E			≥ 0. 01			
Data sets	ER. (gars)	EF	5-CV	L00	CKTA	ES M
austr alian	14.0V-2.10	14-20 / 1 95	14-78 - 1.87	14 30 / 1 85	13.98 / 2.10	44 15 23.30
heart	17.08 + 3.28	18.56 + 3.59	16.91 + 3.64	16.71 ± 3.29	16.75 + 3.50	44.65±4.35
ionosphere	8.981 2.39	9.65 2.58	5.9711.58	6.32 12.33	32.80 ± 8.71	35.68 ± 3.13
breast-cancer	3.59 0.97	3.72 + 1.04	3.77 - 1.09	3.61 0.94	31.72 ± 9.40	4.36±0.93
diabetes	22 30 + 2 30	22 81 12 67	22 13 +2 60	72.06 + 2.31	35.00 + 2.87	35.00 2.87
german <mark>.nu</mark> mer	23.76 + 2.34	26.14 ± 1.70	24.11 ± 2.16	24.14 ± 2.31	30.36 ± 2.57	30.36 ± 2.57
liver-disorders	28.56 ± 3.75	30.80 ± 3.40	29.17 ± 4.24	29.04 ± 4.37	36.83 ± 6.53	40.83 ± 1.72
a2a	17.74 ± 0.95	19.22 ± 1.07	17.80 ± 1.03	17.67 ± 0.90	25.21 ± 1.40	25.21 ± 1.40
						
austr alian	13.46 + 1.91	13 59 + 2 03	14 5 4 2 07	14 41 +1 73	19 89 +6 18	44.15 ± 3.30
heart	16.87 + 3.39	17.12±3.46	17.08 + 3.82	17 16 13 81	40.20 10.03	44.65±4.35
ionosphere	7.07 1.2.24	0 9012 55	5 20 L1 20	K 28 L 1 02	25 75 1 2 04	25 60 12 12
breast-cancer	3.53 - 0.97	4.23 - 1.09	3.79-0.91	3.51 0.94	32.70 ± 6.57	3.84±0.81
diabetes	22.25 1.2.53	22 001-2 75	22 35 + 2 40	22 16 12 25	35.00 ±2.87	35.00 ± 2.87
german.numer	22 88 1 2 28	23.80 + 2.13	24.08 + 2.15	22 00 12 21	20 36 12 57	30.36 ± 2.57
liver-disorders	29.01 29.01 4.19	24 20 1 3 02	20 10 14 12	20.77 + 4.00	25 54 + 7 26	$\frac{30.83 \pm 2.37}{40.83 \pm 4.72}$
a2a	17 01 L1 10	18 11 1 22	17 02 1 01	17.68 ±0.07	25 21 1 40	25 21 1 1 10
	17.01 1.17	10.11-1.22	77.7	1710m = V177	23.2221.70	23.21 11.10
1:00	14 10 1 1 70	14 17 1 50		14 (1 1 0 0	44.07.12.25	44.15 2.20
austraman	14.12+1.62	14 17 +1 58	14 62 42 07	14 61 + 1 86	44 07 + 3 35	44.15 ± 3.30
heart	16.83 + 3.56	17.12±3.30 11.02±2.12	17.08 + 3.01	17.12 + 3.72	44.65±4.35	44.65 ±4.35
ionosphere	7.811-2.60	11,120,10	5.43 1.97	0.57-2-00	35.75 ± 3.04	35.68 ±3.13
breast-cancer	3.43 + 0.95	4.541 1.55	3.53+0.83	3.25 0.94	2010	3.54±0.87
diabetes	20 20 12 52	24 65 1 3 20	25 48 ± 2 22	22.10 12.20 2.20	35.00 + 2.87	35.00 12.87
german.numer	24.57 + 2.38	24.50 ± 2.47	24.24 ± 2.41	24.13 2.37	30.36 + 2.57	30.36 ± 2.57
liver-disorders	29,46 ± 3,69	41.96 ± 1.45	30.38 ± 3.99	30.87 ± 3.42	36.10±6.09	40.83 ± 1.72
a2a	18.17±1.23	18.66±1.31	18.01 ± 1.00	17.83 ± 1.08	25.21 ±1.40	25.21 ± 1.40
/						
austr alian	-13.85 + 1.88	14.19 + 1.71	14.53 + 1.73	14.35 ± 2.06	44.07 ± 3.35	44.07 ± 3.35
heart	17.04 ± 3.62	17.37 ± 3.59	16.70 13.44	17.04 + 3.36	44,65 + 4.35	44.65±4.35
ionosphere	8.894-2.63	14,22 13.74	6.92¥ 1.87	6.76 1.88	36.06 ± 3.06	36.06±3.06
breast-cancer	3.24 - 0.89	5.711-1.59	3.37 - 0.93	3.22 - 1.08	35.04 ± 2.45	3.61 + 0.88
diabetes	23.41 + 3.07	24 00/ 3 13	22.00 12.78	22.54 ± 2.51	35.00 +2.87	35.00 + 2.87
german.numer	27.13 + 2.65	29.64 ± 3.30	26.94 ± 2.86	26.86 + 2.87	30.36 + 2.57	30.36 ± 2.57
liver-dis orders	34,07 + 1,47	41.80 + 4.39	35.35 + 4.46	35.13 + 1.49	39.26 + 4.74	41.86±4.46
a2a	18.79 ± 1.19	-19.26 ± 1.60	18.77±1.21	18.71 + 1.21	25.23 ± 1.43	25.23 ± 1.43
	101171112	12,12021,00				

Table 1: Comparison of mean test errors between our eigenvalues ratio criterion (ER) and other ones including 5-CV, LOO, CKTA, FSM and EP. We bold the numbers of the best method, and underline the numbers of the other methods which are not significantly worse than the best one.

where $C_4 = 12hBk\sqrt{2\kappa}$, $C_5 = 96h^2Bkt + (96k + 22M + 5Bk)\log(3/\delta)$, h = 2(M+D), $C_6 = (D+M)^2/(k-1)$, $B = (D+M)^2$.

The idea of proof is same as that of Theorem 2.

The convergence rate of KRR is $O\left(1/\sqrt{n\beta_t}+1/n\right)$. Under the assumption of algebraically decreasing eigenvalues, the converges rate can reach O(1/n). This theorem also indicates that the kernel with small $R_{\rm emp}(S)$ and $1/\beta_t$ can guarantee good generalization performance.

Least Squares Support Vector Machine (LSSVM)

LSSVM is a popular classifier which has the same loss function as that of KRR. Thus, applying Theorem 3 with M=1, we can obtain the following corollary:

Corollary 1. If the t-eigenvalues ratio of K is β_t , then for

LSSVM, with probability at least
$$1 - \delta$$
, for any $k > 1$,
$$R(S) \leq R_{\rm emp}(S) + C_7 \sqrt{1/(n\beta_t)} + C_8/n + C_9,$$
 where $C_7 = 12hk\sqrt{2\kappa}$, $C_8 = 96Bh^2kt + (96k + 22 + 5Bk)\log(3/\delta)$, $h = 2(1+D)$, $C_9 = (1+D)^2/(k-1)$, $B = (D+1)^2$.

Kernel Selection with Eigenvalues Ratio

In this section, we will present a novel kernel selection criterion with ER to guarantee good generalization performance.

From the generalization error bounds derived in above section, to guarantee good generalization performance, we can choose the kernel function by minimizing $R_{\text{emp}}(S)$ and $1/\beta_t$. Thus, we apply the following eigenvalues ratio criterion for kernel selection:

$$\underset{K \in \mathcal{K}}{\operatorname{arg\,min}} R_{\operatorname{emp}}(S) + \eta \cdot n/\beta_t =: KS(K)$$