

$$\mathbb{E}_t \Delta s_{t,t+k} = \Omega_{0,k} + \Omega_{1,k} Y_t - \Omega_{1,k}^* Y_t^* + \frac{1}{2} \left(Y_t' \Omega_{2,k} Y_t - Y_t^{*'} \Omega_{2,k}^* Y_t^* \right) + \Xi_{t+k},$$

where

$$\begin{aligned} \Omega_{0,k} \equiv & k(\rho_0 - \rho_0^*) + \rho_1' \sum_{j=2}^k \sum_{i=1}^{j-1} (I + K_1^{\mathbb{P}})^{i-1} K_0^{\mathbb{P}} \\ & - \rho_1^{*'} \sum_{j=2}^k \sum_{i=1}^{j-1} (I + K_1^{*\mathbb{P}})^{i-1} K_0^{*\mathbb{P}} \\ & + \frac{1+k}{2} \Lambda_0' \Sigma'^{-1} \Sigma^{-1} \Lambda_0 - \frac{1+k}{2} \Lambda_0^{*'} \Sigma^{*-1} \Sigma^{*-1} \Lambda_0^* \\ & + \Lambda_0' \Sigma'^{-1} \Sigma^{-1} \Lambda_1 \sum_{j=2}^k \sum_{i=1}^{j-1} (I + K_1^{\mathbb{P}})^{i-1} K_0^{\mathbb{P}} \\ & - \Lambda_0^{*'} \Sigma^{*-1} \Sigma^{*-1} \Lambda_1^* \sum_{j=2}^k \sum_{i=1}^{j-1} (I + K_1^{*\mathbb{P}})^{i-1} K_0^{*\mathbb{P}} \\ & + \frac{1}{2} \sum_{j=2}^k \sum_{i=1}^{j-1} K_0^{\mathbb{P}'} (I + K_1^{\mathbb{P}})^{i-1} \Lambda_1' \Sigma'^{-1} \Sigma^{-1} \Lambda_1 \sum_{i=1}^{j-1} (I + K_1^{\mathbb{P}})^{i-1} K_0^{\mathbb{P}} \\ & - \frac{1}{2} \sum_{j=2}^k \sum_{i=1}^{j-1} K_0^{*\mathbb{P}'} (I + K_1^{*\mathbb{P}})^{i-1} \Lambda_1^{*'} \Sigma^{*-1} \Sigma^{*-1} \Lambda_1^* \sum_{i=1}^{j-1} (I + K_1^{*\mathbb{P}})^{i-1} K_0^{*\mathbb{P}} \end{aligned}$$

$$\begin{aligned} \Omega_{1,k} \equiv & \left(\rho_1' + \Lambda_0' \Sigma'^{-1} \Sigma^{-1} \Lambda_1 \right) \left(I + \sum_{j=2}^k (I + K_1^{\mathbb{P}})^{j-1} \right) \\ & + \sum_{j=2}^k \sum_{i=1}^{j-1} K_0^{\mathbb{P}'} (I + K_1^{\mathbb{P}})^{i-1} \Lambda_1' \Sigma'^{-1} \Sigma^{-1} \Lambda_1 (I + K_1^{\mathbb{P}})^{j-1} \end{aligned}$$

$$\begin{aligned} \Omega_{1,k}^* \equiv & \left(\rho_1^{*'} + \Lambda_0^{*'} \Sigma^{*-1} \Sigma^{*-1} \Lambda_1^* \right) \left(I + \sum_{j=2}^k (I + K_1^{*\mathbb{P}})^{j-1} \right) \\ & + \sum_{j=2}^k \sum_{i=1}^{j-1} K_0^{*\mathbb{P}'} (I + K_1^{*\mathbb{P}})^{i-1} \Lambda_1^{*'} \Sigma^{*-1} \Sigma^{*-1} \Lambda_1^* (I + K_1^{*\mathbb{P}})^{j-1} \end{aligned}$$

$$\Omega_{2,k} \equiv \Lambda_1' \Sigma'^{-1} \left(I + \sum_{j=2}^k (I + K_1^{\mathbb{P}})^{j-1} (I + K_1^{\mathbb{P}})^{j-1} \right) \Sigma^{-1} \Lambda_1$$

$$\Omega_{2,k}^* \equiv \Lambda_1^{*'} \Sigma^{*-1} \left(I + \sum_{j=2}^k (I + K_1^{*\mathbb{P}})^{'j-1} (I + K_1^{*\mathbb{P}})^{j-1} \right) \Sigma^{*-1} \Lambda_1^*$$

$$\begin{aligned} \Xi_{t+k} \equiv & \text{trace} \left(\frac{1}{2} \sum_{j=2}^k \sum_{i=1}^{j-1} \Sigma' (I + K_1^{\mathbb{P}})^{'i-1} \Lambda_1' \Sigma'^{-1} \Sigma^{-1} \Lambda_1 \sum_{i=1}^{j-1} (I + K_1^{\mathbb{P}})^{i-1} \Sigma \right) \\ & - \text{trace} \left(\frac{1}{2} \sum_{j=2}^k \sum_{i=1}^{j-1} \Sigma^{*'} (I + K_1^{*\mathbb{P}})^{'i-1} \Lambda_1^{*'} \Sigma^{*-1} \Sigma^{*-1} \Lambda_1^* \sum_{i=1}^{j-1} (I + K_1^{*\mathbb{P}})^{i-1} \Sigma^* \right) \end{aligned}$$