

Semester II

88

Practical no: 1

Topic: Basic of R software

1) R is a software for data analysis and statistical computing

2) This software is used for effective data handling and output storage is possible

3) It is capable of graphical display

4) It a free software

1) $2^2 + \sqrt{25} + 25$

> $2^2 + \text{sqrt}(25) + 25$

[1] 44

2) $2 \times 5 \times 3 + 62 \div 5 + \sqrt{49}$

> $2 * 5 * 3 + 62 / 5 + \text{sqrt}(49)$

[1] 49.4

3) $\sqrt{76 + 4 \times 2 + 3 \div 5}$

> $\text{sqrt}(76 + 4 * 2 + 3 / 5)$

[1] 9.262829

4) $42 + |-10| + 7^2 + 3 \times 9$

> $42 + \text{abs}(-10) + 7^2 + 3 * 9$

[1] 128

34
31
> $x = 20$ find $x+y, x^2+y^2, \sqrt{x^3-y^3}, |x-y|$

> $y = 30$

> $x+y$

[1] 50..

> x^2+y^2

> x^2+y^2

[1] 1300 or

> $\text{sqrt}(y^3-x^3)$

[1] 137.8405,

> $\text{abs}(x-y)$

[1] 10.

6) $c(2, 3, 4, 8)^2$

[1] 4 9 16 25

7) $c(4, 5, 6, 8)*3$

[1] 12 15 18 24

8) $c(2, 3, 5, 7) * c(-2, -3, -5, -4)$

[1] -4 -9 -25 -28

9) $c(2, 3, 5, 7) * c(8, 9)$

[1] 16 27 40 63

88

10) $c(2, 3, 5, 7) \neq c(1, 2, 3)$

Warning message:
longer object length is not a multiple of shorter object lengths

11) $c(1, 2, 3, 4, 5, 6) \neq c(2, 3)$

[1] 1 8 9 64 25 216

12) Find the sum, product, maximum, minimum of the values

5, 8, 6, 7, 9, 10, 15, 5

Soln) $x = c(5, 8, 6, 7, 9, 10, 15, 5)$

> length(x)
[1] 8

> sum(x)
[1] 65

> prod(x)
[1] 11340000

> max(x)
[1] 15

> min(x)
[1] 5

> range(x)
[1] 5 15

35

13) $x = c(1, 2, 3, 4, 5, 6, 7, 8)$ matrix
 $x <- matrix(nrow=4, ncol=3, data=c(1, 2, 3, 4, 5, 6, 7, 8))$

> x
[1,] [2,] [3,]
[1,] 1 5 7
[2,] 2 6 8
[3,] 3 7 9
[4,] 4 8 10

14) $x = \begin{bmatrix} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{bmatrix}$ $y = \begin{bmatrix} 2 & 4 & 10 \\ -2 & 8 & -11 \\ 10 & 6 & 12 \end{bmatrix}$

To find $x+y$, $x*y$, $2x+3y$

> $x <- matrix(nrow=3, ncol=3, data=c(1, 2, 3, 4, 5, 6, 7, 8, 9))$

> $y <- matrix(nrow=3, ncol=3, data=c(2, -2, 10, 4, 8, 6, 10, -11, 12))$

> $x+y$
[1,] [2,] [3,]
[1,] 3 8 17
[2,] 0 13 -3
[3,] 13 12 21

> $x*y$
[1,] [2,] [3,]
[1,] 2 16 70
[2,] -4 40 -88
[3,] 30 36 108

35

	$2^x + 3^y$	x	y
$[1]$	8	0	3
$[2]$	-2	1	4
$[3]$	36	2	5

815) $a = c(2, 4, 6, 1, 3, 5, 7, 18, 16, 14, 17, 19, 3, 2, 5, 0, 15, 9, 14, 18, 10, 12)$

> length(a)

$[1] 23$

> b = table(a)

> transform(b)

$9 \quad F_{deg}$

~~0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20~~

~~2 2~~

~~3 3~~

~~4 1~~

~~5 2~~

~~6 1~~

~~7 1~~

~~8 1~~

~~9 1~~

~~10 1~~

~~12 1~~

~~14 2~~

~~15 1~~

~~16 1~~

~~17 1~~

~~18 2~~

36

> breaks = seq(0, 20, 5)
d = cut(a, breaks, right = FALSE)
e = table(d)
transform(e)

d	F _{deg}
[0, 5)	8
[5, 10)	5
[10, 15)	4
[15, 20)	6

Avg
n=219

Tactical no: 2
Problem on p.d.f and c.d.f.

i) Can the following be p.d.f?

$$\text{ii)} f(x) = \begin{cases} 2-x, & 1 \leq x \leq 2 \\ 0, & \text{o.w.} \end{cases}$$

$$\int f(x) dx = 1$$

$$= \int (2-x) dx$$

$$\Rightarrow \int_0^2 2 dx - \int_0^2 x dx$$

$$= 2x \Big|_0^2 - \frac{x^2}{2} \Big|_0^2$$

$$= (4-2) - (2-0) = 0$$

$$\neq 1$$

$$\text{iii)} f(x) = \begin{cases} 3x^2, & 0 < x < 1 \\ 0, & \text{o.w.} \end{cases}$$

$$\int f(x) dx = 1$$

$$= \int_0^1 3x^2 dx$$

$$= 3 \int_0^1 x^2 dx$$

$$= 3 \cdot \left[\frac{x^3}{3} \right]_0^1$$

$$= \cancel{\frac{3}{3}} \cdot \frac{3}{3} (1-0) = 1 \quad \checkmark$$

It is a p.d.f

$$\text{iv)} f(x) = \begin{cases} \frac{3x}{2} (1-\frac{x}{2}), & 0 \leq x \leq 2 \\ 0, & \text{o.w.} \end{cases}$$

$$= \int_0^2 \frac{3x}{2} \left(1 - \frac{x}{2} \right) dx$$

$$= \int_0^2 \frac{3x}{2} - \frac{3x^2}{4} dx$$

$$= \frac{3}{2} \int_0^2 x - \frac{3}{4} \int_0^2 x^2$$

$$= \frac{3}{2} \left[\frac{x^2}{2} \right]_0^2 - \frac{3}{4} \left[\frac{x^3}{3} \right]_0^2$$

$$= \frac{3}{4} [x]^2_0 - \frac{1}{4} [x^3]^2_0$$

86

$$\therefore \frac{3}{4} [4-0] - \frac{1}{4} [8-0]$$

$$= 3 - 2$$

~~It is a p.d.f~~

Can the following be p.m.f.

i)	x	1	2	3	4	5
	$P(x)$	0.2	0.3	-0.1	0.5	0.1

Since one probability is negative it not apnd

2)	x	0	1	2	3	4	5	6
	$P(x)$	0.1	0.3	0.2	0.2	0.1	0.1	0.1

Since $P(x) > 0 \forall x$ and $\sum P(x) = 1$

It is a p.m.f

$$x = c(0, 1, 2, 3, 4, 5)$$

$$\text{prob} = c(0.1, 0.3, 0.2, 0.2, 0.1, 0.1)$$

sum(prob)

iii) $\begin{array}{ccccccc} x & 10 & 20 & 30 & 40 & 50 \\ P(x) & 0.2 & 0.3 & 0.3 & 0.2 & 0.2 \end{array}$

$$y = c(10, 20, 30, 40, 50)$$

$$\text{prob} = c(0.2, 0.3, 0.3, 0.2, 0.2)$$

sum(prob)

$$[1] 1.2$$

\because Since $P(x) > 0 \forall x$ and $\sum P(x) = 1$

But the value is 1.2
∴ It is not p.m.f

3.) Find $P(x \leq 2)$, $P(2 \leq x \leq 4)$, $P(\text{atleast } 4)$,

$$P(3 < x < 6)$$

x	0	1	2	3	4	5	6
$P(x)$	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$\therefore P(x \leq 2) = P(0) + P(1) + P(2)$$

$$= 0.1 + 0.1 + 0.2$$

$$= 0.4$$

$$\therefore P(2 \leq x \leq 4) = P(2) + P(3) + P(4)$$

$$= 0.2 + 0.2 + 0.1$$

$$= 0.5$$

$$\therefore P(\text{atleast } 4) = P(4) + P(5) + P(6)$$

$$= 0.1 + 0.2 + 0.1$$

$$= 0.4$$

$$\text{iii)} P(3 < x < 6) = P(4) + P(5)$$

$$= 0.1 + 0.2$$

$$= 0.3$$

4) Find c.d.f

i)	x	0	1	2	3	4	5	6
	P(x)	0.1	0.1	0.2	0.2	0.1	0.2	0.1

$$p_{\text{prob}} = c(0.1, 0.1, 0.2, 0.2, 0.1, 0.2, 0.1)$$

cumsum(p_prob)

[1]	0.1	0.2	0.4	0.6	0.7	0.9	1.0
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$$F(x) = 0 \quad \text{if } x < 0$$

$$= 0.2 \quad \text{if } 0 \leq x < 1$$

$$= 0.4 \quad \text{if } 1 \leq x < 2$$

$$= 0.6 \quad \text{if } 2 \leq x < 3$$

$$= 0.7 \quad \text{if } 3 \leq x < 4$$

$$= 0.9 \quad \text{if } 4 \leq x < 5$$

$$= 1.0 \quad \text{if } 5 \leq x < 6$$

ii)

x	1.0	1.2	1.4	1.6	1.8
p(x)	0.2	0.35	0.15	0.2	0.1

$$p_{\text{prob}} = c(0.2, 0.35, 0.15, 0.2, 0.1)$$

cumsum(p_prob)

[1]	0.20	0.55	0.70	0.95	1.00
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$$F(x) = \begin{cases} 0 & \text{if } x < 1 \\ 0.20 & \text{if } 1 \leq x < 2 \\ 0.55 & \text{if } 2 \leq x < 3 \\ 0.70 & \text{if } 3 \leq x < 4 \\ 0.90 & \text{if } 4 \leq x < 5 \\ 1.00 & \text{if } 5 \leq x < 6 \end{cases}$$

A.M
1.279

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HE

Practical no. 3

Topic:- Probability distribution and Binomial distribution

1.) Find the c.d.f. of the following p.d.f. and draw the graph

x	10	20	30	40	50
P(x)	0.15	0.25	0.3	0.2	0.1

$$x = \{10, 20, 30, 40, 50\}$$

$$\text{prob} = \{0.15, 0.25, 0.3, 0.2, 0.1\}$$

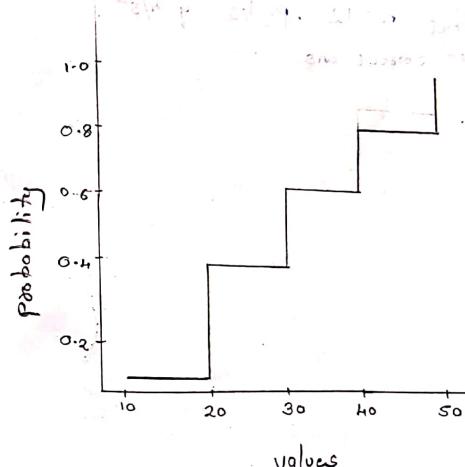
cumsum (prob)

$$[1] 0.15 \quad 0.40 \quad 0.70 \quad 0.90 \quad 1.00$$

$$\begin{aligned} F(x) &= 0 && \text{if } x < 10 \\ &= 0.15 && 10 \leq x < 20 \\ &= 0.40 && 20 \leq x < 30 \\ &= 0.70 && 30 \leq x < 40 \\ &= 0.90 && 40 \leq x < 50 \\ &= 1.00 && x \geq 50 \end{aligned}$$

Graph of c.d.f

40



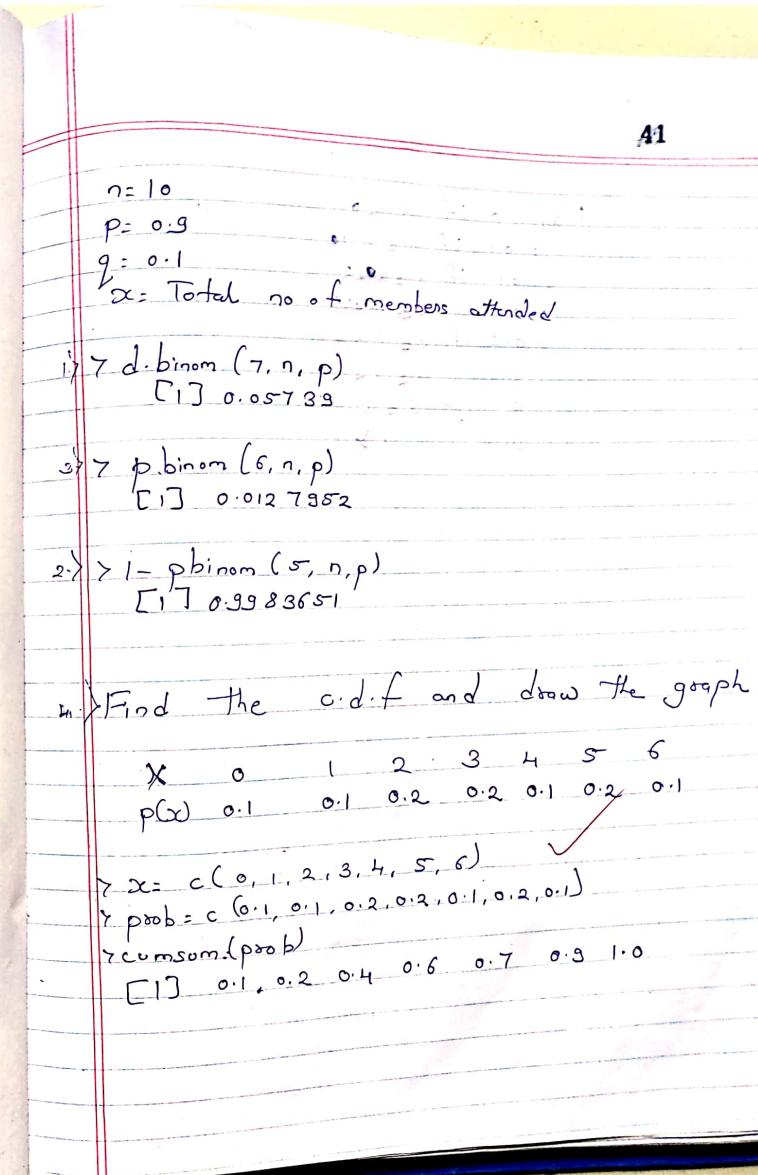
2) Binomial distribution:-

- Suppose there are 12 mca in a test each question has five options and only one of them is correct. Find a probability of having no one
 1) Five correct ans
 2) Atmost 4 correct answers.

Sol If is given that $n = 12$, $p = 1/5$, $q = 4/5$
 x = Total no. of correct ans
 $x \sim B(n, p)$

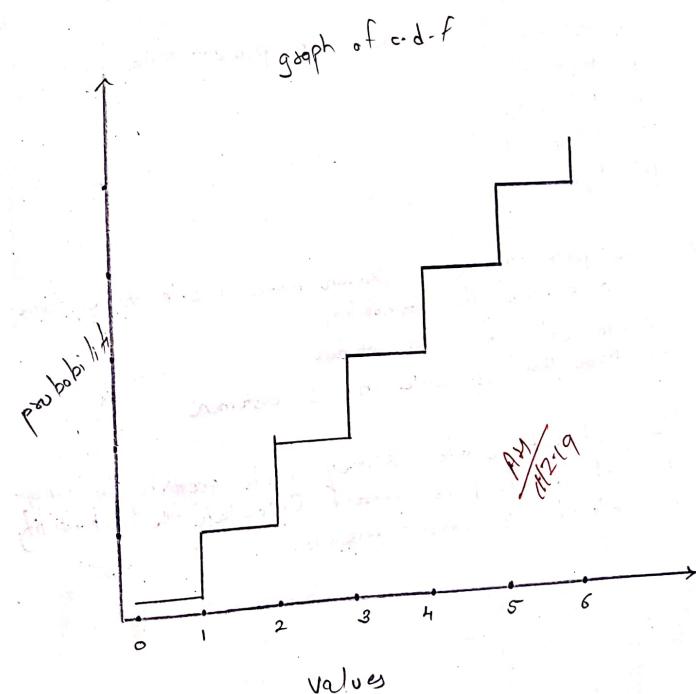
$$\begin{aligned} > n = 12 \\ > p = 1/5 \\ > q = 4/5 \\ > x = 8 \\ > d\text{-binom}(5, 12, 1/5) \\ [1] 0.0531 \\ > p\text{-binom}(4, 12, 1/5) \\ [1] 0.927445 \end{aligned}$$

- 2) There are 10 members in a committee the probability of any member attending a meeting is 0.9. Find the probability
 1) 7 member attended
 2) at least 5 member attended
 3) atmost 6 member attended



$$\begin{aligned}
 F(x) &= 0 \text{ if } x < 0 \\
 &= 0.1 \text{ if } 0 \leq x < 1 \\
 &= 0.1 \text{ if } 1 \leq x < 2 \\
 &= 0.2 \text{ if } 2 \leq x < 3 \\
 &= 0.2 \text{ if } 3 \leq x < 4 \\
 &= 0.1 \text{ if } 4 \leq x < 5 \\
 &= 0.2 \text{ if } 5 \leq x < 6 \\
 &= 1.0 \text{ if } x \geq 6
 \end{aligned}$$

graph of c-d-f



Practical:-4

Biomial Distribution.

- 1) Find the complete b.d when $\mu = 5$ $P = 0.1$
- 2) Find Probability of exactly 10 success in 100 trials $P = 0.1$
- 3) X follows B.D with $n = 12$, $P = 0.25$ find
 - i) $P(X = 5)$
 - ii) $P(X \leq 5)$
 - iii) $P(X > 7)$
 - iv) $P(5 < X < 7)$
- 4) The probability of salesman makes a sale to customer is 0.15 find the Probability.
 - i) No sale for 10 customers
 - ii) More than 3 sales in 20 customers
- 5) A student writes 5-mcq. Each question has 4 options, out of which 1 is correct. Calculate the Probability for atleast 3 correct answers.

43

Note:

- i) To find the value of x for which the Probability is P , the command is $qbinom(x, n, p)$
 - ii) $P(X = x) = dbinom(x, n, p)$
 - iii) $P(X \leq x) = pbisom(x, n, p)$
 - iv) $P(X > x) = 1 - pbisom(x, n, p)$
- v) $n = 5, p = 0.1$
 $> dbinom(0.5, 5, 0.1)$
 $[1] 0.59049 0.32805 0.7290 0.00810$

2) $> n = 100$
 $> p = 0.1$
 $> x = 10$
 $> dbinom(10, 100, 0.1)$
 $[1] 0.1318653$

3) $> n = 12$
 $> p = 0.25$

- i) $> x = 5$
 $> dbinom(5, 12, 0.25)$
 $[1] 0.1032414$

5.) $n=5$
 $x=3$
 $P = \frac{1}{n} = 0.25$
 $1 - P(x \leq 2)$
 $1 - p_{\text{binom}}(2, 5, 0.25)$
[1] 0.1035156

ii.) $n=12$
 $p = 0.25$
 $x = 8$
 $p_{\text{binom}}(5, 12, 0.25)$
[1] 0.9455978

iii.) $n=12$
 $p = 0.25$
 $x > 7$
 $1 - p_{\text{binom}}(7, 12, 0.25)$
[1] 0.00278181

iv.) $n=12$
 $p = 0.25$
 $5 < x < 7$
 $d_{\text{binom}}(5, 12, 0.25)$
[1] 0.04014945

4.) i.) $n=10$
 $p = 0.15$
 $x = 0$
 $d_{\text{binom}}(0, 10, 0.15)$
[1] 0.1968744

ii.) $n=20$
 $p = 0.15$
 $P(x > 3) = 1 - P(x \leq 3)$
 $1 - p_{\text{binom}}(3, 20, 0.15)$
[1] ~ 0.01

26.) X follows binomial distribution with $n=10$, $p=0.4$. Plot the graph of p.m.f & c.d.f

Sol/
 $n=10$
 $p=0.4$
 $x = 0:n$
 $\text{prob} = d_{\text{binom}}(x, n, p)$
 $\text{compprob} = p_{\text{binom}}(x, n, p)$
 $d = \text{data.frame}(x, \text{values}=x, "Probability" = prob)$
 $\text{Point}(d)$

X. values	Probability
0	0.0060466176
1	0.0403107840
2	0.1209323520
3	0.2508226560
4	0.2006581248
5	0.1114767360
6	0.0424673280
7	0.0106168320
8	0.0015728640
9	0.0001048576
10	0.00001048576

$\text{plot}(x, prob, "h")$
 $\text{plot}(x, compprob, "s")$

5.) Normal Distribution

- ① $P[X = x] = d_{\text{norm}}(x, \mu, \sigma)$
- ② $P[X \leq x] = p_{\text{norm}}(x, \mu, \sigma)$
- ③ $P[X \geq x] = 1 - p_{\text{norm}}(x, \mu, \sigma)$
- ④ $P[x_1 < x < x_2] = p_{\text{norm}}(x_2, \mu, \sigma) - p_{\text{norm}}(x_1, \mu, \sigma)$
- ⑤ To find the value of k so that
 $P[X \leq k] = p ; q_{\text{norm}}(p, \mu, \sigma)$
- ⑥ To generate ' n ' random numbers
 $\text{dnorm}[n, \mu, \sigma]$

Q) $X \sim N (\mu = 50, \sigma^2 = 100)$

Find: i.) $P(X \leq 40)$

ii.) $P(X > 55)$

iii.) $P(42 \leq X \leq 60)$

iv.) $P(X \leq k) = 0.7 ; k = ?$

Sol?

① $a = p_{\text{norm}}(40, 50, 10)$
 $\Rightarrow \text{cat} ("p(X \leq 40) = ", a)$
 $p(X \leq 40) = 0.15865553$

② $b = 1 - p_{\text{norm}}(55, 50, 10)$
 $\Rightarrow \text{cat} ("p(X > 55) = ", b)$
 $p(X > 55) = 0.3085375$

③ $c = \text{pnorm}(60, 50, 10) - \text{pnorm}(42, 50, 10)$
 $\text{cat}("p(42 \leq x \leq 60) = ", c)$
 $p(42 \leq x \leq 60) = 0.6294893$

④ $d = \text{qnorm}(0.7, 50, 10)$
 $\text{cat}("p(x \leq k) = 0.7, k = ", d)$
 $p(x \leq k) = 0.7, k = 55.24401$

(2) $X \sim N(\mu = 100, \sigma^2 = 86)$

Find:
i.) $P(X \leq 100)$
ii.) $P(X \leq 95)$
iii.) $P(X > 105)$
iv.) $P(95 \leq X \leq 105)$
v.) $P(X \leq k) = 0.4, k = ?$

Soln
i.) $a = \text{pnorm}(110, 100, 5)$
 $\text{cat}("p(X \leq 110) = ", a)$
 $p(X \leq 110) = 0.9522096$

ii.) $b = \text{pnorm}(95, 100, 5)$
 $\text{cat}("p(X \leq 95) = ", b)$
 $p(X \leq 95) = 0.2023284$

iii.) $c = 1 - \text{pnorm}(115, 100, 5)$
 $\text{cat}("p(X > 115) = ", c)$
 $p(X > 115) = 0.00620965$

iv.) $d = \text{pnorm}(105, 100, 5) - \text{pnorm}(95, 100, 5)$
 $\text{cat}("p(95 \leq X \leq 105) = ", d)$
 $p(95 \leq X \leq 105) = 0.5953432$

v.) $e = \text{qnorm}(0.4, 100, 5)$
 $\text{cat}("p(X \leq k) = 0.4, k = ", e)$
 $p(X \leq k) = 0.4, k = 98.47892$

3.) Generate 10 random numbers from normal distribution with mean = 60 & s.d = 5 also calculate sample mean, variance, median and standard deviation

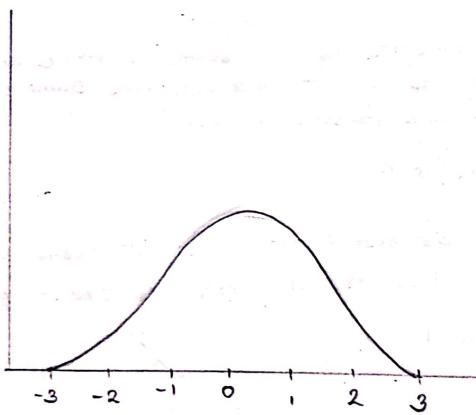
soln
 $x = \text{rnorm}(10, 60, 5)$
 x
61.93112 55.80205 55.07745 50.96845 58.17353
58.15321 61.55288 71.91887 66.57875 66.94407
 $\text{am} = \text{mean}(x)$
 am
60.01123
 $\text{me} = \text{median}(x)$
 me
59.86623
 $n = 10$
 $\text{variance} = (n-1) * \text{var}(x)/n$
 Variance
44.045974
 $\text{sd} = \text{sqrt}(\text{variance})$
 sd
6.667814

④ ~~Ans~~ Draw the graph of standard distribution.

Soln > $x = \text{seq}(-3, 3, by=0.1)$

> $y = \text{dnorm}(x)$

> $\text{plot}(x, y, xlab = "x values", ylab = "probability", main = "Standard Normal Graph")$



Practical no. 6

47

Topic: Z Distribution

1) Test the hypothesis ($H_0: \mu = 10$) against $H_1: \mu \neq 10$. A sample of size four hundred is selected which gives a mean 10.2 & standard deviation 2.25. Test the hypothesis at 5% level of significant.

Sol m0 = mean of population 10 mx = mean of sample 10.2 sd = standard deviation = 2.25 n = sample size 400

> zcal = $(mx - m0) / (sd / \sqrt{n})$

> cat ("zcal is = ", zcal)

• zcal is 1.7778

> pvalue = $2 * (1 - \text{pnorm}(\text{abs}(zcal)))$

> pvalue

[1] 0.07544086

Since 0.075 is more than 0.05 we will accept the H_0 .

2) Test the hypothesis $H_0: \mu = 75$ vs $H_1: \mu \neq 75$. A sample of size 100 is selected and sample mean is 80 with $sd = 3$. Test the hypothesis at 5% level of significant.

Sol m0 = 75, mx = 80, sd = 3, n = 100

> zcal = $(mx - m0) / (sd / \sqrt{n})$

> cat ("zcal is = ", zcal)

• zcal is 16.6667

> pvalue = $2 * (1 - \text{pnorm}(\text{abs}(zcal)))$

> pvalue

[1] 0

3) Test the hypothesis (H_0): $\mu = 25$ against $H_1: \mu \neq 25$ at 5% level of significant. The following sample of 50 is selected.

20 24 27 35 30 46 26 27 10 20 30 37 35
21 22 28 24 25 26 27 28 29 30 38 27
15 19 22 20 18

Solution: $x = c(20, 24, 27, \dots, 18)$

> n = length(x)

> mx = mean(x)

[1] 26.06667

> variance = (n-1) * var(x) / n

> variance

[1] 52.9955

> sd = sqrt(variance)

> sd

[1] 7.27.9805

> zcal = (mx - 25) / (sd / sqrt(n))

> cat("zcal is =", zcal)

[1] zcal is -0.8025454

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.4222375

4) Experience has show that 20% students ⁴⁸ a college one smoke a sample of four hundred student reveal that out of four hundred only 50 smoke test the hypothesis that the experience the give the correct proportion or not.

> P = 0.2

> Q = 1 - P

> p = 50 / 400

> p

[1] 0.125

> n = 400

> zcal = (p - P) / sqrt(P * Q / n)

> cat("zcal is =", zcal)

[1] zcal is -3.75

> pvalue = 2 * (1 - pnorm(abs(zcal)))

> pvalue

[1] 0.0001768346

81) Test the hypothesis $H_0: P = 0.5$ against $H_1: P \neq 0.5$.
 A sample of 200 is selected and the sample proportion is $\hat{P} = 0.56$. Test the hypothesis at 1% level of significance.

Sol:

- > $n = 200$
- > $P = 0.52$
- > $\alpha = 0.05$
- > $\alpha = 1 - P$
- > $Z_{\text{cal}} = (p - P) / (\sqrt{P(1-P)/n})$
- > cat ("Z calculated is", Z_{cal})
- > Z_{cal} is 1.697058
- > pvalue = $2 * (1 - \text{pnorm}(\text{abs}(Z_{\text{cal}})))$
- > pvalue
- [1] 0.08968602

$\approx 2.01^{2.0}$

Practical: 7

49

Topic:- Large Sample Tests.

A study of noise level into hospital is calculated below. test the hypothesis of noise level in two hospital are same or not

	Hos A	Hos B
No. of sample	84	34
abs		
Mean	61	59
S.D	7	8

Q1) H_0 : The noise level are same

$$n_1 = 84$$

$$\bar{x}_1 = 61$$

$$n_2 = 34$$

$$\bar{x}_2 = 59$$

$$s_{dy} = 8$$

$$z = (x_1 - x_2) / \sqrt{(s_{dx}^2/n_1) + (s_{dy}^2/n_2)}$$

z

$$[1] 1.273682$$

cat ("Z calculated is =", z)

$$z_{\text{calculated}} = 1.273682$$

$$> pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

> pvalue

$$[1] 0.04550026$$

Since $pvalue < 0.05$, we reject H_0 at 5% Level of significance.

Q8

- 2) Two random sample of size 1000 and 2000 drawn from two population with a mean, 67.5 and 68 respectively & with the same standard deviation of 2.5 test the hypothesis. The mean of two population are equal.

H_0 : Two population are equal

$$n_1 = 1000$$

$$n_2 = 2000$$

$$m_{x1} = 67.5$$

$$m_{y1} = 68$$

$$S_{dx} = 2.5$$

$$S_{dy} = 2.5$$

$$y = (m_{x1} - m_{y1}) / \sqrt{((S_{dx}^2/n_1) + (S_{dy}^2/n_2))}$$

$$[1] = 5.163978$$

cat("y calculated is = ", y)

$$y \text{ calculated is } = 5.163978$$

$$p \text{ value} = 2 * (1 - pnorm(abs(y)))$$

pvalue

$$[1] 2.417564e-07$$

Since pvalue < 0.05 we reject the H_0 at 5% level of significance.

- 3) In a first year class 20% of a random sample of 400 students had defect eye sight in 5th class 15.5% of 500 students sample had the same defect. Is the difference of proportion is same?

Sol) H_0 : The proportion of population are equal

$$n_1 = 400$$

$$n_2 = 500$$

$$p_1 = 0.2$$

$$p_2 = 0.155$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$q = 1 - p$$

$$P = \frac{0.175}{0.825}$$

$$[1] = 0.8022225$$

$$z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

> z

$$[1] 1.760547$$

$$p \text{ value} = 2 * (1 - pnorm(abs(z)))$$

Since pvalue > 0.05

$$[1] 0.0774$$

Since pvalue < 0.05 we accept the H_0 at 5% level of significance.

4) From each of the boxes of the apple a sample size 200 is collected. It is found that there are 44 bad apples in the first sample and 30 in the second sample. Test the hypothesis that the two boxes are equivalent in term of number of bad apples.

H₀: the two boxes are equivalent.

$$p_1 = 44/200$$

$$p_2 = 30/200$$

$$n_1 = 200$$

$$n_2 = 200$$

$$p = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

$$[1] 0.185$$

$$q = 1 - p$$

$$[1] 0.815$$

$$z = (p_1 - p_2) / \sqrt{p * q * (1/n_1 + 1/n_2)}$$

$$z$$

$$[1] -1.80274$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(z)))$$

$$[1] 0.07142$$

$\therefore \text{pvalue} < 0.05$ we accept the H_0 of 5% level of significance

5) In MA class out of a sample of 60, mean height is 63.5 inch with a sd 2.5 in. In a mcom class out of 580 students mean height 69.5 inch with a sd 2.5. Test the hypothesis that the mean of MA & mcom are same
H₀: hypothesis of the mean of MA & mcom class are same

$$> n1 = 60$$

$$> n2 = 580$$

$$> mx = 63.5$$

$$> my = 69.5$$

$$> sd1 = 2.5$$

$$> sd2 = 2.5$$

$$> y = (mx - my) / \sqrt{(sd1^2/n1) + (sd2^2/n2)}$$

$$> [1] -12.53359$$

> cat("y calculated is = ", y)

> y calculated is = -12.53359

> pvalue = 2 * (1 - pnorm(abs(y)))

pvalue

$$[1] 0$$

Since pvalue > 0.05 we reject the H_0 at 5% level significant

AM/5.210

17.6

Practical: 8

Topic: Small sample test

- 1) The flower 10 are selected and the height are found to be 63, 63, 68, 69, 71, 71, 72, ans.. Test the hypothesis that the mean height is 66 cm at 1%: instant.

Sol: $H_0:$

Mean = 66 cms

 $x = c(63, 63, 68, 69, 71, 71, 72)$
 $t \cdot t \cdot t(x)$

One Sample t-test

data: x

 $t = 47.94, df = 6, p\text{-value} = 8.522e-09$

alternative hypothesis: true mean is not equal to 0

95 percent confidence interval:

64.66479 71.62092

sample estimates:

mean of x

68.14286

 $\therefore p\text{value} < 0.01$ we reject the H_0 of 1% level of significant.

- 2) Two random sample where drawn from two different population

sample1 = 8, 10, 12, 11, 16, 15, 18, 7

sample2 = 20, 15, 18, 9, 8, 10, 11, 12

Test the Hypothesis that there is no difference b/w the 2 population mean at 5% los.

Sol: H_0 : There is no difference in the population means

 $x = c(8, 10, 12, 11, 16, 15, 18, 7)$ $y = c(20, 15, 18, 9, 8, 10, 11, 12)$

Welch Two Sample t-test

data: x and y

 $t = -0.36247, df = 13.837, p\text{-value} = 0.7225$

alternative hypothesis: true difference in means is not equal to 0

95 percent confidence interval:

-5.192719 3.692719

Sample estimates:

mean of x mean of y

12.125 12.875

$p\text{value} > 0.05$ we accept the H_0 of 5% level of significant

82) following are the weight of 10 people before and after a diet program. Test the Ho that the diet program is effective or not.

Before(kg) 100 125 95 96 98 112 115 104 103
After(kg) 95 80 95 98 90 100 110 85 101

Sol) H_0 : The diet program is not effective

> $x = c(100, 125, 95, 96, 98, 112, 115, 104, 103, 110)$

> $y = c(95, 80, 95, 98, 90, 100, 110, 85, 100, 101)$

> `t.test(x, y, paired=T, alternative = "less")`

Paired t-test

data: x & y

$t = 2.6089$, $df = 9$, $p\text{value} = 0.9858$

alternative hypothesis: true difference in means is less than 95 percent confidence interval.

-Inf 18.72908

sample estimates

mean of the differences

11

\therefore As $p\text{value}$ is greater than 0.05 we accept the 5% level of significance.

53

4) The marks before and after a training program are given below

Before 20 25 32 28 27 36 35 25

After 30 35 32 37 37 40 40 23

Test the hypothesis the training program is or not

H_0 : The training program is not effective

$y_a = c(20, 25, 32, 28, 27, 36, 35, 25)$

$y_b = c(30, 35, 32, 37, 37, 40, 40, 23)$

~~Paired t-test~~ $t\text{test}(y_a, y_b, paired=T, alternative)$

data : a and b

$t = -3.3859$, $df = 7$, $p\text{value} = 0.9942$

alternative hypothesis: true diff in means is greater than

95 percent confidence interval:

-8.967399 Inf

sample estimates:

mean of the differences

-5.75

\therefore $p\text{value} > 0.05$ we accept the 5% level of significance.

Practical: 9

Chi square distribution and ANOVA Bar *

- 1) Use the following data to whether the clean
of home depend upon the child

Code of Home			
Code of Child	Clean	Clean	Dirty
fairly	70	50	
Dirty	80	20	
	35	45	

H₀: code of the home and child are independent

> $x = c(70, 80, 35, 50, 20, 45)$

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

> y

```
[1] [2]  
[1] 70 50  
[2] 80 20  
[3] 35 45
```

> pv = chisq.test(y)

> pv

Pearson chi-squared test

data: y

< P value is less than 0.05 at 5% we reject H₀

55

Table below show a relation between the performance of mathematics and computer of cs student.

		Maths		
		HG	MG	LG
Comp	HG	56	71	12
	MG	47	163	38
	LG	14	42	85

H₀: Performance b/w Maths and Computer are independent

> x = c(56, 71, 12, 47, 163, 38, 14, 42, 85)

> m = 3

> n = 2

> y = matrix(x, nrow = m, ncol = n)

```
[1] [2] [3]  
[1] 56 71 12  
[2] 47 163 38  
[3] 14 42 85
```

> pv = chisq.test(y)

> pv
Pearson's chi-squared test

data: y
X-squared = 145.78 df = 4 p-value < 2.2e-16
p-value < 0.05 we reject H₀ at 5% less

Q3

3) Perform ANOVA for the following data:

Varieties	Observation
A	50, 52
B	53, 55
C	60, 58, 57, 58
D	52, 54, 54, 55

H_0 : The mean of variety A, B, C, D are

$$x_1 = c(50, 52)$$

$$x_2 = c(53, 55)$$

$$x_3 = c(60, 58, 57, 58)$$

$$x_4 = c(52, 54, 54, 55)$$

$$d = \text{stack}(c(\text{list}(b_1 = x_1, b_2 = x_2, b_3 = x_3, b_4 = x_4)))$$

> names(d)

[1] "values" "ind"

> oneway.test(values ~ ind, data = d, var.equal = T)

one way analysis of means

data values and ind

$F = 11.735$, num df = 3, denom df = 8, p-value = 0.001

& anova(anova)

	Df	Sum Sq	Mean Sq	F value	P > F
ind	3	71.06	23.688	11.73	0.00183
Residuals	8	13.17	2.019		

As $p < 0.05$ we reject H_0 at 5%.

→ Perform ANOVA for the following data

56

types observation

A 9, 7, 8

B 4, 6, 5

C 8, 6, 10

D 6, 9, 9

H_0 : The mean of variety A, B, C, D equal

$x_1 = c(9, 7, 8)$

$x_2 = c(4, 6, 5)$

$x_3 = c(8, 6, 10)$

$x_4 = c(6, 9, 9)$

> d = stack(c(list(b1 = x1, b2 = x2, b3 = x3, b4 = x4)))

> names(d)

[1] "values" "ind"

> oneway.test(values ~ ind, data = d, var.equal = T)

one way analysis of means

data: Values and ind

$F = 0.667$, num df = 3, denom df = 8, p-value = 0.1139

> anova = anova(values ~ ind, data = d)

> summary(anova)

	Df	Sum Sq	Mean Sq	F value	P > F
ind	3	18	6.00	2.667	0.1139
Residuals	8	18	2.25		

$p_{value} > 0.05$ we accept H_0 at 5% level

> x = read.csv("C:/Users/Administrator/Desktop")

> x

Practical: 10

Q2

Topic: Non Parametric Test

Following are the amount of sulphur oxide emitted by factory

Data: 17, 15, 20, 23, 19, 18, 22, 25, 27, 9, 24, 20, 17, 6, 24, 14, 15, 23, 24, 26

Apply sign test to test the hypothesis that the population median is 21.5 against the alternative it is less than 21.5.

H_0 : Population median equal to 21.5

H_1 : It is less than 21.5

$$x = c($$

$$m = 21.5$$

$$sp = \text{length}(x[x > m])$$

$$sn = \text{length}(x[x < m])$$

$$n = sp + sn$$

$$pv = \text{pbnom}(sp, n, 0.5)$$

$$pv = 0.411$$

P value > 0.05 we accept H_0 at 5% level of significance

Note: If the alternative is greater than median $p_{\text{pbnom}}(sn)$

.57

For the observation 12, 19, 31, 28, 43, 40, 55, 49, 70, 63 apply sign test to test population median is 25 against the alternative if it is more than 25

H_0 : population median equal to 25

H_1 : It is more than 25

$$x = c(12, 19, 31, 28, 43, 40, 55, 49, 70, 63)$$

$$m = 25$$

$$sp = \text{length}(x[x > m])$$

$$sn = \text{length}(x[x \leq m])$$

$$n = sp + sn$$

$$pv = \text{pbnom}(sn, n, 0.5)$$

$$pv$$

$$C) 0.0546875$$

P value is less than 0.05 we reject

58

- 3) For the following data
60, 65, 63, 89, 71, 71, 58, 51, 48, 66 test the hypothesis
using wilcoxon sign rank test for testing the hypothesis
The median is 60 against the alternative it is greater than 60.

Sol

$$H_0: \text{The median is } 60$$

$$H_1: \text{It is greater than } 60$$

$$x = c(60, 65, 63, 89, 61, 71, 58, 51, 48, 66)$$

$$\mu = 60$$

wilcox.test(x, "greater", mu = 60)

(Wilcoxon signed rank test with continuity correction)

Data: x

$$V = 29, p\text{-value} = 0.2386$$

alternative hypothesis: true location is greater than 60
p-value < 0.5 we reject the H_0

Note: If the alternative is less

wilcox.test(x, alter = "less", mu = 60)

If the alternative is not equal to

wilcox.test(x, alter = 2-sided)

Using wilcoxon test
against the alternative hypothesis median is less than 58
12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20

Sol

$$H_0: \text{The median is } 12$$

$$H_1: \text{It is less than } 12$$

$$> x = c(12, 13, 10, 20, 15, 5, 1, 7, 6, 11, 9, 20)$$

> wilcox.test(x, alter = "less", mu = 12)

Wilcoxon signed rank test with continuity correction

Data: x

$$V = 25, p\text{-value} = 0.2521$$

alternative hypothesis: true location is less than 12.

p value value is

AM
10
11
12