

# Training\_Bayes\_Classifier

November 30, 2019

## 0.1 Notebook Imports

```
In [1]: import pandas as pd
import numpy as np
```

## 0.2 Constants

```
In [2]: TRAINING_DATA_FILE = 'SpamData/02_Training/train-data.txt'
TEST_DATA_FILE = 'SpamData/02_Training/test-data.txt'

TOKEN_SPAM_PROB_FILE = 'SpamData/03_Testing/prob-spam.txt'
TOKEN_HAM_PROB_FILE = 'SpamData/03_Testing/prob-nonspam.txt'
TOKEN_ALL_PROB_FILE = 'SpamData/03_Testing/prob-all-tokens.txt'

TEST_FEATURE_MATRIX = 'SpamData/03_Testing/test-features.txt'
TEST_TARGET_FILE = 'SpamData/03_Testing/test-target.txt'

VOCAB_SIZE = 2500
```

## 0.3 Loading features from .txt file into NumPy Array

```
In [3]: sparse_train_data = np.loadtxt(TRAINING_DATA_FILE, delimiter=' ', dtype=int)

In [4]: sparse_test_data = np.loadtxt(TEST_DATA_FILE, delimiter=' ', dtype=int)

In [5]: sparse_train_data[:5]

Out[5]: array([[0, 0, 1, 1],
               [0, 1, 1, 1],
               [0, 2, 1, 1],
               [0, 6, 1, 1],
               [0, 9, 1, 1]])

In [6]: print('Number of rows in training file', sparse_train_data.shape[0])
print('Number of rows in test file', sparse_test_data.shape[0])
```

```
Number of rows in training file 260245
Number of rows in test file 115650
```

```
In [7]: print('Number of emails in training file', np.unique(sparse_train_data[:, 0]).size)
```

Number of emails in training file 4017

```
In [8]: print('Number of emails in test file', np.unique(sparse_test_data[:, 0]).size)
```

Number of emails in test file 1722

## 0.4 Creating Full Matrix from Sparse Matrix

```
In [9]: def make_full_matrix(sparse_matrix, nr_words, doc_idx=0, word_idx=1, cat_idx=2, freq_idx=3):  
        """
```

*Form a full matrix from a sparse matrix. Return a pandas dataframe.*

*Keyword arguments:*

*sparse\_matrix -- numpy array*

*nr\_words -- size of the vocabulary. Total number of tokens.*

*doc\_idx -- position of the document id in the sparse matrix. Default: 1st column*

*word\_idx -- position of the word id in the sparse matrix. Default: 2nd column*

*cat\_idx -- position of the label (spam is 1, nonspam is 0). Default: 3rd column*

*freq\_idx -- position of occurrence of word in sparse matrix. Default: 4th column*  
 """

```
        column_names = ['DOC_ID'] + ['CATEGORY'] + list(range(0, VOCAB_SIZE))
```

```
        doc_id_names = np.unique(sparse_matrix[:, 0])
```

```
        full_matrix = pd.DataFrame(index=doc_id_names, columns=column_names)
```

```
        full_matrix.fillna(value=0, inplace=True)
```

```
        for i in range(sparse_matrix.shape[0]):
```

```
            doc_nr = sparse_matrix[i][doc_idx]
```

```
            word_id = sparse_matrix[i][word_idx]
```

```
            label = sparse_matrix[i][cat_idx]
```

```
            occurrence = sparse_matrix[i][freq_idx]
```

```
            full_matrix.at[doc_nr, 'DOC_ID'] = doc_nr
```

```
            full_matrix.at[doc_nr, 'CATEGORY'] = label
```

```
            full_matrix.at[doc_nr, word_id] = occurrence
```

```
        full_matrix.set_index('DOC_ID', inplace=True)
```

```
        return full_matrix
```

```
In [10]: %%time
```

```
        full_train_data = make_full_matrix(sparse_train_data, VOCAB_SIZE)
```

CPU times: user 8.82 s, sys: 177 ms, total: 9 s

Wall time: 8.75 s

```
In [11]: full_train_data.head()
```

```
Out[11]:
```

	CATEGORY	0	1	2	3	4	5	6	7	8	...	2490	2491	2492	2493	\
DOC_ID											...					
0	1	1	1	1	0	0	0	1	0	0	...	0	0	0	0	
1	1	2	2	2	0	0	4	2	0	0	...	0	0	0	0	
2	1	0	5	4	1	26	0	5	36	2	...	0	0	0	0	
3	1	0	0	0	0	0	0	0	0	0	...	0	0	0	0	
4	1	0	0	0	0	0	0	0	1	0	...	0	0	0	0	

  

	2494	2495	2496	2497	2498	2499
DOC_ID						
0	0	0	0	0	0	0
1	0	0	0	0	0	0
2	0	0	0	0	0	0
3	0	0	0	0	0	0
4	0	0	0	0	0	0

[5 rows x 2501 columns]

## 1 Training the Naive Bayes Model

### 1.1 Calculating the probability of spam

```
In [12]: full_train_data.CATEGORY.size
```

```
Out[12]: 4017
```

```
In [13]: full_train_data.CATEGORY.sum()
```

```
Out[13]: 1252
```

```
In [14]: prob_spam = full_train_data.CATEGORY.sum()/full_train_data.CATEGORY.size
          print('Probability of spam is', prob_spam)
```

Probability of spam is 0.3116753796365447

### 1.2 Total Number of Words

```
In [15]: full_train_features = full_train_data.loc[:, full_train_data.columns != 'CATEGORY']
          full_train_features.head()
```

```
Out[15]:
```

	0	1	2	3	4	5	6	7	8	9	...	\
DOC_ID											...	
0	1	1	1	0	0	0	1	0	0	1	...	
1	2	2	2	0	0	4	2	0	0	2	...	
2	0	5	4	1	26	0	5	36	2	0	...	
3	0	0	0	0	0	0	0	0	0	0	...	

4	0	0	0	0	0	0	0	0	1	0	0	...
---	---	---	---	---	---	---	---	---	---	---	---	-----

  

	2490	2491	2492	2493	2494	2495	2496	2497	2498	2499
DOC_ID										
0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0
2	0	0	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0	0	0

[5 rows x 2500 columns]

```
In [16]: email_lengths = full_train_features.sum(axis=1)
email_lengths.shape
```

```
Out[16]: (4017,)
```

```
In [17]: email_lengths[:5]
```

```
Out[17]: DOC_ID
0      166
1      165
2     1367
3       21
4       24
dtype: int64
```

```
In [18]: total_wc = email_lengths.sum()
total_wc
```

```
Out[18]: 426844
```

### 1.3 Number of Tokens in Spam & Ham Emails

```
In [19]: spam_lengths = email_lengths[full_train_data.CATEGORY == 1]
spam_lengths.shape
```

```
Out[19]: (1252,)
```

```
In [20]: spam_wc = spam_lengths.sum()
spam_wc
```

```
Out[20]: 177155
```

```
In [21]: ham_lengths = email_lengths[full_train_data.CATEGORY == 0]
ham_lengths.shape
```

```
Out[21]: (2765,)
```

```
In [22]: nonspam_wc = ham_lengths.sum()
nonspam_wc
```

```
Out[22]: 249689
```

```
In [23]: spam_wc + nonspam_wc - total_wc
```

```
Out[23]: 0
```

```
In [24]: print('Average number of words in spam emails {:.0f}'.format(spam_wc / spam_lengths.sum()))
         print('Average number of words in ham emails {:.0f}'.format(nonspam_wc / ham_lengths.sum()))
```

```
Average number of words in spam emails 141
```

```
Average number of words in ham emails 90
```

## 1.4 Summing the Tokens occuring in Spam

```
In [25]: full_train_features.shape
```

```
Out[25]: (4017, 2500)
```

```
In [26]: train_spam_tokens = full_train_features.loc[full_train_data.CATEGORY == 1]
         train_spam_tokens.head()
```

```
Out[26]:
```

	0	1	2	3	4	5	6	7	8	9	...	\
DOC_ID											...	
0	1	1	1	0	0	0	1	0	0	1	...	
1	2	2	2	0	0	4	2	0	0	2	...	
2	0	5	4	1	26	0	5	36	2	0	...	
3	0	0	0	0	0	0	0	0	0	0	...	
4	0	0	0	0	0	0	0	1	0	0	...	

  

	2490	2491	2492	2493	2494	2495	2496	2497	2498	2499
DOC_ID										
0	0	0	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0
2	0	0	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	0	0	0
4	0	0	0	0	0	0	0	0	0	0

[5 rows x 2500 columns]

```
In [27]: train_spam_tokens.shape
```

```
Out[27]: (1252, 2500)
```

```
In [28]: summed_spam_tokens = train_spam_tokens.sum(axis=0) + 1
         summed_spam_tokens.shape
```

```
Out[28]: (2500,)
```

```
In [29]: summed_spam_tokens.tail()
```

```
Out [29]: 2495    24
          2496    23
          2497    18
          2498    11
          2499     9
          dtype: int64
```

## 1.5 Summing the Tokens Occuring in Ham

```
In [30]: train_ham_tokens = full_train_features.loc[full_train_data.CATEGORY == 0]
          summed_ham_tokens = train_ham_tokens.sum(axis=0) + 1
```

```
In [31]: summed_ham_tokens.shape
```

```
Out [31]: (2500,)
```

```
In [32]: summed_ham_tokens.tail()
```

```
Out [32]: 2495    11
          2496     1
          2497    20
          2498    12
          2499    18
          dtype: int64
```

## 1.6 $P(\text{word} | \text{Spam})$ - Probability that a Token Occurs given the Email is Spam

```
In [33]: prob_tokens_spam = summed_spam_tokens / (spam_wc + VOCAB_SIZE)
          prob_tokens_spam[:5]
```

```
Out [33]: 0    0.010303
          1    0.004859
          2    0.007832
          3    0.012262
          4    0.006835
          dtype: float64
```

## 1.7 $P(\text{word} | \text{Ham})$ - Probability that a Token Occurs given the Email is Non Spam

```
In [34]: prob_tokens_nonspam = summed_ham_tokens / (nonspam_wc + VOCAB_SIZE)
          prob_tokens_nonspam[:5]
```

```
Out [34]: 0    0.020877
          1    0.009937
          2    0.008069
          3    0.003549
          4    0.006626
          dtype: float64
```

## 1.8 P(Word) - Probability that Token Occurs

```
In [35]: prob_tokens_all = full_train_features.sum(axis=0) / total_wc
```

```
In [36]: prob_tokens_all.sum()
```

```
Out[36]: 1.0
```

## 1.9 Save the Trained Model

```
In [37]: np.savetxt(TOKEN_SPAM_PROB_FILE, prob_tokens_spam)
         np.savetxt(TOKEN_HAM_PROB_FILE, prob_tokens_nonspam)
         np.savetxt(TOKEN_ALL_PROB_FILE, prob_tokens_all)
```

## 1.10 Prepare Test Data

```
In [38]: sparse_test_data.shape
```

```
Out[38]: (115650, 4)
```

```
In [39]: %%time
         full_test_data = make_full_matrix(sparse_test_data, nr_words=VOCAB_SIZE)
```

```
CPU times: user 4.19 s, sys: 122 ms, total: 4.31 s
```

```
Wall time: 4.06 s
```

```
In [40]: X_test = full_test_data.loc[:, full_test_data.columns != 'CATEGORY']
         y_test = full_test_data.CATEGORY
```

```
In [41]: np.savetxt(TEST_TARGET_FILE, y_test)
         np.savetxt(TEST_FEATURE_MATRIX, X_test)
```