

Alabackon Wazini

422 0056

4220056@upm.edu.ss



# part 1:

(a) Image resolution:

Image size: 2048 X 2048 px

i) find resolution (lp/mm) to fit 5x5 cm

Note: 1 cm = 10 mm

$$\therefore \text{pixel per mm} = \frac{\text{number of pixel}}{\text{size (mm)}} = \frac{2048}{50} = \frac{1024}{25} = 40.96 \text{ mm}^{-1}$$

$\therefore$  the pixel needed to fit the image into 5x5 cm space = 40.96 mm.

ii) to calculate resolution in dpi for the image to fit 2x2 inch space.

Note: 1 inch = 25.4 mm

$$\therefore \text{pixel per inch (dpi)} = \frac{\text{Number of pixel}}{\text{size (inch)}} = \frac{2048}{2} = 1024 \text{ dpi (inch)}$$

$\therefore$  the dpi for the image to fit 2x2 inch = 1024 dpi (inch) =

(B) Linear Indexing in 3D Arrays:

$$S = x + M(y + Nz)$$

$$i - S = x + M(y + Nz)$$

$$= x + my + mnz$$

where  $x, y, z$  = coordinates of 3D array element.

$MNP$  = dimension of 3D array along

offset within the current row

$$S = \underline{x} + my + mnz$$

offset base on the number of rows

the offset of how deep the element is in (z)

ii - general form  $N$ -dimension

$$S = X_1 + M_1 (X_2 + M_2 (X_3 + M_3 (X_n + M_n)))$$

where:

$X_1 X_2 \dots X_n$  = indices along each dimension.

$M_1 M_2 \dots M_n$  = size of the dimension.

$$\therefore S = X_1 + M_1 (X_2 + M_2 (X_3 + \dots + M_{n-1} X_n))$$

$\therefore$  This expression provides a framework for calculating the linear index in any  $N$ -dimensional array based on the contributions of each dimension.

©

	$S_1$					$S_2$				
0	0	0	0	0	0	0	0	1	1	0
1	0	0	1	0	0	0	1	0	0	1
1	0	0	1	0	0	1	1	0	0	0
0	0	1	1	1	0	0	0	0	0	0
0	0	1	1	1	0	0	0	1	1	1

$V=1$

$U = \text{None}$

$B = 1$

$A = 1$

## part 2:

**def** bilinear\_interpolation (image, x, y): \* take image of 2D array

\* to get the dimension of the image

width = length (image [0]) \* No. of rows

height = length (image) \* No. of columns

\* the coordinate of the surrounding pixel.

$x_1 = \text{floor}(x)$  \* using floor & ceil function to get the

$x_2 = \text{ceil}(x)$  nearest integer coordinate.

$y_1 = \text{floor}(y)$

$y_2 = \text{ceil}(y)$

\* boundary condition checking

if  $x_1 < 0$  OR  $x_2 \geq \text{width}$  OR  $y_1 < 0$  OR

$y_2 \geq \text{height}$  :

Return "out of bound"

\* getting the value of the surrounding pixel

$v_{11} = \text{image}[y_1][x_1]$  \* top left

$v_{12} = \text{image}[y_1][x_2]$  \* top right

$v_{12} = \text{image}[y_2][x_1]$  \* bottom left

$v_{22} = \text{image}[y_2][x_2]$  \* bottom right

\* calculating the weights & distance from the sampling pixel to  $(x, y)$

$$dx = x - x_1$$

$$dy = y - y_1$$

\* The bilinear interpolation formula &

\* Interpolated value of  $p(x, y)$

$$\begin{aligned} p = & (v_{11} * (1 - dx) * (1 - dy)) + \\ & (v_{21} * dx * (1 - dy)) + \\ & (v_{12} * (1 - dx) * dy) + \\ & (v_{22} * dx * dy) \end{aligned}$$

Return  $p$  \* This is the interpolated value.

The python code based on my pseudocode and sample image

read\_pixel\_from\_image.py interpolation.ipynb waziri-Lab04.ipynb

Managed: http://localhost:8889

```
1 import math
2 def BilinearInterpolation(image, x, y):
3     width = len(image[0])
4     height = len(image)
5     x1 = math.floor(x)
6     x2 = math.ceil(x)
7     y1 = math.floor(y)
8     y2 = math.ceil(y)
9     if x1 < 0 or x2 >= width or y1 < 0 or y2 >= height:
10         return "Out of bounds"
11     Q11 = image[y1][x1]
12     Q21 = image[y1][x2]
13     Q12 = image[y2][x1]
14     Q22 = image[y2][x2]
15     dx = x - x1
16     dy = y - y1
17     P = (Q11 * (1 - dx) * (1 - dy) +
18          Q21 * dx * (1 - dy) +
19          Q12 * (1 - dx) * dy +
20          Q22 * dx * dy)
21     return P
22 image = [
23     [100, 150, 200, 250],
24     [120, 170, 220, 270],
25     [140, 190, 240, 290],
26     [160, 210, 260, 310]
27 ]
28 x = 1.5
29 y = 1.5
30 result = BilinearInterpolation(image, x, y)
31 print("Interpolated value:", result)
```

✓ [2] < 10 ms

Interpolated value: 205.0