实验要求

- 根据扩展欧几里得算法实现求乘法逆元模块
- 根据分组长度n, 生成密钥(A,B)。即可逆矩阵A和向量B。生成的密钥要有随机性, 密钥以文件形式 存储
- 生成A的逆矩阵A-1
- 实现多表代换加密、解密模块
- 实现加密解密软件基本的可视化界面,能够对输入文本框的英文字符串进行加密解密,能够对文本 文件中的文本进行加密解密
- 附加内容
 - o 对长度不是n的倍数的明文的处理,能够对长度不是n的倍数的明文进行加密解密
 - 对空格和标点符号的处理。要求解密时能还原空格和标点符号

实验原理

多表代换密码实现加密过程主要可以分为以下几个步骤:

- 随机生成n*n的可逆矩阵A,且满足A的行列式与所定模N互素,作为密钥A
- 随机生成n*1的矩阵B,作为密钥B
- 对所需明文就行分组
- 通过 Ci = AMi+B (mod 26) 加密变换求出密文

多表代换密码实现解密过程主要可以分为以下几个步骤:

- 对输入的密钥A作为矩阵A,求出矩阵A的逆矩阵
- 对密文进行分组
- 通过 Mi ≡A-1(Ci-B)(mod 26)解密变换求出明文

软件系统设计

随机生成矩阵

此部分主要介绍如何随机生成可逆矩阵A和矩阵B作为密钥A和密钥B,同时实现将密钥作为文件保存

可逆矩阵A

生成可逆矩阵A的主要方法为: 用单位矩阵进行初等变换而成

生成单位矩阵

```
def getIdentityMatrix(n):#生成单位矩阵
A = np.zeros((n,n))
for i in range(n):
    for j in range(n):
        if i == j:
              A[i][j] = 1
        else:
              A[i][j] = 0
return A
```

生成随机可逆矩阵A

```
def getInvertibleMatrix(n,m):#生成可逆矩阵
    while 1:
        A = getIdentityMatrix(n)
        tempArray = np.zeros(n)
        B = np.zeros((n,n))
        transformTime = int(random.randint(0,1000))
        maxint = sys.maxsize
        for i in range(transformTime):
            mainRowNum = int((random.randint(0,n) % (n - 1))) #选择一个主行作初等行变
换
            for k in range(n):
                #元素数值是否会溢出
                if maxint - (A[mainRowNum][k])*(int(random.randint(0,10))) < 0</pre>
and maxint*(-1) - (A[mainRowNum][k])*(int(random.randint(0,10))) > tempArray[k]:
                    tempArray[k] = A[mainRowNum][k]
                else:
                    tempArray[k] = (A[mainRowNum][k]*
(int(random.randint(0,10)))%m
            for j in range(n):
                if mainRowNum != j:
                    for k in range(n):
                        if maxint - A[j][k] < tempArray[k] and maxint * (-1) -
(A[j][k]) > tempArray[k]:
                            A[j][k] = (A[j][k]/4)%m
                        else:
                            A[j][k] = (A[j][k] + tempArray[k])%m
        if gcd(np.linalg.det(A),m) == 1 and np.linalg.det(A) > 0:
            break
    return A
```

其中 transformTime 为随机决定初等行变换的次数,关键是要确保矩阵A的行列式与所定模N互素

故需要此限定的条件: gcd(np.linalg.det(A),m) == 1 and np.linalg.det(A)

矩阵B

```
B = np.zeros((n, 1))
for row in range(n):
   B[row] = int(random.randint(0, 26))
```

这没有什么可以讲的很简单

明文分组加密

预处理

记录空格和符号

字符串初始化转换为纯字母序列

```
for i in range(len(clear)):
    if clear[i] == ',':
        clear[i] = ' '
    while ' ' in clear:
        clear.remove(' ')
```

补位操作

```
if (lenth % n == 0):
    flag = 0
else:
    flag = 1
    offset = n - lenth % n
for i in range(offset):
    CipherText.append('A')
groups = int(len(CipherText) / n)
```

生成M序列

```
M = np.zeros((groups, n))
  index = 0
  for row in range(groups):
    for column in range(n):
        M[row][column] = CipherText[index]
        index = index + 1
```

分组加密

```
for i in range(groups):#实现矩阵乘法和矩阵加法, InA*(C-B)

tmp = np.zeros((n, 1))

tmpp = np.zeros((n, 1))

for row in range(n):#初始化Mi

    tmp[row][0] = M[i][row]

for row in range(n): # 实现C-B

    tmp[row][0] = tmp[row][0] - B[row][0]

for row in range(n):#实现InA*(C-B)mod(N)

    for column in range(n):

        tmpp[row][0] = int(tmpp[row][0] + (int(tmp[column][0]) *

int(A[row][column])))

    tmpp[row][0] = int((tmpp[row][0]) % N)

for row in range(n):
    clearlist.append(NtoA(int(tmpp[row][0])))
```

消除补位影响

```
if flag == 1:
    for i in range(offset):#消除补位影响
    del clearlist[-1]
```

逆矩阵

逆元

```
def InverseElement(b,p):#求逆元
    inv = 1
    while 1:
        if (inv*b)%p == 1:
            break
        inv = inv +1
        return inv
```

行列式

```
def Det(a,n):#求行列式
   b = np.zeros((n, n))#临时数组用于降阶
   sum = int(0)
   sign = int(0)
   p = int(0)
   if n == 1:
       return a[0][0]
   for i in range(n):#此处大循环实现将余子式存入数组b中
       for c in range(n-1):
          for j in range(n-1):
              if c<i:
                  p = 0#当p=0时,行列式只向左移,即消去对应的第一列的数
              else:
                  p = 1#否则行列式左移后再上移
              b[c][j]=a[c+p][j+1]
       if i%2 == 0:
          sign = 1#i为偶数,加法
       else:
          sign = -1#i为奇数, 减法
       sum = sum + a[i][0]*Det(b,n-1)*sign#计算行列式的值
```

伴随矩阵

逆矩阵

```
def InverseMat(a,n,p,ans):
    astar = np.zeros((n, n))
    getAStart(a, n, astar)#求A的伴随矩阵
    deta = int(Det(a,n))#求A的行列式
    if deta < 0:
        deta = deta + p
    inv = int(InverseElement(deta,p))
    for i in range(n):
        for j in range(n):
        ans[i][j] = astar[i][j]*inv
        ans[i][j] = ans[i][j]%p
        if ans[i][j] < 0:
        ans[i][j] = ans[i][j] + p
```

密文分组解密

补位操作

```
if (lenth % n == 0):
    flag = 0
else:
    flag = 1
    offset = n - lenth % n
for i in range(offset):
    CipherText.append('A')
groups = int(len(CipherText) / n)
```

生成M序列

```
M = np.zeros((groups, n))
  index = 0
  for row in range(groups):
    for column in range(n):
        M[row][column] = CipherText[index]
        index = index + 1
```

消除补位影响

```
if flag == 1:
    for i in range(offset):#消除补位影响
    del clearlist[-1]
```

GUI图形界面最终实现

GUI的实现使用的Python自带的tkinter库,实现了错误提示框的弹出和各类操作可视化

```
import random
import tkinter as tk
import numpy as np
from tkinter.simpledialog import *
def gcd(a,b):
    if a%b == 0:
        return b
    else:
        return gcd(b,a%b)
def exgcd(a,b,x,y):
   if b==0:
        x=1
        y=0
    d = exgcd(b,a\%b,y,x)
    y = y - (a/b)*x
    return d
def InverseElement(b,p):#求逆元
    inv = 1
    while 1:
        if (inv*b)%p == 1:
            break
        inv = inv +1
    return inv
def Det(a,n):#求行列式
    b = np.zeros((n, n))#临时数组用于降阶
    sum = int(0)
    sign = int(0)
    p = int(0)
    if n == 1:
```

```
return a[0][0]
   for i in range(n):#此处大循环实现将余子式存入数组b中
       for c in range(n-1):
           for j in range(n-1):
               if c<i:
                   p = 0#当p=0时,行列式只向左移,即消去对应的第一列的数
               else:
                   p = 1#否则行列式左移后再上移
               b[c][j]=a[c+p][j+1]
       if i\%2 == 0:
           sign = 1#i为偶数,加法
       else:
           sign = -1#i为奇数,减法
       sum = sum + a[i][0]*Det(b,n-1)*sign#计算行列式的值
def getAStart(arcs,n,ans):#计算每一行每一列的每个元素所对应的余子式,组成A*
   if n == 1:
       ans[0][0] = 1
   temp = np.zeros((n, n))
   for i in range(n):
       for j in range(n):
           for k in range(n-1):
               for t in range(n-1):
                   temp[k][t] = arcs[(k+1 if k>=i else k)][(t+1 if t>=j else
t)]
               ans[j][i] = Det(temp, n-1)
               if (i+j)\%2 == 1:
                   ans[j][i] = -ans[j][i]
def InverseMat(a,n,p,ans):
   astar = np.zeros((n, n))
   getAStart(a, n, astar)#求A的伴随矩阵
   deta = int(Det(a,n))#求A的行列式
   if deta < 0:
       deta = deta + p
   inv = int(InverseElement(deta,p))
   for i in range(n):
       for j in range(n):
           ans[i][j] = astar[i][j]*inv
           ans[i][j] = ans[i][j]%p
           if ans[i][j] <0:
               ans[i][j] = ans[i][j] + p
   return ans
def AtoN(A):#处理字符和数字的关系
   N = 0
   if(ord(A)>=65 and ord(A)<=90):
       N = ord(A) - ord('A')
   if (ord(A) >= 97 \text{ and } ord(A) <= 122):
       N = ord(A) - ord('a')
   return N
def NtoA(N):
   A = chr(N + ord('A'))
   return A
def Encrypt(clearlist,A,B,n,N):#加密函数
   CipherText = []
   lenth = len(clearlist)
   flag = 0
   offset = 0
   #补位操作
```

```
if(1enth%n == 0):
        flag = 0
    else:
        flag = 1
        offset = n-lenth%n
    for i in range(offset):
        clearlist.append('A')
    groups = int(len(clearlist)/n)
    for i in range(len(clearlist)):
        clearlist[i] = AtoN(clearlist[i])
    #生成M序列
    M = np.ones((groups,n))
    index = 0
    for row in range(groups):
        for column in range(n):
           M[row][column] = clearlist[index]
            index = index + 1
    for i in range(groups):#实现矩阵乘法和矩阵加法, A*M+Bmod(N)
        tmp = np.zeros((n, 1))
        tmpp = np.zeros((n, 1))
        for row in range(n):#初始化Mi
            tmp[row][0] = M[i][row]
        for row in range(n):#实现A*M
            for column in range(n):
                tmpp[row][0] = int(tmpp[row][0] + (int(tmp[column][0]) *
int(A[row][column])))
            tmpp[row][0] = int((tmpp[row][0]) % N)
        for row in range(n):#实现+
            tmpp[row][0] = (tmpp[row][0] + B[row][0]) % N
        for row in range(n):
            CipherText.append(NtoA(int(tmpp[row][0])))
    if flag == 1:
        for i in range(offset):#消除补位影响
           del CipherText[-1]
    return CipherText
def Decrypt(CipherText,A,B,n,N):#解密函数
    clearlist = []
    lenth = len(CipherText)
    flag = 0
    offset = 0
    # 补位操作
    if (lenth % n == 0):
        flag = 0
    else:
        flag = 1
        offset = n - lenth % n
    for i in range(offset):
        CipherText.append('A')
    groups = int(len(CipherText) / n)
    for i in range(len(CipherText)):
        CipherText[i] = AtoN(CipherText[i])
    # 生成M序列
    M = np.zeros((groups, n))
    index = 0
    for row in range(groups):
        for column in range(n):
           M[row][column] = CipherText[index]
            index = index + 1
```

```
#求C-B
    for i in range(groups):#实现矩阵乘法和矩阵加法, InA*(C-B)
        tmp = np.zeros((n, 1))
        tmpp = np.zeros((n, 1))
        for row in range(n):#初始化Mi
            tmp[row][0] = M[i][row]
        for row in range(n): # 实现C-B
            tmp[row][0] = tmp[row][0] - B[row][0]
        for row in range(n):#实现InA*(C-B)mod(N)
            for column in range(n):
                tmpp[row][0] = int(tmpp[row][0] + (int(tmp[column][0]) *
int(A[row][column])))
            tmpp[row][0] = int((tmpp[row][0]) % N)
        for row in range(n):
            clearlist.append(NtoA(int(tmpp[row][0])))
    if flag == 1:
        for i in range(offset):#消除补位影响
            del clearlist[-1]
    return clearlist
def getIdentityMatrix(n):#生成单位矩阵
    A = np.zeros((n,n))
    for i in range(n):
        for j in range(n):
            if i == j:
                A[i][j] = 1
            else:
                A[i][j] = 0
    return A
def getInvertibleMatrix(n,m):#生成可逆矩阵
    while 1:
        A = getIdentityMatrix(n)
        tempArray = np.zeros(n)
        B = np.zeros((n,n))
        transformTime = int(random.randint(0,1000))
        maxint = sys.maxsize
        for i in range(transformTime):
            mainRowNum = int((random.randint(0,n) % (n - 1)))#选择一个主行作初等行变
换
            for k in range(n):
                #元素数值是否会溢出
                if maxint - (A[mainRowNum][k])*(int(random.randint(0,10))) < 0</pre>
and maxint*(-1) - (A[mainRowNum][k])*(int(random.randint(0,10))) > tempArray[k]:
                    tempArray[k] = A[mainRowNum][k]
                else:
                    tempArray[k] = (A[mainRowNum][k]*
(int(random.randint(0,10)))%m
            for j in range(n):
                if mainRowNum != j:
                    for k in range(n):
                        if maxint - A[j][k] < tempArray[k] and maxint * (-1) -
(A[j][k]) > tempArray[k]:
                            A[j][k] = (A[j][k]/4)%m
                        else:
                            A[j][k] = (A[j][k] + tempArray[k])%m
        if gcd(np.linalg.det(A),m) == 1 and np.linalg.det(A) > 0:
            break
    return A
def nnb():
```

```
messagebox.showinfo("Succesfull", "File is in your computer!")
def newwind(n,m):
    winNew = Toplevel(window)
    winNew.geometry('320x400')
    winNew.title('Random Key')
    lb1 = tk.Label(winNew, text='Random A Key', font=('Arial', 16), width=40,
height=2)
    lb1.pack(fill='x')
    nt1 = tk.Text(winNew, height=8, width=40)
    nt1.pack(fill='x')
    lb2 = tk.Label(winNew, text='Random B Key', font=('Arial', 16), width=40,
height=2)
    1b2.pack(fill='x')
    nt2 = tk.Text(winNew, height=8, width=40)
    nt2.pack(fill='x')
    nb = tk.Button(winNew, text='Save', font=('Arial', 12), width=10, height=1,
command=nnb)
    nb.pack()
    lb3 = tk.Label(winNew, text='@FZU-IS-404 ZERO-A-ONE', font=('Arial', 10),
width=40, height=2)
    1b3.pack(fill='x')
    B = np.zeros((n, 1))
    A = getInvertibleMatrix(n,m)
    for row in range(n):
        B[row] = int(random.randint(0, 26))
    At = open('A_key.txt', 'w')
    Bt = open('B_key.txt', 'w')
    for row in range(n):
        str1 = ""
        for line in range(n):
            str1 += str(int(A[row][line]))
            str1 += ' '
        str1 += "\n"
        At.write(str1)
        nt1.insert("%d.%d" % (0, int(row)),str1)
    At.close()
    for row in range(n):
        str2 = ""
        str2 += str(int(A[row][0]))
        str2 += "\n"
        Bt.write(str2)
        nt2.insert("%d.%d" % (0, int(row)), str2)
    Bt.close()
def nb1():
    fo = open("text.txt", "r+")
    str = fo.read()
    tt2.insert(INSERT, str)
    fo.close()
def buttonRK():
    if e1.get() != "" and e2.get() != "":
        n = int(e1.get())
        m = int(e2.get())
        newwind(n,m)
    else:
        messagebox.showinfo("Error", "Please input n")
def n2wind(ans,n):
    n2wind = Toplevel(window)
    n2wind.geometry('300x130')
```

```
n2wind.title('Inverse Matrix')
    n2nt2 = tk.Text(n2wind, height=8, width=40)
    n2nt2.pack(fill='x')
    for row in range(n):
        str1 = ""
        for line in range(n):
            str1 += str(int(ans[row][line]))
            str1 += ' '
        str1 += "\n"
        n2nt2.insert("%d.%d" % (0, int(row)),str1)
def Dewin():#解密函数GUI
    if t1.get("0.0","end") != "" and t2.get("0.0","end") != "" and e1.get() !=
"" and e2.get() != "":
        n = int(e1.get())
        m = int(e2.get())
        A = np.zeros((n, n))
        B = np.zeros((n, 1))
        InA = np.zeros((n, n))
        Atex = t1.get("1.0", "end")
        stringA = ' '.join(Atex.split())
        listA = list(stringA.split(' '))
        index = 0
        for row in range(n):
            for column in range(n):
                A[row][column] = int(listA[index])
                index = index + 1
        Btex = t2.get("1.0", "end")
        stringB = ' '.join(Btex.split())
        listB = list(stringB.split(' '))
        index = 0
        for row in range(n):
            B[row][0] = int(listB[index])
            index = index + 1
        clear = tt2.get("1.0", "end")
        clear = list(clear)
        InA = InverseMat(A, n, m, InA)
        klist = np.zeros(len(clear))
        index = 0
        for i in range(len(clear)):
            if clear[i] == ' ':
                klist[index] = int(i)
                index = index + 1
        dlist = np.zeros(len(clear))
        index = 0
        for i in range(len(clear)):
            if clear[i] == ',':
                dlist[index] = int(i)
                index = index + 1
        for i in range(len(clear)):
            if clear[i] == ',':
                clear[i] = ' '
        while ' ' in clear:
            clear.remove(' ')
        print(dlist)
        print(klist)
        clearlist = Decrypt(clear, InA, B, n, m)
        print(clearlist)
        clearlist = list(clearlist)
```

```
for i in range(len(klist)):
            if klist[i] == 0:
                break
            ind = int(klist[i])
            clearlist.insert(ind, " ")
        for i in range(len(dlist)):
            if dlist[i] == 0:
                break
            ind = int(dlist[i])
            clearlist.insert(ind, ",")
        str = ""
        for i in range(len(clearlist)):
            str += clearlist[i]
        t3.insert(INSERT, str)
        n2wind(InA,n)
    else:
        messagebox.showinfo("Error", "Please input n,m,A key,B key")
def Enwin():#加密函数GUI
    if t1.get("0.0", "end") != "" and t2.get("0.0", "end") != "" and e1.get() !=
"" and e2.get() != "":
        n = int(e1.get())
        m = int(e2.get())
        A = np.zeros((n, n))
        B = np.zeros((n, 1))
        Atex = t1.get("1.0", "end")
        stringA = ' '.join(Atex.split())
        listA = list(stringA.split(' '))
        index = 0
        for row in range(n):
            for column in range(n):
                A[row][column] = int(listA[index])
                index = index + 1
        print(A)
        Btex = t2.get("1.0", "end")
        stringB = ' '.join(Btex.split())
        listB = list(stringB.split(' '))
        index = 0
        for row in range(n):
            B[row][0] = int(listB[index])
            index = index + 1
        print(B)
        clear = tt2.get("1.0", "end")
        clear = list(clear)
        klist = np.zeros(len(clear))
        index = 0
        for i in range(len(clear)):
            if clear[i] == ' ':
                klist[index] = int(i)
                index = index + 1
        dlist = np.zeros(len(clear))
        index = 0
        for i in range(len(clear)):
            if clear[i] == ',':
                dlist[index] = int(i)
                index = index + 1
        print(dlist)
        print(klist)
        for i in range(len(clear)):
```

```
if clear[i] == ',':
                clear[i] = ' '
        while ' ' in clear:
            clear.remove(' ')
        CipherText = Encrypt(clear,A,B,n,m)
        print(CipherText)
        CipherText = list(CipherText)
        print(CipherText)
        for i in range(len(klist)):
            if klist[i] == 0:
                break
            ind = int(klist[i])
            CipherText.insert(ind," ")
        for i in range(len(dlist)):
           if dlist[i] == 0:
               break
           ind = int(dlist[i])
           CipherText.insert(ind,",")
        str = ""
        for i in range(len(CipherText)):
            str += CipherText[i]
        t3.insert(INSERT, str)
    else:
        messagebox.showinfo("Error", "Please input n,m,A key,B key")
if __name__ == '__main__':
   #主窗口
    window = tk.Tk()
   window.title('Multi-table')
   window.geometry('300x950')
    #随机密钥
    b = tk.Button(window, text='Random Key', font=('Arial', 12), width=10,
height=1,command=buttonRK)
    b.pack()
    # 2标签
    12 = tk.Label(window, text='Please input n', font=('Arial', 16), width=40,
height=2)
   12.pack(fill='x')
    # 输入框控件entry
    e1 = tk.Entry(window, show=None, width=8, justify = 'center') # 显示成明文形式
    e1.pack()
    # 3标签
    13 = tk.Label(window, text='Please input M', font=('Arial', 16), width=40,
height=2)
   13.pack(fill='x')
    # 输入框控件entry
    e2 = tk.Entry(window, show=None, width=8, justify='center') # 显示成明文形式
    e2.pack()
    #4标签
    14 = tk.Label(window, text='A Key', font=('Arial', 16), width=40, height=2)
    14.pack(fill='x')
    t1 = tk.Text(window, height=8,width = 40)
   t1.pack(fill='x')
    #5标签
    15 = tk.Label(window, text='B Key', font=('Arial', 16), width=40, height=2)
   15.pack(fill='x')
    # Text
    t2 = tk.Text(window, height=8, width=40)
```

```
t2.pack(fill='x')
    # 5标签
    115 = tk.Label(window, text='Text', font=('Arial', 16), width=20, height=2)
    115.pack(fill='x')
    # Text
    tt2 = tk.Text(window, height=8, width=20)
    tt2.pack(fill='x')
    b1 = tk.Button(window, text='File', font=('Arial', 12), width=10, height=1,
command=nb1)
    b1.pack()
    # 加密
    De = tk.Button(window, text='Decrypt', font=('Arial', 12), width=10,
height=1,command=Dewin)
   De.pack()
    #解密
    En = tk.Button(window, text='Encrypt', font=('Arial', 12), width=10,
height=1,command=Enwin)
    En.pack()
    # 6标签
    16 = tk.Label(window, text='SOLUTION', font=('Arial', 16), width=20,
height=2)
   16.pack(fill='x')
    # Text
   t3 = tk.Text(window, height=8, width=20)
    t3.pack(fill='x')
    # 8标签
    18 = tk.Label(window, text='@FZU-IS-404 ZERO-A-ONE', font=('Arial', 10),
width=40, height=2)
   18.pack(fill='x')
    window.mainloop()
```

重要的实现细节

GUI界面的实现

GUI界面的实现极大的方便了使用者的使用体验,降低了使用门槛,使得本程序的实用化程度大大提升

三目运算符的使用

在求A的伴随矩阵时,使用了三目运算符,简化了程序,使思路更清晰

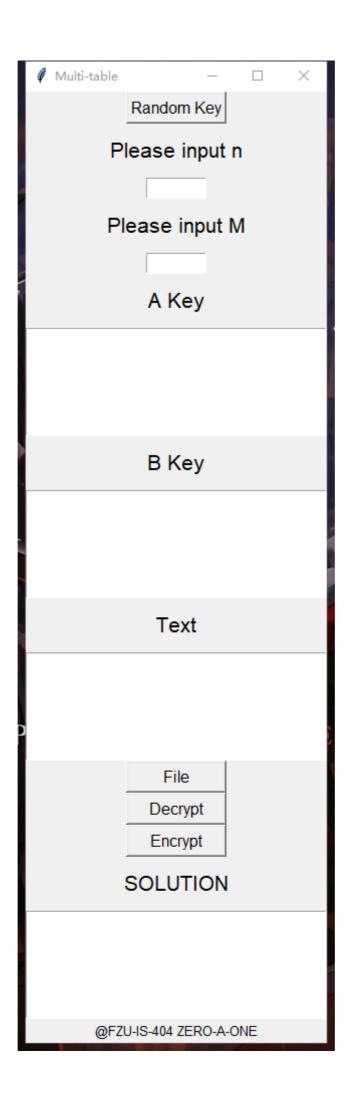
```
temp[k][t] = arcs[(k+1 if k>=i else k)][(t+1 if t>=j else t)]
```

随机生成在模下可逆矩阵

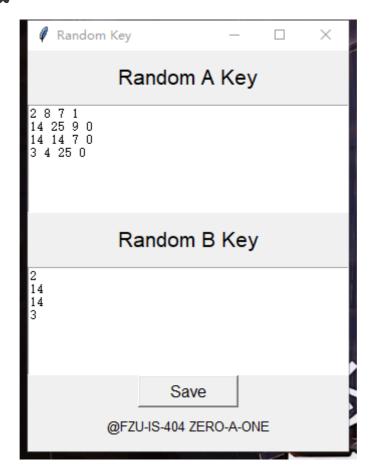
通过模拟初等变换实现的可逆矩阵,更重要的是保证了矩阵A的行列式与所定模N互素。且在随机化的过程中,通过判断保证了数据不会溢出

```
 \label{eq:continuous_section}  \mbox{if maxint - } (A[mainRowNum][k])*(int(random.randint(0,10))) < 0 \mbox{ and maxint*}(-1) - (A[mainRowNum][k])*(int(random.randint(0,10))) > tempArray[k]:
```

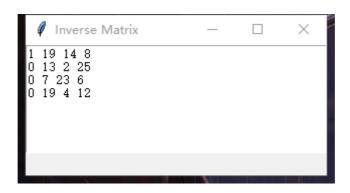
实现效果



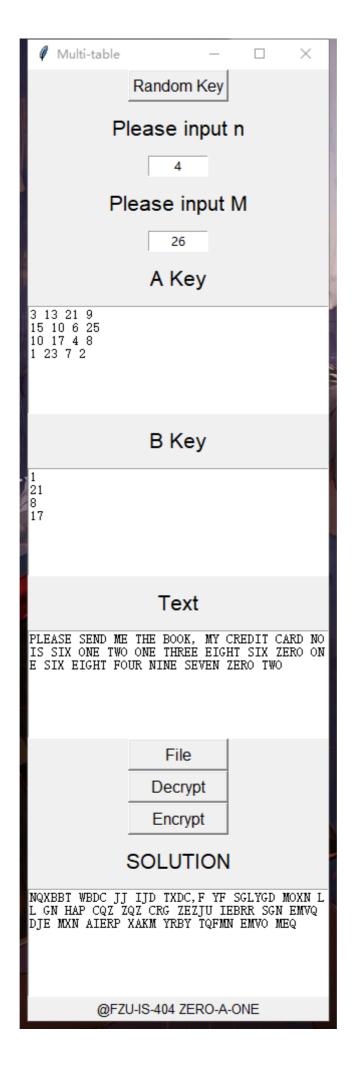
随机矩阵生成

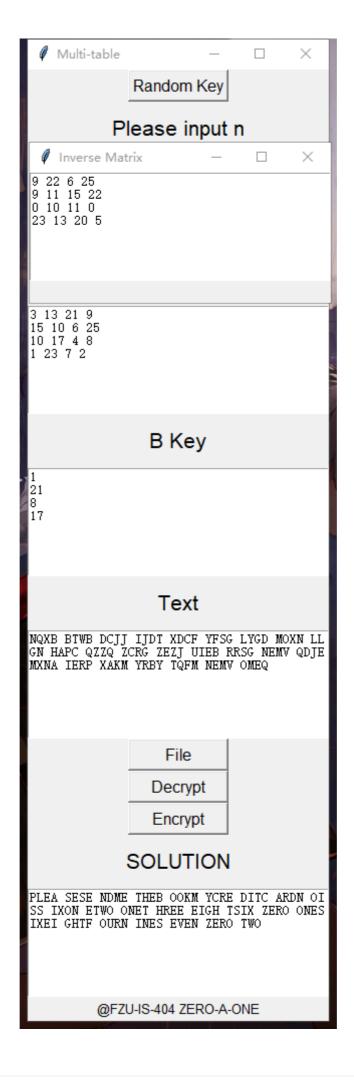


逆矩阵



例题加密





多表代换密码为古典密码学中一种较为经典的加密方式,对于多表替换加密来说,加密后的字母几乎不再保持原来的频率,对于词频和字频分析有了一定的抵抗能力

本人的系统有如下亮点:

- 实现了全部的GUI可视化操作
- 实现了对长度不是n的倍数的明文的处理,能够对长度不是n的倍数的明文进行加密解密
- 实现了对空格和标点符号的处理。要求解密时能还原空格和标点符号
- 实现了对文件的读写操作
- 实现了调用系统API实现错误弹窗功能