



## ELEC4844/8844 Practical Class – Week 6, 2024

### Complex Signals & Spectral Viewing

#### TASK 1

Given a linear chirp signal

$$x(t) = \cos(2\pi f_1 t + \pi \mu t^2)$$

in which  $f_1 = 4$  kHz and  $\mu = 100$  kHz/s.

a) Generate the discrete-time signal  $x[n]$  from  $x(t)$  that last for 50 ms, using sampling frequency  $f_s = 80$  kHz. Obtain the power spectral density (PSD) of  $x[n]$  using its DFT  $X[k]$  and the expression below ( $N$  is the number of samples in the discrete-time signal), and plot the result in decibel units.

$$\text{PSD}_x\left(\frac{kf_s}{N}\right) = \frac{1}{Nf_s} |X[k]|^2$$

b) Make sure  $N$  is an odd number. Verify the spectrum  $X[k]$  of the real-valued signal  $x[n]$  is Hermitian, and plot the real and imaginary parts of  $X[k]$ .

c) Generate the analytic signal  $\tilde{x}[n]$  of  $x[n]$  using Hilbert transform. Obtain the PSD of  $\tilde{x}[n]$ , and plot the result in decibel units. For comparison, set the same display range of the plot as that of the  $\text{PSD}_x$  plotted in (a), except adding a bias of 6 dB to the vertical axis.

d) Apply frequency translation to  $\tilde{x}[n]$  to obtain  $\tilde{s}[n]$ , which is centred at  $f_c = 16$  kHz. Obtain the PSD of  $\tilde{s}[n]$ , and plot the result in decibel units. For comparison, set the same display range of the plot as that of the PSD of  $\tilde{x}[n]$  plotted in (c).

e) Obtain the real-valued signal  $s[n] = \text{Re}\{\tilde{s}[n]\}$ . Plot the spectrum of  $s[n]$ , and verify it is Hermitian.

#### TASK 2

Recall using correlation to estimate the impulse response of an LTI system (Lecture 6, p.13),

$$r_{yx}(t) = y(t) * x(-t) = h(t) * r_{xx}(t)$$

$$R_{yx}(\omega) = H(\omega)R_{xx}(\omega)$$

If  $R_{xx}(\omega)$  is a constant, which can be realised using a white noise as the system input, the impulse response  $h(t)$  can be estimated from the cross-correlation between the system output and the input.

a) Generate a row vector containing  $N = 1000$  normally distributed random number  $e[n]$  with zero mean and standard deviation  $\sigma = 2$ . Compute the autocorrelation  $r_{xx}[n]$  of  $e[n]$  using the MATLAB function `xcorr`. Plot it out using `stem` centred at the origin  $n = 0$ .

- b) Compute the DFT  $R_{xx}[k]$  of  $r_{xx}[n]$ . Plot the magnitude of  $R_{xx}[k]$  in both linear and dB units. Calculate the mean  $E(R_{xx}[k])$  of  $R_{xx}[k]$ , and verify  $E(R_{xx}[k]) = N\sigma^2$ .
- c) For the following two systems, using the correlation method to estimate their respective impulse response, and compare the results with the actual impulse responses.

$$y[n] + 0.5y[n-1] = x[n]$$

$$H(z) = \frac{2.24 + 2.49z^{-1} + 2.24z^{-2}}{1 - 0.4z^{-1} + 0.75z^{-2}}$$

### TASK 3

- a) Refer to textbook Exercise 3.13 (p.90), use the RTL-SDR device and MATLAB script “...\spectrum\sweep\rtlsdr\_rx\_specsweep.m” to sweep the RF spectrum from 25MHz to 1.75GHz and explore the obtained spectrum for your local area.

Find out from the code how to set up an RTL-SDR object using the comm.SDRRTLReceiver function, and run the object using the step function.

- b) Write your own MATLAB code to use the RTL-SDR device. Set the central frequency to 96.9 MHz, the gain to 40 dB, and the sampling rate  $f_s = 2.8$  MHz to record one block of signal containing  $N = 4096$  samples. Obtain its power spectral density (PSD) using DFT as expressed below

$$\text{PSD}_X\left(\frac{kf_s}{N}\right) = \frac{1}{Nf_s} |X(k)|^2$$

Plot the PSD in decibel unit for the frequency range from  $-f_s/2$  to  $f_s/2$ .

- c) Display the PSD of the recorded signal use either periodogram or dsp.SpectrumAnalyzer function in MATLAB, and compare to the result obtained in (a). **Note:** By default, dsp.SpectrumAnalyzer uses Hann window.