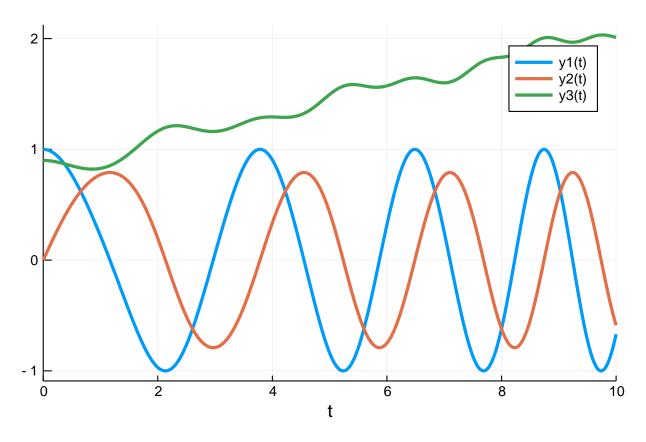
Rigid Body Work-Precision Diagrams

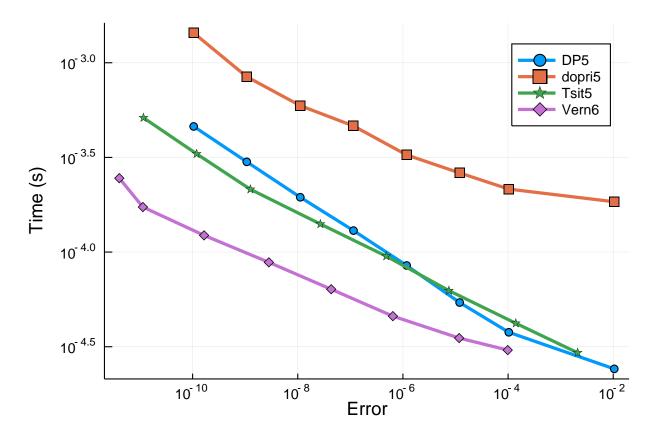
Chris Rackauckas

September 26, 2019

```
{\tt using} \ {\tt OrdinaryDiffEq}, \ {\tt ParameterizedFunctions}, \ {\tt ODE}, \ {\tt ODEInterfaceDiffEq}, \ {\tt LSODA}, \\
      Sundials, DiffEqDevTools
k(t) = 0.25*sin(t)^2
g = @ode_def RigidBody begin
  dy1 = I_1*y2*y3
  dy2 = I_2*y1*y3
  dy3 = I_3*y1*y2 + k(t)
end I_1 I_2 I_3
p = [-2.0, 1.25, -0.5]
prob = ODEProblem(g,[1.0;0.0;0.9],(0.0,10.0),p)
abstols = 1.0 ./ 10.0 .^{(6:13)}
reltols = 1.0 ./ 10.0 .^ (3:10);
sol = solve(prob, Vern7(), abstol=1/10^14, reltol=1/10^14)
test_sol = TestSolution(sol)
using Plots; gr()
plot(sol)
```



 $\label{lem:workPrecisionSet} Work Precision Set (prob, abstols, reltols, setups; appxsol=test_sol, save_every step=true, numruns=100, maxipulot (wp)$



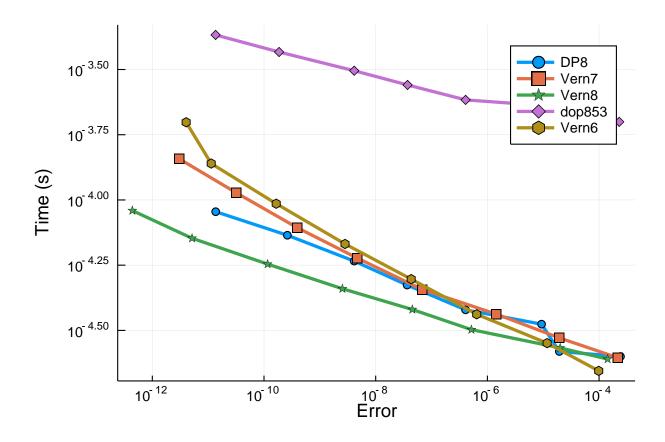
The DifferentialEquations.jl algorithms once again pull ahead. This is the first benchmark we've ran where ode45 doesn't fail. However, it still doesn't do as well as Tsit5. One reason why it does so well is that the maximum norm that ODE.jl uses (as opposed to the L2 norm of Sundials, DifferentialEquations, and ODEInterface) seems to do really well on this problem. dopri5 does surprisingly bad in this test.

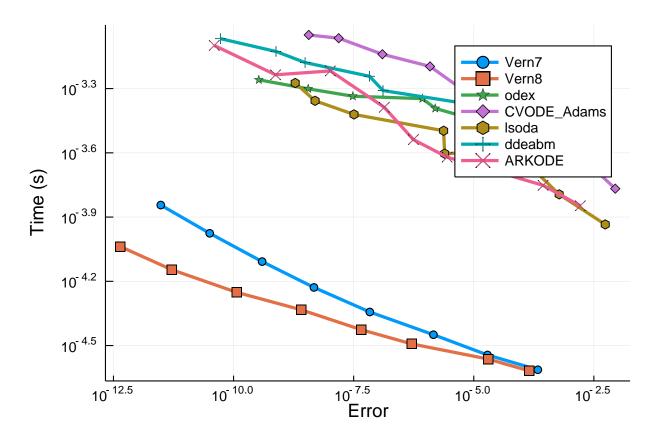
0.1 Higher Order

setups = [Dict(:alg=>DP8())

#Dict(:alg=>ode78()) # fails

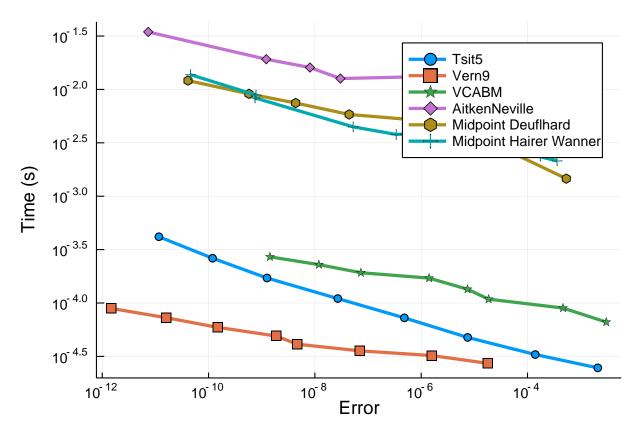
```
Dict(:alg=>Vern7())
    Dict(:alg=>Vern8())
    Dict(:alg=>dop853())
    Dict(:alg=>Vern6())
]
wp =
    WorkPrecisionSet(prob,abstols,reltols,setups;appxsol=test_sol,save_everystep=false,numruns=100,maxplot(wp)
```

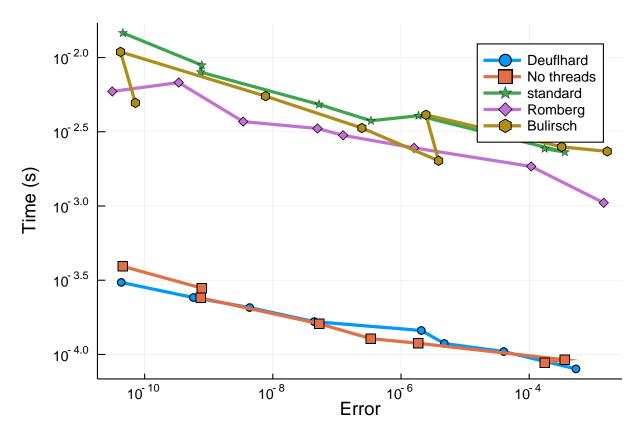


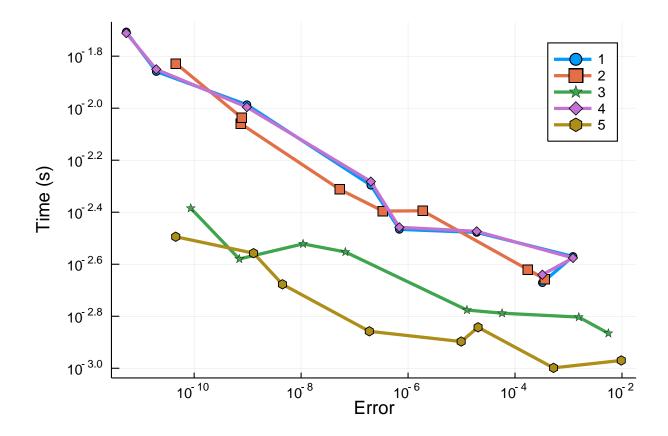


0.2 Comparison with Non-RK methods

Now let's test Tsit5 and Vern9 against parallel extrapolation methods and an Adams-Bashforth-Moulton:







0.2.1 Conclusion

Once again, the OrdinaryDiffEq.jl pull far ahead in terms of speed and accuracy.

```
using DiffEqBenchmarks
DiffEqBenchmarks.bench_footer(WEAVE_ARGS[:folder],WEAVE_ARGS[:file])
```

0.3 Appendix

These benchmarks are a part of the DiffEqBenchmarks.jl repository, found at: https://github.com/JuliaDirous locally run this tutorial, do the following commands:

```
using DiffEqBenchmarks
DiffEqBenchmarks.weave_file("NonStiffODE","RigidBody_wpd.jmd")
```

Computer Information:

```
Julia Version 1.2.0

Commit c6da87ff4b (2019-08-20 00:03 UTC)

Platform Info:

OS: Linux (x86_64-pc-linux-gnu)

CPU: Intel(R) Xeon(R) CPU E5-2680 v4 @ 2.40GHz

WORD_SIZE: 64

LIBM: libopenlibm

LLVM: libLLVM-6.0.1 (ORCJIT, haswell)
```

Environment:

JULIA NUM THREADS = 16

Package Information:

```
Status: `/home/crackauckas/.julia/dev/DiffEqBenchmarks/Project.toml`
[a134a8b2-14d6-55f6-9291-3336d3ab0209] BlackBoxOptim 0.5.0
[f3b72e0c-5b89-59e1-b016-84e28bfd966d] DiffEqDevTools 2.15.0
[1130ab10-4a5a-5621-a13d-e4788d82bd4c] DiffEqParamEstim 1.8.0
[a077e3f3-b75c-5d7f-a0c6-6bc4c8ec64a9] DiffEqProblemLibrary 4.5.1
[ef61062a-5684-51dc-bb67-a0fcdec5c97d] DiffEqUncertainty 1.2.0
[7073ff75-c697-5162-941a-fcdaad2a7d2a] IJulia 1.20.0
[7f56f5a3-f504-529b-bc02-0b1fe5e64312] LSODA 0.6.1
[76087f3c-5699-56af-9a33-bf431cd00edd] NLopt 0.5.1
[c030b06c-0b6d-57c2-b091-7029874bd033] ODE 2.5.0
[54ca160b-1b9f-5127-a996-1867f4bc2a2c] ODEInterface 0.4.6
[09606e27-ecf5-54fc-bb29-004bd9f985bf] ODEInterfaceDiffEq 3.4.0
[1dea7af3-3e70-54e6-95c3-0bf5283fa5ed] OrdinaryDiffEq 5.17.1
[65888b18-ceab-5e60-b2b9-181511a3b968] ParameterizedFunctions 4.2.1
[91a5bcdd-55d7-5caf-9e0b-520d859cae80] Plots 0.26.3
[c3572dad-4567-51f8-b174-8c6c989267f4] Sundials 3.7.0
[44d3d7a6-8a23-5bf8-98c5-b353f8df5ec9] Weave 0.9.1
[b77e0a4c-d291-57a0-90e8-8db25a27a240] InteractiveUtils
[d6f4376e-aef5-505a-96c1-9c027394607a] Markdown
[44cfe95a-1eb2-52ea-b672-e2afdf69b78f] Pkg
[9a3f8284-a2c9-5f02-9a11-845980a1fd5c] Random
```