

Homework: Formal Relational Languages

Emp (eid: integer, ename: string, age: integer, salary: real)

Works (eid: integer, did: integer, pc_time: integer)

Dept (did: integer, dname: string, budge: real, managerid: integer)

1. Return names of every employee who works in the "Hardware", "Software", and "Research" departments.

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Datalog:
    Q1(ename) :- Emp(eid, ename, _, _), Works(eid, did, _), Dept(did, "Hardware",
_, _)
    Q1(ename) :- Emp(eid, ename, _, _), Works(eid, did, _), Dept(did, "Software",
_, _)
    Q1(ename) :- Emp(eid, ename, _, _), Works(eid, did, _), Dept(did, "Research",
_, _)
```

```
Relational Algebra:
     $\pi(ename)(\sigma(dname = "Hardware" \vee dname = "Software" \vee dname = "Research")(Dept \bowtie Works \bowtie Emp))$ 
```

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Relational Calculus:
    Q1(eid, ename, age, salary) =  $\exists eid (Emp(eid, ename, age, salary) \wedge Works(eid, did, pc\_time) \wedge Dept(did, dname, budge, managerid) \wedge (dname = "Hardware" \vee dname = "Software" \vee dname = "Research"))$ 
```

2. Return the names of every department without any employee.

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Datalog:
    Q2(dname) :- Dept(did, dname, _, _), Not Works(_, did, _)
```

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Relational Algebra:
     $\pi(dname)(Dept) - \pi(dname)(\sigma(did = did)(Dept \bowtie Works))$ 
```

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Relational Calculus:
    Q2(did, dname, budge, managerid) =  $Dept(did, dname, budge, managerid) \wedge \text{not}(\exists eid (Works(eid, did, pc\_time)))$ 
```

3. Print the managerid of managers who manage only departments with budgets greater than \$1.5 million.

```
Datalog:
    Q3(managerid) :- Dept(_, _, budge, managerid), budge > 1500000
```

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Relational Algebra:
     $\pi(managerid)(\sigma(budge > 1500000)(Dept))$ 
```

Relational Calculus:

$Q3(\text{managerid}) = \forall \text{did} (\text{Dept}(\text{did}, \text{dname}, \text{budge}, \text{managerid}) \rightarrow \text{budge} > 1.5 \text{ million})$

4. Print the name of employees whose salary is less than or equal to the salary of every employee.

Datalog:

$Q4(\text{ename}) :- \text{Emp}(_, \text{ename}, _, \text{salary}), \text{not } (\text{Emp}(_, _, _, \text{salary2}), \text{salary} > \text{salary2}).$

Relational Algebra:

$\pi(\text{ename}) (\sigma(\text{salary} \leq \sigma(\pi(\text{salary}) (\text{Emp})) (\text{Emp}))$

Relational Calculus:

$Q4(\text{eid}, \text{ename}, \text{age}, \text{salary}) = \text{Emp}(\text{eid}, \text{ename}, \text{age}, \text{salary}) \wedge \forall \text{eid2} (\text{Emp}(\text{eid2}, \text{ename2}, \text{age2}, \text{salary2}) \rightarrow \text{salary} \leq \text{salary2})$

Notes:

Datalog:

Movie(mid, title, year, earned)

Actor(aid, aname, b-year)

Plays(mid, aid)

actor who played in a movie whose earned = \$20

$Q1(\text{aname}) :- \text{Actor}(\text{aid}, \text{aname}, _), \text{Plays}(\text{mid}, \text{aid}), \text{Movie}(\text{mid}, _, _, 20)$

actors who played in a movie whose earned = 20 AND movies made in 1998

$Q2(\text{aname}) :- \text{Actor}(\text{aid}, \text{aname}, _), \text{Plays}(\text{mid1}, \text{aid}), \text{Movie}(\text{mid1}, _, _, 20), \\ \text{Plays}(\text{mid2}, \text{aid}), \text{Movie}(\text{mid2}, _, 1998, _)$

actors who played in a movie whose earned = 20 OR movies made in 1990

$Q3(\text{aname}) :- \text{Actor}(\text{aid}, \text{aname}, _), \text{Plays}(\text{mid}, \text{aid}), \text{Movie}(\text{mid}, _, _, 20) \\ Q3(\text{aname}) :- \text{Actor}(\text{aid}, \text{aname}, _), \text{Plays}(\text{mid}, \text{aid}), \text{Movie}(\text{mid}, _, 1990, _)$

actors who played in a movie with earned >= 20 OR a movie made after 1990

$Q4(\text{aname}) :- \text{Actor}(\text{aid}, \text{aname}, _), \text{Plays}(\text{mid}, \text{aid}), \text{Movie}(\text{mid}, _, _, \text{earned}), \\ \text{earned} > 20 \\ Q4(\text{aname}) :- \text{Actor}(\text{aid}, \text{aname}, _), \text{Plays}(\text{mid}, \text{aid}), \text{Movie}(\text{mid}, _, \text{year}, _), \text{year} > 1990$

all actors who did NOT play in a movie with "Rob"

$UQ5(\text{aid}, \text{aname}, \text{b-year}) :- \text{Actor}(\text{aid1}, \text{aname}, _), \text{Plays}(\text{mid}, \text{aid1}), \text{Plays}(\text{mid}, \text{aid2}), \text{Actor}(\text{aid2}, \text{"Rob"}, _) \text{ \# make a table with all actors who did play with Rob}$

```
Q5(aname) :- Actor(_, aname, _), NOT UQ5(aid, aname, b-year) # select all actores
not in table UQ5
```

Relational Algebra (RA):

Selection: σ = SELECT rows

Projection: π = SELECT columns

Cross-product: X = combines two relations in all combinations

Set-difference: - = tuples in table1 but not in table 2

Union: U = tuples in table 1 and in table 2

Join: \bowtie = cross product but on an id

Movie(mid, title, year, earned)

Actor(aid, aname, b-year)

Plays(mid, aid)

Actor:

aid = 1, 2, 3

aname = rob, al, jon

b-year = 1954, 1958, 1992

Plays:

mid = 20, 30

aid = 1, 2

1. select actor who birth year is greater than 1990

$\sigma(b\text{-year} > 1990)\text{Actor}$

2. select only actors names

$\pi(\text{aname})\text{Actor}$

3. make a single table out of Actor and Plays

$\text{Actor} \bowtie \text{Plays}$

4. make a single table out of Actor and Plays, match on aid

$R \bowtie cS = \sigma c(R \bowtie S)$

$\text{Actor} \bowtie (\text{Actor.aid} = \text{Plays.aid})\text{Plays}$

Relational Calculus (RC):

Atom: $\text{Actor}(_, _, _)$

Conjunction: $P \wedge P$

Disjunction: $P \vee P$

Implication: $P \rightarrow P$

Negaction: $\text{not}(P)$

For all x P holds: $\forall x.P$

For an x P holds: $\exists x.P$ = existential(not used, = $_$)

1. actors who played in a movie with earned = 2000

```
Q1(_, _, _) =  $\exists$ _.(Actor(aid, _, _) ^ Plays(mid, aid) ^ Movie(mid, _, _, 2000))
```

2. actors who played only in movies produced in 1990

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Q2(x) =  $\forall$ y.Play(y, x)  $\rightarrow$   $\exists$ z. $\exists$ t.Movie(y, z, 1990, t)
```

3. actors who played in some movies with only one actor

```
Q3(x) =  $\exists$ y.Play(y, x) ^  $\forall$ z. $\forall$ t(Play(y, z) ^ Play(y, t)  $\rightarrow$  z = t)
```