

Ensemble Learning: Decision Trees

AAA-Python Edition



Plan

- 1- Decision Trees
- 2- Impurity
- 3- Mechanisms of binary decision trees
- 4- Decision Tree classifier example
- 5- Decision Tree regressor example
- 6- Visualization



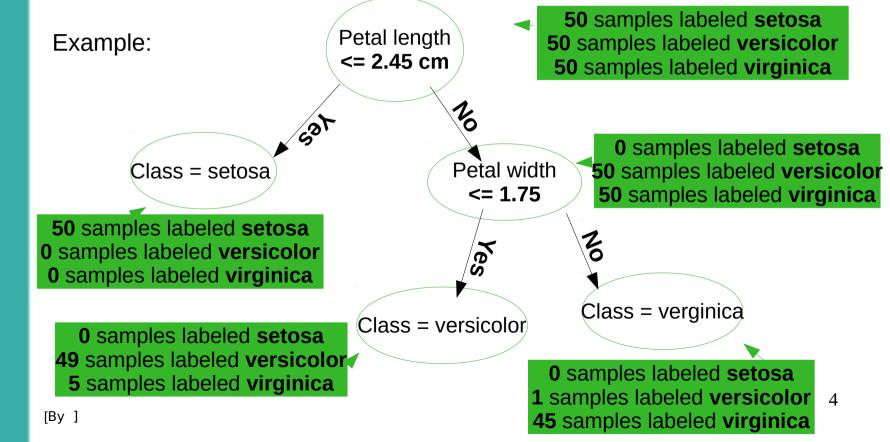
Concept

- Decision Trees are an other type of learning models. Trained on labeled data.
- They are used for both classification and regression.
- The model is trained, by spliting the dataset in order to reduce their impurity using a tree structure.
- The non-leaf nodes are the decision nodes: they perform a test or apply a rule on feature values. The result of the test will split the data into other sets ==> other nodes
- The leaf nodes: are **non splittable** nodes. They represent the final result of the classification or the regression.



Binary Decision Trees

In a binary decision trees: each node will split the data into 2 sets.





Decision Trees in scikit-learn

- Scikit-learn implement an optimized version of the Classification And Regression Tree (CART) algorithm.
- It is a Binary tree that uses one feature to be tested regarding one threshold to split the data.
- The chosen feature and threshold are those which minimize the impurity value after each split <==> information gain
- The impurity caluclation formula, can be considered as the cost function.
- For classification, scikit-learn implements the following impurity measures: **gini**, **entropy** and **miclassification** measures.
- For regression, it implements these measures: the mean squared and mean absolute errors.





Entropy

 $p_{mk} = 1/N_m * \sum_{x_i \in R_m} I(y_i = k)$

Entropy value for a node:

$$H(X_m) = -\sum_k p_{mk} \log_2(p_{mk})$$

From the Previous example

$$H(X_{left}) = -0 - 0.907*log_2(0.907) - 0.093*log_2(0.093)$$

= 0.446

Entropy value for the partition

$$J = rac{N_{left}}{(N_{left} + N_{right})} * H(X_{left.node}) + rac{N_{right}}{(N_{left} + N_{right})} * H(X_{right.node})$$

J=
$$54/(54+46) * 0.446 + 46/(54+46) * H(Xright) = 0.24 + 0.46 * H(Xright)$$

Parent node

$$P_{\text{0left}} = 0/(0+49+5) = 0/54 = 0$$

 $P_{\text{1left}} = 49/(0+49+5) = 0.907$
 $P_{\text{2left}} = 5/(0+49+5) = 0.093$

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With the convention:

 $0 \cdot \log_2(0) = 0$





Gini

$$p_{mk} = 1/N_m * \sum_{x_i \in R_m} I(y_i = k)$$

Gini measure for a node:

$$H(X_m) = \sum_k p_{mk} (1 - p_{mk}) = 1 - \sum_k p_{mk}^2$$

From the previous example

$$H(X_{loft}) = 1 - 0^2 - (0.907)^2 - (0.093)^2 = 0.169$$

$$P_{\text{oleft}} = 0/(0+49+5) = 0/54 = 0$$

$$P_{1leff} = 49 / (0+49+5) = 0.907$$

$$P_{2left} = 5 / (0+49+5) = 0.093$$

Gini value for the partition

$$J = rac{N_{left}}{(N_{left} + N_{righ})} * H(X_{left.node}) + rac{N_{right}}{(N_{left} + N_{righ})} * H(X_{right.node})$$

J=
$$54/(54+46) * 0.169+ 46/(54+46) * H(Xright)=$$

= $0.09 + 0.46 * H(Xright)$





Mean and absolute Square Error

$${ar y}_m = rac{1}{N_m} \sum_{i \in N_m} y_i$$

Mean squared error for a node:

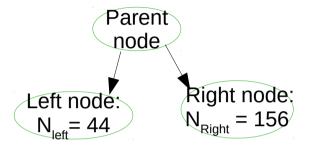
$$H(X_m) = rac{1}{N_m} \sum_{i \in N_m} (y_i - {ar y}_m)^2$$

Mean absolute error for a node:

$$H(X_m) = rac{1}{N_m} \sum_{i \in N_m} |y_i - ar{y}_m|$$

Error at the partition

$$J = rac{N_{left}}{(N_{left} + N_{righ})} * H(X_{left.node}) + rac{N_{right}}{(N_{left} + N_{righ})} * H(X_{right.node})$$



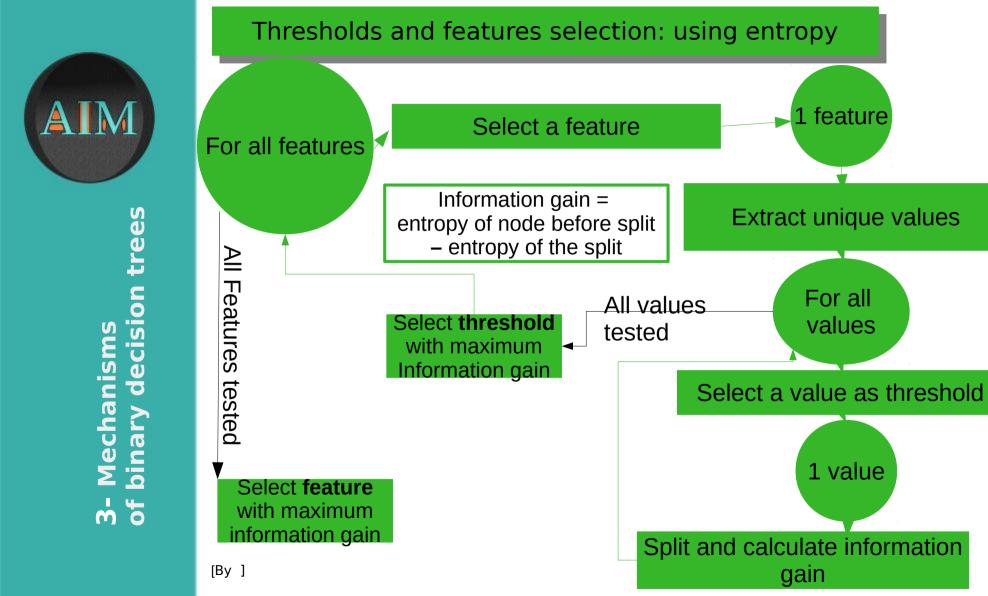
We suppose that:

$$\sum_{i=1}^{++} y_i = 0.69$$

So: $y_{\text{left}}^- = (1/44)*0.69=0.157$

And :
$$H(X_{left}) = 1/44*$$

$$\sum_{i=1}^{1} (y_i - 0.157)^2$$





Mechanisms binary decision

Training

- After the selection of the (feature, threshold) pair, the root node is split into 2 other nodes using that pair.
- The process is repeated for the new nodes until:
 - Max depth of the tree is reached (the number of levels) or
 - Min samples by node is reached or
 - Other parameters or
 - No other split that reduces impurity is possible.
 - A value is attributed to each final node (the leaf):
 - For a classification: it is a class number that represents the most represented class in that node.
 - For a regression: it is the average values of the y labels corresponding to all the samples belonging to that node. 10

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Predicting

- You start from the root: you compare the values of the features selected in that node with the threshold value of the noce.
- The result : if it is True you go to the left, else you go to the right node.
- You repeat this process, until you rich a leaf.

Classification

- If you are doing classification, the predicted class for your sample, will be the class corresponding to that leaf.
- A probability of belonging to that class can be computed: count of samples belonging to that class (in that node) / count of all samples (in that node)

Regression

If your are doing a regression, the predicted value will be the value related to that leaf.



Training

```
#import iris plant datasets tools
from sklearn.datasets import load_iris

# import the decision tree classifier
from sklearn.tree import DecisionTreeClassifier

# import numpy
import numpy as np

#import train_test_split from model_selection
from sklearn.model_selection import train_test_split

myIris = load_iris()
X = myIris.data
y = myIris.target
x_train,x_test,y_train,y_test= train_test_split(X, y, test_size=0.25)
myModel = DecisionTreeClassifier(max_depth=5)
myModel.fit(X, y)
```

- max_depth: the root node's depth ==0 (level 0).
- The first split's depth ==1 (level 1), and so on.
- So, max_depth==5 means that we can not generate a tree with more than 5 levels

Iris plant database:

- 150 samples, equally distributed in 3 classes:
 - Iris-Setosa,
 - Iris-Versicolor,
 - Iris-Virginica
- Each sample is described by 4 features:
 - Sepal length
 - Sepal width
 - Petal length
 - Petal width

Other default parameters:

- criterion='gini'
- min samples leaf=1
- min samples split=2



t-Decision Tree classifier example

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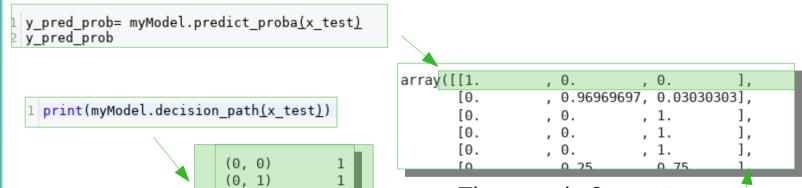
Predicting

(1, 0) (1, 2)

(1, 3)

(1, 4) (2, 0)

(2, 2)



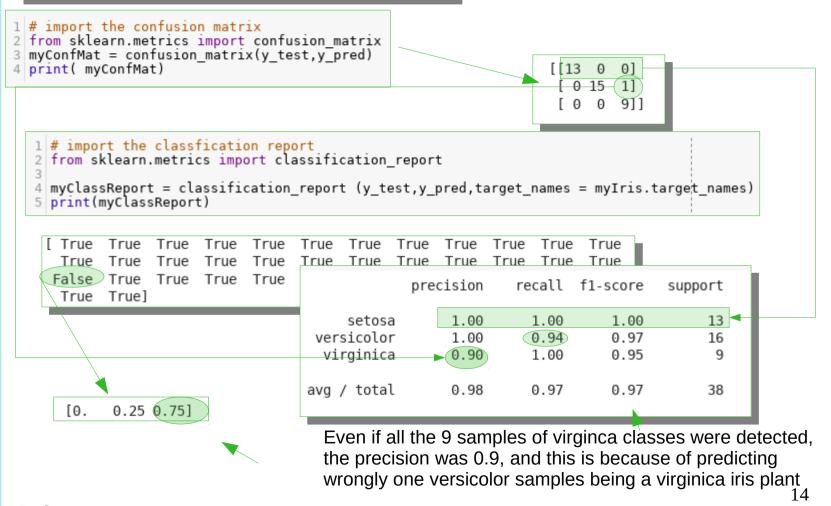
- The sample **0** went to node **0**, then to node **1**.
- The node contained only "setosa" iris plant classes.

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4-Decision Tree classifier example

Analyze the results





5- Decision Tree Regressor example

Training

```
from sklearn.datasets import make_regression
from mpl_toolkits.mplot3d import Axes3D

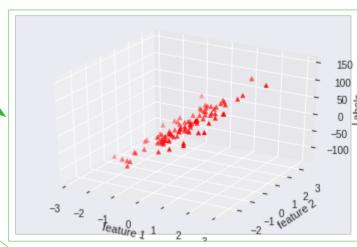
%matplotlib inline

# generate a random regression problem
xr,yr= make_regression( n_features=2)

fig=plt.figure()
ax = fig.add_subplot(111, projection='3d')

ax.scatter(xr[:,0], xr[:,1], yr,marker="^",c="r")
ax.set_xlabel('feature 1')
ax.set_ylabel('feature 2')
ax.set_zlabel("Labels")
plt.show()
```

Ploting in 3D (2 features, and y labels)



Generate random points that can be modeled by a regressor

```
from sklearn.tree import DecisionTreeRegressor

xr_train,xr_test,yr_train,yr_test= train_test_split(xr, yr, test_size=0.25)

myModelR = DecisionTreeRegressor(max_depth=6)
myModelR.fit(xr_train, yr_train)
```



5- Decision Tree Regressor example

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Predicting

```
xr new f1= np.linspace(-3,3,1000)
xr new f2= np.linspace(-3,3,1000)
xr newl = xr new fl.reshape(-1,1)
                                               The
xr_new2 = xr_new_f2.reshape(-1,1)
                                               model:different
xr_new = np.append(xr new1,xr new2,axis=1)
                                               from a regular
                                               regression
fig=plt.figure()
                                               model
vrPred1 = mvModelR.predict(xr new)
ax2 = fig.add_subplot(111, projection='3d')
ax2.scatter(xr_train[:,0],xr_train[:,1],yr_train)
ax2.set_xlabel('feature 1')
ax2.set_ylabel('feature 2')
ax2.set zlabel("Labels")
ax3 = fig.gca(projection='3d')
ax3.plot(xr new f1,xr new f2, yrPred1,c="r")
plt.tight layout()
            yrPred2 = myModelR.predict(xr test)
plt.show()
            fig=plt.figure()
            ax4 = fig.add subplot(111, projection='3d')
            ax4.scatter(xr_test[:,0],xr_test[:,1],yr_test,c="g",marker=".")
            ax4.set xlabel('feature 1')
            ax4.set_ylabel('feature 2')
            ax4.set_zlabel("Labels")
            ax4.scatter(xr_test[:,0],xr_test[:,1],yrPred2,c="r",marker="+")
            plt.tight layout()
            plt.show()
                                                                                                      16
```



5- Decision Tree Regressor example

Analyze the results

the r2 coefficient determination
myModelR.score(xr_test,yr_test)

The score is calculated as follow:

$$R^2 = 1 - \left(\frac{u}{v}\right)$$

$$u = \sum (y_{true} - y_{pred})^2$$

$$v = \sum (y_{true} - \hat{y_{true}})^2$$

 y_{true} : The true labels

 y_{pred} : The predicted labels

 $\hat{\mathcal{Y}_{true}}$: The mean of the true labels

0.9108786174105965

- If the score was near 0, we would say, that the model is not different than calculating the mean (which is a bad thing)
- If it was negative, we would say, that the model is worse than calculating the mean value
- Since its value is approaching 1 (which is the best score), we can say that the model is good.

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Graphviz

You have first to install graphviz package (system install)

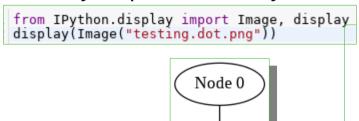
!apt-get install graphviz

1 !pip install graphviz

Then you have to install the corresponding python graphviz library

1 import graphviz

Finally, import the library



Node 1

Graphviz is a graph vizualization software. Scikitlearn enables you to export the trees into graphivz formats like .dot format.

```
import graphviz
        from graphviz import Digraph
       dot = Digraph(comment='Testing Graphviz')
        dot.node('A', 'Node 0')
       dot.node('B', 'Node 1')
dot.edge('A', 'B')
        print(dot.source)
                    // Testing Graphviz
                    digraph {
                             A [label="Node 0"]
                             B [label="Node 1"]
                             A -> B
1 dot.render('testing.dot',format = "png")
                     'testing.dot.png'
```

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Visualize a decision tree classifier

```
1 #import export graphviz to export the tree as a graphviz (graph) file
 2 from sklearn.tree import export graphviz
 4 # export to .dot file
    export graphviz(myModel,out file="iris tree.dot",feature names=myIris.feature names[:],
                         class names=myIris.target names,rounded=True,filled=True)
   from IPython.display import Image, display
                                                                     Export to a dot file
      read the dot file
   with open("iris tree.dot") as f:
         dot graph = f.read()
12
13 # create a graph from the dot file: Verbatim DOT source code string(dot graph)
14 #to be rendered by Graphviz.
                                                                                       petal length (cm) <= 2.45
    g = graphviz.Source(dot graph, format="png")
                                                                                           aini = 0.665
    # save the source and render with graphivs engine
                                                                                          samples = 112
                                                                                         value = [37, 34, 41]
                                                                                          class = virginica
    display(Image(g.render()))
                                                                                                petal width (cm) \leq 1.75
                                                                                    gini = 0.0
                                                                                                   aini = 0.496
                                                                                   samples = 37
                                                                                                   samples = 75
                                                                                  value = [37, 0, 0]
                                                                                                  value = [0, 34, 41]
                                                                                  class = setosa
                                                                                                  class = virginica
                                   The petal
[5. 3.5 1.6 0.6]
                                    length==1.6
                                                                                       oetal length (cm) <= 4.95
                                                                                                         petal length (cm) <= 4.85
                                                                                          aini = 0.193
                                    <=2.45 ==> goes
                                                                                         samples = 37
                                                                                                             samples = 38
                                                                                        value = [0, 33, 4]
                                                                                                            value = [0, 1, 37]
                                                                                        class = versicolor
                                                                                                            class = virginica
                                    to the left
                                                                             gini = 0.059
                                                                                            gini = 0.375
                                                                                                            gini = 0.444
                                    node==> classed
                                                                                                                          qini = 0.0
                                                                             samples = 33
                                                                                           samples = 4
                                                                                                            samples = 3
                                                                                                                         samples = 35
                                                                            value = [0, 32, 1]
                                                                                          value = [0, 1, 3]
                                                                                                           value = [0, 1, 2]
                                                                                                                        value = [0, 0, 35]
                                                                            class = versicolor
                                                                                          class = virginica
                                                                                                          class = virginica
                                                                                                                        class = virginica
                                    setosa.
```



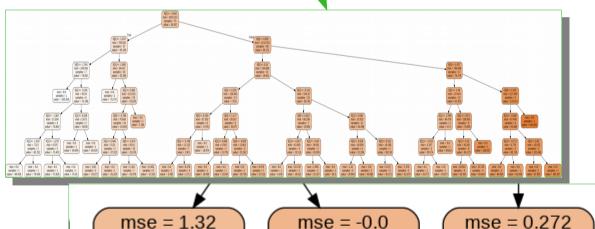
Visualize a decision tree regressor

```
# export to .dot file
export_graphviz(myModelR,out_file="iris_treeR.dot",rounded=True,filled=True)

# read the dot file
with open("iris_treeR.dot") as f:
    dot_graphR = f.read()

# create a graph from the dot file: Verbatim DOT source code string(dot_graph)
# to be rendered by Graphviz.
g2 = graphviz.Source(dot_graphR, format="png")
# save the source and render with graphivs engine

display(Image(g2.render()))
```



In the leafs we have float values instead of classes

mse = 1.32 samples = 5 value = 28.964 mse = -0.0 samples = 1 value = 42.882 mse = 0.272 samples = 3 value = 35.371 mse = 7.376 samples = 2 value = 42.279

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References

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Thank you!

FOR ALL YOUR TIME