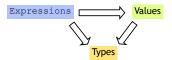
CSE 130 Programming Languages

Datatypes



Review so far



Many kinds of expressions:

- 1. Simple
- 2. Variables
- 3. Functions

Review so far

- We've seen some base types and values:
 - Integers, Floats, Bool, String etc.
- Some ways to build up types:
 - Products (tuples), records, "lists"
 - Functions
- Design Principle: Orthogonality
 - Don't clutter core language with stuff
 - Few, powerful orthogonal building techniques
 - Put "derived" types, values, functions in libraries

Next: Building datatypes

Three key ways to build complex types/values

1. "Each-of" types

Value of T contains value of T1 and a value of T2

2. "One-of" types

Value of T contains value of T1 or a value of T2

3. "Recursive"

Value of T contains (sub)-value of same type T

Next: Building datatypes

Three key ways to build complex types/values

1. "Each-of" types (T1 * T2)

Value of T contains value of T1 and a value of T2

2. "One-of" types

Value of T contains value of T1 or a value of T2

3. "Recursive"

Value of T contains (sub)-value of same type T

Suppose I wanted ...

- ... a program that processed lists of attributes
- Name (string)
- Age (integer)
- ...

Suppose I wanted ...

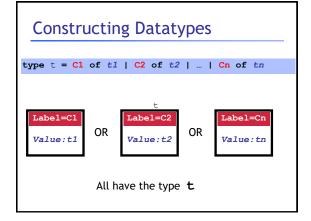
- ... a program that processed lists of attributes
- · Name (string)
- Age (integer)
- DOB (int-int-int)
- Address (string)
- Height (float)
- Alive (boolean)
- Phone (int-int)
- email (string)

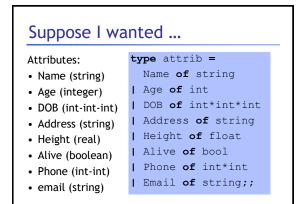
Many kinds of attributes (too many to put in a record)

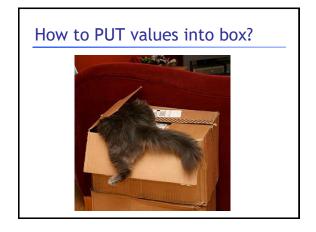
• can have multiple names, addresses, phones, emails etc.

Want to store them in a list. Can I?

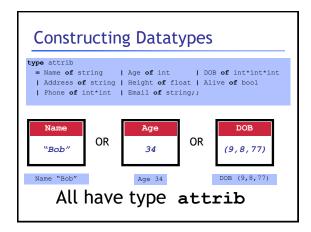
type t = C1 of t1 | C2 of t2 | ... | Cn of tn t is a new datatype. A value of type t is either: a value of type t1 placed in a box labeled C1 Or a value of type t2 placed in a box labeled C2 Or ... Or a value of type tn placed in a box labeled Cn

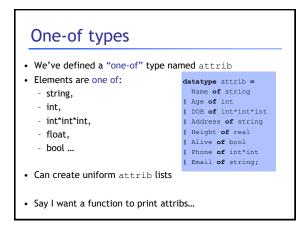






```
How to PUT values into box?
 How to create values of type attrib?
# let a1 = Name "Bob";;
val x : attrib = Name "Bob"
# let a2 = Height 5.83;
val a2 : attrib = Height 5.83
                                                  type attrib =
                                                    Name of string
                                                  | Age of int
# let year = 1977 ;;
val year : int = 1977
                                                 | DOB of int*int*int
# let a3 = DOB (9,8,year) ;;
                                                 | Address of string
val a3 : attrib = DOB (9,8,1977)
# let a_l = [a1;a2;a3];;
val a3 : attrib list = ...
                                                 | Height of float
                                                  | Alive of bool
                                                  | Phone of int*int
                                                  | Email of string;;
```









```
How to tell whats in the box?

| match e with | Name s | -> printf "%s" s | Age i | -> printf "%d" i | DOB (d, m, y) | -> printf "%d" i | Address s | -> printf "%s" s | Height h | -> printf "%s" b | Alive b | -> printf "%b" b s | Phone (a, r) | -> printf "%b" b ar

| Pattern-match expression: check if e is of the form ...

• On match:

• value in box bound to pattern variable

• matching result expression is evaluated

• Simultaneously test and extract contents of box
```

```
How to tell whats in the box?
                        match e with
                         | Name s -> ...(*s: string *)
| Age i -> ...(*i: int *)
| DOB(d,m,y)-> ...(*d: int,m: int,y: int*)
 Name of string
| Age of int
| DOB of int*int*int
                          Address a -> ... (*a: string*)
Height h -> ... (*h: int *)
Alive b -> ... (*b: bool*)
| Address of string
| Height of float
                          Phone (a,r) -> ... (*a: int, r: int*)
| Alive of bool
| Phone of int*int
 Pattern-match expression: check if e is of the form ...
 · On match:
    value in box bound to pattern variable
    matching result expression is evaluated
 · Simultaneously test and extract contents of box
```

How to tell whats in the box

```
# match (Name "Bob") with
     | Name s -> printf "Hello %s\n" s
     | Age i -> printf "%d years old" i
;;
Hello Bob
- : unit = ()
```

None of the cases matched the tag (Name)
Causes nasty *Run-Time Error*



Beware! Handle All TAGS!

```
# match (Name "Bob") with
    | Age i -> Printf.printf "%d" I
    | Email s -> Printf.printf "%s" s
;;
Exception: Match Failure!!
```

None of the cases matched the tag (Name)
Causes nasty *Run-Time Error*

Compiler to the Rescue!

None of the cases matched the tag (Name)

Causes nasty *Run-Time Error*

Compiler To The Rescue!!

Compile-time checks for:

missed cases: ML warns if you miss a case!

Compiler To The Rescue!!

```
# let printAttrib a = match a with
    | Name s -> Printf.printf "%s" s
    | Age i -> Printf.printf "%d" I
    | DOB (d,m,y) -> Printf.printf "%d / %d / %d" d m y
    ...
    | Age i -> Printf.printf "%d" i ;;
Warning U: this match case is unused.
```

Compile-time checks for:

redundant cases: ML warns if a case never matches

Another Few Examples

```
# let printAttrib a = match a with

| Name s -> Printf.printf "%s" s
| Age i -> Printf.printf "%d" I
| DOB (d,m,y) -> Printf.printf "%d / %d / %d" d m y
...

| Age i -> Printf.printf "%d" i ;;
| Warning U: this match case is unused.
```

See code text file

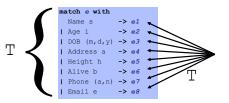
match-with is an Expression

```
match e with
    C1 x1 -> e1
| C2 x2 -> e2
| ...
| Cn xn -> en
```

Type Rule

- e1, e2,...,en must have same type T
- Type of whole expression is ${\mathbb T}$

match-with is an Expression



Type Rule

- e1, e2,..., en must have same type T
- Type of whole expression is T

Benefits of match-with

```
match e with type t =  C1 \times 1 -> e1  C1 of t1 | C2 x2 -> e2 | C2 of t2 | ... | Cn of tn
```

- 1. Simultaneous test-extract-bind
- Compile-time checks for: missed cases: ML warns if you miss a t value redundant cases: ML warns if a case never matches

Next: Building datatypes

Three key ways to build complex types/values

1. "Each-of" types t1 * t2

Value of T contains value of T1 and a value of T2

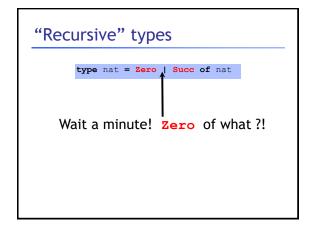
2. "One-of" types type t = C1 of t1 | C2 of t2
Value of T contains value of T1 or a value of T2

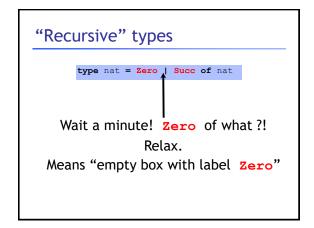
3. "Recursive" type

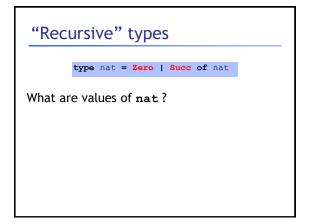
Value of T contains (sub)-value of same type T

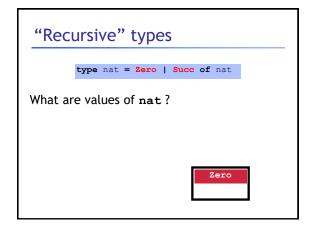
"Recursive" types

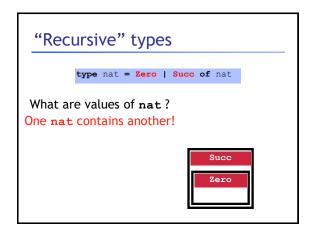
type nat = Zero | Succ of nat

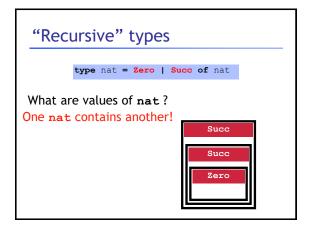


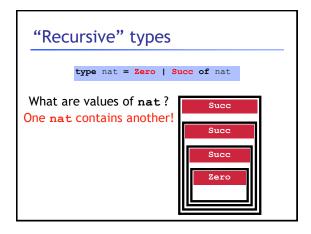


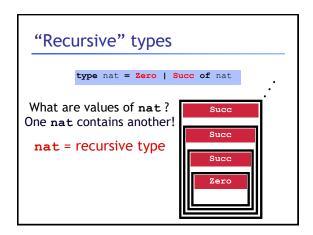












Next: Building datatypes

Three key ways to build complex types/values

1. "Each-of" types t1 * t2

Value of T contains value of T1 and a value of T2

2. "One-of" types type t = C1 of t1 | C2 of t2

Value of T contains value of T1 or a value of T2

3. "Recursive" type type t = ... | C of (...*t)

Value of T contains (sub)-value of same type T

Next: Lets get cosy with Recursion
Recursive Code Mirrors Recursive Data

Next: Lets get cosy with Recursion

Code Structure = Type Structure!!!

to_int : nat -> int

type nat =
| Zero
| Succ of nat

let rec to_int n =

```
to_int : nat -> int

type nat =

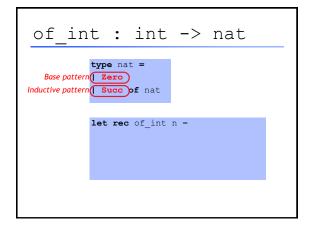
Base pattern Zero
Inductive pattern Succ of nat

let rec to_int n =
```

```
of_int : int -> nat

type nat =
| Zero
| Succ of nat

let rec of_int n =
```

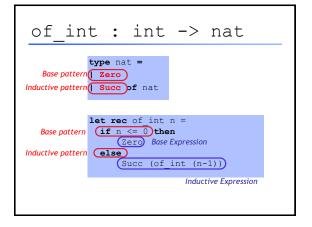


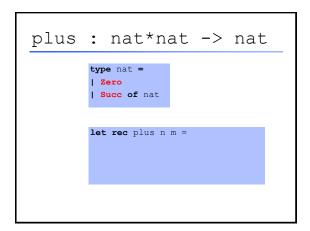
```
of_int : int -> nat

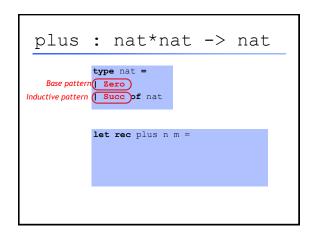
type nat =
Base pattern( Zero)
Inductive pattern( Succ of nat

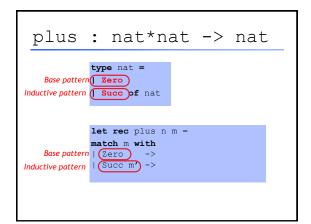
let rec of_int n =
Base pattern( if n <= 0) then

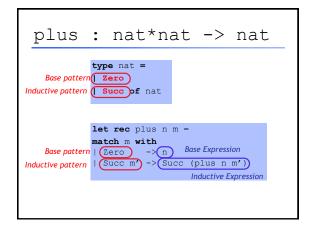
Inductive pattern( else)
```







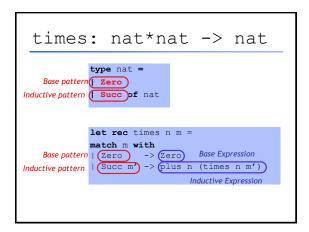




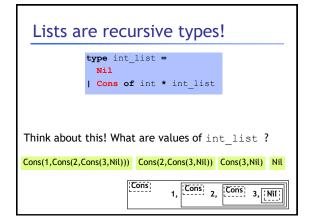
times: nat*nat -> nat

type nat =
Base pattern Zero
Inductive pattern Succ of nat

let rec times n m =



Next: Lets get cosy with Recursion Recursive Code Mirrors Recursive Data



Lists aren't built-in!

datatype int_list = Nil | Cons of int * int_list

Lists are a derived type: built using elegant core!

1. Each-of

2. One-of

3. Recursive

:: is just a pretty way to say "Cons"

[] is just a pretty way to say "Nil"

| Some functions on Lists: Length

| let rec len 1 = | match 1 with | with | lons(h,t) | with | lons(h,t) | with | lons(h,t) | match 1 with | lons(h,t) | lons(h,t

Some functions on Lists: Append

let rec append (11,12) =

- Find the right induction strategy
 - Base case: pattern + expression
 - Induction case: pattern + expression

Well designed datatype gives strategy

Some functions on Lists: Max

let rec max xs =

- Find the right induction strategy
 - Base case: pattern + expression
 - Induction case: pattern + expression

Well designed datatype gives strategy

null, hd, tl are all functions ...

Bad ML style: More than aesthetics!

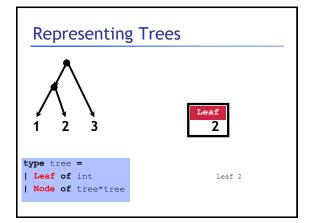
Pattern-matching better than test-extract:

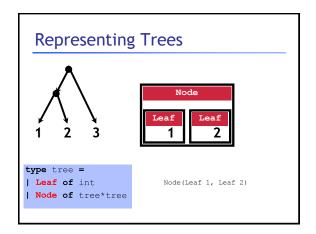
- ML checks all cases covered
- ML checks no redundant cases
- ...at compile-time:
 - fewer errors (crashes) during execution
 - get the bugs out ASAP!

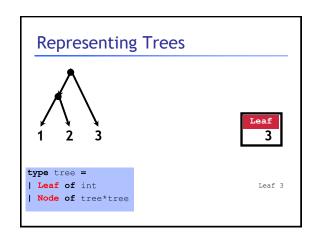
Next: Lets get cosy with Recursion

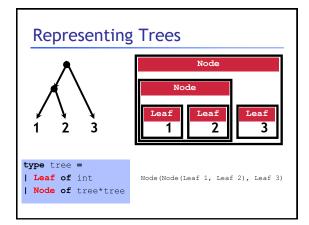
Recursive Code Mirrors Recursive Data

Representing Trees Leaf 1 Leaf of int Node of tree*tree









Next: Lets get cosy with Recursion
Recursive Code Mirrors Recursive Data

```
sum_leaf: tree -> int

"Sum up the leaf values". E.g.

# let t0 = Node(Node(Leaf 1, Leaf 2), Leaf 3);;
-: int = 6
```

```
sum_leaf: tree -> int

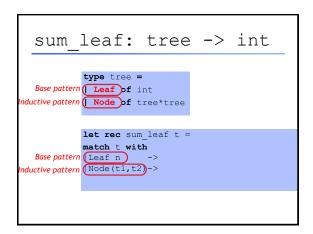
type tree =
    | Leaf of int
    | Node of tree*tree

let rec sum_leaf t =
```

```
sum_leaf: tree -> int

type tree =
Base pattern Leaf of int
Inductive pattern Node of tree*tree

let rec sum_leaf t =
```



sum_leaf: tree -> int

type tree =

Base pattern | Leaf of int
Inductive pattern | Node of tree*tree

let rec sum_leaf t =

Base pattern | Leaf n | -> n Base Expression
Inductive pattern | Node (t1,t2) -> (sum leaf t1 + sum leaf t2)

Inductive Expression

Recursive Code Mirrors Recursive Data

Code almost writes itself!

Another Example: Calculator

Want an arithmetic calculator to evaluate expressions like:

- 4.0 + 2.9
- 3.78 5.92
- (4.0 + 2.9) * (3.78 -5.92)

Another Example: Calculator

Want an arithmetic calculator to evaluate expressions like:

- 4.0 + 2.9 ====> 6.9
- 3.78 5.92 ====> **-2.14**
- (4.0 + 2.9) * (3.78 -5.92) ====> -14.766

Whats a ML TYPE for REPRESENTING expressions?

Another Example: Calculator

Want an arithmetic calculator to evaluate expressions like:

- 4.0 + 2.9 ====> **6.9**
- 3.78 5.92 ====> **-2.14**
- (4.0 + 2.9) * (3.78 -5.92) ====> -14.766

Whats a ML TYPE for REPRESENTING expressions?

```
type expr =
| Num of float
| Add of expr*expr
| Sub of expr*expr
| Mul of expr*expr
```

Another Example: Calculator

Want an arithmetic calculator to evaluate expressions like:

- 4.0 + 2.9 ====> **6.9**
- 3.78 5.92 ====> **-2.14**
- (4.0 + 2.9) * (3.78 -5.92) ====> -14.766

Whats a ML FUNCTION for EVALUATING expressions?

```
type expr =
| Num of float
| Add of expr*expr
| Sub of expr*expr
| Mul of expr*expr
```

Another Example: Calculator

Want an arithmetic calculator to evaluate expressions like:

- 4.0 + 2.9 ====> **6.9**
- 3.78 5.92 ====> **-2.14**
- (4.0 + 2.9) * (3.78 -5.92) ====> -14.766

Whats a ML FUNCTION for EVALUATING expressions?

Another Example: Calculator

Want an arithmetic calculator to evaluate expressions like:

- 4.0 + 2.9 ====> 6.9
- 3.78 5.92 ====> **-2.14**
- (4.0 + 2.9) * (3.78 -5.92) ====> -14.766

Whats a ML FUNCTION for EVALUATING expressions?

