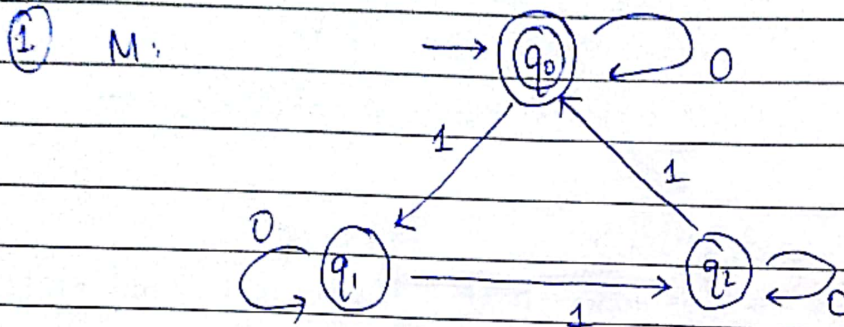


MC-304

THEORY OF COMPUTATION.



(a) 01110  $\delta(q_0, 01110) = \delta(q_0, 1110) = \delta(q_1, 110)$   
 $= \delta(q_2, 10) = \delta(q_0, 0) = q_0$

Hence 01110 is accepted as  $q_0$  is a final state

(b) 10001  $\delta(q_0, 10001) = \delta(q_1, 0001) = \delta(q_1, 001) = \delta(q_1, 01)$   
 $= \delta(q_1, 1) = q_2$

Hence  $q_2$  is not accepted as  $q_2$  is not a final state.

(c) 01010  $\delta(q_0, 01010) = \delta(q_0, 1010) = \delta(q_1, 010) = \delta(q_1, 10)$   
 $= \delta(q_2, 0) = q_2$

Not accepted

(d) 11111  $\delta(q_0, 11111) = \delta(q_1, 1111) = \delta(q_2, 111) = \delta(q_3, 11)$   
 $= \delta(q_1, 1) = \delta(q_2, \Lambda) = q_2$   
 Not accepted.

(ii) (a) 0110 and 01100

0110 is accepted as seen above

$$\begin{aligned} \delta(q_0, 01100) &= \delta(q_0, 1100) = \delta(q_1, 100) = \delta(q_2, 00) \\ &= \delta(q_2, 0) = \delta(q_2, 1) = q_2 \end{aligned}$$

As  $q_2$  is a final state 01100 is also accepted.

(b) 10001 and 10000

As seen in previous part 10001 has final state  $q_2$  so it is accepted.

$$\begin{aligned} \delta(q_0, 10000) &= \delta(q_1, 0000) = \delta(q_1, 000) = \delta(q_1, 00) \\ &= \delta(q_1, 0) = q_1 \end{aligned}$$

As  $q_1$  is not final it is not accepted.

(c) 0110 and 011101

$$\delta(q_0, 0110) = \delta(q_0, 110) = \delta(q_1, 10) = \delta(q_2, 0) = q_2$$

It is accepted

$$\begin{aligned} \delta(q_0, 011101) &= \delta(q_0, 111101) = \delta(q_1, 11101) = \delta(q_2, 1101) \\ &= \delta(q_0, 101) = \delta(q_1, 01) = \delta(q_1, 1) = q_2 \end{aligned}$$

It is accepted

So 0110 and 011101 are accepted.

(d)  $0^{2n}$   $n \geq 1$  but not  $1^{2n}$   $n \geq 1$  $0^{2n} = 00000 \dots$  Accepted as always  $q_0$  $1^{2n} = 1111 \dots$  Depends on number

Hence false.



(Q.) Let us make the following states

$q_0$  = No money collected

$q_1$  = 5 cents collected

$q_2$  = 10 cents collected

$q_3$  = 15 cents collected

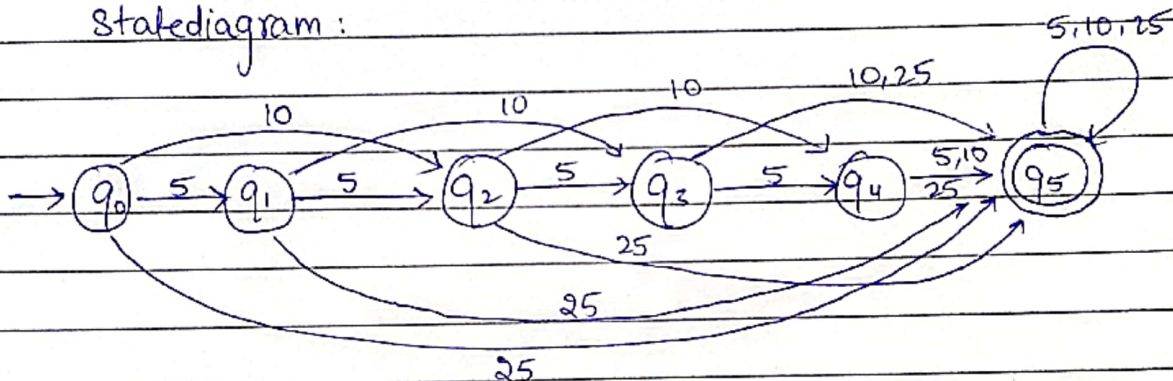
$q_4$  = 20 cents collected

$q_5$  = 25 cents collected.

$$Q = \{q_0, q_1, q_2, q_3, q_4, q_5\}$$

$$\Sigma = \{5, 10, 25\} \quad q_0 = \{q_0\} \quad F = \{q_5\}$$

State diagram:



Since no change is given all extra money also takes us to  $q_5$ .

Next State

Present State	$a=5$	$a=10$	$a=25$
$q_0$	$q_1$	$q_2$	$q_5$
$q_1$	$q_2$	$q_3$	$q_5$
$q_2$	$q_3$	$q_4$	$q_5$
$q_3$	$q_4$	$q_5$	$q_5$
$q_4$	$q_5$	$q_5$	$q_5$
$q_5$	$q_5$	$q_5$	$q_5$