

Software language engineering with ART

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Chapter 0

The Royal Holloway course

This chapter is for students studying Software Language Engineering at Royal Holloway where we approach the material in a particular order designed to allow students to complete their projects within the footprint of a one semester course.

Holloway students start with internal syntax and reduction semantics and only then learn about external syntax parsers and the use of GIFT operators to generate terms in their chosen internal syntax, before moving on to attribute-action systems. After studying that core material we look at topics in lexicalisation and ambiguity management.

Experienced readers will note that this is a ‘semantics-first’ approach: we encourage students to first enumerate the features of their language as a set of signatures, then write reduction rules to interpret those signatures, and only then to consider the external appearance of phrases in their language. We justify and expand on this general approach in Chapter 6.

For readers who are not following the Holloway course:

if you are using ART just as a parser, or have a particular interest in one or other approach to semantics you may want to take a different route and should probably skip straight to Chapter 1.

0.1 Aims and motivation

Welcome to the Software Language Engineering course. You have been engineering *with* software languages for at least two years now. This course, though, is about the engineering *of* software languages: you will learn how to build languages using concise notations from which the implementation could be automatically generated.

All forms of engineering are a mixture of creative insight and disciplined implementation. For instance, the architect of a bridge will try to design an aesthetically pleasing structure that meets the requirements, but ultimately they will rely on detailed structural engineering calculations on that structure to test whether it will withstand daily use. Ideally, this would be true for software too: our creativity would be expressed only through sound and principled techniques; that is techniques that have been found to be safe and efficient using mathematical and other forms of analysis.

In practice we mostly write software in a hopeful way, and then use testing to try and fill the gaps in our understanding. Unfortunately, programming languages are inherently difficult to test since they are designed to be flexible notations with very many combinations of interacting features.

We aim to tame this complexity by using *high level abstractions* that allow us to see the specification of a complete language in a few pages. We can then use this specification to guide either a hand crafted, efficient implementation, or automatically generate interpreters for the language which will probably be less efficient, but may be adequate for many applications.

The overall goal is to make language processors that can be comfortably maintained and extended by the engineers that take forward our work after we have moved on to other projects. To do that, we need to provide concise, self documenting descriptions of the syntax and semantics of our languages that everybody can understand and work with.

0.2 Learning outcomes

After working through these notes, you will

1. know how to use *Context Free Grammar* rules to define programming language syntax;
2. be able to use grammar idioms and the *GIFT annotations* to create *derivation trees* with useful properties;
3. understand how to write *reduction semantics* rules that the rewriter uses to interpret programs;
4. be able to write *attribute-action rules* that may provide more efficient implementations;

5. understand the types and operations of a *Value system*, and how to use a *plugin* to connect to Java classes; and
6. be able to recognise ambiguity in language specifications and progressively eliminate it using *choosers*.

0.3 Assessment

Your command of these learning outcomes will be assessed *via* a substantial personal project and an invigilated examination.

The focus of this course is on the constructs of general purpose programming languages, but to motivate the project work we offer three project variants to construct a *Domain Specific Language* for

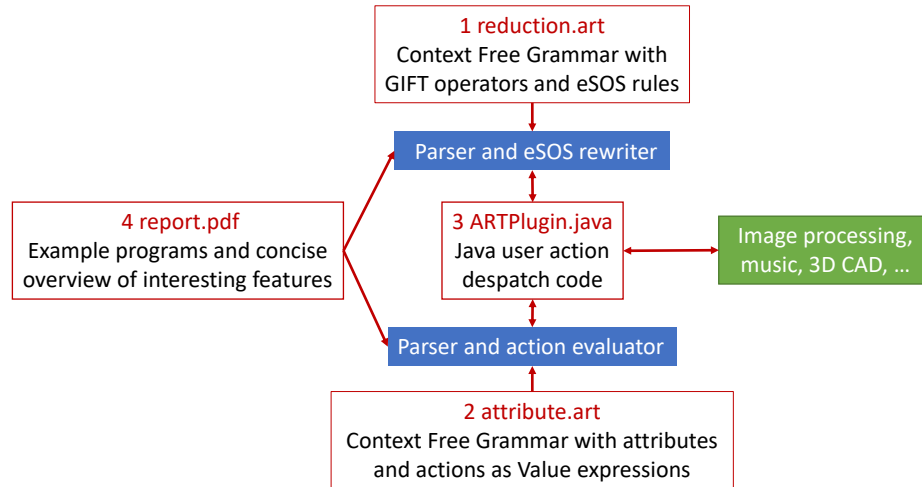
1. music generation *via* the Java MIDI interface;
2. image processing using the two-dimensional (2D) features of Java FX; and
3. Computer Aided Design for 3D printing using an extended form of the three-dimensional (3D) features of Java FX.

You must commit to one of these topics by the end of the week 2 lab. To help you decide, please read the background material on each of these in Appendices [A](#), [B](#) and [C](#).

The project work is to be submitted at the end of the course, and requires the following four deliverables.

1. **reduction.art** - a reduction semantics interpreter specified by eSOS rules and a context free grammar annotated with GIFT operators.
2. **attribute.art** - an attribute-action interpreter specified by a context free grammar annotated with attributes and actions written as Value expressions.
3. **ARTPlugin.java** - a plugin which connects your interpreters to your chosen domain specific actions
4. **report.pdf** - a concise report highlighting interesting and novel features, along with example programs that work with both the reduction and attribute interpreters.

Here is a diagram showing how these deliverables interact with the ART system:



The blue boxes above represent language interpretation mechanisms that are built into the ART tool; their behaviour is specified by the rules that you write in `reduction.art` and `attribute.art`. The green box represents arbitrary Java code that you can connect to *via* a despatch routine in `ARTPlugin.java`. You demonstrate the utility of your language using example programs listed in `report.pdf`

After each weekly lab session, you will submit a snapshot of your work. These snapshots will not be assessed, but will be automatically analysed so that your progress can be tracked. If you are falling behind then you *must* ask for help.

0.4 Protocol for asking questions

When asking for help, I need to be able to reproduce your issue on my machine. Please send a single email, the body of which should contain a concise explanation of your concern, with these attachments `artLog.txt`, `reduction.art`, `attribute.art` and `ARTPlugin.java`. Do not send screenshots; only text file attachments of these standard files are acceptable.

0.5 Teaching week by week

So as to help you prepare your project submission in a timely manner, we approach the learning outcomes in this order.

Week	Chapter	Lecture topic	Laboratory session
1	1	Two interpreters for GCD	Alero 3D design
2	3	Terms and pattern matching	termTool
3	4	eSOS	eSOS for expressions
4	3	The ART Value system	eSOS for control flow
5	2	Context Free Grammars	OSBRD parsing

6	2	GIFT operators	Generation of eSOS terms
7	5	Attribute-action interpreters	mini expression languages
8	5	Delayed attributes	mini control flow languages
9	2	Paraterminals and lexicalisation	mini with custom token patterns
10	2	Ambiguity management	lexical and phrase level choice

Chapter 1

First examples

How do programming language standards documents specify languages?

Here is an extract from the Pascal report

9.2.2.1. If statements.

The if statement specifies that the statement following the symbol then be executed only if the Boolean expression yields true.

IfStatement = “if” BooleanExpression “then” Statement

Here is an extract from one of the *Java Language Specification* documents:

14.9. The if Statement

The if statement allows conditional execution of a statement.

IfThenStatement:

if (Expression) Statement

The Expression must have type boolean or Boolean, or a compile-time error occurs.

14.9.1. The if-then Statement

An if-then statement is executed by first evaluating the Expression.

If evaluation of the Expression completes abruptly for some reason, the if-then statement completes abruptly for the same reason.

Otherwise, execution continues by making a choice based on the resulting value:

- ◇ If the value is true, then the contained Statement is executed; the if-then statement completes normally if and only if execution of the Statement completes normally.
- ◇ If the value is false, no further action is taken and the if-then statement completes normally.

And here is a corresponding extract from one of the draft ANSI-C standards:

6.8.4 Selection statements

Syntax

selection-statement:

if (expression) statement

Semantics

A selection statement selects among a set of statements depending on the value of a controlling expression.

A selection statement is a block whose scope is a strict subset of the scope of its enclosing block. Each associated substatement is also a block whose scope is a strict subset of the scope of the selection statement.

6.8.4.1 The if statement

Constraints

The controlling expression of an if statement shall have scalar type.

Semantics

The substatement is executed if the expression compares unequal to 0.

All three extracts describe the same language feature: the simple conditional statement. If we write in C or Java the program fragment

```
z = 0; if (x == y) z = 3;
```

then we expect that after execution the variable **z** will hold the value 3 only if the variables **x** and **y** hold the same value. We get the same effect in Pascal by writing

```
z := 0; if x = y then z := 3;
```

From these examples we can deduce the following:

- ◊ All three languages have conditional statements that ‘do the same thing’ in some sense;
- ◊ the textual form of the program fragments for Java and C are the same, but the Pascal fragment has a different form, even though the meanings are the same.

In programming languages, the meaning of a fragment is best thought of as its effect on the *state* of the computer, where the state is the set of values maintained by a program, which could simply be the contents of the computer’s memory along with any changes to the computer’s input and output devices.

We call the written form of a programming language fragment its *syntax*.

syntax

We call the meaning of a fragment its *semantics* (that is the effect on the state of the computer).

semantics

1.1 Specification styles for semantics

The extracts above from Pascal, C and Java language standards are all trying to explain the syntax and semantics of a conditional statement. In each case the semantics is described in careful English prose (what we might call ‘legalistic’ English) but with differing levels of detail. Nearly all programming language standards adopt this approach, but that is not ideal because it is hard to check that a prose specification is complete (that is, there aren’t any special cases that have been left undefined) and consistent (that is, that there aren’t any conflicting statements). It is even harder to check that a programming language processor, such as the Java compiler, correctly implements all aspects of the standard. Since so much of modern life is mediated by software written in programming languages, this vagueness in the underlying specification of languages and their implementations is worrying.

In an ideal world, we would have a commonly understood concise notation for describing the semantics of a language fragment with which we could construct arguments for the completeness and consistency of a programming language standard, and which we could use to check the correctness of compilers, interpreters and other language processors perhaps using a computer itself to do the checking. A semantics described this way would be called a *formal semantics*.

formal semantics

In fact such notations do exist, but they have not been widely adopted by programming language designers, for perhaps two reasons: firstly they are conventionally presented in a mathematical style that deters many software practitioners; and secondly complete language descriptions are very dense and can be quite long. Now, the second reason is not a very good one, because legalistic English prose descriptions of semantics are also very dense and long: the Java Language Specification for Java 22 runs to 876 pages.

The ART tool that we are using here to study software language engineering contains an interpreter for one style of formal semantics called *Structural Operational Semantics* (SOS).

Structural Operational Semantics

Our particular version is called *eSOS* because it allows certain parts of a specification to be elided away, which saves writing. eSOS is designed to appeal to those with a background in procedural languages: in Chapter 4 we give programs that show how eSOS rules are interpreted so that software engineers can reason about the way in which their specifications will be processed.

eSOS

Now, some aspects of our presentation would induce a sharp intake of breath from those who prefer a more declarative and mathematically rigorous approach to semantics, but we hope that eSOS will de-mystify SOS for programmers who

are wary of mathematical treatments, and perhaps encourage the use of SOS as a design and prototyping medium for domain specific languages where sometimes the only available language definition is the code of an implementation.

semi-formal semantics

Our kind of SOS is perhaps best thought of as a *semi-formal semantics*

attribute-action

ART also supports *attribute-action* systems: a style of semantics that is common in traditional parser generators such as the Bison tool which is distributed with most Unix systems; Chapter 5 describes the approach in detail. These kinds of specifications can usually be executed more efficiently than an eSOS interpretation, but in our experience attribute-action systems are more likely to be incomplete or inconsistent (i.e. buggy) than an eSOS specification. In Chapter 6 we discuss our preferred approach, which is to prototype in eSOS and then, if necessary for performance reasons, to transform to an equivalent but more efficient attribute-action.

1.2 Specification styles for syntax

Although formal semantics has not achieved much traction with language designers, there is almost complete agreement that syntax should be specified using a *Context Free Grammar* (CFG), and that is evident in the extracts above; they all give a context free grammar rule for the syntax, although the notation used for the rule varies slightly.

For Pascal we have

IfStatement = “if” BooleanExpression “then” Statement

The doubly-quoted symbols are Pascal keywords. The other symbols are placeholders for language fragments. For instance, a `BooleanExpression` could simply be the constant `true` or an expression like `x = y`.

Clearly the placeholders could represent arbitrarily long pieces of program but when focussing on the syntax and semantics of the conditional statement, we don’t want to have to specify their exact form. This is an example of *abstraction*, that is the hiding of unnecessary detail so that we can focus on the matter in hand.

abstraction

The purpose of a CFG rule, then, is to give a template for one feature of the language: the rule tells us that a conditional statement starts with the keyword `if` which must be followed by an expression over the booleans, then the keyword `then` followed by an arbitrary statement. Somewhere else in the grammar we expect to see definitions for the placeholders `BooleanExpression` and `Statement`. A complete set of such rules with no missing definitions is called a Context Free Grammar. ART contains tools for processing and visualising grammars in various ways that we shall discuss in Chapter 2.

1.3 A running example: the MiniGCD language

We shall use as a running example a tiny language which illustrates the core procedural concepts of variables, assignment, arithmetic and control flow in the form of conditionals and loops.

The inspiration for our language is Euclid's integer Greatest Common Divisor algorithm, described in the second proposition of *Elements VII* some 2,300 years ago. It is worth looking up the original description which is written in quite verbose prose. Here is a version written in Java.

```
1 public class GCD {  
2     public static void main(String[] args) {  
3         int a = 6;  
4         int b = 9;  
5  
6         while (a != b) {  
7             if (a > b)  
8                 a = a - b;  
9             else  
10                b = b - a;  
11        }  
12        int gcd = a;  
13    }  
14 }
```

Java programs need quite a lot of setting up and anyway this is a course on language design, so let us construct our own, more compact programming notation to express the same program.

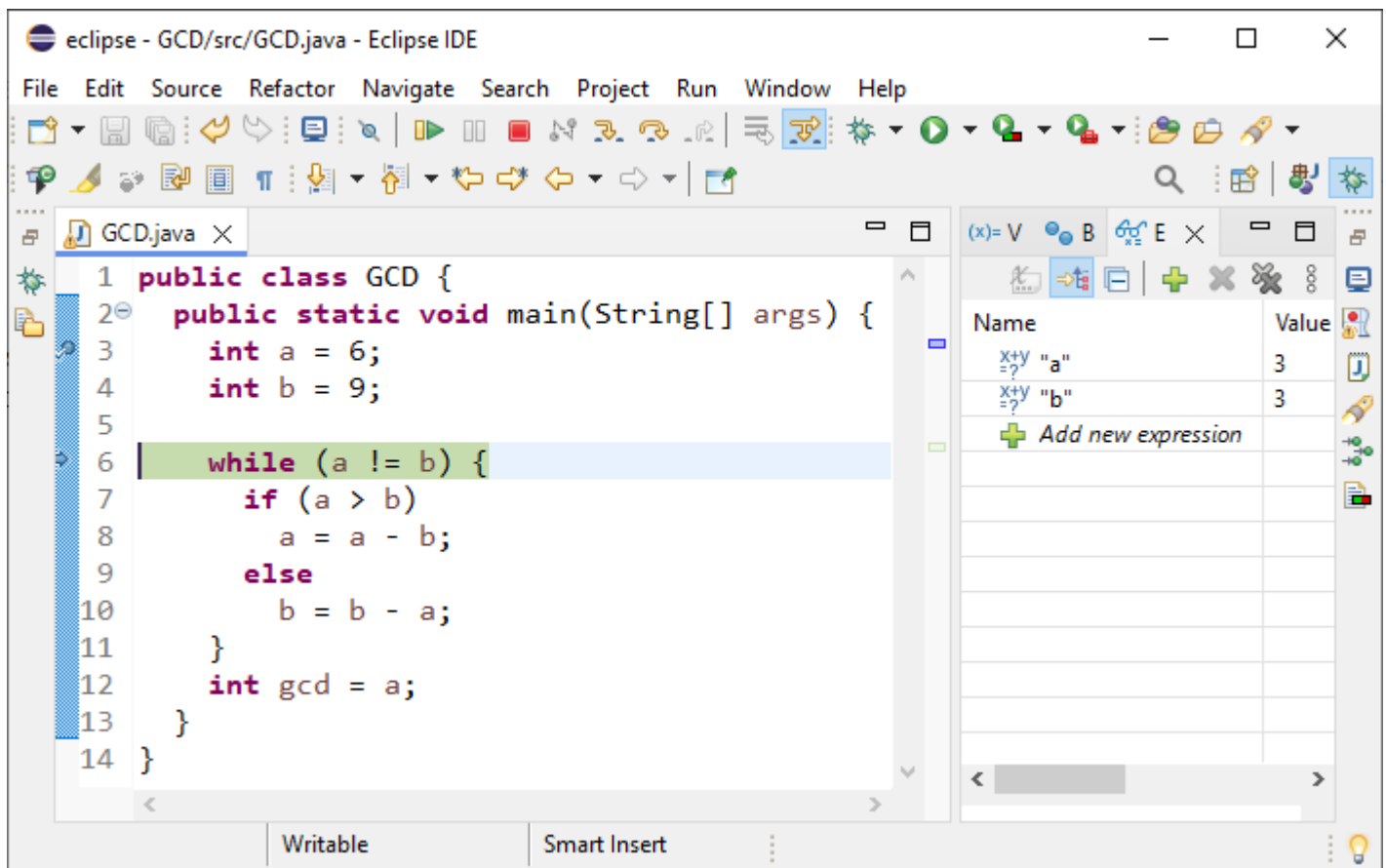
```
1 a := 6;  
2 b := 9;  
3  
4 while a != b {  
5     if a > b  
6         a := a - b;  
7     else  
8         b := b - a;  
9 }  
10 gcd := a;
```

We shall call this notation the MiniGCD language. Note that assignment to a variable is denoted by $:=$, not by $=$. As in C and Java, statements are terminated with (not separated by) a semi-colon and can be grouped within braces. Variable names are not pre-declared. MiniGCD only contains the features used here: it does not even provide addition (though we will extend it later).

1.4 The fixed-code-and-program-counter interpretation

In almost all modern computing devices most programs are lists of instructions that reside in the memory or *store*. The instructions for a particular program do not change as it is being executed. A special register called the *Program Counter* (PC) which points to the next piece of code to be executed, and is usually simply incremented as each instruction is executed which induces sequential execution of the instructions. At a branch point we may test a condition and update the PC with a new values depending on that outcome; that causes the processor to start execution at some new location.

The sequence of values displayed by the program counter during a program's execution records the *control flow* for this particular input. The easiest way to visualise the control flow for a program is to load it into a development environment such as Eclipse and then run it under the controller of the debugger, which can execute it one line at a time. Here is a screen shot from Eclipse showing our Java GCD which is currently at line 6 on the final iteration.



We can see the program's Java code on the left and the state of the store with variables `a` and `b`, both presently mapped to the value 3. The program counter value is represented by the small arrow in the margin at line 6.

1.5 The problem with assignment

The *substitution model* for variables that is used when thinking mathematically is much simpler to reason about than the *assignment model* for variables used in procedural programming languages. In mathematics, if I say $x = 3$ then, whilst that version of x remains in scope, I mean that x and 3 are synonyms and so anywhere that x appears subsequently in that scope I could cross it out and write 3. In procedural programming languages like Java, if I write $x = 3$ I may subsequently write $x = 4$ in the same scope region, and so the relationship between x and its value depends on the most recent assignment to x according to the history execution history for a particular input. Hence assignment in languages like Java is fundamentally different to mathematical equality (and that is why programming languages use different symbols to denote assignment and equality).

substitution model

assignment model

A physical store is a fixed set of cells, each with a fixed address but containing a value which may be changed. A useful mathematical model of a store is as a set of *bindings* where each binding associates an identifier with a value.

bindings

****mutable map vs making a new map**

Evaluating a *declaration* in the program term has the effect of creating a new store S' from S which has all of the bindings in S and the new binding required by the declaration. Assigning a new value to a variable has the effect of changing the mapping of one variable in the store, and using a variable in an expression requires us to look up the value mapped to the variable's identifier.

1.6 The problem with the program counter

Our hardware works with (mostly) static code and a program counter but that does not mean that a formal model of program execution must take the same view. Just as aviation pioneers had to learn that wing-flapping was not a useful way to get humans airborne (propellers, jet engines and aerofoils being a better engineering proposition) the pioneers of formal approaches to programming language semantics had to find a way of dispensing with both assignment and the program counter. Why is this?

The substitution model is simple and easy to reason about but the assignment model has the great advantage of being efficient in that identifiers may be re-used within a scope rather than having to have fixed content throughout the runtime of a program and that saves both memory and allocation time. The use of assignment to variables presents a challenge to formal analyses of program semantics though it is manageable as we shall see. However it is *particularly* problematic that the program counter itself works by assignment because that obscures the control flow within a program, and that makes it difficult to decide whether two programs states are the same.

1.7 The reduction interpretation

There is an alternative way of thinking about program execution that does not require the use of a program counter. The trick is to think of the program code itself as something that can be progressively rewritten until all that we have left is a result, coupled to a set of bindings that record changes to variables.

Consider this program

```

1 x := 3;
2 y := 10+2+4;
```

The first thing the program does is assign **3** to variable **x**, that is create the store binding $x \mapsto 3$.

Now, there is a sense in which the program fragment **x := 3; y := 10+2+4;** coupled to the empty store $\{\}$ is equivalent to the program fragment **y := 10+2+4;** with the store $\{x \mapsto 3\}$ because they both lead to the same final result. We could start with either and get the same result.

It is helpful to think of the store as representing the computer's state, and the program fragment as representing 'that which is left to do', so we can represent the execution of a program as a sequence of pairs comprising a program that represents only what remains to be done and a store:

1. **x := 3; y := 10+2+4;**, $\{\}$
2. **y := 10+2+4;**, $\{x \mapsto 3\}$

Next we need to evaluate expression **10+2+4** before we can assign the result to **y**. In detail, the computer can only execute one arithmetic operator at a time so we must pick a sub-expression to evaluate first; let us choose to execute **10+2** and rewrite it to the result **12**.

3. **y := 12+4;**, $\{x \mapsto 3\}$

Now we do the other arithmetic operation: **12+4** is rewritten to **16**.

4. **y := 16;**, $\{x \mapsto 3\}$

Finally we can assign to **y** and set the program fragment to **__done** which is a special value indicating that there is no more computation required.

5. **__done**, $\{x \mapsto 3, y \mapsto 16\}$

Execution is now complete. Note that we could start in any of the five states above and end up with the same output.

reduction trace

reduction step

We call this kind of display of machine states the *reduction trace* for our program, and each line represents a *reduction step*—so called because usually the program fragment reduces in size at each step (though not always, as we shall

see in the next section). The steps match up rather well with the individual machine level instructions that would be executed by a real computer, and at every point we have a complete record of the state of the machine as well as being able to see what else we have to do.

1.8 The problem with loops

A reduction semantics for linear code and conditional code is straightforward, but we need to think carefully about loops. The approach we use here is to make use of a *program identity*, that is a program transformation that does not change the semantics of a program term, but does change the syntax, and thus the reduction trace. If we have a loop of the form

while booleanExpression **do** statement;

then we can *always* transform it into

if booleanExpression { statement; **while** booleanExpression **do** statement; }

We have effectively unpacked the first iteration of the loop and are handling it directly with an **if** statement followed by a new copy of the **while** loop which will compute any further iterations. When we have completed all of the iterations we shall encounter a term like

if false { statement; **while** booleanExpression **do** statement; }

which can then be rewritten away. This device, then, allows us to treat **while** loops using only **if** statements.

1.9 A reduction evaluation of GCD in MiniGCD

Figure 1.1 on page 11 presents the reduction semantics trace for the GCD algorithm written in MiniGCD program shown on page 5.

There are a large number of steps in this trace, which make for intimidating reading, but bear in mind that a step (very roughly) corresponds to a machine operation such as fetching an operand or adding two numbers. Useful programs entail the execution of a *lot* of operations: some of the programs we run on modern processors take an appreciable amount of time to execute even though a 4GHz processor will, in just two seconds, execute one instruction for every person on the planet—a number well beyond our abilities to directly comprehend. This is just a roundabout way of saying that machine operations are fine grained, and we need an awful lot of them to do useful work. Any attempt to list all of the steps that are gone through by a non-trivial running program is going to generate a long list.

We shall use a slightly more compact form to display the steps. First, we write the entire program term on a single line: rather than the nicely laid out version shown on page 5, we say

```
a=6; b=9; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a;
```

As before, our starting point is the whole program term coupled to an empty store:

```
a=6; b=9; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {}
```

Each step of our trace involves identifying a part of the program term that we shall execute next, and then rewriting the program term to represent what is left to do of the original term. We call the subterm that is to be replaced a *reducible expression* or *redex* for short. In the trace below, we have highlighted the chosen redex in red at each stage. Sometimes there is a choice of redexes available: for instance when processing the GCD program initialisations of **a** and **b**, it does not matter which order we process them in. We have chosen to do **a** first.

redex

When reading the reduction trace below, the bold headings should simply be treated as comments: they are there to break up the reductions into related blocks as an aid to comprehension and have no part in the formal description of program execution. At each step look for the highlighted redex: the following step should contain a term which has all of the blue parts from its predecessor, and a replacement for the redex. The black part of each reduction step will record any changes arising from side effects of the reduction, which for this program are limited to creating or updating bindings but in general might also include changes to the input and output, the raising of exceptions, and other so-called *semantic entities*.

semantic entities

The execution terminates when we get to a term for which no further reductions are available, that is, a term that contains no redexes. We call such terms *normal forms*. In this case, the final term is empty, which naturally has no redexes.

normal forms

Upon termination, the variable **gcd** is bound to **3** which is indeed the greatest common divisor of 6 and 9.

1.10 Executable semantics and automation

Manually constructing the execution trace shown in Figure 1.1 would be time consuming, although it does have the benefit of showing very clearly and concisely what each step of the computation does (as opposed to the legalise English commentaries that we showed at the start of this chapter).

The whole point of this way of thinking about programming languages is allow *automation*. We need descriptions of programming languages that facilitate the mechanical construction of language processors. Ideally, we should like to be able to specify both the syntax and the semantics of a language like GCD in a few pages, and then have the computer run GCD programs for us so that we can test the specification and satisfy ourselves that it works the way we want it to. We call this prototyping style of language execution an *Executable*

Start of trace

```

a=6; b=9; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {}
b=9; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6}
Rewrite using while p s → if p { s ; while p s }
while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
Evaluate a ≠ b with store {a ↦ 6, b ↦ 9}
if a!=b { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 6, b ↦ 9}
if 6!=b { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 6, b ↦ 9}
if 6!=9 { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 6, b ↦ 9}
if true { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 6, b ↦ 9}
Evaluate a > b with store {a ↦ 6, b ↦ 9}
if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
if 6>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
if 6>9 a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
if false a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
Evaluate b - a with store {a ↦ 6, b ↦ 9}
b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
b:=b-6; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
b:=9-6; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
b:=3; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 9}
Rewrite using while p s → if p { s ; while p s }
while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
Evaluate a ≠ b with store {a ↦ 6, b ↦ 3}
if a!=b { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 6, b ↦ 3}
if 6!=b { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 6, b ↦ 3}
if 6!=3 { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 6, b ↦ 3}
if true { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 6, b ↦ 3}
Evaluate a > b with store {a ↦ 6, b ↦ 3}
if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
if 6>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
if 6>3 a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
if true a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
Evaluate a - b with store {a ↦ 6, b ↦ 3}
a:=a-b; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
a:=a-3; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
a:=6-3; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
a:=3; while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 6, b ↦ 3}
Rewrite using while p s → if p { s ; while p s }
while a!=b if a>b a:=a-b; else b:=b-a; gcd=a; {a ↦ 3, b ↦ 3}
Evaluate a ≠ b with store {a ↦ 3, b ↦ 3}
if a!=b { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 3, b ↦ 3}
if 3!=b { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 3, b ↦ 3}
if 3!=3 { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 3, b ↦ 3}
if false { if a>b a:=a-b; else b:=b-a; while a!=b if a>b a:=a-b; else b:=b-a; } gcd=a; {a ↦ 3, b ↦ 3}
Assign result
gcd=a; {a ↦ 3, b ↦ 3}
, {a ↦ 3, b ↦ 3 gcd ↦ 3}

```

Figure 1.1 Reduction trace for the GCD algorithm with inputs 6,9


```

seq ::= statement^^ | statement seq
statement ::= assign^^ | while^^ | if^^ | '{'^ seq '}'^
assign ::= &ID ':='^ expression ';'^
while ::= 'while'^ expression 'do'^ statement
if ::=
    'if'^ expression 'then'^ statement
  | 'if'^ expression 'then'^ statement 'else'^ statement
expression ::= rels^^
rels ::= adds^^ | gt^^ | ne^^
    gt ::= adds '>'^ adds
    ne ::= adds '!='^ adds
adds ::= operand^^ | sub^^ | add^^
    add ::= adds '+'^ operand
    sub ::= adds '-'^ operand
operand ::= __int32^^ | deref^^
__int32 ::= &INTEGER
deref ::= &ID

--- seq(_C1->__done, _C2) -> _C2
--- if(_E->True, _C1,_C2) -> _C1
--- if(_E->False,_C1,_C2) -> _C2
--- while(_E, _C) -> if(_E, seq(_C, while(_E,_C)), __done)
--- assign(_X, _E->n:__int32) -> __done, __put(_sig, _X, _n)
--- deref(_R) -> __get(_sig, _R), _sig
--- gt (_E1->n1:__int32, _E2->n2:__int32) -> __gt (_n1, _n2)
--- ne (_E1->n1:__int32, _E2->n2:__int32) -> __ne (_n1, _n2)
--- sub(_E1->n1:__int32, _E2->n2:__int32) -> __sub(_n1, _n2)

!try "a := 6; b := 9; while a != b do if a > b then a := a - b; else b := b - a;"

```

Figure 1.2 An eSOS specification for MiniGCD

Executable semantics

semantics to distinguish it from an efficient production-quality compiler.

In this testing phase, we would be prepared to accept quite poor performance because our test programs would be small. If we were building a general purpose language we would probably need to then move on to a more efficient style of implementation, though still guided by the specification which would be the ultimate arbiter of correctness. However, it turns out that on modern hardware, for many applications needing a small language, an executable semantics might be fast enough on its own. We shall revisit this topic in Chapter 6.

** ART

```

!global variables:__map

statements ::= statement | statement statements

statement ::=
  ID '=' subExpr ';'  statement.v = __put(variables, ID1.v, subExpr1.v)
| 'if' relExpr statement 'else' statement
  statement.v = relExpr.v ? statement1.v !! statement2.v
| 'while' relExpr statement  statement.v = relExpr.v @ statement.v !! __done

relExpr ::=
  subExpr                relExpr.v = subExpr1.v
| relExpr '>' subExpr      relExpr.v = __gt(relExpr.v, subExpr.v)
| relExpr '!=' subExpr    relExpr.v = __ne(relExpr.v, subExpr.v)

subExpr ::=
  operand                subExpr.v = operand.v
| subExpr '-' operand    subExpr.v = __sub(subExpr.v, operand.v)

operand ::=
  ID                    operand.v = __get(variables, ID.v)
| INTEGER               operand.v = INTEGER1.v
| '(' subExpr ')'      operand.v = subExpr1.v

```

Figure 1.3 An attribute-action specification for MiniGCD

1.11 An eSOS specification for MiniGCD

1.12 An attribute-action specification for MiniGCD

1.13 Exercises

Chapter 2

Context Free Grammars

- 2.1 A languages is a set of strings**
- 2.2 A Context Free Grammar generates a language**
- 2.3 A derivation records rule applications**
- 2.4 A parser constructs derivations**
- 2.5 GIFT operators rewrite derivations**
- 2.6 Paraterminals specify the lexer-parser interface**
- 2.7 Choosers reduce ambiguity**

Chapter 3

Term rewriting

3.1 The Value system and plugins

Chapter 4

Reduction semantics with eSOS

Chapter 5

Attribute action interpreters

Chapter 6

Advice on language design

Appendix A

Music making with Java MIDI

Appendix B

Image processing operations

Appendix C

3D modelling

Appendix D

ART reference documentation

D.1 Relation symbols

```
-ss    --- x -> y
-ssKleene    --- x ->* y
-ssRepeated  --- x ->> y
-bs    --- x => y
-bsKleene    --- x =>* y
-bsRepeated  --- x =>> y
-user1    --- x -\ y
-user1Kleene    --- x -\* y
-user1Repeated  --- x -\> y
-user2    --- x -/ y
-user2Kleene    --- x -/* y
-user2Repeated  --- x -/> y
-anywhereRewrite    --- x ~> y
-anywhereRewriteKleene    --- x ~>* y
-anywhereRewriteRepeated  --- x ~>> y
```

D.2 Lexical builtins

&CHAR_BQ	`C
&ID	AlphanumericIdentifier
&INTEGER	123
&REAL	12.3
&STRING_BRACE	{ A string delimited by braces }
&STRING_BRACE_NEST	{ A string { with nested instances } delimited by braces }
&STRING_DOLLAR	\$ A string delimited by dollar signs \$
&STRING_DQ	" A string delimited by double quotes "
&STRING_PLAIN_SQ	' A string delimited by single quotes with no escapes '
&STRING_SQ	' A string delimited by single quotes '

These builtins can only appear as an argument to the whitespace directive

```
&SIMPLE_WHITESPACE
&COMMENT_BLOCK_C      /* a C style block comment */
&COMMENT_LINE_C // a C style line comment
&COMMENT_NEST_ART (* An ART style comment (* which nests *) *)
```


Glossary

- abstraction the hiding of unnecessary detail, page 4
- assignment model , page 7
- attribute-action , page 4
- bindings , page 7
- control flow , page 6
- eSOS , page 3
- formal semantics , page 3
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- semantics the meaning of a language, page 3
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- state the set of values maintained by a program, page 2
- store , page 6
- Structural Operational Semantics , page 3
- substitution model , page 7
- syntax the written form of a language, page 3