OptaDOS: User Guide Version 1.0

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Further information about OPTADOS may be obtained from: www.optados.org

Nota bene: OPTADOS, optados or OptaDOS, but never OPTADOS.

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Chapter 1

Introduction

1.1 Background

OPTADOS is a code for calculating optical, core-level excitation spectra along with full, partial and joint electronic density of states (DOS). The code was developed by merging the Lindos code of Andrew Morris and Chris Pickard at University College London with the optical properties code of Rebecca Nicholls and Jonathan Yates at Oxford University. OPTADOS is written in Fortran 95 and may be run in parallel using MPI. At present OPTADOS interfaces with CASTEP output files, although it is extendable to perform calculations on any set of band eigenvalues and their derivatives generated by any electronic structure code.

The code is freely available through the GPL licence with the request that the following citation (quoted in full) is required in any publication resulting from the use of OPTADOS.

Andrew J. Morris, R. J. Nicholls, C. J. Pickard and Jonathan R. Yates, OptaDOS: A Tool for Obtaining Density of States, Core-level and Optical Spectra from Electronic Structure Codes, Insert Journal Here (201X).

Further information and examples can be found at

www.optados.org

1.2 Features

OPTADOS generates optical, core-level excitation spectra along with full, partial and joint electronic DOS. The DOS, PDOS and JDOS take advantage of the linear and adaptive broadening schemes which are more accurate than standard Gaussian broadening since they exploit knowledge of the gradients of the bands at each k-point in the Brillouin zone. These DOS are the basis of the more advanced functionality of OPTADOS, the core and optical spectra.

Along with data text files OPTADOS also generates .agr files of results to be read by grace.

Chapter 2

Theoretical Background

2.1 Integrals over the Brillouin Zone

Many energy-resolved spectral properties of a material take the form of an integration of some function, $F_{nm}(\mathbf{k})$ in reciprocal space over the BZ; where $F_{nm}(\mathbf{k})$ are the elements of a periodic operator which commutes with the crystal translational symmetry. Perhaps the two simplest examples of integrals, hereinafter referred to as type (a) and type (b), take the form at T=0 K of,

$$I^{(a)}(E) = \sum_{n} \int_{BZ} \frac{d\mathbf{k}}{(2\pi)^3} F_{nn}(\mathbf{k}) \delta(E_{n\mathbf{k}} - E), \qquad (2.1)$$

and,

$$I^{(b)}(E) = \sum_{n}^{\text{occ}} \sum_{m}^{\text{unocc}} \int_{BZ} \frac{d\mathbf{k}}{(2\pi)^3} F_{nm}(\mathbf{k}) \delta(E - (E_{m\mathbf{k}} - E_{n\mathbf{k}})), \tag{2.2}$$

where $E_{n\mathbf{k}}$ are the energy eigenvalues of the system. They are also extendable to integration over spin-polarised channels in a straightforward way.

2.2 Brillouin Zone Sampling Schemes

Since the crystal momentum, \mathbf{k} , is a continuous quantum number the band structure in an ab initio calculation is approximated using specific k-points within the first Brillouin zone. These k-points may be chosen through symmetry perhaps using a Monkhorst-Pack grid [?] or the multi-k-point generalisation to the Baldereschi scheme[?, ?].

Obtaining the energy bands from a set of eigenenergies at discrete k-points is non-trivial. This simplest way of assigning bands, by counting eigenvalues at k-points, implicitly assumes that there are no band crossings in the BZ. This is further complicated by "band kissing" where bands approach, but due to small interactions between the bands breaking the degeneracy they remain continuous[?, ?]. Considering band coefficients and the overlap matrix it has been shown how to assign bands to individual eigenenergies[?, ?], however these still require a broadening scheme to obtain a DOS. Below we detail some approaches to obtaining a DOS from a set of eigenenergies.

2.2.1 Gaussian broadening

The reciprocal space is discretised into sub-cells each containing a k-point which contributes to the integral corresponding to the energy of the k-point at their centre. Band dispersion may be crudely approximated by smearing each sub-cell's contribution by a fixed-width Gaussian function, of some width, ω ,

$$\delta(E_{n\mathbf{k}} - E) \to \frac{1}{\omega\sqrt{2\pi}} \exp\left(-\frac{1}{2}((E_{n\mathbf{k}} - E)/\omega)^2\right).$$
 (2.3)

This approach requires a large number of k-points to converge the DOS since when choosing ω there is a trade-off between representing the sharp features, such as van Hove singularities[?] and not introducing spurious oscillations due to the limited k-point sampling. The band crossing problem is not present since the bands are modelled as dispersionless.

Fixed-width Gaussian broadening may be chosen for OptaDOS calculations with, broadening : fixed.

2.2.2 Interpolative schemes

In the linear tetrahedron interpolative scheme the BZ is divided into roughly equal size tetrahedra with the band energy calculated at each vertex [?]. The DOS contribution of each tetrahedron is then calculated analytically by linear interpolation.

Linear interpolation suffers from the band crossing problem, since the interpolation always joins the lowest energy bands together, which has the effect of avoiding all band crossing and kissing. The method also does not describe van Hove singularities well since the interpolation is linear.

Higher-order interpolation schemes, such as the quadratic tetrahedron scheme, have been proposed which converge the singularities more rapidly than the linear scheme [?, ?, ?], but these still require a high-density k-point grid to mitigate the band-crossing problem.

2.2.3 Extrapolative schemes

Extrapolating from each k-point rather than interpolating between adjacent points eliminates the band-crossing problem. Müller and Wilkins show that for free electron bands the DOS is a smooth parabola when using the extrapolative method and a rough unconverged spectrum with the interpolative approach when using the same k-point mesh [?].

The linear extrapolative scheme still does not represent van Hove singularities as well as a second-order approach. Band curvatures may be combined with Löwdin perturbation theory to extrapolate to higher order [?, ?].

Linear extrapolative broadening may be chosen for OPTADOS calculations with, broadening : linear.

2.2.4 Adaptive broadening schemes

An approximation to linear extrapolation method was proposed by Yates *et al.* [?]. Each sub-cell's contribution to the DOS is broadened by a Gaussian function whose width, ω , is proportional to the energy band gradient as its k-point. This simple approach removes the spurious oscillations of the fixed broadening whilst maintaining the sharper features.

Adaptive broadening may be chosen for OPTADOS calculations with, broadening : adaptive.

2.3 Density of Electronic States

When $F_{nm}(\mathbf{k}) = 1$ the type (a) integral represents the electronic density of states (DOS) at E and the total ground-state energy, E_{gs} is obtained by integrating over the occupied energies,

$$E_{gs} = \int_0^{E_F} I^{(a)}(E; F_{nm}(\mathbf{k}) = 1) dE, \qquad (2.4)$$

where E_F is the Fermi energy.

The DOS is plotted with OPTADOS using the task: dos command.

The partial, or projected DOS (PDOS), I_{μ} is obtained by projecting the DOS onto local orbitals, μ , at each atomic site[?]. In this case,

$$F_{\mu n}(\mathbf{k}) = \Re \left\{ T_{\mu n}^{\dagger}(\mathbf{k}) T_{\nu n}(\mathbf{k}) S_{\nu \mu}(\mathbf{k})^{-1} \right\}, \tag{2.5}$$

where $T_{\mu n}(\mathbf{k}) = \langle \Psi_n(\mathbf{k}) | \phi_{\mu}(\mathbf{k}) \rangle$ are the overlap matrices between LCAO (linear combination of atomic orbitals) basis, ϕ_{μ} and planewave states, Ψ_n , and $S_{\mu n}(\mathbf{k}) = \langle \phi_n(\mathbf{k}) | \phi_{\mu}(\mathbf{k}) \rangle$, the overlap matrices of the LCAO basis.

The PDOS is plotted with OPTADOS using the task: pdos command. The projection is defined using the pdos keyword as described in the user manual.

In the case of the type (b) integral when $F_{nm}(\mathbf{k}) = 1$, we obtain the joint-DOS, (JDOS), for frequency, ω . The JDOS is plotted with OPTADOS using the task: jdos command.

2.4 Dielectric response

Core-level spectra and optical properties are related to the complex dielectric function $\varepsilon_1 + i\varepsilon_2$. Within the random phase approximation, the imaginary part of the dielectric function is

$$\varepsilon_2(\omega) = \frac{\pi e^2}{\varepsilon_0 \Omega} \frac{1}{q^2} \left| \langle \psi_{\mathbf{k}}^c | e^{-i\mathbf{q} \cdot \mathbf{r}} | \psi_{\mathbf{k}+\mathbf{q}}^v \rangle \right|^2, \tag{2.6}$$

where e is the charge on an electron, ε_0 is the permittivity of free space, Ω is the volume of the unit cell and \mathbf{q} is the momentum transfer [?]. Using the dipole approximation, expressing \mathbf{q} as $q \hat{\mathbf{u}}$ and taking the limit that $q \to 0$, ε_2 can be written as an integral of type (b),

$$\varepsilon_{2}(\omega) = \frac{\pi e^{2}}{\varepsilon_{0}\Omega} I^{(b)}(\hbar\omega), \qquad (2.7)$$

where,

$$F_{nm}(\mathbf{k}) = |\langle \psi_{\mathbf{k}}^c | \hat{\mathbf{u}} \cdot \mathbf{r} | \psi_{\mathbf{k}}^v \rangle|^2.$$
 (2.8)

Once ε_2 is known, it is possible to use the Kramers-Kronig relations to obtain ε_1 and hence obtain an expression for the full dielectric function. The dielectric function is a tensor and in OPTADOS it is either possible to output the full dielectric tensor or calculate dielectric function for the isotropic average of \mathbf{q} , a particular direction of \mathbf{q} or the average of \mathbf{q} over a plane perpendicular to a given direction. Once the dielectric function has been calculated, core-level spectra and optical properties can be calculated.

Core-level and low-loss EELS spectra are all related to the loss function, which is defined as [?]:

$$\Lambda = \Im\left(\frac{-1}{\varepsilon_1 + i\varepsilon_2}\right). \tag{2.9}$$

2.4.1 Core-level spectra

For core-level spectroscopy (core-loss EELS and x-ray absorption near edge spectroscopy (XANES)) the incident perturbation is far from resonance and since $\varepsilon_1 \approx 1$ and $\varepsilon_2 \gg 1$ equation 2.9 reduces to $\Lambda = \varepsilon_2$ [?]. The type (b) integral in equation 2.7 becomes a type (a) integral as the energy of the core state is fixed. Emission spectra (transitions from valence to core XAS) can also be calculated by considering a sum over the occupied rather than unoccupied states. Core-level spectra are calculated in OPTADOS using the task: core command.

Several different experimental geometries are possible for core-level experiments and OPTA-DOS allows the calculation of spectra with **q** in a particular direction or an isotropic average. In core-level absorption spectra there are several sources of broadening coming from the experimental set up and lifetime effects. These can be included in OPTADOS by broadening the theoretical spectrum using a combination of Gaussian and Lorentzian functions. To include instrumentation and lifetime effects, core_LAI_broadening should be set to true.

2.4.2 Optical properties

In the low-loss EELS regime, the approximations used for core-level spectroscopy do not hold and the full form of the loss function needs to be calculated. This is done by calculating ε_2 using equations 2.7 and 2.8 and then using the Kramers-Kronig relations to find ε_1 . Once the dielectric function has been calculated, the loss-function is simulated (without local field effects) using equation 2.9. As the dielectric function has been calculated, several other optical properties (which are listed below) can also be computed [?].

Conductivity, in units of Sm^{-1} , is computed using:

$$\sigma_1 = \varepsilon_0 \varepsilon_2 \omega, \tag{2.10}$$

$$\sigma_2 = \varepsilon_0 \left(1 - \varepsilon_1 \right) \omega. \tag{2.11}$$

The refractive index is calculated using:

$$N = n + ik (2.12)$$

where n and k are obtained from,

$$n^{2} = \frac{1}{2}([\varepsilon_{1}^{2} + \varepsilon_{2}^{2}]^{\frac{1}{2}} + \varepsilon_{1}) \quad \text{and} \quad k^{2} = \frac{1}{2}([\varepsilon_{1}^{2} + \varepsilon_{2}^{2}]^{\frac{1}{2}} - \varepsilon_{1}). \tag{2.13}$$

The absorption coefficient, (in units of m⁻¹), is computed using

$$\eta = \frac{2k\omega}{c},\tag{2.14}$$

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and reflection coefficient, R, from,

$$R = \frac{(n-1)^2 + k^2}{(n+1)^2 + k^2}. (2.15)$$

All optical properties are calculated in OptaDOS using the task: optics command.

2.4.3 Intraband term

For metals it is necessary to consider an intraband contribution to the optical response, i.e. a term when n=m in equation 2.2 [?, ?]. The contribution to ε can be written as a type (a) integral with $\hbar\omega$ set to E_F ,

$$\varepsilon_1^{\text{intra}}(\omega) = 1 - \frac{e^2}{\varepsilon_0 \Omega} \frac{1}{(\omega^2 + \Gamma^2)} I^{(a)}(E_F), \qquad (2.16)$$

$$\varepsilon_2^{\text{intra}}(\omega) = \frac{e^2}{\varepsilon_0 \Omega} \frac{\Gamma}{\omega(\omega^2 + \Gamma^2)} I^{(a)}(E_F), \qquad (2.17)$$

where Γ denotes the relaxation rate.

Chapter 3

Getting Started

3.1 Installation

OPTADOS is usually obtained in a gzipped tarball, optados-X.X.tar.gz. Extract this (tar -xzf optados-X.X.tar.gz) in the desired directory. Inside the optados/ directory are a number of sub directories, documents/, examples/. The code may be compiled using the Makefile in the optados/ directory. The SYSTEM, BUILD, COMMS_ARCH and PREFIX flags must be set, either in the makefile.system, or from the command line (for example make BUILD=fast).

3.1.1 SYSTEM

Choose which compiler to use to make OPTADOS. The valid values are:

- g95 (default)
- gfortran
- ifort
- nag
- pathscale
- pgf90
- sun

3.1.2 BUILD

Choose the level of optimisations required when making OptaDOS. The valid values are:

- fast (default) All optimisations

- debug No optimisations, full debug information

3.1.3 COMMS_ARCH

Whether to compile for serial or parallel execution. The valid values are:

```
- serial (default)
```

 $-\ \mathtt{mpi}$

3.1.4 PREFIX

Choose where to place the OPTADOS binary. The default is the OPTADOS directory.

3.2 Usage

```
optados.x86_64 [seedname]
```

• seedname: If a seedname string is given the code will read its input from a file seedname.odi. The default value is CASTEP.

Chapter 4

Structure of the Program

The schematic structure of the program is outlined in Fig. 4.1. Each rounded-cornered box represents a Fortran95 module and the lines represent module dependencies. Modules only use data and subroutines from lower modules in the diagram. The modules are grouped into functional, structural, utility and low level. Low level modules set up the environment for communication in serial or parallel between nodes and to disk. The utility modules are not context dependent on the problem, and contain general algorithms and an interface to write xmgrace input files. Structural modules define data structures, hold data and perform low-level operations on them. The functional modules perform the higher-level data operations and generate output.

A description of the purpose of each module is given below.

- algorithms: subroutines not specific to electronic structure
- cell: real and reciprocal space data manipulation and storage, (e.g. cell vectors and k-points)
- comms: interfaces to parallel libraries
- constants: definition of constants and conversion factors
- core: perform core-level calculation
- dos: perform DOS calculation
- dos_utils: perform type (a) integral evaluation
- electronic: read electronic eigenvalue data. Store electronic data variables
- io: error handling, timing, and input and output units
- jdos: perform JDOS calculation
- jdos_utils: perform type (b) integral evaluation
- optados: main program

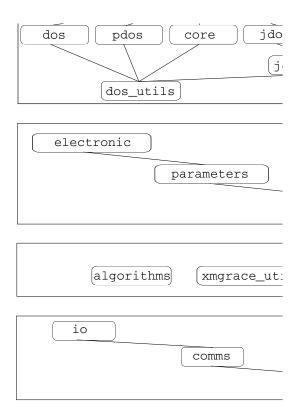


Figure 4.1: Schematic structure of the program

- optics: calculate dielectric function then generate optical properties
- parameters: read, store and check input file parameters
- pdos: perform PDOS calculation
- xmgrace_utils: routines to write out data in xmgr format

Chapter 5

Parameters

5.1 seedname.odi File

The OptaDOS input file seedname.odi has a flexible free-form structure.

The ordering of the keywords is not significant. Case is ignored (so smearing_width is the same as Smearing_Width). Characters after !, or # are treated as comments. Most keywords have a default value that is used unless the keyword is given in seedname.odi. Keywords may be set in any of the following ways

```
smearing_width = 0.4
smearing_width : 0.4
smearing_width 0.4
```

A logical keyword can be set to .true. using any of the following strings: T, true, .true..

5.2 General Parameters

5.2.1 character(len=20) :: task

Tells the code what to compute.

The valid options for this parameter are:

- dos (default)
- compare_dos
- compare_jdos
- jdos
- pdos
- optics
- core
- all

Several tasks can be specified *e.g.* to compute dos and jdos use task: dos jdos. However, the compare_dos and compare_jdos tasks can only be combined with each other, and no additional tasks. compare_dos and compare_jdos calculate the DOS and JDOS respectively using all broadening schemes. It is good practice to check the quality of the underlying DOS before other tasks are requested.

5.2.2 character(len=50) :: broadening

Specified the scheme used to broaden a discrete sampling of the Brillouin Zone to a continuous spectral function.

The valid options for this parameter are:

- adaptive (default)
- fixed
- linear
- quad (not currently implemented)

5.2.3 integer :: iprint

This indicates the level of verbosity of the output from 1, the bare minimum: 2, with progress reports: to 3, which corresponds to full debugging output.

The default value is 1.

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5.2.4 character(len=20) :: energy_unit

The energy unit to be used for writing quantities in the output files.

The valid options for this parameter are:

- eV (default)
- Ry
- Ha

5.2.5 logical :: legacy_file_format

- TRUE Read CASTEP input compatible with versions < 6.0.
- FALSE (Default) Read CASTEP input compatible for use with CASTEP versions 6.0+ and generated with the castep spectral task.

5.2.6 real(kind=dp) :: adaptive_smearing

Set the relative smearing in the adaptive scheme.

Default value is 0.4

5.2.7 real(kind=dp) :: fixed_smearing

Smearing width for fixed broadening.

If spectral_scheme = fixed default value is 0.3eV.

5.2.8 real(kind=dp) :: linear_smearing

Smear the linear broadening with a Gaussian of this width.

Default value is 0.0.

5.2.9 character(len=20) :: efermi

Choose which Fermi energy to use.

The valid options for this parameter are:

- optados (default) Optados recalculates the Fermi energy by performing a DOS calculation.
- file Take the value from the output of the ab-initio calculation.

- insulator Assume that the material is an insulator and counts filled bands to find the Fermi energy.
- <real number> User supplied value.

The default value is optados.

5.2.10 character(len=20) :: output_format

Format in which to output data.

The valid options for this parameter are:

- gnuplot
- grace (default)

5.2.11 logical :: finite_bin_correction

Force each Gaussian to be larger than a single energy bin. (Useful for adaptive smearing and semi-core states when numerical_intdos=TRUE).

Default value TRUE.

5.2.12 logical :: numerical_intdos

Calculate the integrated dos by numerical integration instead of semi-analytically. (Useful for comparison with Lindos.)

Default value FALSE.

5.2.13 logical :: hybrid_linear

Switch from linear broadening scheme to adaptive broadening when band gradient less than hybrid_linear_grad_tol. This allows for a good description of very flat bands such as defect and semi-core states. May also be used in conjunction with finite_bin_correction further improving the DOS and band energy

Default value FALSE.

5.2.14 real(kind=dp) :: hybrid_linear_grad_tol

Tolerance for switching from linear to adaptive broadening when using hybrid_linear option. The default value is $0.01 \mathrm{eV/\mathring{A}}$.

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5.2.15 character(len=50) :: devel_flag

Not a regular keyword. Its purpose is to allow a developer to pass a string into the code to be used inside a new routine as it is developed.

No default.

5.3 DOS Parameters

5.3.1 logical :: compute_band_energy

Compute the band energy by summing bands both using CASTEP's eigenvalue and OPTA-DOS's density of states.

Default value TRUE.

5.3.2 logical :: compute_band_gap

Compute the optical, thermal and average band gap.

Default value FALSE.

5.3.3 logical :: dos_per_volume

Present DOS per simulation cell volume.

Default value FALSE.

5.3.4 real(kind=dp) :: dos_min_energy

Lower energy range for DOS and related properties.

Default value is 5eV below the lowest eigenvalue in the bands file.

5.3.5 real(kind=dp) :: dos_max_energy

Upper energy range for DOS and related properties.

Default value is 5eV above the highest eigenvalue in the bands file.

5.3.6 real(kind=dp) :: dos_nbins

Instead of setting a Default value dos_spacing the total number of DOS bins may be given. (Useful for comparison with LinDOS.)

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5.3.7 real(kind=dp) :: dos_spacing

Resolution at which to compute the DOS and related properties.

Default value is 0.1eV

5.3.8 logical :: set_efermi_zero

Shift energy scales so that the Fermi energy is at 0.

Default value FALSE.

5.4 JDOS Parameters

5.4.1 real(kind=dp) :: jdos_max_energy

Upper energy range for JDOS and related properties.

Default value is the difference between the valence band maximum (or Fermi level) and the highest eigenvalue in the bands file.

5.4.2 real(kind=dp) :: jdos_spacing

Resolution at which to compute the DOS and related properties.

Default value is 0.01eV.

5.4.3 real(kind=dp) :: scissor_op

Value of the scissor operator.

Default value is 0 eV (i.e. not used)

5.4.4 real(kind=dp) :: exclude_bands

This allows a list of bands which are NOT to be included in the JDOS or OPTICS calculation to be specified. The bands 1, 2, 4, 5, 6, for example, can be specified using exclude_bands = 1,2,4-6.

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5.5 PDOS Parameters

5.5.1 character :: pdos

Defines which components to include in the pdos analysis:

```
- angular (decompose as s,p,d etc.)
```

- species (decompose onto atomic species C, H etc.)
- sites (decompose onto atomic sites C1, H1, H2 etc.)
- species_ang (decompose onto angular momentum channels and species Cs, Cp etc.)
- C:H (decompose onto Carbon and Hydrogen sites)
- C1:C3:C4-C8 (decompose onto atoms C1, C2 and C4,C5,C6,C7,C8)
- Si1(s;d) (decompose onto 's' and 'd' channels for atom Si1)
- sum:C1:C3:C4-C8 (decompose onto atoms C1, C2 and C4,C5,C6,C7,C8 and combine into the single projection)

5.6 Optics Parameters

5.6.1 character(len=20) :: optics_geom

Specifies the geometry for the optics calculation. Possible options:

- polycrystalline (Isotropic average)
- polarized
- unpolarized
- tensor (Full dielectric tensor)

The default is polycrystalline.

5.6.2 real(kind=dp) :: optics_qdir(3)

Direction of polarisation. Must be specified if optics_geom = polarized or optics_geom = unpolarized.

There is no default value

5.6.3 logical :: optics_intraband

If true, the intraband contribution to the dielectric function will be calculated. (Important for metals.)

The default is FALSE.

5.6.4 real(kind=dp) :: optics_drude_broadening

Value of broadening included in the Drude term expressed in s^{-1} .

The default value is 1E-14.

5.6.5 real(kind=dp) :: optics_lossfn_broadening

FWHM of Gaussian used to broaden the loss function.

The default value is 0 (*i.e.* no broadening is used).

5.7 Core-level Parameters

5.7.1 character(len=20) :: core_type

Determines if we want absorption (transition from core to conduction ELNES / XANES) or emission (transition from valence to core XAS). It is also possible to plot both.

- absorption (default)
- emission
- all

5.7.2 character(len=20) :: core_geom

Specifies the geometry for the core-spectra calculation. Possible options:

- polycrystalline (Isotropic average)
- polarized

The default is polycrystalline.

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5.7.3 real(kind=dp) :: core_qdir(3)

Direction of polarisation. Must be specified if core_geom = polarized.

There is no default value.

5.7.4 logical :: core_LAI_broadening

Include life-time and instrumentation broadening.

The default is FALSE.

5.7.5 real(kind=dp) :: LAI_gaussian_width

FWHM of Gaussian function used to broaden spectrum.

The default value, if core_LAI_broadening = true, is 0 (i.e. no Gaussian used).

5.7.6 real(kind=dp) :: LAI_lorentzian_width

FWHM of fixed Lorentzian function used to broaden spectrum.

The default value, if core_LAI_broadening = true, is 0 (i.e. no fixed Lorentzian used).

5.7.7 real(kind=dp) :: LAI_lorentzian_scale

Variation of Lorentzian function with energy i.e. the width of the Lorentzian is (energy above the Fermi level x core_lorentzian_scale). If set to zero, no energy dependent broadening is included. If core_lorentzian_scale and core_lorentzian_width are both specified, the total width of the Lorentzian used will be core_lorentzian_width + (energy above the Fermi level x core_lorentzian_scale).

The default value, if core_LAI_broadening = true, is 0.1.

5.7.8 real(kind=dp) :: LAI_lorentzian_offset

Energy (in eV) above the Fermi level that the energy dependent broadening starts.

The default value, if core_LAI_broadening = true, is 0.

Chapter 6

Examples

Each example in the examples/ directory contains example CASTEP input files and a sample OPTADOS input file. To keep the OPTADOS distribution light CASTEP output files for the examples have not been provided. You need to run CASTEP on the CASTEP input files before running OPTADOS on the examples.

6.1 Density of States

- Outline: This is a simple example of using OptaDOS for calculating electronic density of states of crystalline silicon in a 2 atom cell.
- Input Files:
 - examples/Si2_DOS/Si2_dos.cell The CASTEP cell file containing information about the simulation cell.
 - examples/Si2_DOS/Si2_dos.param The CASTEP param file containing information about the parameters for the SCF and spectral calculations.
 - examples/Si2_DOS/Si2_dos.odi The OPTADOS input file, containing the parameters necessary to run OPTADOS.
- Perform a CASTEP calculation on the bulk silicon using the Si2_dos.cell and Si2_dos.param input files.

\$ castep Si2

This should take a couple of seconds to run. More help can be found in the tutorials on the CASTEP website www.castep.org.

- 2. Perform an OptaDOS calculation. Add LEGACY_FILE_FORMAT: true in the Si2_DOS.odi input file, if the CASTEP version you are using is before 6.0. Then execute:
 - \$ optados.<SYSTEM>.<BUILD>.<COMMS_ARCH>.x86_64 Si2

This generates 3 files:

- Si2.odo OptaDOS general output file.
- Si2.adaptive.dat The adaptive broadened DOS raw output data.
- Si2.adaptive.agr The adaptive broadened DOS in a file suitable to be plotted by xmgrace.
- 3. Open the Si2.odo file in a text editor (e.g. vi or emacs). OPTADOS has performed a Density of States calculation.

It has used the integrated DOS to work out the Fermi level, and has suggested the error in the integration by indicating the number of electrons at the Fermi level. Since we had 4 up electrons and 4 down in the input file this analysis seems satisfactory.

Since we had efermi: optados, OPTADOS sets the internal value of the Fermi level to the one it has derived from the DOS. This is important for subsequent calculations. Other valid options are file, where OPTADOS uses the value calculated by the electronic structure code that generated the eigenvalues; insulator, where OPTADOS uses a value calculated from assuming the system is non-metallic; or a value set by the user.

OPTADOS now performs some analysis of the DOS at the Fermi level,

From this we may assume that there is a band gap.

Importantly, then OPTADOS calculates the band energy from the DOS is has calculated.

As the quality of the OptaDOS calculation is increased these two values should converge to the same answer.

Finally OptaDOS shifts the Fermi level to 0 eV, for the output files.

4. The DOS is outputted to Si2.adaptive.dat. This contains 5 columns as described in the header of the file:

```
#
            OptaDOS output file
#
#
   Density of States using adaptive broadening
 Generated on 12 Feb 2012 at 16:50:37
 Column
          Data
#
   1
        Energy (eV)
   2
        Up-spin DOS (electrons per eV)
   3
        Down-spin DOS (electrons per eV)
#
        Up-spin Integrated DOS (electrons)
   4
        Down-spin Integrated DOS (electrons)
```

This file can be plotted by your favourite graph-plotting software. However, OPTADOS has made things easy and generated a Si2.adaptive.agr file which is directly plottable using xmgrace as shown in Fig. 6.1.

- \$ xmgrace Si2.adaptive.agr.
- 5. We now try again with a better sampling of the DOS, by setting DOS_SPACING: 0.001 and also analyse the band gap, by setting COMPUTE_BAND_GAP: true. You can remove all of the OPTADOS output files by using ./tools/optados_clean in your working directory. If you have a parallel version of OPTADOS compiled, now might be the time to try it out, if not, the serial version will be fine, but just take a bit longer. You can set IPRINT: 2 to see a progress report in Si2.odo. In parallel:
 - \$ mpirun -np <nprocs> optados.SYSTEM.BUILD.COMMS_ARCH.x86_64 Si2 but your MPI implementation may be different.
- 6. In Si2.odo we now have a new section analysing the band gap in various ways.

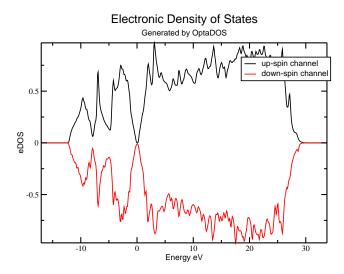


Figure 6.1: Density of States of Silicon generated by adaptive broadening and a very coarse energy sampling of 0.1 eV.

Thermal Bandgap : 0.6676272107 eV Between VBM kpoint : 0.05000 0.05000 0.05000 and CBM kpoint: -0.45000 -0.05000 -0.45000 ==> Indirect Gap	
Optical Bandgap	
Spin : 1 : 2.5542517447 eV	<- OBg
Spin: 2: 2.5542463024 eV	<- OBg
Number of kpoints with this gap	1
Spin : 1 : 1	1
Spin : 2 : 1	1
Average Bandgap	
Spin : 1 : 3.8121372691 eV	<- ABg
Spin : 2 : 3.8121342659 eV	<- ABg
Weighted Average : 3.8121357675 eV	<- wAB

OPTADOS is very careful in its band gap analysis. It uses the bare eigenvalues (unbroadened) and works out the nature and size of the thermal gap, optical gap and the average gap over all of the Brillouin zone. In cases of multi-valleyed semiconductors OPTADOS will report the number of conduction band minima or valence band maxima with identical energies, but will not report the nature of the gap.

Increasing the number of integration points has improved the band energy of the adaptive smearing:

Band energy (Adaptive broadening) : 1.3623 eV <- BEA |

7. Now set TASK: compare_dos and re-run OPTADOS. OPTADOS will calculate DOS using all the broadening methods, this is good practice to see whether the broadening widths are appropriate before more advanced tasks are carried out, such as Joint-DOS, core and optical calculations.

Plotting the linear broadened DOS over the adaptive we see that the default adaptive broadening is appropriate,

```
xmgrace Si2.adaptive.agr -nxy Si2.linear.dat
```

Linear broadening, although a massive improvement over fixed broadening, sometimes appears noisy if used with very low numbers of k-points. Linear and adaptive DOS should be compared and ADAPTIVE_SMEARING may be tuned by eye until the adaptive DOS contains the features of the linear DOS, but with less noise. Adding a random shift to a k-point mesh can greatly increase the quality of the DOS, especially if the k-point set contained the Γ -point. It generally pays off in computational time to have a coarse mesh at low symmetry points, than a fine mesh centred on high symmetry points.

Both fixed and adaptive broadening can fail to plot the sharpest features, such as semi-core states, if the bin widths are too broad. These sharp features may be forced to be present using the narrowest Gaussian still reproducible by the chosen bin widths by setting FINITE_BIN_CORRECTION: true.

Linear broadening may also be improved by using HYBRID_LINEAR: true. Van Hove singularities and other sharp features are now described at the adaptive broadening level if the bands are flatter than HYBRID_LINEAR_GRAD_TOL. Hybrid linear may also take advantage of the finite bin correction if required.

8. Compare the fixed and adaptive DOS and see the advantage of adaptive broadening over standard Gaussian smearing.

6.2 Projected Density of States

We assume the reader is familiar with the previous section on Density of States calculations and is now familiar with choosing broadening widths, and running OPTADOS.

- Outline: This is a simple example of using OptaDOS for calculating electronic density of states of 2 atoms of crystalline silicon projected onto LCAO basis states.
- Input Files:
 - examples/Si2_PDOS/Si2_dos.cell The CASTEP cell file containing information about the simulation cell.
 - examples/Si2_PDOS/Si2_dos.param The CASTEP param file containing information about the parameters for the SCF and spectral calculations.
 - examples/Si2_PDOS/Si2_dos.odi The OPTADOS input file, containing the parameters necessary to run OPTADOS.

- 1. Choose a broadening scheme for the projected-DOS calculation and test using TASK: compare_dos as explained in the previous example. Checking that the DOS_SPACING is sufficiently fine for the band energies to match.
- 2. Once the DOS looks suitable, switch to TASK: pdos. We choose to decompose the DOS into angular momentum channels (PDOS: angular) and as in the previous example we choose to recalculate the Fermi level using the calculated DOS, rather than use the Fermi level suggested by CASTEP.
- 3. Execute Optados.
- 4. The output can be found in Si2.pdos.dat.

```
#
          OptaDOS output
#
# Generated on 13 Feb 2012 at 10:15:10
Partial Density of States -- Projectors
#+-----
#| Projector:
         1 contains:
           AngM Channel
       Atom
#|
      Si 1
                  S
#| Projector:
         2 contains:
           AngM Channel
       Atom
#|
      Si 1
                  р
      Si
#| Projector:
         3 contains:
           AngM Channel
      Atom
#|
      Si
                   d
         1
      Si
                   d
#| Projector:
         4 contains:
      Atom
           AngM Channel
#|
      Si
         1
                   f
#|
      Si
```

The header shows that there are four projectors described below. The first containing the s-channels of both silicon atoms, the second the p-channels etc.

5. The output is easily plotted using xmgrace:

```
xmgrace -nxy Si2.pdos.dat
```

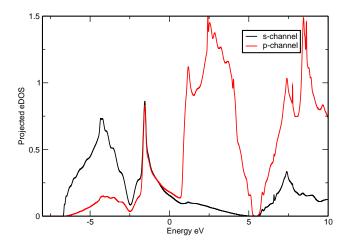


Figure 6.2: Density of States of Silicon generated by adaptive broadening projected onto LCAO momentum states.

- 6. Setting DOS_SPACING: 0.001 gives a high quality plot, as shown in Fig 6.2
- 7. Other things to try are:
 - PDOS: Si1;Si2(s) Output the PDOS on Si atom 1 and the PDOS on the s-channel of Si atom 2. (Resulting in two projectors)
 - PDOS: sum:Si1-2(s) Output the sum of the s-channels on the two Si atoms.
 (Resulting in one projector)
 - PDOS: Si1(p) Output the p-channel on Si atom 1. (Resulting in one projector)

6.3 JDOS

See examples/Si2_JDOS/. This is a simple example of using OPTADOS for calculating joint electronic density of states. We choose to recalculate the Fermi level using the calculated DOS, rather than use the Fermi level suggested by CASTEP and so EFERMI: OPTADOS is included in the Si2.odi file.

- 1. Execute OPTADOS using the example files. The JDOS is outputted to Si2.jadaptive.dat. A file suitable for plotting using xmgrace is written to Si2.jadaptive.agr.
- 2. Check the effect of changing the sampling by increasing and decreasing the value of JDOS_SPACING in the Si2.odi file.
- 3. If TASK: compare_jdos is used instead, OPTADOS will calculate the JDOS using all the broadening methods. This is good practice to see whether the broadening widths are appropriate before more advanced tasks are carried out.

6.4 OPTICS

Two sets of example files are provided for calculations of optical properties. For each example, the CASTEP files containing all the cell and simulation parameters are included, along with an OPTADOS input file. We assume that the reader is familiar with the previous sections on DOS and JDOS.

- examples/Si2_OPTICS/ This is a simple example of using OPTADOS to calculate the optical properties of crystalline silicon, which is an insulator.
- examples/Al_OPTICS/ This is a simple example of using OPTADOS to calculate the optical properties of a metal, aluminium.

6.4.1 Silicon

- 1. Choose a broadening scheme for the JDOS as explained in the JDOS example. Once the JDOS looks suitable, switch the task from JDOS to OPTICS and execute OPTADOS to calculate the optical properties. Several *.dat files are produced:
 - Si2_OPTICS_absorption.dat: This file contains the absorption coefficient (second column) as function of energy (first column).
 - Si2_OPTICS_conductivity.dat: This file contains the conductivity outputted in SI units (Siemens per metre). The columns are the energy, real part and imaginary part of the conductivity respectively.
 - Si2_OPTICS_epsilon.dat: This file contains the dielectric function. The columns are the energy and real and imaginary parts of the dielectric function respectively. The file header also includes the result of the sum rule $\int_{o}^{\omega'} Im\epsilon(\omega)d\omega = N_{eff}(\omega')$. N_{eff} is the effective number of electrons contributing to the absorption process, and is a function of energy.
 - Si2_OPTICS_loss_fn.dat: This file contains the loss function (second column) as a function of energy (first column). The header of the file shows the results of the two sum rules associated with the loss function $\int_o^{\omega'} Im\left(\frac{-1}{\epsilon(\omega)}\right) \omega \, d\omega = N_{eff}(\omega')$ and $\int_o^{\omega'} Im\left(\frac{-1}{\epsilon(\omega)}\right) \frac{1}{\omega} \, d\omega = \frac{\pi}{2}$.
 - Si2_OPTICS_reflection.dat: This file contains the reflection coefficient (second column) as a function of energy (first column).
 - Si2_OPTICS_refractive_index.dat: This file contains the refractive index. The
 columns are the energy and real and imaginary parts of the refractive index respectively.

Corresponding *.agr files are also generated which can be plotted easily using xmgrace.

2. Change parameters JDOS_SPACING and JDOS_MAX and check the effect on the optical properties. Note: all of the other optical properties are derived from the dielectric function.

- 3. The OPTADOS input file has been set up to calculate the optical properties in the polycrystalline geometry (optics_geom = polycrystalline). It is possible to calculate either polarised or unpolarised geometries, or to calculate the full dielectric tensor. To calculate the full dielectric tensor set optics_geom = tensor. This time only the file Si2_OPTICS_epsilon.dat is generated. The format of this file is the same as before (the columns are the energy and the real and imaginary parts of the dielectric function respectively), but this time the six different components of the tensor are listed sequentially in the order ϵ_{xx} , ϵ_{yy} , ϵ_{zz} , ϵ_{xy} , ϵ_{xz} and ϵ_{yz} .
- 4. Additional broadening can be included in the calculation of the loss function. This is done by including the keyword optics_lossfn_broadening in the OPTADOS input file. If you include this keyword and re-run OPTADOS, you will find that the file Si2_OPTICS_loss_fn.dat now has three columns. These are the energy, unbroadened spectrum and broadened spectrum respectively.

6.4.2 Aluminium

- 1. As for the silicon example, a broadening scheme for the JDOS should first be determined.
- 2. Aluminium is a metal so we need to include both the interband and intraband contributions to the dielectric function. To include the intraband contribution optics_intraband = true must be included in the OPTADOS input file. When you run OPTADOS the same files are generated as when only the interband term is included.
 - The Al_OPTICS_epsilon.dat file has the same format as before, but it now contains sequentially the interband contribution, the intraband contribution and the total dielectric function. (The file Al_OPTICS_epsilon.agr only contains the interband term.) In the same way, Al_OPTICS_loss_fn.dat contains the interband contribution, intraband contribution and total loss function. All other optical properties are calculated from the total dielectric function and the format of the output files remains the same.
- 3. In the case where the dielectric tensor is calculated and the intraband term is included, only the Al_OPTICS_epsilon.dat file is generated. As before it contains each component, but this time it lists sequentially the interband contribution, intraband contribution and total dielectric function for each component.
- 4. This time, if additional broadening for the loss function is included by using the key word optics_lossfn_broadening, AL_OPTICS_loss_fn.dat will contains four sequential data sets. These are the interband contribution, the intraband contribution, the total loss function without the additional broadening and the broadened total loss function.

6.5 CORE

See examples/Si2_CORE/. This is a simple example of using OPTADOS for calculating core level absorption spectra for crystalline silicon. We assume that the reader is familiar with the previous section on calculating DOS.

1. We begin by running a CASTEP calculation using the files provided in examples/Si2_CORE. Note that we do not specify pseudopotentials in the Si2_CORE.cell file hence require CASTEP to generate on-the-fly pseudopotentials. This is important as most pseudopotential formats do not contain enough information for the PAW reconstruction needed for a CORE calculation. For any atom a CORE spectra is to be calculated an On-the-fly pseudopotential must be used.

Execute OPTADOS using the OPTADOS input file provided and the file Si2_CORE_core_edge.dat will be created. The file contains two columns, the first is the energy and the second is the spectrum. This file contains the following edges:

```
# Si 1 K1
# Si 1 L1,
# Si 1 L2,3
# Si 2 K1
# Si 2 L1,
```

i.e. all edges from all atoms are produced.

2. To include a core-hole in the calculation, first one atom is chosen to have the excitation. To begin, we will keep two atoms in the unit cell and distinguish one atom by changing the <code>%BLOCK POSITIONS_FRAC</code>

```
%BLOCK POSITIONS_FRAC
Si:exi 0.000000000 0.000000000 0.000000000
Si 0.250000000 0.250000000 0.2500000000
%ENDBLOCK POSITIONS_FRAC
```

in the Si2_CORE.cell file. The atom Si:exi is the one to have a core-hole. To create a core-hole we remove a 1s electrons from the electronic configuration used in the generation of the pseudopotential. We have already generated an on-the-fly pseudopotential without a core-hole in the previous section. Information about the pseudopotentials is included at the top of the Si2_CORE.castep file.

```
| Pseudopotential Report - Date of generation 16-05-2012
| Element: Si Ionic charge: 4.00 Level of theory: LDA
                Reference Electronic Structure
          Orbital
                          Occupation
                                              Energy
             3s
                             2.000
                                              -0.400
             Зр
                              2.000
                                              -0.153
                  Pseudopotential Definition
         Beta
                  1
                         е
                                Rс
                                        scheme
                                                 norm
```

-	1	0	-0.400	1.797	qc	0	1	
	2	0	0.250	1.797	qc	0	- 1	
	3	1	-0.153	1.797	qc	0	- 1	
	4	1	0.250	1.797	qc	0	- 1	
	loc	2	0.000	1.797	pn	0		
							-	
	Augmentation c	harge	e Rinner =	1.298			-	
	Partial core o	orre	ction Rc =	1.298			1	
1	"2 1.8 1.8 1.3 2 3 4 30:31:32LGG(qc=4)"							
I	Author: C	hris	J. Pickar	d, Cambr	idge Uni	versity	1	

The line

```
2|1.8|1.8|1.3|2|3|4|30:31:32LGG(qc=4)
```

specifies the parameters used to create the pseudopotential. We use this as the starting point and then remove one of the core 1s electrons to create a core-hole pseudopotential. This is done by including {1s1.00} in the pseudopotential string as shown:

```
2|1.8|1.8|1.3|2|3|4|30:31:32LGG{1s1.00}(qc=4)
```

If, instead of removing a 1s electron, we wanted to remove a 2s electron from the core, we would have included {2s1.00} instead of {1s1.00} in the pseudopotential string.

We are only interested in the spectra from the atom with the core-hole and so copy the pseudopotential file generated by the previous calculation (Si_OFT.usp) to Si_LDA.usp. Then include

```
%BLOCK SPECIES_POT
Si:exi 2|1.8|1.8|1.3|2|3|4|30:31:32LGG{1s1.00}(qc=4)
Si Si_LDA.usp
%ENDBLOCK SPECIES_POT
```

in the CASTEP Si2_CORE.cell file.

To maintain the neutrality of the cell, we include

```
CHARGE: +1
```

in the Si2_CORE.param file. Run the calculation. This time the Si2_CORE_core_edge.dat file will contain only the edges from the core-hole atom. Compare the K-edge from the core-hole calculation with the previous non-core-hole calculation.

3. The periodic images of the core-hole will interact with one another. As this is unphysical, we need to increase the distance between the core-holes. This is done by creating a supercell. To start with we use a face-centred unit cell rather than the primitive unit cell. This is done by changing the lattice parameters and fractional co-ordinates to:

 $exttt{OptaDOS} : User \ Guide$

```
%BLOCK LATTICE_CART
       5.46 0.00 0.00
       0.00 5.46 0.00
       0.00 0.00 5.46
%ENDBLOCK LATTICE_CART
%BLOCK POSITIONS_FRAC
       Si:exi
                 0.000000000
                                 0.000000000
                                                 0.000000000
       Si
                 0.5000000000
                                 0.5000000000
                                                 0.000000000
                 0.5000000000
                                 0.000000000
       Si
                                                 0.5000000000
                 0.000000000
       Si
                                 0.5000000000
                                                 0.5000000000
       Si
                 0.2500000000
                                 0.2500000000
                                                 0.2500000000
                 0.7500000000
                                 0.2500000000
                                                 0.7500000000
       Si
       Si
                 0.2500000000
                                 0.7500000000
                                                 0.7500000000
       Si
                 0.7500000000
                                 0.7500000000
                                                 0.2500000000
```

Run OPTADOS and compare the spectrum from the face-centred unit cell with that from the primitive unit cell. Continue constructing larger unit cells until the core-hole spectrum stops changing with increasing separation between the periodic images.

4. Other things to try include

40

- Changing the geometry from polycrystalline to polarised
- Including life-time and instrumentation broadening

%ENDBLOCK POSITIONS_FRAC

Chapter 7

Frequently Asked Questions

7.1 OptaDOS crashes complaining that it can't read the seed.bands or seed.cst_ome file.

Which version of CASTEP are you using? See Sect. 5.2.5.

7.2 The examples do not work and I'm using castep version 6.0

CASTEP version 6.0 was released during the transition of the spectral module and features. The easiest way to solve this is to obtain a copy of CASTEP > 6.0, where OPTADOS will work "out of the box". However, to make the examples work with CASTEP 6.0 the OPTADOS examples require a few tweaks outlined below.

- Replace SPECTRAL_KPOINTS_MP_GRID in the cell file with BS_KPOINTS_MP_GRID and OPTICS_KPOINTS_MP_GRID.
- Remove SPECTRAL_TASK : DOS from the param file.
- Add DEVEL_FLAG:old_filename to the odi file.
- Read Section 7.3 if you are planning to do a partial density of states calculation.

7.3 I'm getting odd results for my PDOS calculation when using castep version 6.0

The spectral module in CASTEP 6.0 generates the pdos weights commensurate with the optics grid you have chosen. However this gets overwritten by the main routines. Hence to get the right PDOS weights you must set PDOS_CALCULATE_WEIGHTS: FALSE in the param file.

7.4 I'd like OptaDOS to do X as well

Contact the developers we're always interested in discussing new functionality.

7.5 I'd like to help, what can I do?

Contact the developers, there's always more functionality that we'd like to add to the code.

7.6 I think I've found a bug: what should I do?

- Check and re-check that it is a bug.
- Check the output of the electronic structure code.
- Check that you're using the latest version of OptaDOS.
- Email the developers the input and output files with iprint: 3 and as much information about the problem as possible.

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