

Adaptive Efficiency Tests

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April 29, 2019

```
using Distributed
addprocs(2)

@everywhere begin
    using DiffEqMonteCarlo, StochasticDiffEq, DiffEqBase, DiffEqProblemLibrary,
        DiffEqNoiseProcess, Plots, ParallelDataTransfer
    using DiffEqProblemLibrary.SDEProblemLibrary: importsdeproblems; importsdeproblems()
    import DiffEqProblemLibrary.SDEProblemLibrary: prob_sde_additive,
        prob_sde_linear, prob_sde_wave

    probs = Matrix{SDEProblem}(undef,3,3)
    p1 = Vector{Any}(undef,3)
    p2 = Vector{Any}(undef,3)
    p3 = Vector{Any}(undef,3)
    ## Problem 1
    prob = prob_sde_linear
    probs[1,1] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
    probs[1,2] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
    probs[1,3] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
    ## Problem 2
    prob = prob_sde_wave
    probs[2,1] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
    probs[2,2] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
    probs[2,3] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
    ## Problem 3
    prob = prob_sde_additive
    probs[3,1] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
    probs[3,2] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
    probs[3,3] =
        SDEProblem(prob.f,prob.g,prob.u0,prob.tspan,prob.p,noise=WienerProcess(0.0,0.0,0.0,rswn=RSWM(adapt
end
```

Error: On worker 2:

ArgumentError: Package DiffEqMonteCarlo not found in current path:

- Run `import Pkg; Pkg.add("DiffEqMonteCarlo")` to install the DiffEqMonteCarlo package.

```

require at ./loading.jl:823
top-level scope at none:3
eval at ./boot.jl:328
#116 at /buildworker/worker/package_linux64/build/usr/share/julia/stdlib/v1
.1/Distributed/src/process_messages.jl:276
run_work_thunk at /buildworker/worker/package_linux64/build/usr/share/julia
/stdlib/v1.1/Distributed/src/process_messages.jl:56
run_work_thunk at /buildworker/worker/package_linux64/build/usr/share/julia
/stdlib/v1.1/Distributed/src/process_messages.jl:65
#102 at ./task.jl:259
#remotecall_wait#154(::Base.Iterators.Pairs{Union{},Union{},Tuple{},NamedTu
ple{(),Tuple{}}}, ::Function, ::Function, ::Distributed.Worker, ::Module, :
:Vararg{Any,N} where N) at /buildworker/worker/package_linux64/build/usr/sh
are/julia/stdlib/v1.1/Distributed/src/remotecall.jl:421
remotecall_wait(::Function, ::Distributed.Worker, ::Module, ::Vararg{Any,N}
 where N) at /buildworker/worker/package_linux64/build/usr/share/julia/stdl
ib/v1.1/Distributed/src/remotecall.jl:412
#remotecall_wait#157(::Base.Iterators.Pairs{Union{},Union{},Tuple{},NamedTu
ple{(),Tuple{}}}, ::Function, ::Function, ::Int64, ::Module, ::Vararg{Any,N
} where N) at /buildworker/worker/package_linux64/build/usr/share/julia/std
lib/v1.1/Distributed/src/remotecall.jl:433
remotecall_wait(::Function, ::Int64, ::Module, ::Vararg{Any,N} where N) at
/buildworker/worker/package_linux64/build/usr/share/julia/stdlib/v1.1/Distr
ibuted/src/remotecall.jl:433
(::getfield(Distributed, Symbol("##163#165")){Module,Expr})() at ./task.jl:
259

```

...and 124 more exception(s).

```

fullMeans = Vector{Array}(undef,3)
fullMedians = Vector{Array}(undef,3)
fullElapsed = Vector{Array}(undef,3)
fullTols = Vector{Array}(undef,3)
offset = 0

```

```
Ns = [17 23 17]
```

```

1×3 Array{Int64,2}:
 17  23  17

```

Timings are only valid if no workers die. Workers die if you run out of memory.

```

for k in 1:size(probs,1)
    println("Problem $k")
    ## Setup
    N = Ns[k]

    msims = Vector{Any}(undef,N)
    elapsed = Array{Float64}(undef,N,3)
    medians = Array{Float64}(undef,N,3)
    means   = Array{Float64}(undef,N,3)
    tols    = Array{Float64}(undef,N,3)

    ## Compile
    prob = probs[k,1]
    ParallelDataTransfer.sendto(workers(), prob=prob)
    monte_prob = MonteCarloProblem(prob)

    solve(monte_prob,SRIW1(),dt=1/2^(4),adaptive=true,num_monte=1000,abstol=2.0^(-1),reltol=0)

```

```

println("RSwM1")
for i=1+offset:N+offset
    tols[i-offset,1] = 2.0^(-i-1)
    msims[i-offset] = DiffEqBase.calculate_monte_errors(solve(monte_prob,SRIW1(),
                                                              num_monte=1000,abstol=2.0^(-i-1),
                                                              reltol=0,force_dtmin=true))
    elapsed[i-offset,1] = msims[i-offset].elapsedTime
    medians[i-offset,1] = msims[i-offset].error_medians[:final]
    means[i-offset,1] = msims[i-offset].error_means[:final]
end

println("RSwM2")
prob = probs[k,2]

ParallelDataTransfer.sendto(workers(), prob=prob)
monte_prob = MonteCarloProblem(prob)

solve(monte_prob,SRIW1(),dt=1/2^(4),adaptive=true,num_monte=1000,abstol=2.0^(-1),reltol=0)

for i=1+offset:N+offset
    tols[i-offset,2] = 2.0^(-i-1)
    msims[i-offset] = DiffEqBase.calculate_monte_errors(solve(monte_prob,SRIW1(),
                                                              num_monte=1000,abstol=2.0^(-i-1),
                                                              reltol=0,force_dtmin=true))
    elapsed[i-offset,2] = msims[i-offset].elapsedTime
    medians[i-offset,2] = msims[i-offset].error_medians[:final]
    means[i-offset,2] = msims[i-offset].error_means[:final]
end

println("RSwM3")
prob = probs[k,3]
ParallelDataTransfer.sendto(workers(), prob=prob)
monte_prob = MonteCarloProblem(prob)

solve(monte_prob,SRIW1(),dt=1/2^(4),adaptive=true,num_monte=1000,abstol=2.0^(-1),reltol=0)

for i=1+offset:N+offset
    tols[i-offset,3] = 2.0^(-i-1)
    msims[i-offset] = DiffEqBase.calculate_monte_errors(solve(monte_prob,SRIW1(),
                                                              adaptive=true,num_monte=1000,abstol=2.0^(-i-1),
                                                              reltol=0,force_dtmin=true))
    elapsed[i-offset,3] = msims[i-offset].elapsedTime
    medians[i-offset,3] = msims[i-offset].error_medians[:final]
    means[i-offset,3] = msims[i-offset].error_means[:final]
end

fullMeans[k] = means
fullMedians[k] = medians
fullElapsed[k] = elapsed
fullTols[k] = tols
end

Error: UndefVarError: probs not defined

gr(fmt=:svg)

Error: UndefVarError: gr not defined

lw=3
leg=String["RSwM1","RSwM2","RSwM3"]

```

```

titleFontSize = 16
guideFontSize = 14
legendFontSize = 14
tickFontSize = 12

for k in 1:size(probs,1)
    p1[k] = Plots.plot(fullTols[k],fullMeans[k],xscale=:log10,yscale=:log10,
        xguide="Absolute Tolerance",yguide="Mean Final Error",title="Example
        $k"
        ,linewidth=lw,grid=false,lab=leg,titlefont=font(titleFontSize),legendfont=font(legendFontSize),ti
    p2[k] =
        Plots.plot(fullTols[k],fullMedians[k],xscale=:log10,yscale=:log10,xguide="Absolute
        Tolerance",yguide="Median Final Error",title="Example
        $k",linewidth=lw,grid=false,lab=leg,titlefont=font(titleFontSize),legendfont=font(legendFontSize),
    p3[k] =
        Plots.plot(fullTols[k],fullElapsed[k],xscale=:log10,yscale=:log10,xguide="Absolute
        Tolerance",yguide="Elapsed Time",title="Example $k"
        ,linewidth=lw,grid=false,lab=leg,titlefont=font(titleFontSize),legendfont=font(legendFontSize),ti
end

Error: UndefVarError: probs not defined

Plots.plot!(p1[1])

Error: UndefVarError: Plots not defined

Plots.plot(p1[1],p1[2],p1[3],layout=(3,1),size=(1000,800))

Error: UndefVarError: p1 not defined

#savefig("meanvstol.png")
#savefig("meanvstol.pdf")

plot(p3[1],p3[2],p3[3],layout=(3,1),size=(1000,800))

Error: UndefVarError: p3 not defined

#savefig("timevstol.png")
#savefig("timevstol.pdf")

plot(p1[1],p3[1],p1[2],p3[2],p1[3],p3[3],layout=(3,2),size=(1000,800))

Error: UndefVarError: p1 not defined

using DiffEqBenchmarks
DiffEqBenchmarks.bench_footer(WEAVE_ARGS[:folder],WEAVE_ARGS[:file])

```

0.1 Appendix

These benchmarks are a part of the DiffEqBenchmarks.jl repository, found at: <https://github.com/JuliaDiffeq/DiffEqBenchmarks.jl>

To locally run this tutorial, do the following commands:

```

using DiffEqBenchmarks
DiffEqBenchmarks.weave_file("AdaptiveSDE","AdaptiveEfficiencyTests.jmd")

```

Computer Information:

Julia Version 1.1.0

Commit 80516ca202 (2019-01-21 21:24 UTC)

Platform Info:

OS: Linux (x86_64-pc-linux-gnu)

CPU: Intel(R) Xeon(R) CPU E5-2680 v4 @ 2.40GHz

WORD_SIZE: 64

LIBM: libopenlibm

LLVM: libLLVM-6.0.1 (ORCJIT, haswell)

Package Information:

Status: `~/home/crackauckas/.julia/environments/v1.1/Project.toml`

```
[c52e3926-4ff0-5f6e-af25-54175e0327b1] Atom 0.8.5
[bcd4f6db-9728-5f36-b5f7-82caef46ccdb] DelayDiffEq 5.2.0
[bb2cbb15-79fc-5d1e-9bf1-8ae49c7c1650] DiffEqBenchmarks 0.1.0
[459566f4-90b8-5000-8ac3-15dfb0a30def] DiffEqCallbacks 2.5.2
[f3b72e0c-5b89-59e1-b016-84e28bfd966d] DiffEqDevTools 2.7.2+
[77a26b50-5914-5dd7-bc55-306e6241c503] DiffEqNoiseProcess 3.1.0
[055956cb-9e8b-5191-98cc-73ae4a59e68a] DiffEqPhysics 3.1.0
[a077e3f3-b75c-5d7f-a0c6-6bc4c8ec64a9] DiffEqProblemLibrary 4.1.0
[0c46a032-eb83-5123-abaf-570d42b7fbaa] DifferentialEquations 6.3.0
[b305315f-e792-5b7a-8f41-49f472929428] Elliptic 0.5.0
[e5e0dc1b-0480-54bc-9374-aad01c23163d] Juno 0.7.0
[7f56f5a3-f504-529b-bc02-0b1fe5e64312] LSODA 0.4.0
[c030b06c-0b6d-57c2-b091-7029874bd033] ODE 2.4.0
[54ca160b-1b9f-5127-a996-1867f4bc2a2c] ODEInterface 0.4.5
[09606e27-ecf5-54fc-bb29-004bd9f985bf] ODEInterfaceDiffEq 3.1.0
[1dea7af3-3e70-54e6-95c3-0bf5283fa5ed] OrdinaryDiffEq 5.5.0
[65888b18-ceab-5e60-b2b9-181511a3b968] ParameterizedFunctions 4.1.1
[91a5bcdd-55d7-5caf-9e0b-520d859cae80] Plots 0.24.0
[d330b81b-6aea-500a-939a-2ce795aea3ee] PyPlot 2.8.1
[90137ffa-7385-5640-81b9-e52037218182] StaticArrays 0.10.3
[789caeaf-c7a9-5a7d-9973-96adeb23e2a0] StochasticDiffEq 6.1.1
[c3572dad-4567-51f8-b174-8c6c989267f4] Sundials 3.3.0+
[92b13dbe-c966-51a2-8445-caca9f8a7d42] TaylorIntegration 0.4.1
[44d3d7a6-8a23-5bf8-98c5-b353f8df5ec9] Weave 0.9.0
```