

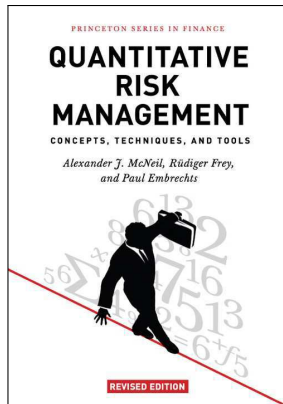
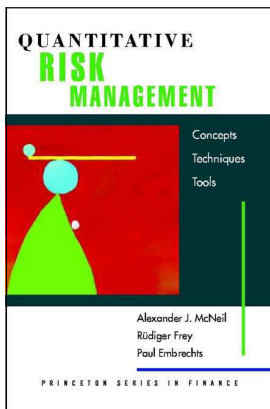
Quantitative Risk Management

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Last update: 2017-04-10

Course information

- Website: <http://www.qrmtutorial.org>
- Book: A. J. McNeil, R. Frey, P. Embrechts
Quantitative Risk Management (1st edition: 2005; revised edition: 2015)



Overview

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