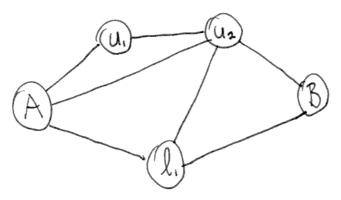
- · iterate over bags X;
- . at each "introduce" bag, compute d(x,v) for v the new node and x each node in  $X_i$ , current bag
- . then compute, for each yEG already visited:

$$d(y,v) = \min_{x \in X_i} \left( d(y,x) + d(x,v) \right)$$

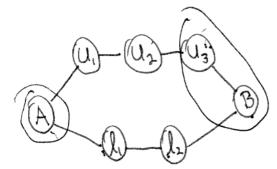
 $O(K \cdot N)$  per bag.



Nice Path Decomposition

non: 
$$A = \begin{pmatrix} A & A & A \\ U_1 & U_2 & U_2 \\ \vdots & \vdots & \vdots \\ A & U_1 & U_2 & A \\ \end{pmatrix} \begin{pmatrix} A & U_2 & U_2 \\ U_2 & U_2 \\ \end{pmatrix} \begin{pmatrix} U_2 & U_2 \\ U_1 & U_2 \\ \end{bmatrix} \begin{pmatrix} U_2 & U_2 \\ U_2 & U_2 \\ \end{bmatrix} \begin{pmatrix} U_2 & U_2 \\ U_2 & U_2 \\ \end{bmatrix} \begin{pmatrix} U_2 & U_2 \\ U_2 & U_2 \\ \end{bmatrix}$$

When does this break?



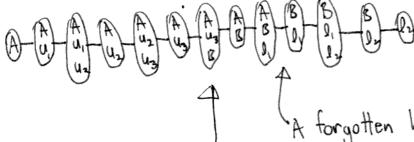
distances computed

A, u, = 1

A, u<sub>2</sub> = 2

A, B = 4

$$\times$$



'A forgotten here, we never check  $A \sim l_1 \sim B = \text{length } 3 \text{ path.}$ 

## If it's broke, fix it

## Lessons:

- . research is hard and involves a lot of trial and evvor
- · when something doesn't work, try fixing by checking your assumptions!
  - did I assume something I didn't realize?
  - can we introduce an assumption that makes things work?