



## Lab 5

### Camera calibration with OpenCV

#### Learning Objectives:

- *To use OpenCV for camera calibration*
- *Detect chessboard corners for calibration.*
- *Compute intrinsic parameters and distortion coefficients.*
- *Apply image undistortion to remove lens distortion.*
- *Use calibration for real-world applications like AR and robotics.*

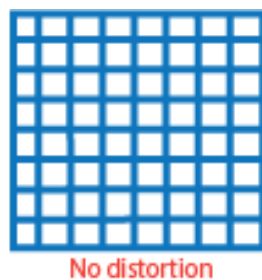
#### Introduction:

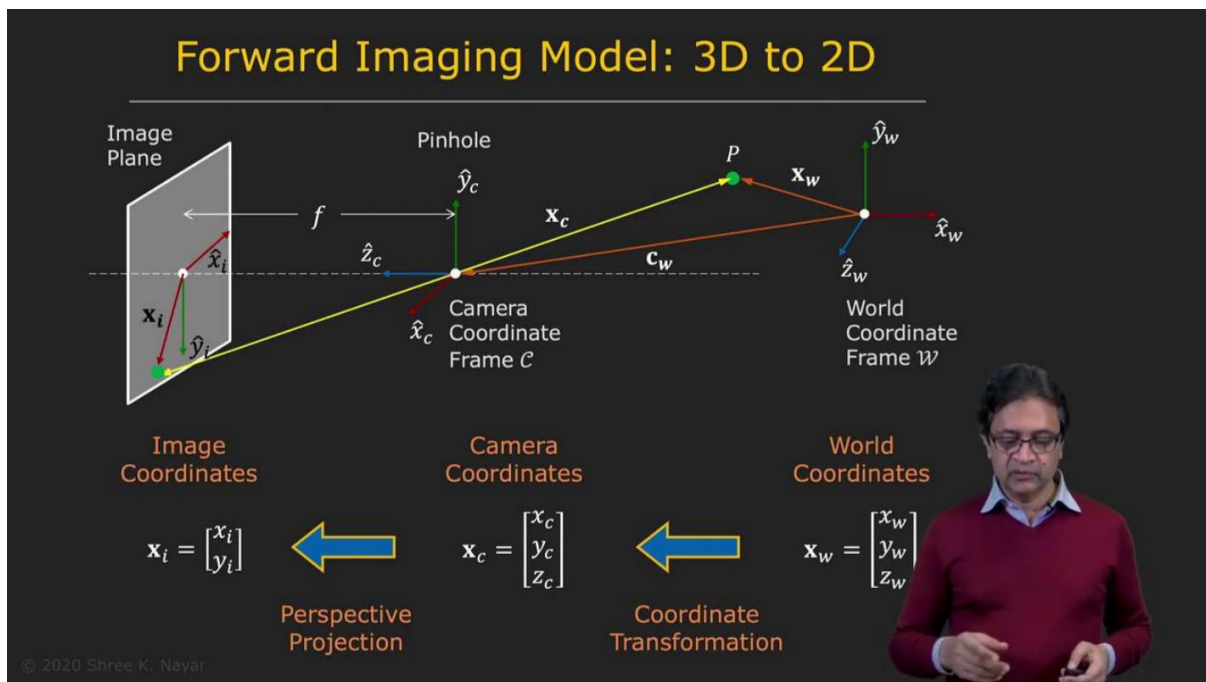
Camera calibration is an essential process in computer vision that allows us to correct distortions caused by a camera lens and accurately map real-world points onto an image. Calibration estimates the intrinsic and extrinsic parameters that define how a camera perceives the environment. This process is crucial for applications such as augmented reality (AR), 3D reconstruction, autonomous navigation, and object tracking.

Generally when we have a scene and we want to project it into an image 3D to 2D we need to find the projection matrix which include the intrinsic and extrinsic parameters , finding this matrix is camera calibration

#### Why Do We Need Camera Calibration:

When an image is captured using a camera, distortions cause straight lines to appear curved, affecting depth estimation and object localization. Calibration corrects these distortions, ensuring **accurate mapping of 3D world coordinates onto a 2D image plane**.





How 3D scene become a 2D image

## Projection Matrix $P$

Camera to Pixel

$$\begin{bmatrix} \tilde{u} \\ \tilde{v} \\ \tilde{w} \end{bmatrix} = \begin{bmatrix} f_x & 0 & o_x & 0 \\ 0 & f_y & o_y & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x_c \\ y_c \\ z_c \\ 1 \end{bmatrix}$$

$\tilde{\mathbf{u}} = M_{int} \tilde{\mathbf{x}}_c$

World to Camera

$$\begin{bmatrix} x_c \\ y_c \\ z_c \\ 1 \end{bmatrix} = \begin{bmatrix} r_{11} & r_{12} & r_{13} & t_x \\ r_{21} & r_{22} & r_{23} & t_y \\ r_{31} & r_{32} & r_{33} & t_z \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix}$$

$\tilde{\mathbf{x}}_c = M_{ext} \tilde{\mathbf{x}}_w$

Combining the above two equations, we get the full projection matrix  $P$ :

$$\tilde{\mathbf{u}} = M_{int} M_{ext} \tilde{\mathbf{x}}_w = P \tilde{\mathbf{x}}_w$$

$$\begin{bmatrix} \tilde{u} \\ \tilde{v} \\ \tilde{w} \end{bmatrix} = \begin{bmatrix} p_{11} & p_{12} & p_{13} & p_{14} \\ p_{21} & p_{22} & p_{23} & p_{24} \\ p_{31} & p_{32} & p_{33} & p_{34} \end{bmatrix} \begin{bmatrix} x_w \\ y_w \\ z_w \\ 1 \end{bmatrix}$$

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The final form of the projection Matrix

## Camera Model: Intrinsic and Extrinsic Parameters:

A camera model consists of:

1. **Intrinsic Parameters** (Internal camera properties):
  - **Focal length (fx, fy)**: Defines how much the camera magnifies the scene.
  - **Principal point (cx, cy)**: The image center where the optical axis meets the image plane.
  - **Distortion coefficients (k1, k2, p1, p2, k3)**: Corrects radial and tangential distortions.
2. **Extrinsic Parameters** (Defines camera position and orientation):
  - **Rotation matrix (R)**: Describes how the camera is rotated.
  - **Translation vector (T)**: Defines the camera's position in space.

Mathematical Model: The relationship between 3D world coordinates and 2D image points is:

$$\begin{bmatrix} u \\ v \\ 1 \end{bmatrix} = K \begin{bmatrix} R & T \end{bmatrix} \begin{bmatrix} X \\ Y \\ Z \\ 1 \end{bmatrix}$$

where K is the intrinsic matrix, and [R | T] represents the extrinsic parameters.

## Steps of Camera Calibration:

### Step 1: Capture Chessboard Images

- **Why?** A checkerboard pattern provides well-defined corners, which help estimate distortion parameters.
- The images used for calibration must be taken from different angles to ensure accurate parameter estimation.

### Step 2: Detect Chessboard Corners

- **Why?** Detecting corner points provides a mapping between the real-world 3D structure and the 2D image.
- This function detects the corners required for calibration.

```
ret, corners = cv2.findChessboardCorners(gray, checkerboard_size, None)
```

### Step 3: Store Object Points and Image Points

- **Why?** Object points represent real-world 3D coordinates, and image points represent their corresponding 2D projections.

```
objpoints.append(objp)  
imgpoints.append(corners)
```

- These lists store real-world and detected points for calibration.

### Step 4: Compute Camera Calibration Parameters

- **Why?** Computes intrinsic parameters (camera matrix) and distortion coefficients.

```
ret, mtx, dist, rvecs, tvecs = cv2.calibrateCamera(objpoints,  
imgpoints, gray.shape[::-1], None, None)
```

- **mtx:** Intrinsic matrix (focal length, principal point).
- **dist:** Distortion coefficients (radial and tangential distortion).
- **rvecs:**
- **tvecs:**

## 📌 Step 5: Apply Calibration to Remove Distortion

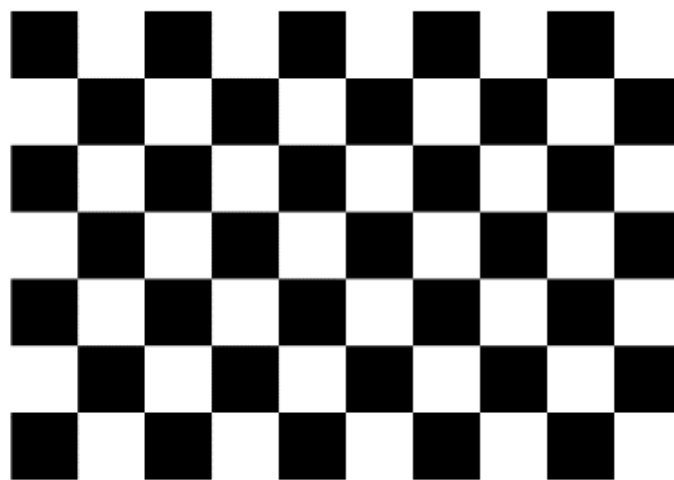
- **Why?** Corrects lens distortion and produces an undistorted image.

```
undistorted_img = cv2.undistort(img, mtx, dist, None, new_camera_mtx)
```

- cv2.undistort() removes distortions using the calibration parameters.

Lets do step 1 and 2

Task: Find Chessboard Corners for Calibration



The file is a 6x9 checkerboard pattern

```
import cv2
import numpy as np

# Load a checkerboard image
img = cv2.imread('checkerboard.jpg')
gray = cv2.cvtColor(img, cv2.COLOR_BGR2GRAY)

# Define chessboard size (columns, rows)
checkerboard_size = (6, 9)

# Find chessboard corners
ret, corners = cv2.findChessboardCorners(gray, checkerboard_size, None)

# Draw detected corners
if ret:
    img = cv2.drawChessboardCorners(img, checkerboard_size, corners, ret)
    cv2.imshow('Detected Corners', img)
    cv2.waitKey(0)
    cv2.destroyAllWindows()
```

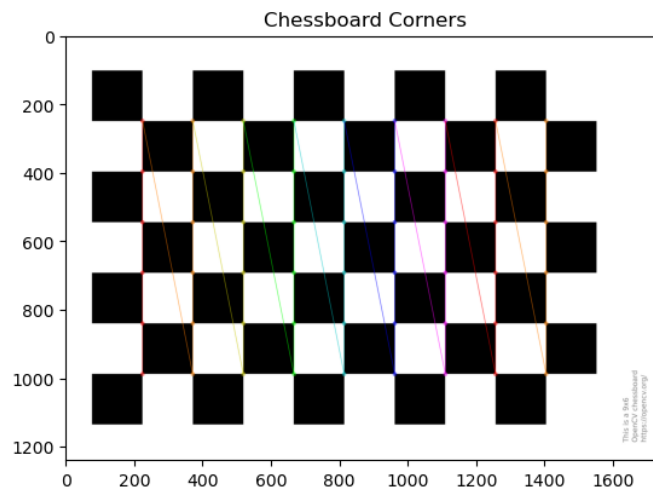
Lets do step 3 and 4

### Task: Compute Camera Parameters

- **Step 1:** Different viewpoints of check-board image is captured.



- **Step 2:** Find Chessboard Corners for each image



- **Step 3:** Store Object Points and Image Points
- **Step 4:** given all previous information we can calculate the camera parameters using *calibrateCamera()* function
- **Step 5:** print the extrinsic and intrinsic parameters

## Code Example:

```

import cv2
import numpy as np
import glob
import os

# Define the chessboard size (columns, rows)
checkerboard_size = (6, 9)

# Prepare object points
objp = np.zeros((checkerboard_size[0] * checkerboard_size[1], 3), np.float32)
objp[:, :2] = np.mgrid[0:checkerboard_size[0],
0:checkerboard_size[1]].T.reshape(-1, 2)

# Store object points and image points
objpoints = [] # Real world 3D points
imgpoints = [] # 2D points in image plane

# Define the path to the folder containing calibration images
image_folder = r'C:\Users\m.nasif\Desktop\CV\Lab 5\Images'

# Get all image file paths in the folder
image_files = glob.glob(os.path.join(image_folder, '*.jpg')) # Change '*.jpg'
to '*.png' if needed
# Process each image
for fname in image_files:
    img = cv2.imread(fname)

    if img is None:
        print(f"Warning: Could not read {fname}")
        continue

    gray = cv2.cvtColor(img, cv2.COLOR_BGR2GRAY)
    ret, corners = cv2.findChessboardCorners(gray, checkerboard_size, None)

    if ret:
        objpoints.append(objp)
        imgpoints.append(corners)

# Perform camera calibration
ret, mtx, dist, rvecs, tvecs = cv2.calibrateCamera(objpoints, imgpoints,
gray.shape[::-1], None, None)
# Print the camera matrix and distortion coefficients
print("Camera Matrix:\n", mtx)
print("Distortion Coefficients:\n", dist)

```

**Exercise 1:** Read image pattern from camera or folder and detect the pattern corners.

**Exercise 2:** Perform camera calibration using webcam and print the calibration parameters.

### **Bonus Task: Augmented Reality (AR) with Calibration**

#### **Objective:**

Use camera calibration data to overlay a **virtual object** in a real-world scene.

#### **Task:**

1. **Detect a chessboard pattern in real-time video.**
  2. **Correct distortions** using the camera matrix.
  3. **Overlay a 3D virtual object (cube or marker).**
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#### Reference:

- [Open CV camera calibration](#)
- [Video Tutorials for the theoretical part](#)