

# Game Theory & the Evolution of Cooperation

*Course 5*

Open Collaboration and Peer Production  
( i290m )



*Ceci n'est pas une pipe.*

Magritte

# Prisoner's Dilemma

		Column Player	
		Cooperate	Defect
Row Player	Cooperate	$R = 3, R = 3$	$S = 0, T = 5$
	Defect	$T = 5, S = 0$	$P = 1, P = 1$

R : reward  
 T : temptation  
 P : punishment  
 S : sucker  
 $T > R > P > S$

## Game properties :

Communication is “cheap”

*only commitment count (i.e. played game)*

Nash equilibrium : Defect - Defect

*embodies fundamental selfishness of biological and human entities in nature*

# Computer Tournaments (late 1970s)

## Tournament 1

14 strategy submissions + RANDOM = 15 strategies  
played pairwise : 225 rounds

### Submissions from

*psychology, sociology*

*political science, economics*

*computer science, mathematics*

**Winner :**

**TIT FOR TAT**

# Lessons from Tournament 1

## Rules :

- 1. be nice at first ( unlike DOWNING )*
- 2. retaliate immediately ( TIT FOR TAT )*
- 3. forgive (e.g. TIT FOR TAT, TIT FOR TWO TATS)*

## Observations :

- 1. Strategies were two competitive*
- 2. Some strategies could have outperformed Tit for Tat  
(e.g. Downing, Tit for Two Tat)*

# Computer Tournaments

Tournament 2

*63 strategies*

*3969 pairwise games*

**Results & analysis of Tournament 1 were known !**

**Winner :**

**TIT FOR TAT *again !***



## Lessons from Tournament 2

*1. Be nice and forgiving,*

*2. If others are going to be nice and forgiving,  
it pays to try to take advantage of them*

**⇒ Second lesson was exploitative of the first !**

## TIT FOR TAT

nice, retaliation, forgiveness

(like for Tournament 1)

+ clarity !

# Evolutionary Perspective

## Observation

*Strategies have mutated between Tournaments !*

## Question

*Does this strategy resist any kind of environment ?*

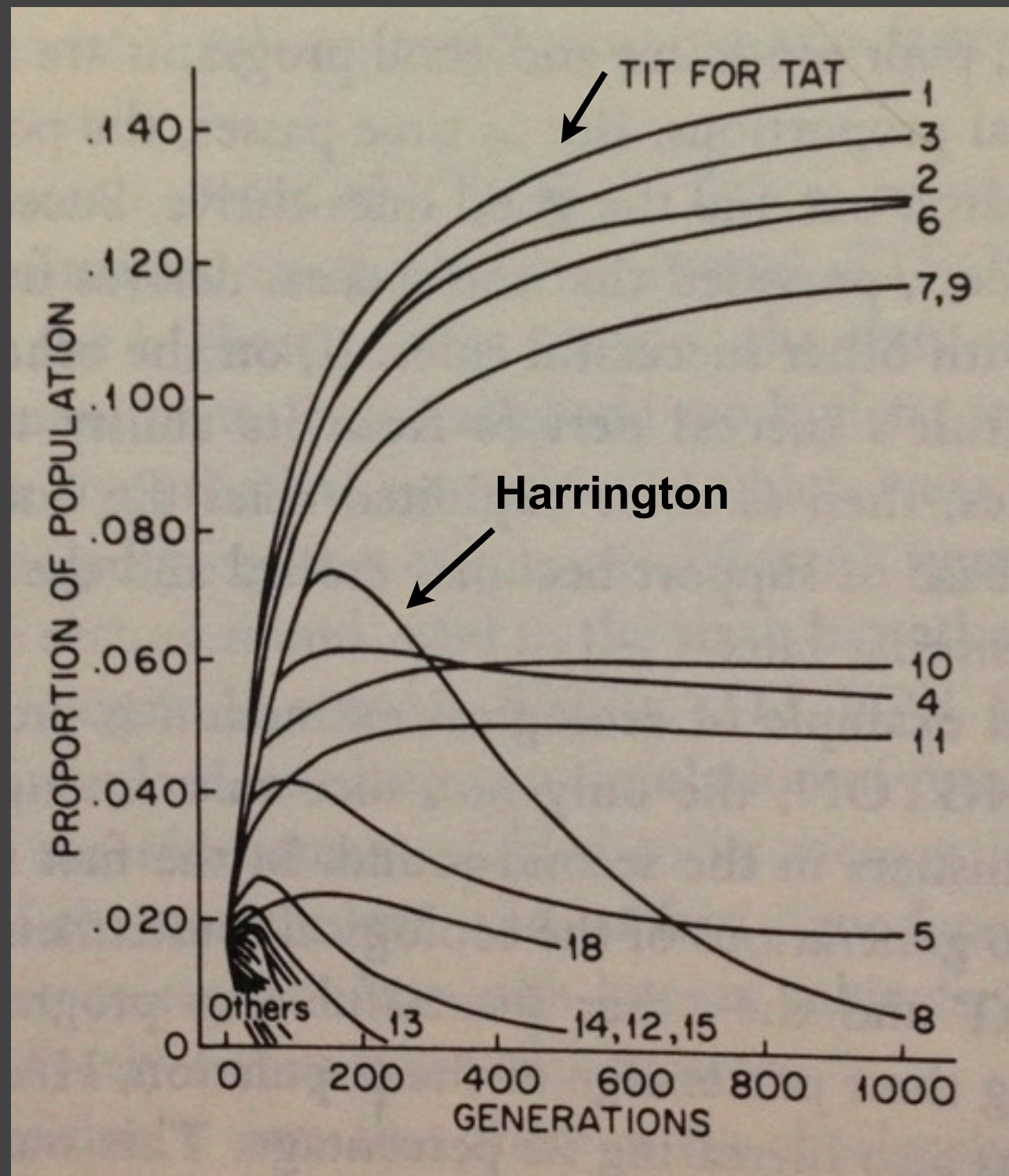
*actually*

**TIT FOR TAT**

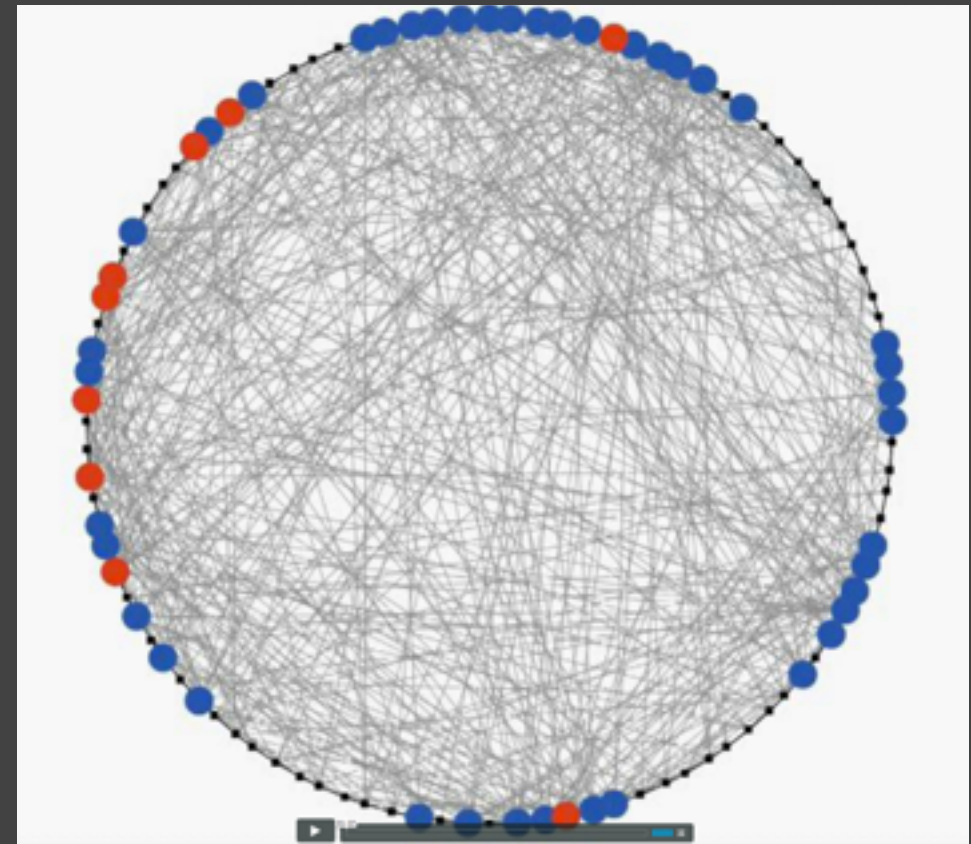
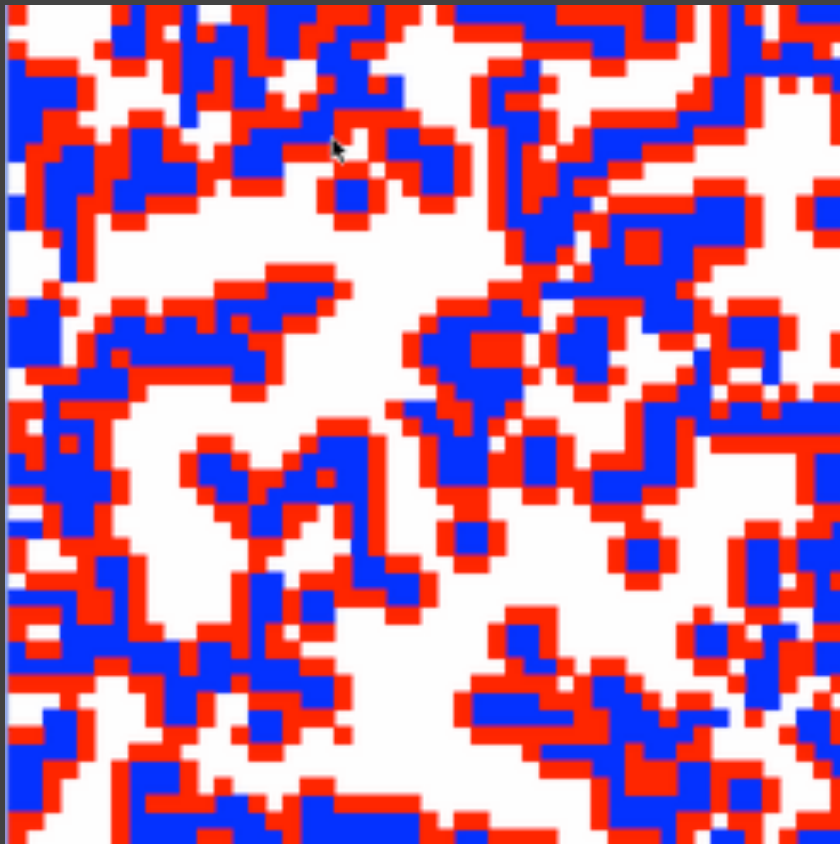
*performs best with low discount rate (i.e.  $w$  close to 1)*



# Evolutionary Perspective



# The Emergence of Cooperation



Dirk Helbing and Wenjian Yu, "The outbreak of cooperation among success-driven individuals under noisy conditions." *Proceedings of the National Academy of Sciences*, Vol. 106, No. 8, Feb. 23, 2009.

# **Application of Game Theory to Open Collaboration**

Article 1 ( today )

**Initiating private-collective innovation:**

**The fragility of knowledge sharing**

( Simon Gächter, Georg von Krogh, Stefan Haefliger )

Article 2 ( 11/15 )

**The architecture of participation: Does code architecture mitigate  
free riding in the open source development model?**

( Baldwin, C. Y. & Clark, K. B. )

# Incentives to Innovate

## **Private investment model**

*innovators privately fund innovation*

## **Collective action model**

*public subsidies + non-rivalry + non-exclusivity*

## **Private-collective model**

*innovators privately fund public good innovations*

# The Fragility of Knowledge Sharing : Initiation

*retain intellectual property rights  
(patent, trade secrets) and keep exclusive rights*

or

share knowledge as a public good

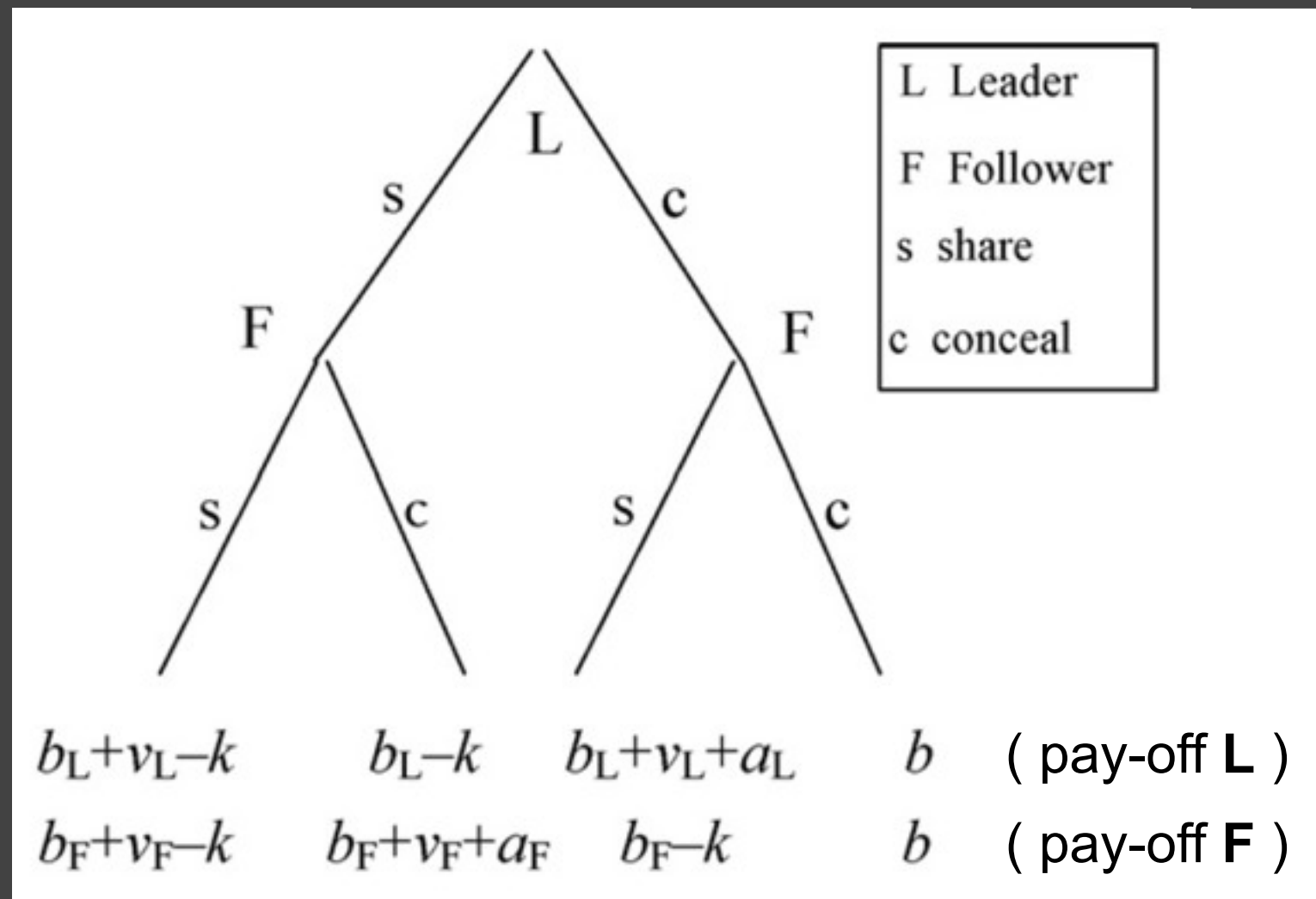
**Under many circumstances, the innovator's incentive to conceal rather than to share knowledge is strong.**

# Assumptions

1. Knowledge sharing enhances value for the party that receives the knowledge.
2. Mutual knowledge sharing makes knowledge public and precludes the exclusivity of received knowledge for one's own private financial benefit. By implication, a necessary (but not sufficient) condition for exclusive appropriation is unilateral knowledge sharing.



# The Knowledge Sharing Game



$b_i$  : base pay-off

$v_i$  : value from sharing

$a_i$  : exclusivity pay-off

$k$  : expense for sharing

## Game with multiple equilibria



# Proposition 1

## Knowledge sharing based on rationality and self-interest

1. *Mutual concealment is always an equilibrium outcome*

2. *A necessary condition for mutual sharing  
as an equilibrium outcome is that  $a_F = 0$*

*A necessary and sufficient condition for sharing  
in all subgames is that exclusivity payoffs  
are zero for both players (  $a_L = a_F = 0$  )*

3. *In all constellations of exclusivity payoffs  
(  $a_L \geq 0$  )  $\times$  (  $a_F \geq 0$  ),*

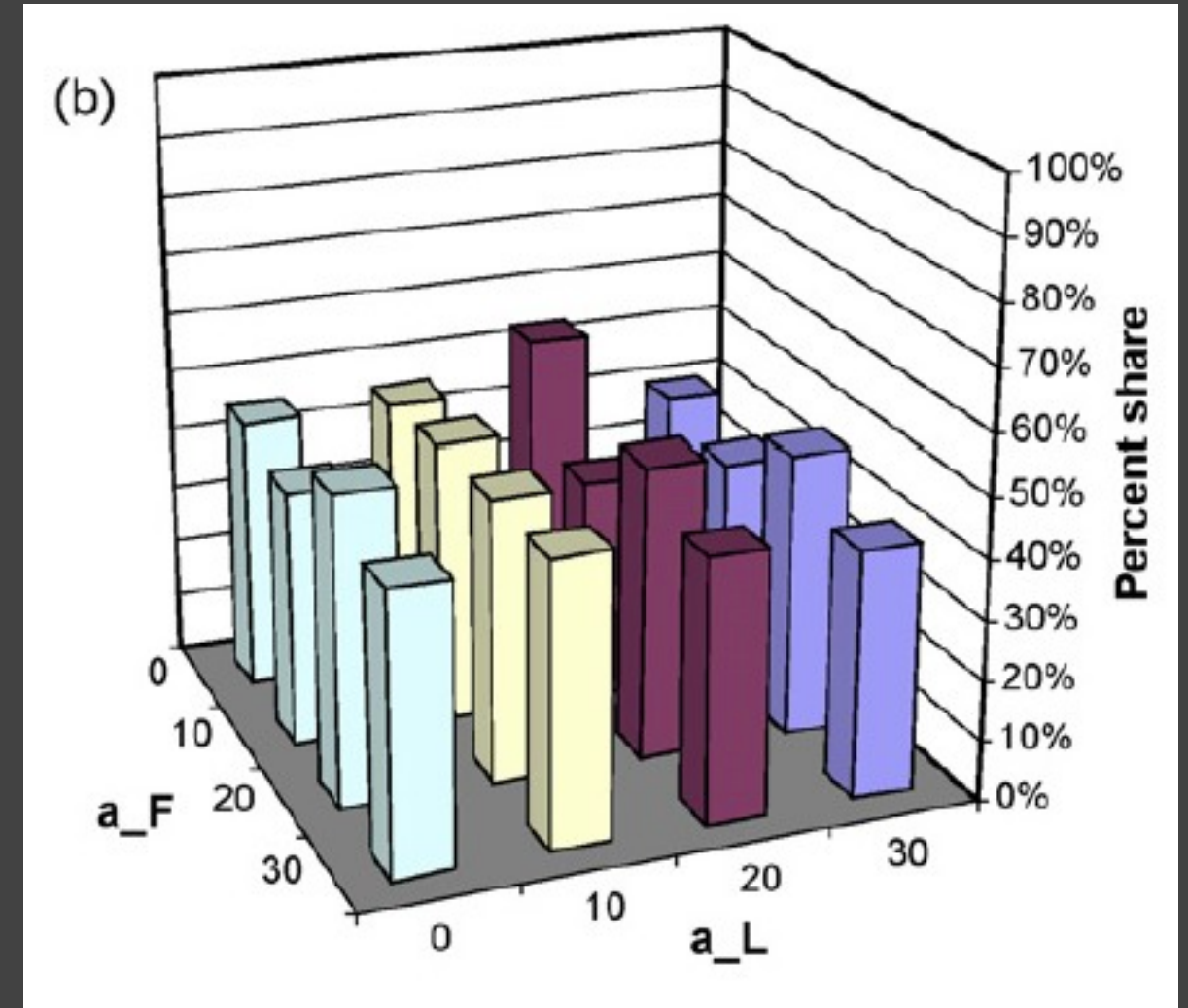
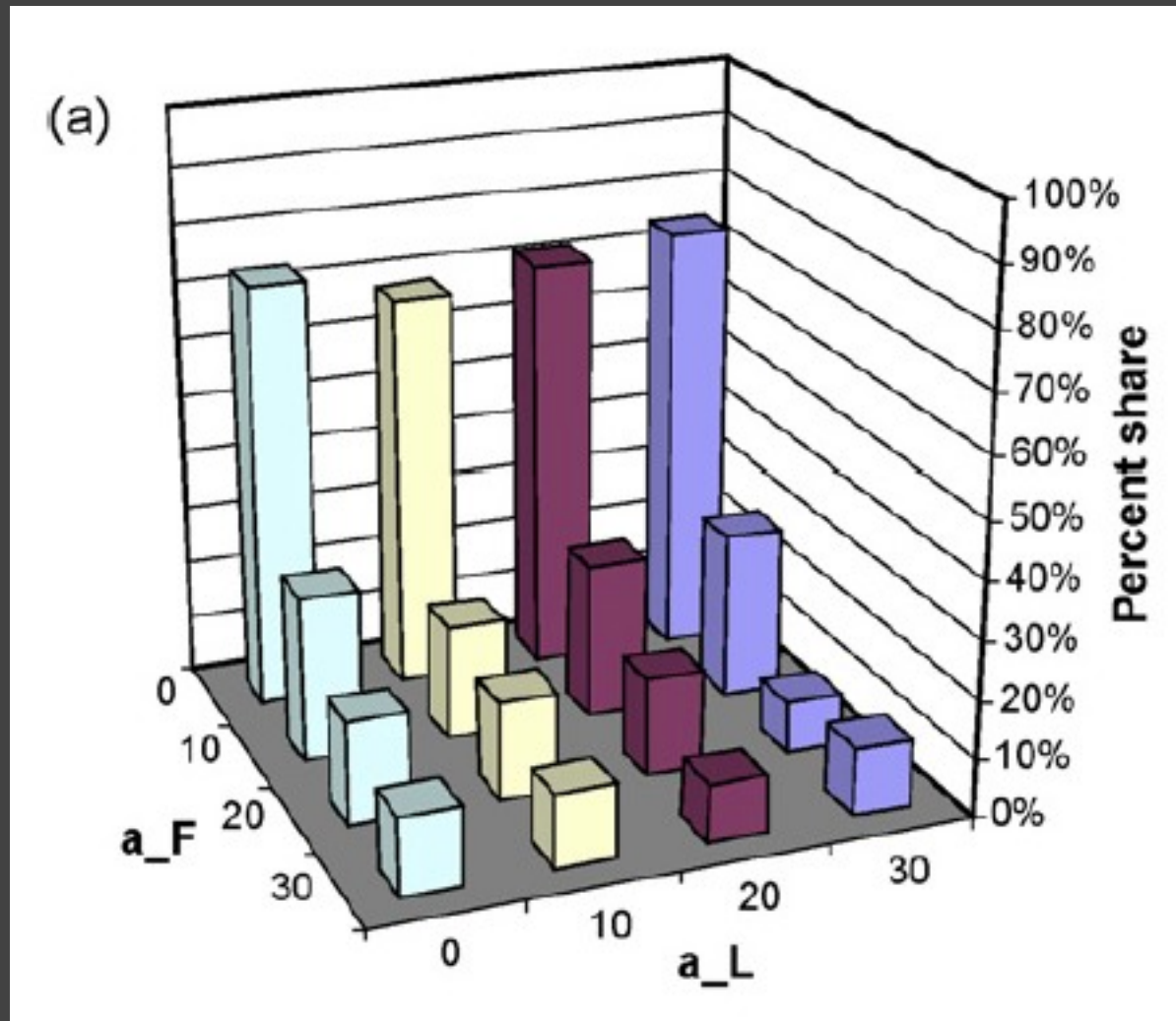
*there always exist equilibria with unilateral knowledge sharing*

## Proposition 2

### Knowledge sharing under inequity aversion

- 1. If followers are even slightly inequity averse they will always conceal if the leader has concealed. If the leader shares the follower will also share, if he or she is sufficiently inequity averse. The degree of inequity aversion needed to induce a follower to share increases in the follower's exclusivity payoff  $a_F$ .*
- 2. The leader will always share if he expects the follower to share and conceal if the follower conceals.*

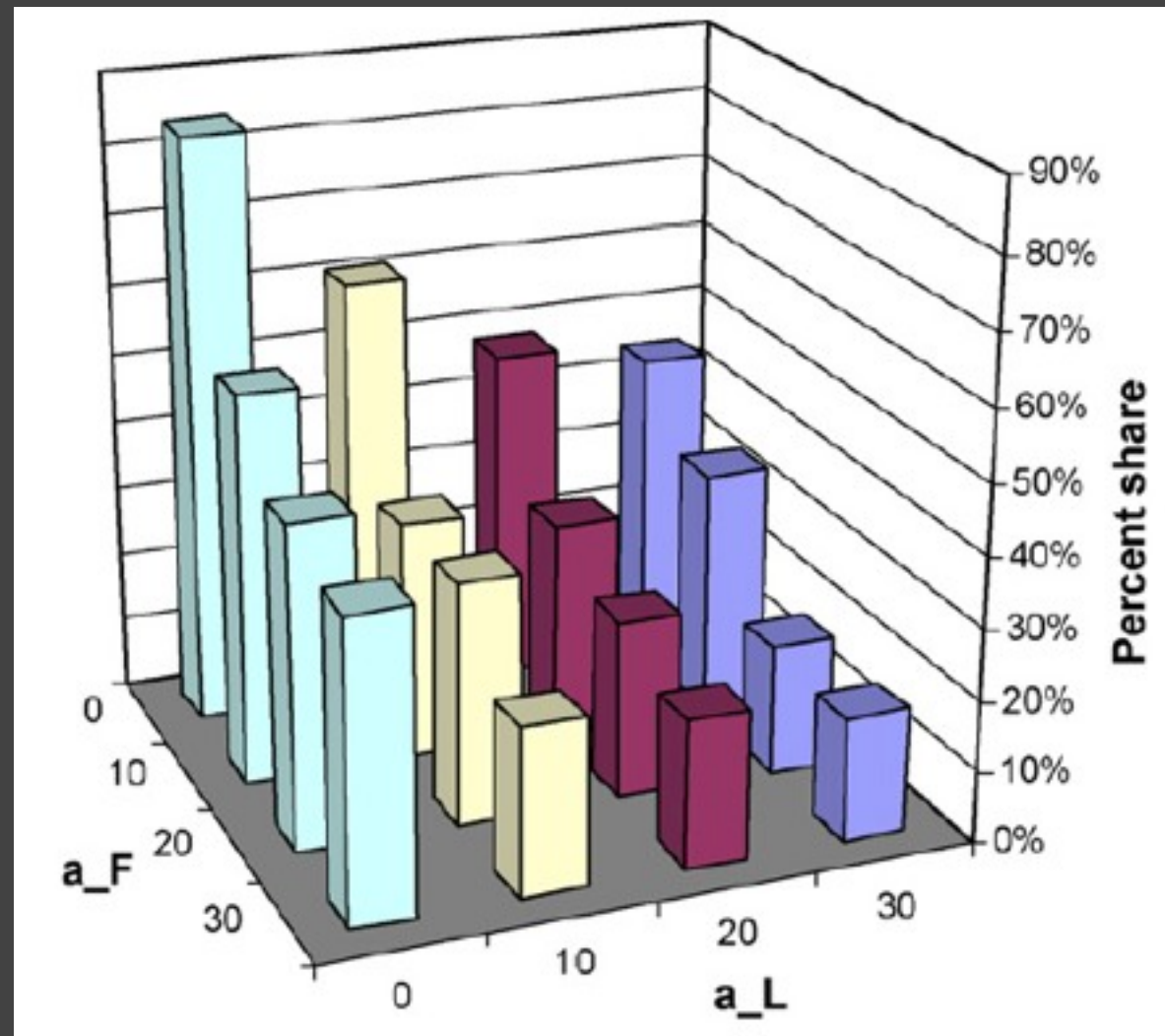
# Result 1



1. Contingent on the leader sharing, followers share in about 73% if  $a_F = 0$ .  
If  $a_F > 0$  the probability that the follower shares drops.

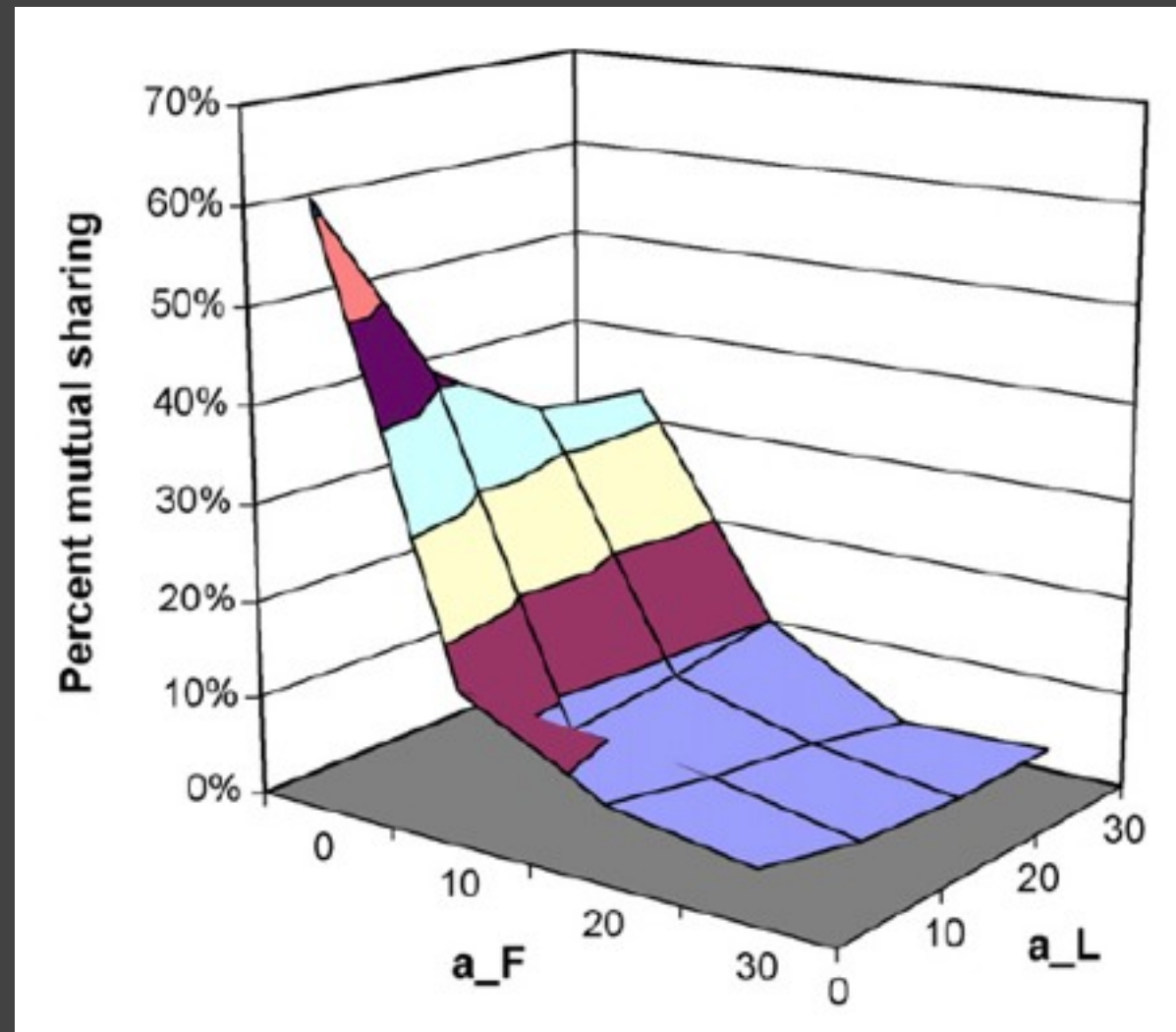
2. When the leader conceals, the probability of followers sharing is on average 45.3% across all  $a_F \times a_L$  combinations.

## Result 2



The probability that leaders share is affected negatively by both their own and their followers' exclusivity payoffs.

## Result 3



Knowledge sharing is substantially more fragile in  $a_F$  than in  $a_L$ .