn common but irrelevant correlations in the data (e.g., frequent words such as “,” “,” and “is”). In contrast, MRE is capable of identifying “said”, “reported”, “announced”, “noted”, “gained”, and “told” correctly, suggesting that MRE enables HMMs to better discover intended correlations in the data.

**Comparison with CRF Autoencoders** We also compare our approach with CRF Autoencoders (Ammar, Dyer, and Smith 2014), which also builds on an encoding-reconstruction framework but allows for incorporating features. A surprising finding is that CRF Autoencoders achieves the highest accuracy with 50 states but obtains the lowest VI with 10 states. Our approach achieves the best accuracy and VI both with 50 states. While our approach slightly lags behind CRF Autoencoders in terms of VI, the improvements in terms of accuracy are statistically signifi-

| criterion | model   | C → E | E → C |
|-----------|---------|-------|-------|
| MLE       | Model 1 | 43.07 | 45.89 |
|           | Model 2 | 40.28 | 42.38 |
| MRE       | Model 1 | 41.90 | 45.39 |
|           | Model 2 | 38.33 | 41.73 |

Table 5: Comparison between MLE and MRE on IBM translation models for unsupervised word alignment. The evaluation metric is alignment error rate (AER).

|         | MLE    |           | MRE    |
|---------|--------|-----------|--------|
| article | 0.4932 | article   | 0.5428 |
| the     | 0.1924 | articles  | 0.0995 |
| says    | 0.0586 | says      | 0.0624 |
| points  | 0.0293 | published | 0.0497 |
| an      | 0.0263 | points    | 0.0349 |

Table 6: Example translation probabilities of the Chinese word “wenzhang”.

cant ( $p < 0.01$ ).

## Evaluation on Word Alignment

**Setting** We used the FBIS corpus as the training corpus, which contains 240K Chinese-English parallel sentences with 6.9M Chinese words and 8.9M English words. We used the TsinghuaAligner development and test sets (Liu and Sun 2015), which both contain 450 sentence pairs with gold-standard annotations. The evaluation metric is *alignment error rate* (AER) (Och and Ney 2003). Both MLE and MRE use the following training scheme: 5 iterations for IBM Model 1 and 5 iterations for IBM Model 2. As IBM Model 1 is a simplified version of IBM Model 2, the parameters of Model 1 at iteration 5 are used to initialize Model 2. We distinguish between two translation directions: Chinese-to-English ( $C \rightarrow E$ ) and English-to-Chinese ( $E \rightarrow C$ ).

**Comparison with MLE** Table 5 shows the comparison between MLE and MRE. We find that MRE outperforms MLE for both translation directions. All the differences are statistically significant ( $p < 0.01$ ).

Table 6 shows example translation probabilities (i.e.,  $p(x|y)$ ) of the Chinese word “wenzhang” (i.e., “article”). We find that MLE tends to identify frequent words such as “the” and “an” as candidate translations while MRE finds more relevant candidate translations. This finding further confirms that MRE is more robust to common but irrelevant correlations.

**Comparison with CRF Autoencoders** On the same dataset, CRF Autoencoders achieve much lower AERs: 32.54 for  $C \rightarrow E$  and 29.81 for  $E \rightarrow C$ , respectively. The reason is that CRF Autoencoders are a discriminative latent-variable model capable of including more expressive IBM Model 4 as features. In contrast, our approach focuses on providing better training criterion for generative latent-