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Paaras Thakur

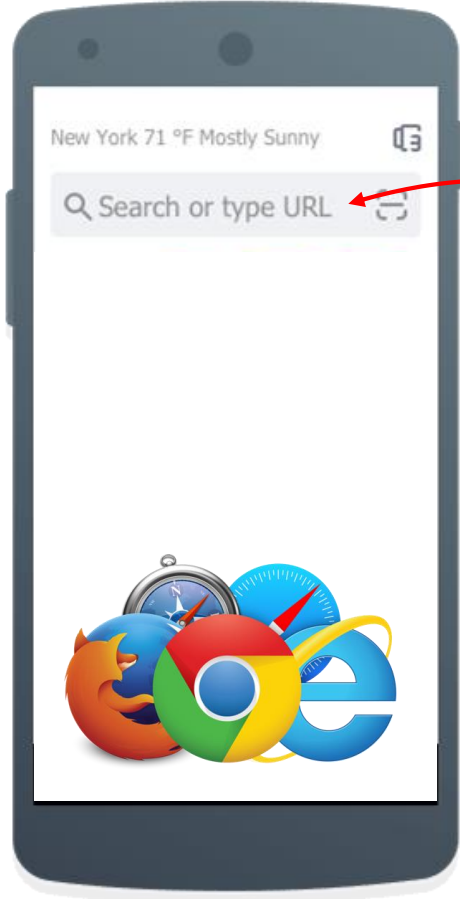


Thermodynamics

Lecture

5





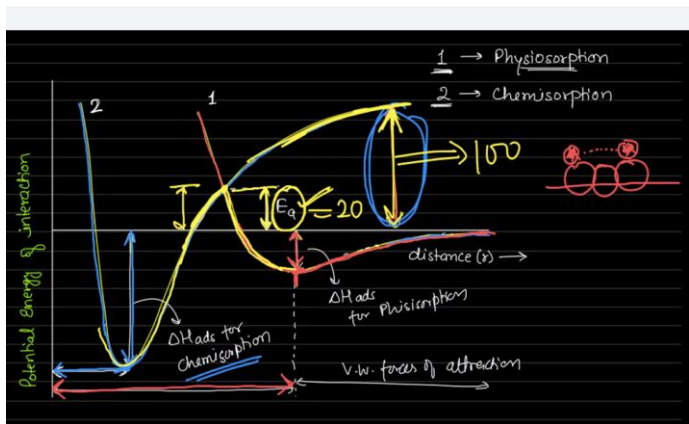
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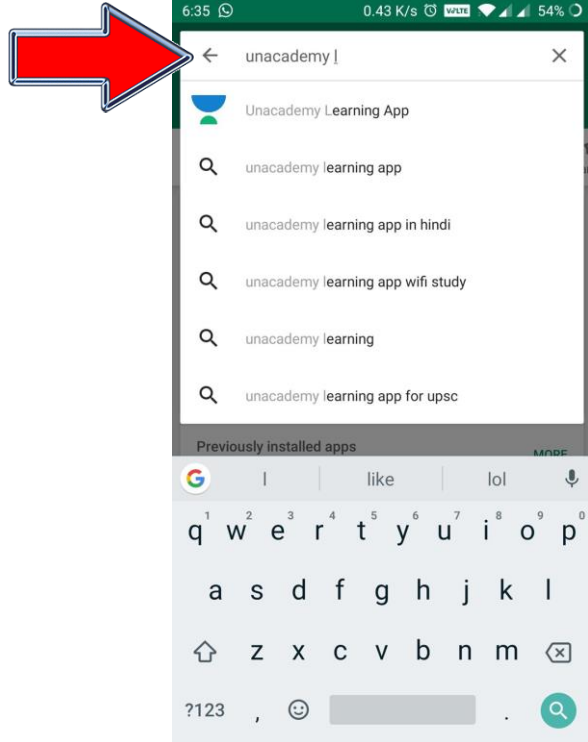
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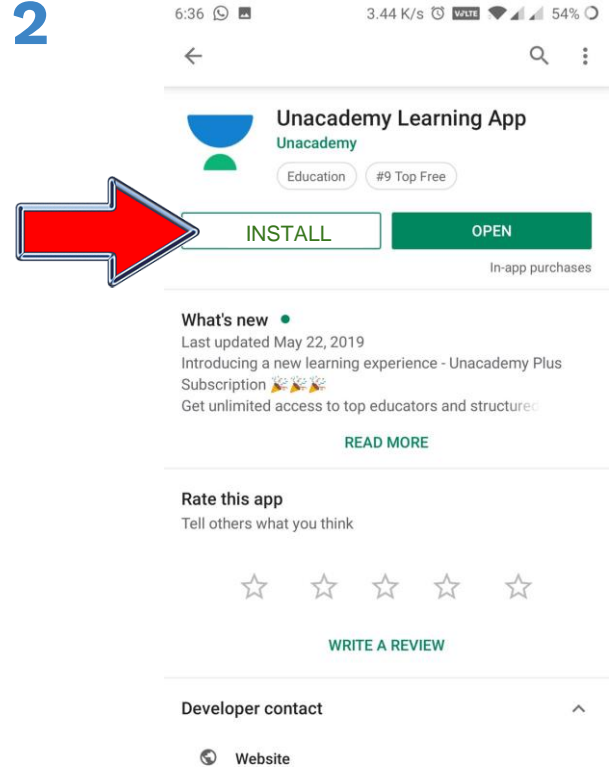
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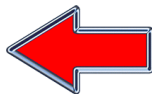
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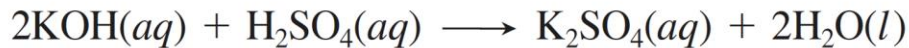
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Comparing ΔE and ΔH

Knowing the enthalpy change of a system tells us a lot about its energy change as well.

- ✓ Reactions that do not involve gases.

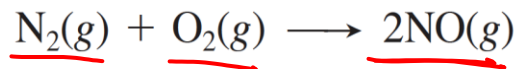


$$\Delta H \approx \Delta U$$

$$\begin{aligned}\Delta H &= \Delta U + \Delta(PV) \\ &= \Delta U + \Delta n_g RT\end{aligned}$$

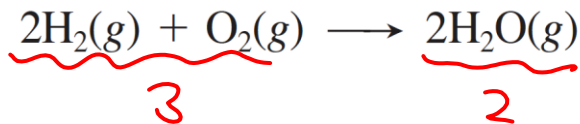
$$\Delta n_g = 0$$

- ✓ Reactions in which the amount (mol) of gas does not change.



$$\Delta n_g = 2 - 2 = 0 \Rightarrow \Delta H = \Delta U$$

- ✓ Reactions in which the amount (mol) of gas does change.



$$\Delta n_g = 2 - 3 = -1$$

$$\Delta H = \Delta U - RT$$



Example

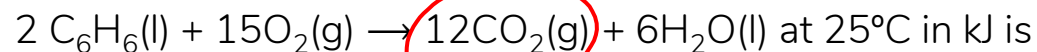
- a) $\text{H}_2(\text{g}) + \text{Cl}_2(\text{g}) \rightarrow 2\text{HCl}(\text{g})$; $\Delta H = \Delta U$ *b'caz* $\Delta n_g = 0$
- b) $\text{PCl}_5(\text{g}) \rightarrow \text{PCl}_3(\text{g}) + \text{Cl}_2(\text{g})$; $\Delta H = \Delta U + RT$
- c) $\text{CO}(\text{g}) + \frac{1}{2} \text{O}_2(\text{g}) \rightarrow \text{CO}_2(\text{g})$; $\Delta H = \Delta U - \frac{1}{2}RT$





Example

The difference between heats of reaction at constant pressure and constant volume for the reaction :



(a) -7.43

(c) -3.72

(b) $+3.72$

(d) $+7.43$

IIT - 1991

$\Delta n_g = -3$

$\Delta H - \Delta U = ?$

$\Delta H = \Delta U + \Delta n_g RT$

$= \Delta U - 3RT$

$\Delta H - \Delta U = -3RT$

$= -3 \times 8.314 \times 298 \text{ J}$





Example

One mole of a non-ideal gas undergoes a change of state (2.0 atm, 3.0L, 95(K) \rightarrow (4.0 atm, 5.0 L, 245K) with a change in internal energy, $\Delta U = 30.0 \text{ Latm}$. The change in enthalpy (ΔH) of the process in L atm is

IIT 2002

(a) 40.0

(b) 42.3

☒ (c) 44.0

(d) not defined, because pressure is not constant

$$\Delta U = 30 \text{ Latm}$$

$$\Delta H = ?$$

$$\Delta H = \Delta U + \Delta(PV)$$

$$\Delta H = \Delta U + (P_2V_2 - P_1V_1)$$

$$= 30 \text{ Latm} + (20 - 6) \text{ Latm}$$

$$= 44 \text{ Latm}$$





Example

Two moles of an ideal gas is expanded isothermally and reversibly from 1 litre to 10 litre at 300 K. The enthalpy change (in kJ) for the process is

IIT 2004

(a) 11.4 kJ (b) ~~-11.4 kJ~~

(c) 0 kJ

(d) 4.8 kJ

$$\text{Isothermal, } \Delta U = 0 \\ = q + w$$

$$q = +2.303nRT \quad q = -w$$

$$= +2.303 \times 2 \times 8.314 \times 300 \quad = (+) \\ \xrightarrow{(1000)} \text{ kJ}$$





Calorimetry: Measuring the Heat of a chemical or physical process

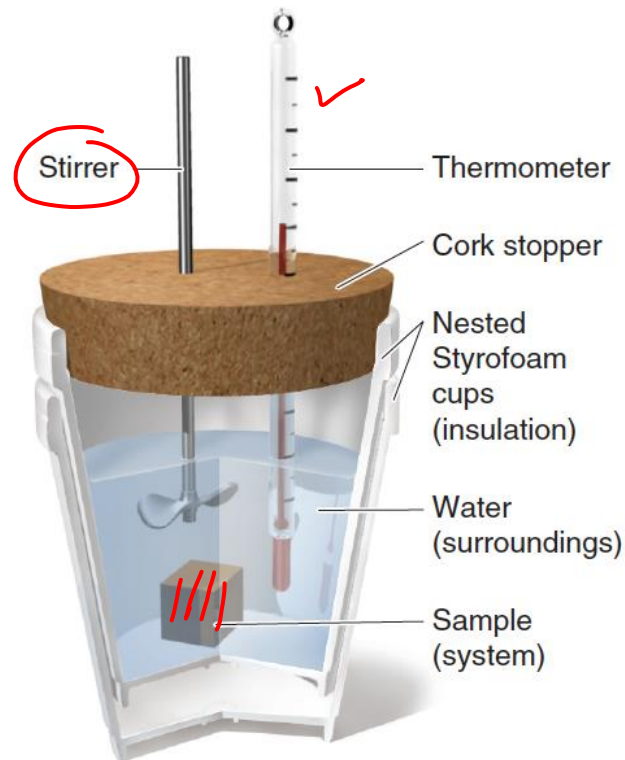
How do we know the heat of an acid-base reaction or the Calories in a teaspoon of sugar?

Constant-Pressure Calorimetry: For processes that take place at constant pressure, the heat transferred (q_p) is often measured in a coffee-cup calorimeter

$$mC\Delta T_{\text{sam}} = mC\Delta T_{\text{sample}}$$

$T_1 = 80^\circ\text{C}$

heat lost by sample = heat gained by calorimeter





Calorimetry: Bomb Calorimeter or Constant-Volume Calorimetry

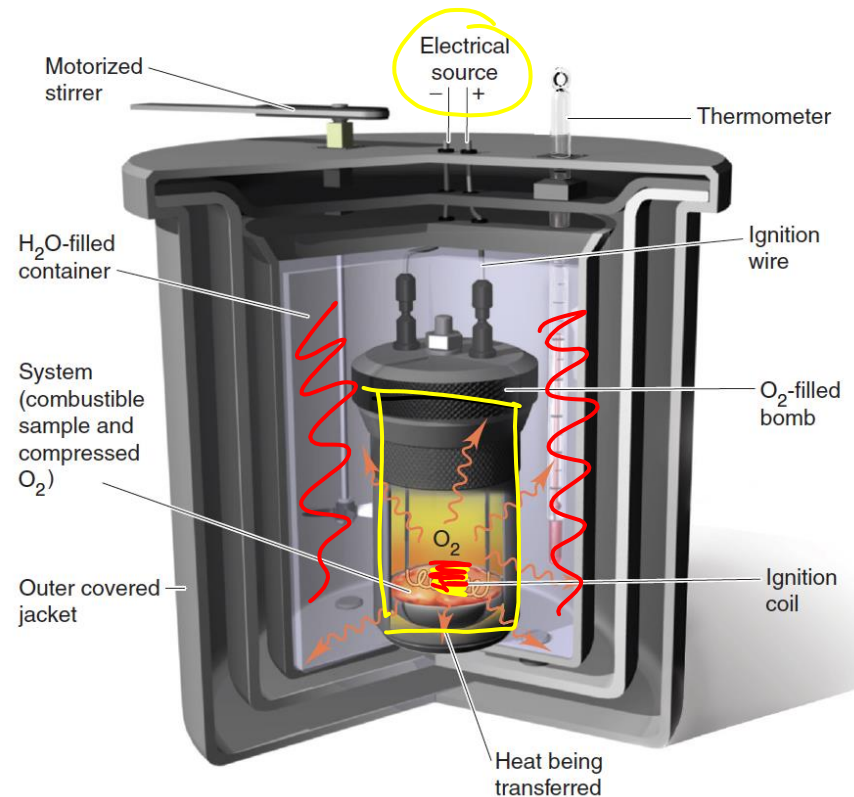
Constant-volume calorimetry is carried out in a bomb calorimeter, a device commonly used to measure the heat of combustion reactions, such as for fuels and foods.

$$\Delta U = q + w = q - P\Delta V$$

$$V = \text{const}$$

$$\Delta U = q_v$$

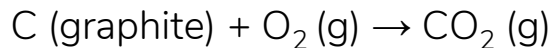
heat lost
by bomb = heat gained
by calorimeter
= $mc\Delta T$





Example

1g of graphite is burnt in a bomb calorimeter in excess of oxygen at 298 K and 1 atmospheric pressure according to the equation.



During the reaction, temperature rises from 298 k to 299 k. If the heat capacity of the bomb calorimeter is 20.7kJ/K. What is the enthalpy change for the above reaction at 298 K and 1 atm?

HW
NCERT





Example

For the reaction $\text{FeCO}_3(\text{s}) \xrightarrow{\Delta} \text{FeO}(\text{s}) + \text{CO}_2(\text{g})$; $\Delta H = 80 \text{ kJ}$ at 25°C
What is ΔU at 25°C ?

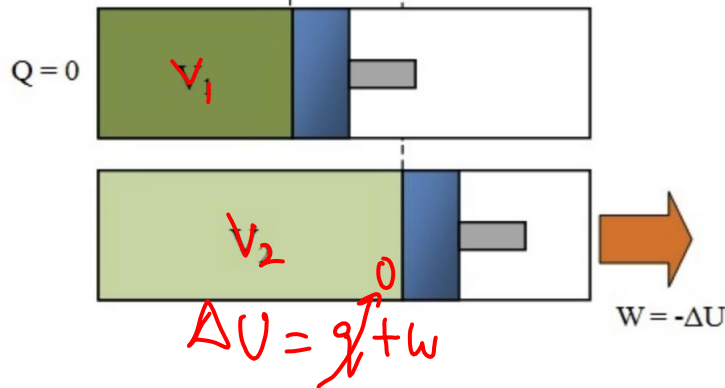
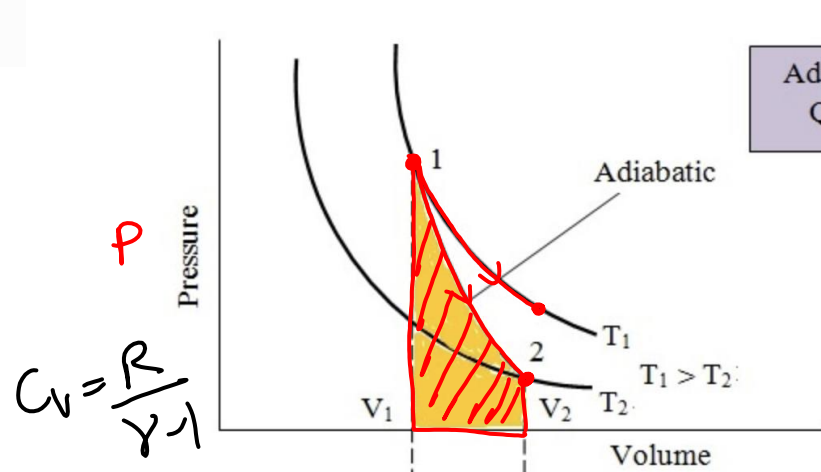
HW

$$\Delta H = \Delta U + \Delta n_g RT$$





Adiabatic Process



Adiabatic
 $Q = 0$

$$\Delta U = w$$

$$nC_v dT = -P_{ext} dV \quad \left[PV = nRT \right]$$

$$nC_v dT = -\frac{nRT}{V} dV$$

$$\int_{T_1}^{T_2} C_v \frac{dT}{T} = \int_{V_1}^{V_2} -\frac{R}{V} dV$$

$$\int_{T_1}^{T_2} \frac{dT}{T} = (1 - \gamma) \int_{V_1}^{V_2} \frac{dV}{V}$$

$$\ln\left(\frac{T_2}{T_1}\right) = (1 - \gamma) \ln\left(\frac{V_2}{V_1}\right)$$

Example

Derive $PV^\gamma = \text{const.}$ from $TV^{\gamma-1} = \text{constant}$

$$\ln\left(\frac{T_2}{T_1}\right) = (1-\gamma) \ln\left(\frac{V_2}{V_1}\right)$$

$$\ln\left(\frac{T_2}{T_1}\right) = \ln\left(\frac{V_2}{V_1}\right)^{1-\gamma}$$

$$\frac{T_2}{T_1} = \left(\frac{V_2}{V_1}\right)^{1-\gamma} = \left(\frac{V_1}{V_2}\right)^{\gamma-1}$$

$$T_2 V_2^{\gamma-1} = T_1 V_1^{\gamma-1}$$

$$TV^{\gamma-1} = \text{const}$$

$$PV^\gamma = \text{const}$$

$$\left(\frac{P_2 V_2}{P_1 V_1}\right) = \left(\frac{V_1}{V_2}\right)^{\gamma-1}$$

$$P_2 V_2 V_2^{\gamma-1} = P_1 V_1 V_1^{\gamma-1}$$

valid only for reversible
adiabatic

$$T^\gamma P^{1-\gamma} = \text{const}$$

Ideal gas eq.

$$PV = RT$$

$$\frac{T_2}{T_1} = \frac{P_2 V_2}{P_1 V_1}$$





Calculation of work for **Adiabatic Process**

Reversible Adiabatic:

$$\hookrightarrow \Delta U = \cancel{q} + \overset{0}{w}, \text{ we know } PV^\gamma = K \quad P_1 V_1^\gamma = P_2 V_2^\gamma = K$$

for rev process, $P_{\text{ext}} \approx P_{\text{int}}$

$$P = \frac{K}{V^\gamma}$$

$$\Delta U = -w$$
$$w = \int_{V_1}^{V_2} -P dV$$

$$w = - \int_{V_1}^{V_2} \frac{K dV}{V^\gamma} = -K \int_{V_1}^{V_2} V^{-\gamma} dV = -K \left[\frac{V^{-\gamma+1}}{-\gamma+1} \right]_{V_1}^{V_2}$$

$$w_{\text{Rev.}} = \frac{P_2 V_2 - P_1 V_1}{\gamma - 1}$$

$$= \frac{-P_2 V_2^{\gamma} \cdot V_2^{1-\gamma} + P_1 V_1^{\gamma} \cdot V_1^{1-\gamma}}{1-\gamma}$$



Calculation of work for **Adiabatic Process**

Irreversible Adiabatic:

$$W = -P_{\text{ext}} \Delta V$$

since $\Delta U = W$

$$nC_v \Delta T = W$$

$$W_{\text{IRR}} = nC_v \Delta T$$

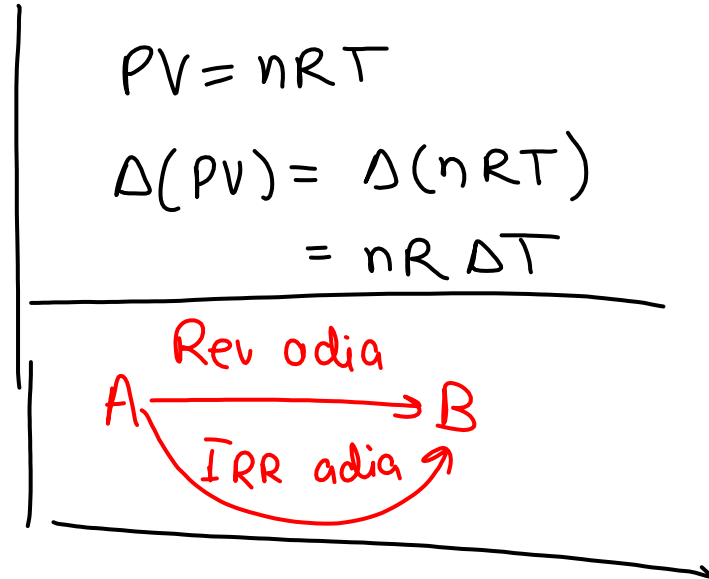
Diagram illustrating the calculation of work for an adiabatic process:

From state A to state B, the work done is:

$$W_{\text{Rev}} = \frac{nR(T_2 - T_1)}{\gamma - 1} = \frac{nR\Delta T}{\gamma - 1} = \frac{P_2 V_2 - P_1 V_1}{\gamma - 1}$$

From state A to state C, the work done is:

$$W_{\text{IRR}} = \frac{nR\Delta T}{\gamma - 1}$$





Example

What is the final temperature of 0.10 mol mono-atomic ideal gas that performs 75 cal. Of work adiabatically if the initial temperature is 227°C .

- a) 250 K
- b) 350 K
- c) 150 K
- d) 275 K





Example

For a reversible adiabatic ideal gas expansion $\frac{dP}{P}$ is equal to

a) $\gamma \cdot \frac{dV}{V}$

b) $-\gamma \cdot \frac{dV}{V}$

c) $\left(\frac{\gamma}{\gamma-1}\right) \cdot \frac{dV}{V}$

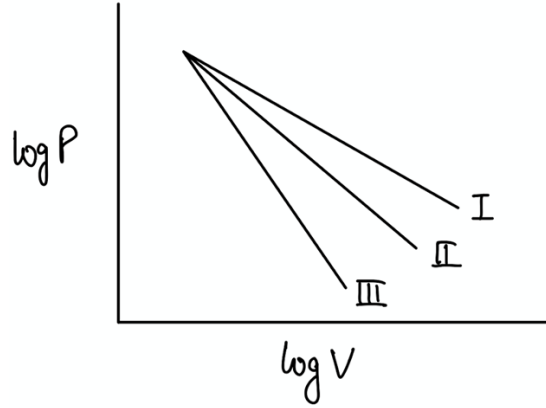
d) $\frac{dV}{V}$





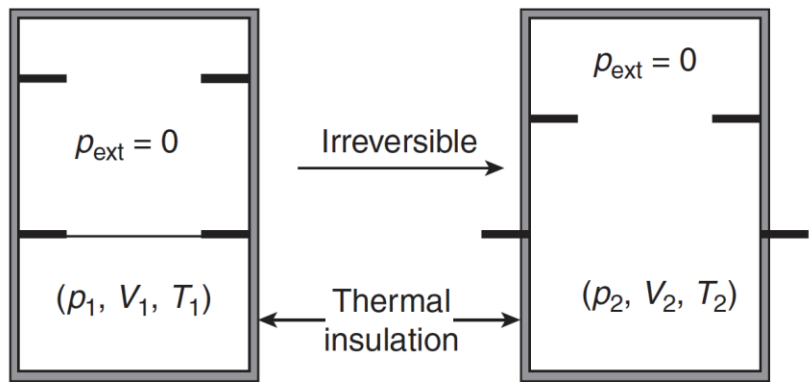
Example

The following curves represent adiabatic expansions of gases He, O_2 and CO_2 . Which curve represents He?



Example

An ideal gas in a thermally insulated vessel at internal pressure = p_1 , volume = V_1 and absolute temperature = T_1 expands irreversibly against zero external pressure, as shown in the below diagram. The final internal pressure, volume and absolute temperature of the gas are p_2 , V_2 and T_2 , respectively. For this expansion,



(a) $q = 0$

(c) $p_2 V_2 = p_1 V_1$

(b) $T_2 = T_1$

(d) $p_2 V_2^\gamma = p_1 V_1^\gamma$

(JEE Advanced 2014)





Example

During an adiabatic process, the pressure of gas is found to be proportional to the cube of the absolute temperature. The ratio of C_p/C_v for the gas is

$$\frac{3}{2}$$

$$\frac{5}{3}$$

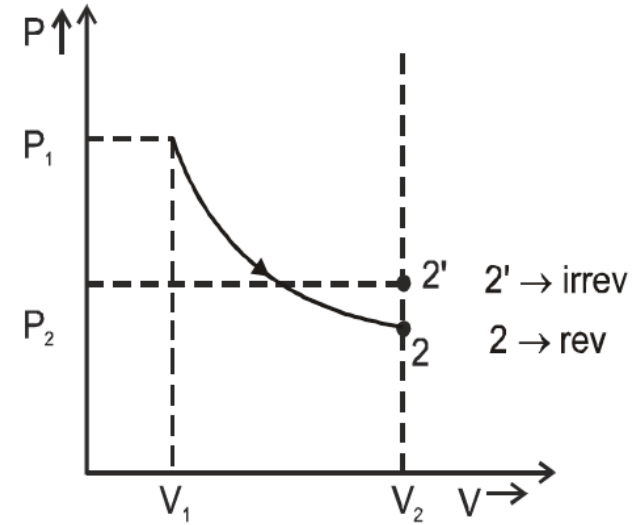
$$\frac{7}{2}$$

$$\frac{4}{3}$$





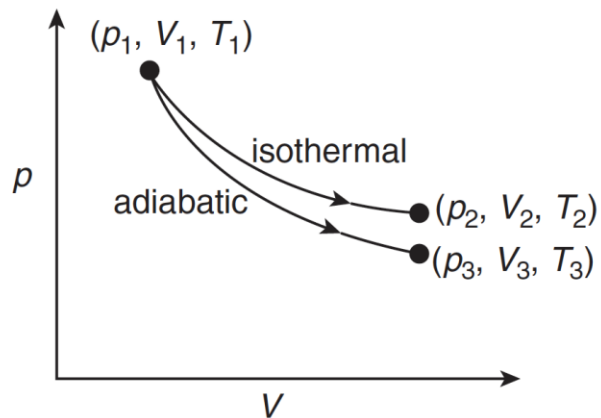
Comparison of **Adiabatic** Expansion





Example

The reversible expansion of an ideal gas under adiabatic and isothermal conditions is shown in the below figure. Which of the following statement(s) is (are) correct?



- (a) $T_1 = T_2$ (b) $T_3 > T_1$
(c) $w_{\text{isothermal}} > w_{\text{adiabatic}}$ (d) $\Delta U_{\text{isothermal}} > \Delta U_{\text{adiabatic}}$

(IIT-JEE 2012)





Example

A liquid of volume of 100L and at the external pressure of 10 atm. The liquid is confined inside an adiabatic bath. External pressure of the liquid is suddenly increased to 100 atm and the liquid gets compressed by 1 L against this pressure then find,

- a) Work
- b) ΔU
- c) ΔH





Example

Two separate experiments were carried out involving adiabatic reversible expansion, taking monoatomic gas in one case and a diatomic gas in the second case. In each case, the initial temperature was T_i and expansion was from volume V_1 to volume V_2 . The final temperatures attained were T_M for monoatomic gas and T_D for diatomic gas. Then

- a) $T_M = T_D < T_i$
- b) $T_M < T_D < T_i$
- c) $T_D > T_M > T_i$
- d) $T_i < T_M < T_f$





Example

Which of the following statements is not correct?

- (a) Final temperature in reversible adiabatic expansion is greater than that in irreversible adiabatic expansion.
- (b) When heat is supplied to an ideal gas in isothermal process, kinetic energy of gas remains constant.
- (c) When an ideal gas is subjected to adiabatic expansion, it gets cooled.
- (d) Entropy increases when an ideal gas expands isothermally.





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