Pleiades Work-Precision Diagrams

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using OrdinaryDiffEq, ODE, ODEInterfaceDiffEq, LSODA, Sundials, DiffEqDevTools

prob =

abstols = 1.0 ./ 10.0 .^ (6:9) reltols = 1.0 ./ 10.0 .^ (3:6);

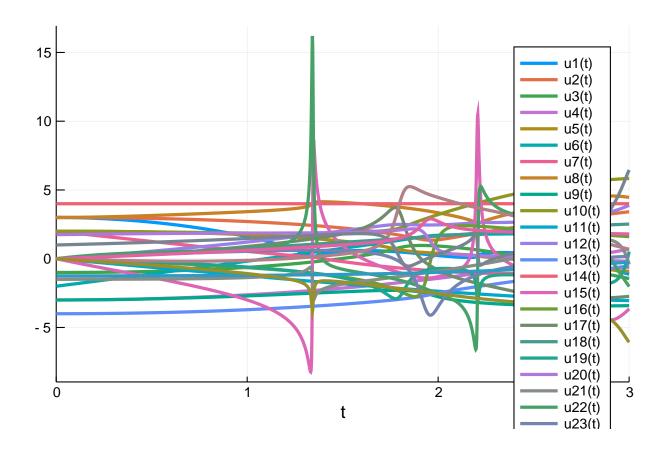
test_sol = TestSolution(sol);

using Plots; gr()

plot(sol)

```
f = (du,u,p,t) \rightarrow begin
 @inbounds begin
 x = view(u, 1:7)
                   # x
  y = view(u, 8:14) # y
 v = view(u, 15:21) # x/
  w = view(u, 22:28) # y'
  du[1:7] = v
  du[8:14].= w
  for i in 14:28
    du[i] = zero(u[1])
  for i=1:7, j=1:7
    if i != j
      r = ((x[i]-x[j])^2 + (y[i] - y[j])^2)^(3/2)
      du[14+i] += j*(x[j] - x[i])/r
      du[21+i] += j*(y[j] - y[i])/r
  end
  end
end
```

sol = solve(prob, Vern8(), abstol=1/10^12, reltol=1/10^10, maxiters=1000000)



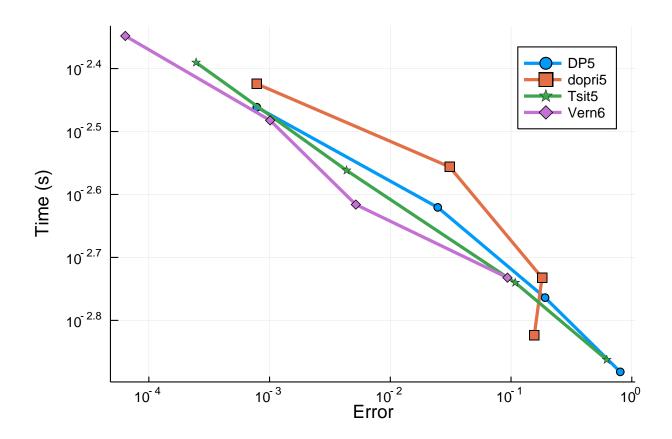
0.1 Low Order

#wp =

#setups = [Dict(:alg=>ode45())]

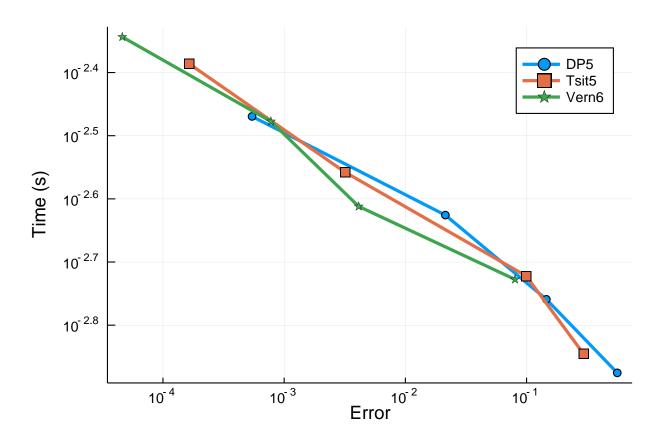
ODE.jl had to be discarded. The error estimate is off since it throws errors and aborts and so that artificially lowers the error the time is serverly diminished.

 $\textit{WorkPrecisionSet} (\textit{prob}, \textit{abstols}, \textit{reltols}, \textit{setups}; \textit{appxsol=test_sol}, \textit{save_everystep=false}, \textit{numruns=100}, \textit{maximum}, \textit{abstols}, \textit{reltols}, \textit{setups}; \textit{appxsol=test_sol}, \textit{save_everystep=false}, \textit{numruns=100}, \textit{maximum}, \textit{abstols}, \textit{abstols}, \textit{abstols}, \textit{abstols}, \textit{abstols}, \textit{appxsol=test_sol}, \textit{save_everystep=false}, \textit{aumruns=100}, \textit{maximum}, \textit{abstols}, \textit{abst$



0.1.1 Interpolation

 $\label{lem:workPrecisionSet} Work Precision Set (prob, abstols, reltols, setups; appxsol=test_sol, numruns=100, maxiters=10000, error_estplot(wp)$



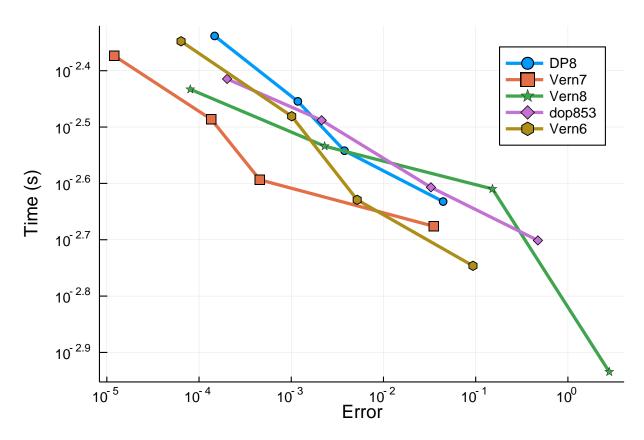
0.2 Higher Order

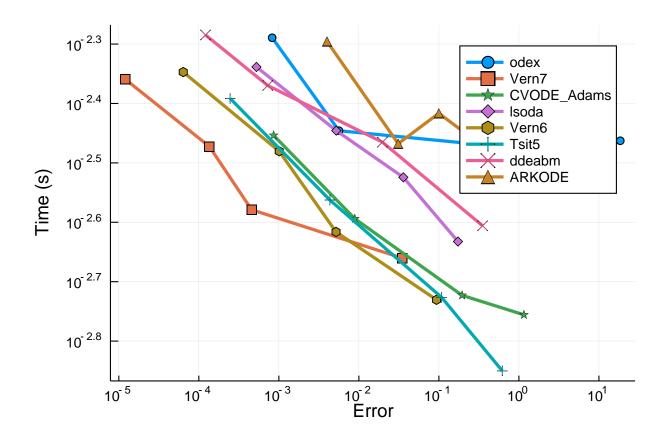
#wp =

#setups = [Dict(:alg=>ode78())]

Once again ODE.jl had to be discarded since it errors.

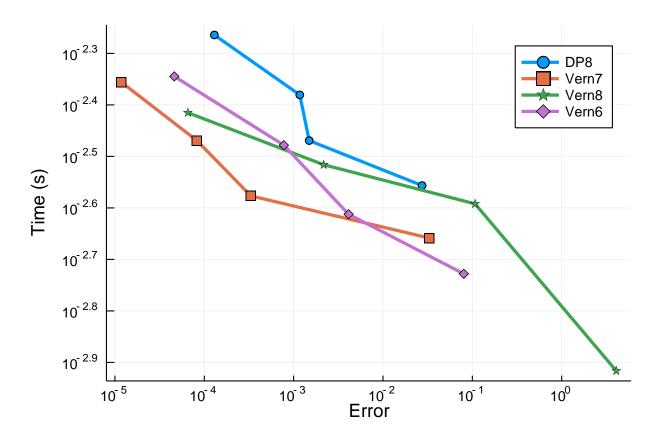
 $\label{lem:workPrecisionSet} Work Precision Set (prob, abstols, reltols, setups; appxsol=test_sol, save_every step= false, numruns=100, maxipul (wp)$





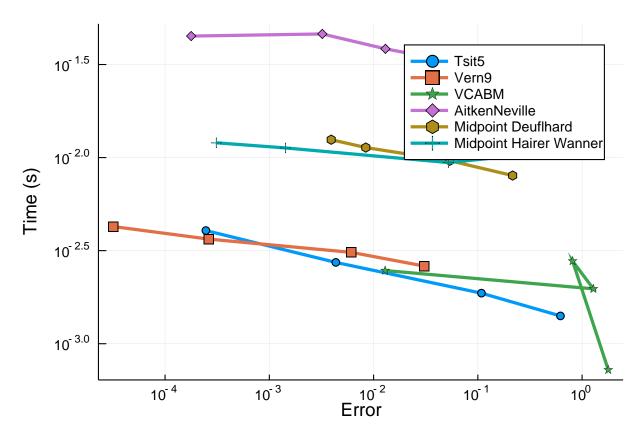
0.2.1 Interpolations

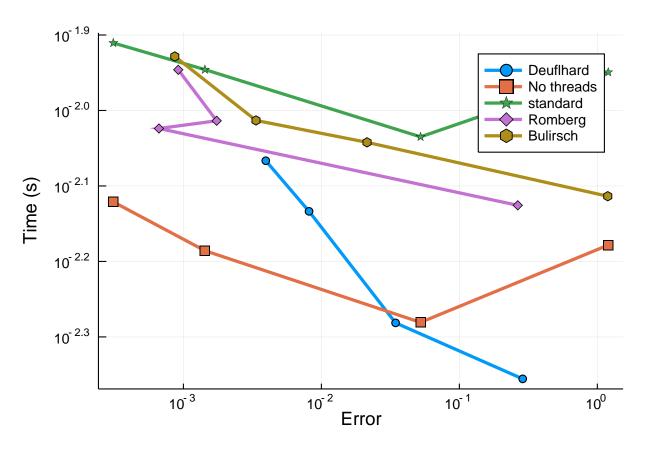
 $\label{lem:workPrecisionSet} Work Precision Set (prob, abstols, reltols, setups; appxsol=test_sol, numruns=100, maxiters=1000, error_estiplot(wp)$

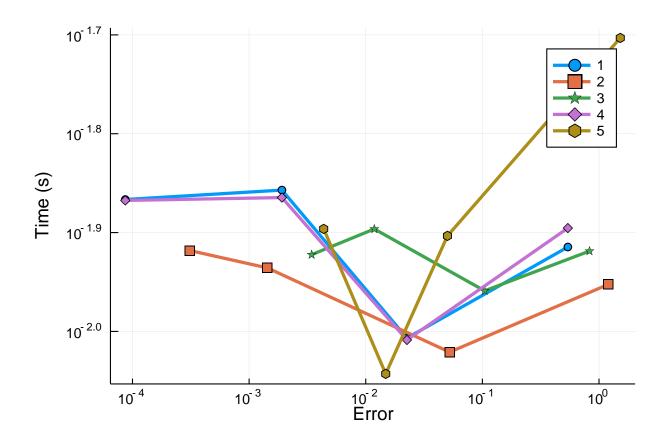


0.3 Comparison with Non-RK methods

Now let's test Tsit5 and Vern9 against parallel extrapolation methods and an Adams-Bashforth-Moulton:







0.4 Conclusion

One big conclusion is that, once again, the ODE.jl algorithms fail to run on difficult problems. Its minimum timestep is essentially machine epsilon, and so this shows some fatal flaws in its timestepping algorithm. The OrdinaryDiffEq.jl algorithms come out as faster in each case than the ODEInterface algorithms. Overall, the Verner methods have a really good showing once again. The CVODE_Adams method does really well here when the tolerances are higher.

```
using DiffEqBenchmarks
DiffEqBenchmarks.bench_footer(WEAVE_ARGS[:folder],WEAVE_ARGS[:file])
```

0.5 Appendix

These benchmarks are a part of the DiffEqBenchmarks.jl repository, found at: https://github.com/JuliaDirous locally run this tutorial, do the following commands:

```
using DiffEqBenchmarks
DiffEqBenchmarks.weave_file("NonStiffODE","Pleiades_wpd.jmd")
```

Computer Information:

```
Julia Version 1.2.0
Commit c6da87ff4b (2019-08-20 00:03 UTC)
Platform Info:
```

OS: Linux (x86_64-pc-linux-gnu)

CPU: Intel(R) Xeon(R) CPU E5-2680 v4 @ 2.40GHz

WORD_SIZE: 64 LIBM: libopenlibm

LLVM: libLLVM-6.0.1 (ORCJIT, haswell)

Environment:

JULIA NUM THREADS = 16

Package Information:

Status: `/home/crackauckas/.julia/dev/DiffEqBenchmarks/Project.toml` [a134a8b2-14d6-55f6-9291-3336d3ab0209] BlackBoxOptim 0.5.0 [f3b72e0c-5b89-59e1-b016-84e28bfd966d] DiffEqDevTools 2.15.0 [1130ab10-4a5a-5621-a13d-e4788d82bd4c] DiffEqParamEstim 1.8.0 [a077e3f3-b75c-5d7f-a0c6-6bc4c8ec64a9] DiffEqProblemLibrary 4.5.1 [ef61062a-5684-51dc-bb67-a0fcdec5c97d] DiffEqUncertainty 1.2.0 [7073ff75-c697-5162-941a-fcdaad2a7d2a] IJulia 1.20.0 [7f56f5a3-f504-529b-bc02-0b1fe5e64312] LSODA 0.6.1 [76087f3c-5699-56af-9a33-bf431cd00edd] NLopt 0.5.1 [c030b06c-0b6d-57c2-b091-7029874bd033] ODE 2.5.0 [54ca160b-1b9f-5127-a996-1867f4bc2a2c] ODEInterface 0.4.6 [1dea7af3-3e70-54e6-95c3-0bf5283fa5ed] OrdinaryDiffEq 5.17.1 [65888b18-ceab-5e60-b2b9-181511a3b968] ParameterizedFunctions 4.2.1 [91a5bcdd-55d7-5caf-9e0b-520d859cae80] Plots 0.26.3 [c3572dad-4567-51f8-b174-8c6c989267f4] Sundials 3.7.0 [44d3d7a6-8a23-5bf8-98c5-b353f8df5ec9] Weave 0.9.1 [b77e0a4c-d291-57a0-90e8-8db25a27a240] InteractiveUtils [d6f4376e-aef5-505a-96c1-9c027394607a] Markdown [44cfe95a-1eb2-52ea-b672-e2afdf69b78f] Pkg [9a3f8284-a2c9-5f02-9a11-845980a1fd5c] Random