

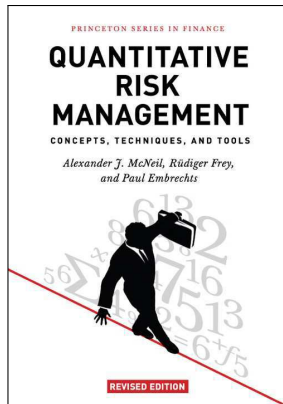
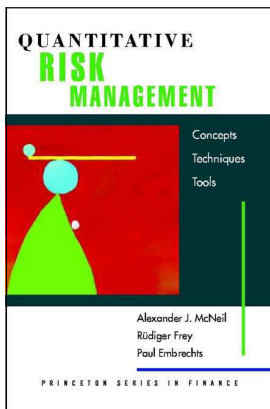
# Quantitative Risk Management

<http://www.qrmtutorial.org>

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# Course information

- Website: <http://www.qrmtutorial.org>
- Book: A. J. McNeil, R. Frey, P. Embrechts  
*Quantitative Risk Management* (1st edition: 2005; revised edition: 2015)



# Overview

- 1 Risk in perspective**
- 2 Basics concepts in risk management**
- 3 Empirical properties of financial data**
- 4 Financial time series**
- 5 Extreme value theory**
- 6 Multivariate models**
- 7 Copulas and dependence**
- A Appendix**

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