

# Homework: Formal Relational Languages

Emp (eid: integer, ename: string, age: integer, salary: real)

Works (eid: integer, did: integer, pc\_time: integer)

Dept (did: integer, dname: string, budge: real, managerid: integer)

1. Return names of every employee who works in the "Hardware", "Software", and "Research" departments.

```
Datalog:
    Q1(ename) :- Emp(eid, ename, _, _), Works(eid, did, _), Dept(did, "Hardware",
_, _)
    Q1(ename) :- Emp(eid, ename, _, _), Works(eid, did, _), Dept(did, "Software",
_, _)
    Q1(ename) :- Emp(eid, ename, _, _), Works(eid, did, _), Dept(did, "Research",
_, _)
```

```
Relational Algebra:
     $\pi(\text{ename})(\sigma(\text{dname} = \text{"Hardware"} \vee \text{dname} = \text{"Software"} \vee \text{dname} = \text{"Research"})(\text{Dept} \bowtie \text{Works} \bowtie \text{Emp}))$ 
```

```
Relational Calculus:
    Q1(eid, ename, age, salary) =  $\exists \text{eid}(\text{Emp}(\text{eid}, \text{ename}, \text{age}, \text{salary}) \wedge \text{Works}(\text{eid}, \text{did}, \text{pc\_time}) \wedge \text{Dept}(\text{did}, \text{dname}, \text{budge}, \text{managerid}) \wedge (\text{dname} = \text{"Hardware"} \vee \text{dname} = \text{"Software"} \vee \text{dname} = \text{"Research"}))$ 
```

2. Return the names of every department without any employee.

```
Datalog:
    Q2(dname) :- Dept(did, dname, _, _), Not Works(_, did, _)
```

```
Relational Algebra:
     $\pi(\text{dname})(\text{Dept}) - \pi(\text{dname})(\sigma(\text{did} = \text{did})(\text{Dept} \bowtie \text{Works}))$ 
```

```
Relational Calculus:
    Q2(did, dname, budge, managerid) =  $\text{Dept}(\text{did}, \text{dname}, \text{budge}, \text{managerid}) \wedge \text{not}(\exists \text{eid}(\text{Works}(\text{eid}, \text{did}, \text{pc\_time})))$ 
```

3. Print the managerid of managers who manage only departments with budgets greater than \$1.5 million.

```
Datalog:
    Q3(managerid) :- Dept(_, _, budge, managerid), budge > 1500000
```

```
Relational Algebra:
```

```
 $\pi(\text{managerid}) (\sigma(\text{budge} > 1500000) (\text{Dept}))$ 
```

Relational Calculus:

```
Q3(managerid) =  $\forall \text{did} (\text{Dept}(\text{did}, \text{dname}, \text{budge}, \text{managerid}) \rightarrow \text{budge} > 1.5 \text{ million})$ 
```

4. Print the name of employees whose salary is less than or equal to the salary of every employee.

Datalog:

```
Q4(ename) :- Emp(_, ename, _, salary), not (Emp(_, _, _, salary2), salary > salary2).
```

Relational Algebra:

```
 $\pi(\text{ename}) (\sigma(\text{salary} \leq \sigma(\pi(\text{salary}) (\text{Emp})) (\text{Emp}))$ 
```

Relational Calculus:

```
Q4(eid, ename, age, salary) = Emp(eid, ename, age, salary)  $\wedge$   
 $\forall \text{eid2} (\text{Emp}(\text{eid2}, \text{ename2}, \text{age2}, \text{salary2}) \rightarrow \text{salary} \leq \text{salary2})$ 
```

Notes:

Datalog:

```
Movie(mid, title, year, earned)
```

```
Actor(aid, aname, b-year)
```

```
Plays(mid, aid)
```

actor who played in a movie whose earned = \$20

```
Q1(aname) :- Actor(aid, aname, _), Plays(mid, aid), Movie(mid, _, _, 20)
```

actors who played in a movie whose earned = 20 AND movies made in 1998

```
Q2(aname) :- Actor(aid, aname, _), Plays(mid1, aid), Movie(mid1, _, _, 20),  
Plays(mid2, aid), Movie(mid2, _, 1998, _)
```

actors who played in a movie whose earned = 20 OR movies made in 1990

```
Q3(aname) :- Actor(aid, aname, _), Plays(mid, aid), Movie(mid, _, _, 20)  
Q3(aname) :- Actor(aid, aname, _), Plays(mid, aid), Movie(mid, _, 1990, _)
```

actors who played in a movie with earned >= 20 OR a movie made after 1990

```
Q4(aname) :- Actor(aid, aname, _), Plays(mid, aid), Movie(mid, _, _, earned),  
earned > 20
```

```
Q4(aname) :- Actor(aid, aname, _), Plays(mid, aid), Movie(mid, _, year, _), year > 1990
```

all actors who did NOT play in a movie with "Rob"

```

    UQ5(aid, aname, b-year) :- Actor(aid1, aname, _), Plays(mid, aid1), Plays(mid,
aid2), Actor(aid2, "Rob", _) # make a table with all actors who did play with Rob
    Q5(aname) :- Actor(_, aname, _), NOT UQ5(aid, aname, b-year) # select all actores
not in table UQ5

```

Relational Algebra (RA):

Selection:  $\sigma$  = SELECT rows

Projection:  $\pi$  = SELECT columns

Cross-product: X = combines two relations in all combinations

Set-difference: - = tuples in table1 but not in table 2

Union: U = tuples in table 1 and in table 2

Join:  $\bowtie$  = cross product but on an id

Movie(mid, title, year, earned)

Actor(aid, aname, b-year)

Plays(mid, aid)

Actor:

aid = 1, 2, 3

aname = rob, al, jon

b-year = 1954, 1958, 1992

Plays:

mid = 20, 30

aid = 1, 2

1. select actor who birth year is greater than 1990

$\sigma(b\text{-year} > 1990)\text{Actor}$

2. select only actors names

$\pi(\text{aname})\text{Actor}$

3. make a single table out of Actor and Plays

$\text{Actor} \bowtie \text{Plays}$

4. make a single table out of Actor and Plays, match on aid

$\# R \bowtie cS = \sigma c(R \bowtie S)$

$\text{Actor} \bowtie (\text{Actor.aid} = \text{Plays.aid})\text{Plays}$

Relational Calculus (RC):

Atom:  $\text{Atom}(\_, \_, \_)$

Conjunction:  $P \wedge P$

Disjunction:  $P \vee P$

Implication:  $P \rightarrow P$

Negaction:  $\text{not}(P)$

For all  $x$   $P$  holds:  $\forall x.P$

For an  $x$   $P$  holds:  $\exists x.P$  = existential(not used, =  $\_$ )

1. actors who played in a movie with earned = 2000  

$$Q1(\_, \_, \_) = \exists \_. (\text{Actor}(\text{aid}, \_, \_) \wedge \text{Plays}(\text{mid}, \text{aid}) \wedge \text{Movie}(\text{mid}, \_, \_, 2000))$$
2. actors who played only in movies produced in 1990  

$$Q2(x) = \forall y. \text{Play}(y, x) \rightarrow \exists z. \exists t. \text{Movie}(y, z, 1990, t)$$
3. actors who played in some movies with only one actor  

$$Q3(x) = \exists y. \text{Play}(y, x) \wedge \forall z. \forall t. (\text{Play}(y, z) \wedge \text{Play}(y, t) \rightarrow z = t)$$