

Date

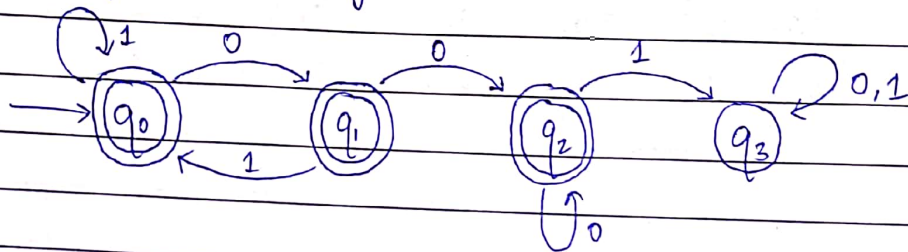
THEORY OF COMPUTATION

MC-304

ASSIGNMENT-1

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2K18/MC/008

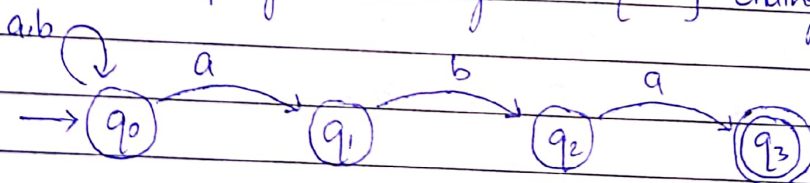
- ① DFA that accepts all strings over $\{0,1\}$ except those containing the substring 001:



State Table:

	0	1
$\rightarrow q_0$	q_1	q_0
q_1	q_2	q_0
q_2	q_2	q_3
q_3	q_3	q_3

- ② NDFA accepting the strings over $\{a,b\}$ ending in aba



$$M = (\{q_0, q_1, q_2, q_3\}, \{a, b\}, \delta, q_0, \{q_3\})$$

$$\text{Let } Q = \{q_0, q_1, q_2, q_3\}$$

A DFA accepting the same set of strings is:

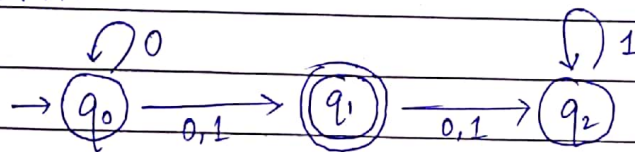
$$M' = (Q, \{a, b\}, s', [q_0], F)$$

where $F = ([q_3], [q_3, q_0], [q_3, q_1], [q_3, q_2], [q_3, q_0, q_1], [q_3, q_0, q_2], [q_3, q_1, q_2], [q_3, q_0, q_1, q_2])$

State Table:

State Σ	a	b
$\rightarrow [q_0]$	$[q_0, q_1]$	$[q_0]$
$[q_0, q_1]$	$[q_0, q_1]$	$[q_0, q_2]$
$[q_0, q_2]$	$[q_0, q_1, q_3]$	$[q_0]$
$[q_0, q_1, q_3]$	$[q_0, q_1]$	$[q_0, q_2]$

(3) NDFA:



$$M = (Q, \{0, 1\}, s, q_0, \{q_1\})$$

where $Q = \{q_0, q_1, q_2\}$

State Table

State Σ	0	1
$\rightarrow q_0$	q_0, q_1	q_1
(q_1)	q_2	q_2
q_2		q_2

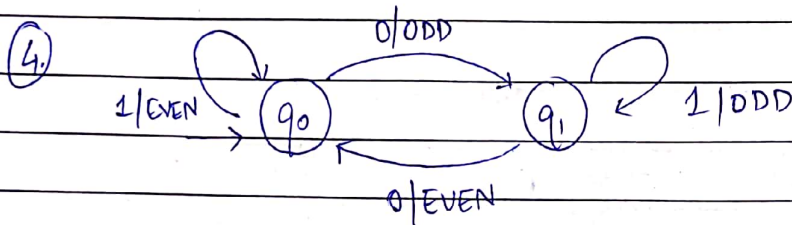
Corresponding DFA:

$$M' = (Q, \{0, 1\}, s', [q_0], F)$$

where $F = (\{q_1\}, [q_1, q_0], [q_1, q_2], [q_1, q_0, q_2])$

and δ' is defined by state table:

State / Σ	0	1
$\rightarrow [q_0]$	$[q_0, q_1]$	$[q_1]$
$[q_0, q_1]$	$[q_0, q_1, q_2]$	$[q_1, q_2]$
$[q_1]$	$[q_2]$	$[q_2]$
$[q_0, q_1, q_2]$	$[q_0, q_1, q_2]$	$[q_1, q_2]$
$[q_1, q_2]$	$[q_2]$	$[q_2]$
$[q_2]$	\emptyset	$[q_2]$



State Table:

Present State	Next State	
	Input $a=0$ state Output	Input $a=1$ state Output
$\rightarrow q_0$	q_1 ODD	q_0 EVEN
q_1	q_0 EVEN	q_1 ODD

⑤ Since q_2 and q_3 are associated with different outputs, we split them into q_{20}, q_{21} and q_{30}, q_{31} respectively. The table can be reconstructed as:

Present / Next	$a=0$		$a=1$	
$\rightarrow q_1$	q_1	1	q_{20}	0
q_{20}	q_4	1	q_4	1
q_{21}	q_4	1	q_4	1
q_{30}	q_{21}	1	q_{31}	1
q_{31}	q_{21}	1	q_{31}	1
q_4	q_{30}	0	q_1	1

Corresponding Moore Machine:

Present State	Next State		Output
	a=0	a=1	
→ q ₁	q ₁	q ₂₀	1
q ₂₀	q ₄	q ₄	0
q ₂₁	q ₄	q ₄	1
q ₃₀	q ₂₁	q ₃₁	0
q ₃₁	q ₂₁	q ₃₁	1
q ₄	q ₃₀	q ₁	1

⑥ Mealy Machine:

Present State	Next State		Output
	a=0 State	a=1 State	
→ q ₀	q ₁	q ₂	1
q ₁	q ₃	q ₂	1
q ₂	q ₂	q ₁	0
q ₃	q ₀	q ₃	1

⑦

State	Input	
	a	b
→ q ₀	q ₀	q ₃
q ₁	q ₂	q ₅
q ₂	q ₃	q ₄
q ₃	q ₀	q ₅
q ₄	q ₀	q ₆
q ₅	q ₁	q ₄
q ₆	q ₁	q ₃

$$\pi_0 = \{ \{q_6\}, \{q_0, q_1, q_2, q_3, q_4, q_5\} \}$$

$$\pi_1 = \{ \{q_6\}, \{q_0, q_1, q_2, q_3, q_5\}, \{q_4\} \}$$

$$\pi_2 = \{ \{q_6\}, \{q_0, q_1, q_2\}, \{q_3, q_5\}, \{q_4\} \}$$

$$\pi_3 = \{ \{q_6\}, \{q_0\}, \{q_1\}, \{q_3\}, \{q_2, q_5\}, \{q_4\} \}$$

$$\pi_4 = \{ \{q_6\}, \{q_0\}, \{q_1\}, \{q_3\}, \{q_2\}, \{q_5\}, \{q_4\} \}$$

Hence the minimum state automaton is same as the given automata.

8. Transition table for the given automata.

State	Input	
	0	1
→ q ₀	q ₁	q ₃
q ₁	q ₀	q ₃
q ₂	q ₁	q ₄
q ₃	q ₅	q ₅
q ₄	q ₃	q ₃
q ₅	q ₅	q ₅

$$\pi_0 = \{ \{q_3, q_5\}, \{q_0, q_1, q_2, q_4\} \}$$

$$\pi_1 = \{ \{q_3, q_5\}, \{q_0, q_1\}, \{q_2\}, \{q_4\} \}$$

$$\pi_2 = \{ \{q_3, q_5\}, \{q_0, q_1\}, \{q_2\}, \{q_4\} \}$$

As $\pi_1 = \pi_2$, π_1 gives us the equivalence classes

Minimum State Automata:

$$M' = (Q', \{0, 1\}, \delta', q_0', F')$$

where

$$Q' = \{[q_3, q_5], [q_0, q_1], [q_2], [q_4]\}$$

$$q_0' = [q_0, q_1]$$

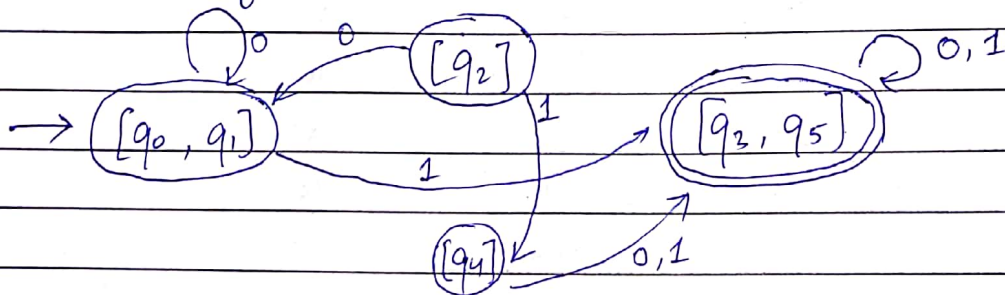
$$F' = [q_3, q_5]$$

and

δ' is defined by the following table:

State / Σ	0	1
$\rightarrow [q_0, q_1]$	$[q_0, q_1]$	$[q_3, q_5]$
$[q_2]$	$[q_0, q_1]$	$[q_4]$
$[q_3, q_5]$	$[q_3, q_5]$	$[q_3, q_5]$
$[q_4]$	$[q_3, q_5]$	$[q_3, q_5]$

Transition diagram:



- ⑩ DFAs can be used for Artificial Intelligence language. State machines are certainly not the most sophisticated means of implementing artificially intelligent agents in games, but many games include characters with simple, state-based behaviours that are easily and effectively modeled using state machines.

For example, the classic game of Pac-Man.

The ghosts in Pac-Man have four behaviours and their transitions are dictated by the situation in the game. Hence its an application of DFA.

Another application of DFA is Markov Chain which is widely used in probability and statistics. Rather than fixed transition rules, we have probabilistic rules.

(9.) let M be the finite Automata

$$M = (Q, \Sigma, \delta, q_0, F)$$

where $Q =$ $q_0 \equiv$ Nothing is done

$q_a \equiv$ Stove is lit

$q_b \equiv$ Water is boiled

$q_c \equiv$ filter has water

$q_d \equiv$ filter holder has the filter

$q_e \equiv$ ground coffee is in filter

$q_f \equiv$ filter holder over cup

$q_g \equiv$ Coffee is prepared

$q_h \equiv$ Mess is made

$$\Sigma = \{a, b, c, d, e, f, g\}$$

$$F = \{q_g\}$$

Transition diagram:

