

Supervised Learning: Multivariable Regressor & Classifiers

AAA-Python Edition



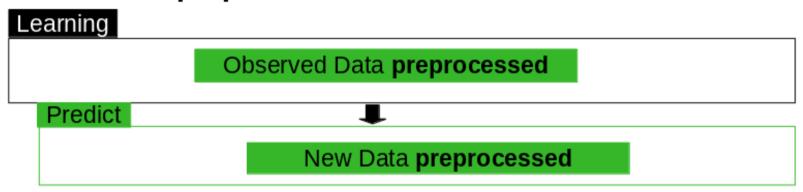
Plan

- 1- Preprocessing Data
- 2- A single variable regressor
- 3- A multivariable regressor
- 4- Regularization
- 5- Logistic Regression Classifier
- 6- Confusion matrix



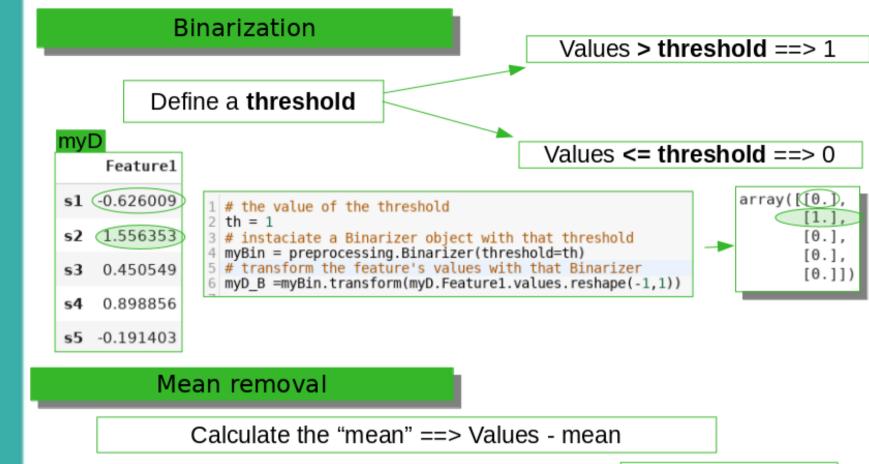
Introduction

- Before going further, we have to focus in one important task: **preprocessing data.**
- Before starting the learning (and the predicting) process, the used data must be prepared or transformed.



- The different processes that can be applied to the data are:
 - Binarization
 - Mean removal
 - Scaling
 - Normalization





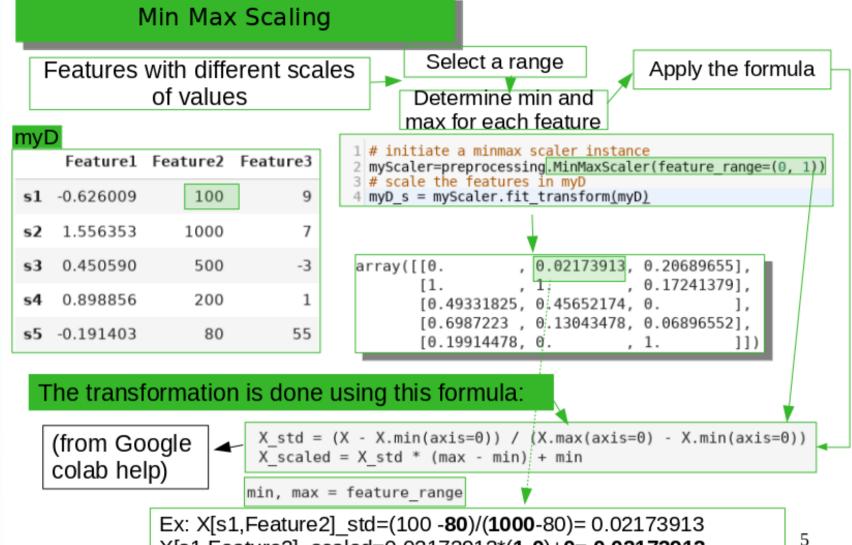
```
Previous mean== 0.502482
```

[By Amina Delali]

New mean: new mean ≈ 0

array([[-0.11428357], [-0.34343912], [0.13638221], [1.27876145], [-0.95742096]])

T **Preprocessin**



[By Amina Delali]

X[s1,Feature2] scaled=0.02173913*(1-0)+0= 0.02173913



Normalization

Least Absolute Deviations: L1

Sum of absolute features values for each sample row will be == 1

```
# Normalize myD using L1 normalization
 myD l1 = preprocessing.normalize(myD, norm='l1')
|-5.71040582e-03|+
                               array([[-5.71040582e-03,
                                                          9.12192288e-01.
                                                                           8.20973059e-02]
                                        1.54314927e-03,
                                                          9.91516237e-01,
                                                                           6.94061366e-031,
[9.12192288e-01]+
                                        8.95003420e-04,
                                                          9.93146120e-01, -5.95887672e-031,
| 8.20973059e-02|==1
                                        4.45201136e-03.
                                                                           4.95297507e-031.
                                                          9.90595014e-01.
                                      [-1.41579269e-03.
                                                                           4.06830603e-0111)
                                                          5.91753604e-01.
```

[-1.97154737e-03,

Least Squares: L2



Sum of **the square of** features values for each sample row will be == 1

9.95955081e-01.

8.24040323e-01,

8.96359573e-021

5.66527722e-01]])

```
1 # Normalize myD using L2 normalization
 myD l2 = preprocessing.normalize(myD, norm='l2')
```

```
(-6.23476844e-03)<sup>2</sup>+
(9.95955081e-01)2+
(8.96359573e-02)^2==1
```

array([[-6.23476844e-03. 6.99982003e-03], 1.55631299e-03, 9.99974290e-01, 9.01163413e-04, 9.99981594e-01, -5.99988957e-03], 4.49417844e-03. 9.99977401e-01. 4.99988701e-031.

[By Amina Delali]



Variable Single ressor 2- A Regi

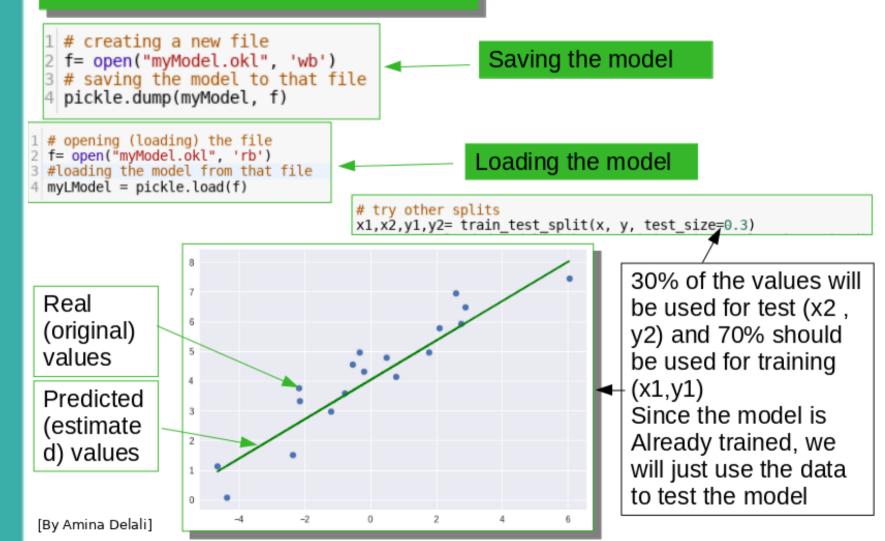
Training and testing set **Learning: regression (with 1 feature)** build Mathematical model parameters with Fit: determine the value of parameters Observed Labeled Data X: described by 1 feature and the labels y. The data is split into: training and testing set Parameters determined using training set **Prediction** is **made** using the **testing** set Compute the error using predicted and test labels from sklearn.model_selection import train_test_split/ # srpliting the data into test and training sets x train, x test, y train, y test = train test split(x, y, test size=0.2) # create an instance of a Linear regressor myModel = linear model.LinearRegression() # predict using testing set # train the model using the training sets y_test_pred = myModel.predict(x test) myModel.fit(x train, y train) Mean of absolute # Compute mean absolute error differences between test print("Mean absolute error =", sm.mean_absolute_error(y_test,y_test_pred)) # Compute mean squared error labels and predicted labels print("Mean squared error =", sm.mean_squared_error(y_test,y_test_pred))

[By Amina Delali] Mean of square of the differences between test labels and predicted labels



Variable Single ressor Reg

Loading and saving models





3- A Multivariable Regressor

Multiple features

Learning : regression (with multiple features)

build

Mathematical model

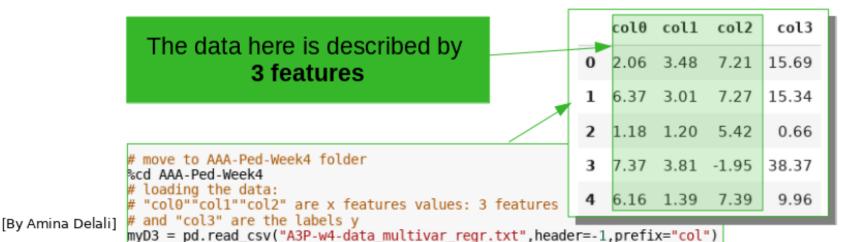
with

parameters

Fit: determine the value of parameters

Observed Labeled Data X:

- described by 1 feature, then new features are generated:
 like polynomial features
- described by multiple features: they are used as they are
- described by multiple features, and new features are generated





Simple Linear Regression (with **multiple** features)

Learning: Simple linear regression (with multiple features)

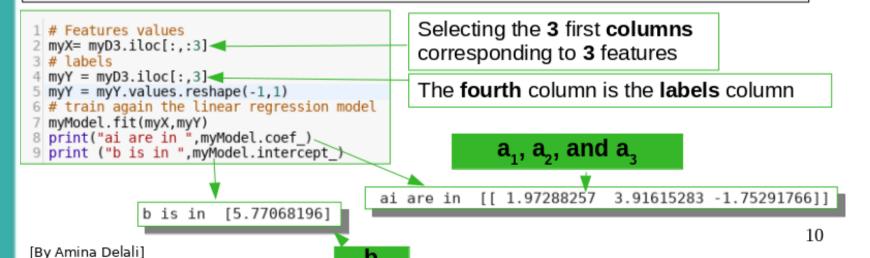
build

Mathematical model== $\mathbf{y} = \mathbf{a}_1 \times \mathbf{x}_1 + \mathbf{a}_2 \times \mathbf{x}_2 + \dots + \mathbf{a}_n \times \mathbf{x}_n + \mathbf{b}$

with **n+1** parameters: **a**_i and **b**

Fit: determine the value of **a**, and **b**

Observed **Labeled** Data: **X** described by **multiple features** the **labels**: **y**



Reg



Polynomial Basis Function (with **multiple** features)

Learning: Linear regression (with 3 features, order == 2)

build

```
Mathematical model==
y= a<sub>1</sub>*x<sub>1</sub>+a<sub>2</sub>*x<sub>2</sub>+ a<sub>3</sub>*x<sub>3</sub>+a<sub>4</sub>*x<sub>1</sub><sup>2</sup>+ a<sub>5</sub>*x<sub>1</sub>*x<sub>2</sub>
  +a_{5}*x_{1}*x_{2}+a_{7}*x_{2}^{2}+a_{5}*x_{3}*x_{4}+a_{6}*x_{2}^{2}+b
```

10 parameters: **a**, and **b**

Fit: determine the value of **a**, and **b**

Observed Labeled Data: X described by multiple features + Polynomial features are generated the **labels**: y

-3.60516775e-02 3.01335037e-02 -5.82113466e-03 2.13183791e-02

with

```
from sklearn.preprocessing import PolynomialFeatures
# polynomial features generator of degree 2
polynomial = PolynomialFeatures(degree=2, include_bias=False)
# generate the new features
x poly = polynomial.fit transform(myX)
# fit the model
myModel.fit(x_poly,myY)
                 ai are in [[ 2.24816066e+00     4.01398972e+00 -1.95742341e+00 -3.11506706e-02
```

[By Amina Delali] b is in [5.67788315]

-4.29337992e-0411



Introduction

Mathematical model **overfit** data ==**Fits** very well to the training set. But, **doesn't perform** well on the **testing** or the **new data** sets

Introduce penalties to the model

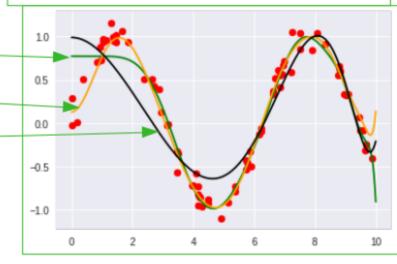
Lasso Regression (L1 regularization): Penalizes the sum of absolute values (1-norms) of regression parameters: **a**_i and **b**

Lasso Regression (L1 regularization): Penalizes the sum of squares (2norms) of the regressions parameters: **a**_i and **b**

Linear model without regularization

Ridge model

Lasso model



[By Amina Delali]



Ridge Regression (L2 regularization)

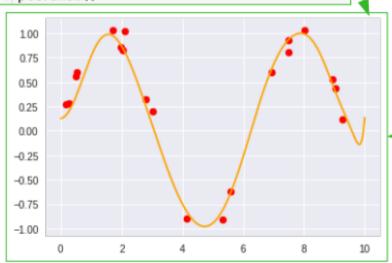
Penalty formula

$$p = \alpha * \sum_{n=1}^{N} \theta_n^2$$

a Ridge regressor: linear regressor with L2 regularization
regressor2 =Ridge(alpha=0.1)

a Ridge regressor with polynomial features
myRModel= make_pipeline(PolynomialFeatures(17), regressor2)

- 2 myRModel.fit(x_tr,y_tr)
- y pred2 = myRModel.predict(x plot)
- 1 y test pred = myRModel.predict(x plot)
- 2 plt.scatter(x_te, y_te, color="red")
- 3 plt.plot(x_plot, y_pred2, color="orange")
- 4 plt.show()

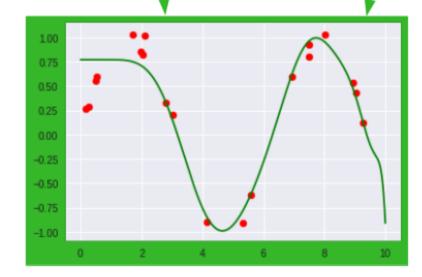


[By Amina Delali]

The first linear model without regularization and the test values

Smoother and more fitting to the test data

y_test_pred = myModel2.predict(x_plot)
plt.scatter(x_te, y_te, color="red")
plt.plot(x_plot, y_pred, color="green")
#x_tes= np.linspace(0, 10, 1000)
plt.show()





Lasso Regression (L1 regularization)

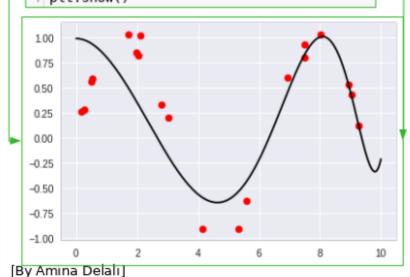
Penalty formula

$$p = \alpha * \sum_{n=1}^{N} |\theta_n|$$

a Lasso regressor: linear regressor with L1 regularization
regressor3 =Lasso(alpha=0.1)

a Lasso regressor with polynomial features
myLModel = make pipeline(PolynomialFeatures(17), regressor3)
myLModel.fit(x_tr,y_tr)
v pred3 = myLModel.predict(x plot)

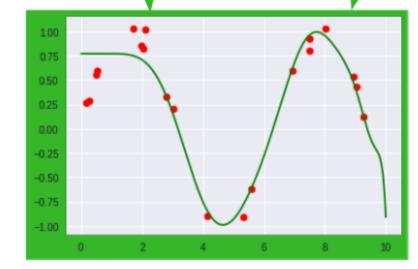
1 y_test_pred = myLModel.predict(x_plot)
2 plt.scatter(x_te, y_te, color="red")
3 plt.plot(x_plot, y_pred3, color="black")
4 plt.show()



The first linear model without regularization and the test values

More smoother but less fitting to the test data

y_test_pred = myModel2.predict(x_plot)
plt.scatter(x_te, y_te, color="red")
plt.plot(x_plot, y_pred, color="green")
#x_tes= np.linspace(0, 10, 1000)
plt.show()







Definition

Classification with a logistic regression

build

Fit

Mathematical model == a logistic Regression defined by a regression model and the sigmoid function S:

$$s(z) = \frac{1}{1 + e^{-z}}$$

where z is :the prediction value obtained by a regression model

with

Tunable parameters: The regression model parameter

Observed **Labeled** Data: a defined cost function is used for the logistic Regression. The S values are the probabilities of the samples data belonging to a Certain class.

Predict the knows Categories

New Data: each sample is classed into one of the known categories. If the probability value is higher than a certain threshold, the sample Is affected to that class. And if it is not, it is affected to the other class.



Classification with 2 classes # instance of a logistic regressor myModel_reg = linear_model.LogisticRegression() # train the model myModel_reg.fit(x2_train, y2_train) # predict for test values: y2 test pred= myModel reg.predict(x2 test) The "+" marks colors y axis: represent the **predicted** second feature classes. The "." marks colors values represent the **real** values x axis : first feature values This sample was predicted to be in class2 (2), but in fact, it 1 # the coefficients calculated of the regression model belongs to calss1 (1) a = mvModel reg.coef [0] # the intercept of the rgression model # the corresponding probabilities predicted the 3 first samples b= myModel req.intercept y2 test pr = myModel reg.predict proba(x2 test)[0:3] v2 test pr Calculated parameters array([-0.12507469]) array([[0.0145635 0.9854365 Probabilities for for the [0.99701667 0.002983331 regression belonging to class2 0.9982999611 [0.00170004] model 16 array([1.34836231, -2.05135853]) [By Amina Delali]



Regressor

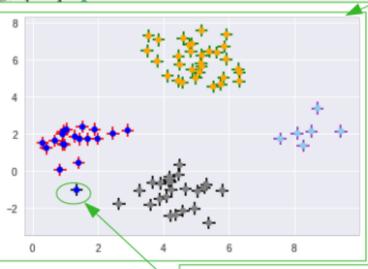
Classification with more than 2 classes: One vs all

- The logistic regression is run for each class against all the other classes (considered as one class).
- Select the class for which the probability of belonging is the greatest.

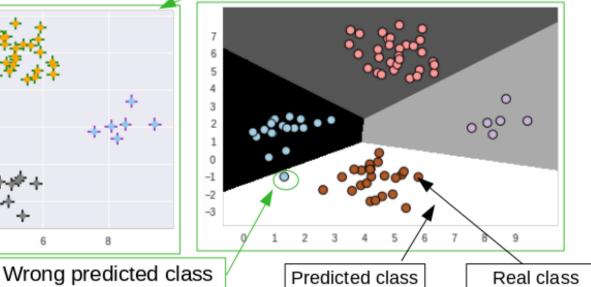
An other way for visualization (the code is from : Joshi Prateek. Artificial intelligence with Python. Packt Publishing, 2017 link)

instance of a logistic regressor
myModel_reg = linear_model.LogisticRegression()
train the model
myModel_reg.fit(x2_train, y2_train)
predict for test values:
y2_test_pred= myModel_reg.predict(x2_test)

Same code as logistic regression with 2 classes



[By Amina Delali]





Definition

prediction) **Negatives** (prediction in class 0)

True Negatives:
number of samples
predicted to be in class 0
and they are in class 0

raise Positives:
number of samples
predicted to be in class 0
but they are in class 1

Predicted wrong

Well Predicted redicted to be in class 1 but they are in class 0

rue Positives:
number of samples
predicted to be in class 1
and they are in class 1

true_classes = [1,1,1,0,1,0,1,0,1,0,1,0]
pred_classes = [1,0,1,0,1,0,1,0,1,0]
Create confusion_matrix
myConfusionMat = confusion_matrix(true_classes, pred_classes)

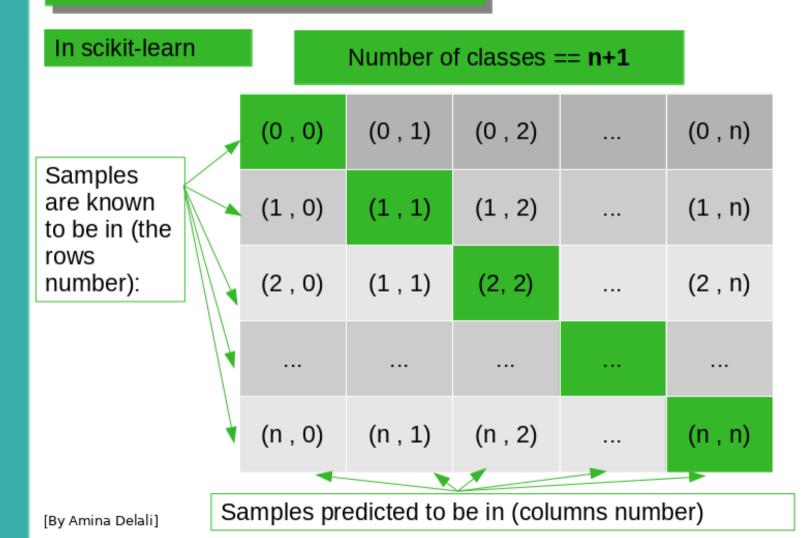
2 samples are known to be in class 0, and they
were predicted to be in class 0: True (the good

3 samples are known to be in class 0, and they were predicted to be in class 1: False (the wrong prediction) Positives (prediction in class 1)

[By Amina Delali]

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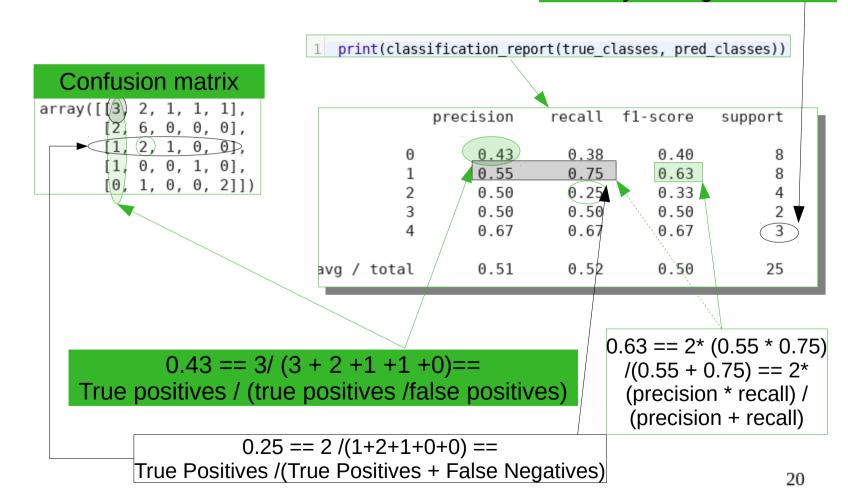
More than 2 classes





Confusion Matrix Report

Number of samples that truly belongs to class 4



[By Amina Delali]



References

- Joshi Prateek. Artificial intelligence with Python. Packt Publishing, 2017.
- Jake VanderPlas. Python data science handbook: essential tools for working with data. O'Reilly Media, Inc, 2017.
- Scikit-learn.org. scikit-learn, machine learning in python.
 On-line at scikit-learn.org/stable/. Accessed on 03-11-2018



Thank you!

FOR ALL YOUR TIME