

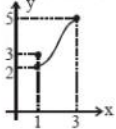
DPP 8 INTRODUCTION OF CONTINUITY , EXISTENCE OF CONTINUITY

- Function $f(x) = \begin{cases} 1+x, & \text{when } x < 2 \\ 5-x, & \text{when } x > 2 \end{cases}$; is continuous at $x = 2$, if $f(2)$ equals -
 (A) 0 (B) 1 (C) 2 (D) 3
- If $f(x) = \begin{cases} x \cos \frac{1}{x}, & x \neq 0 \\ k, & x = 0 \end{cases}$ is continuous at $x = 0$, then
 (A) $k > 0$ (B) $k < 0$ (C) $k = 0$ (D) $k \geq 0$
- If $f(x) = |x-2|$, then
 (A) $\lim_{x \rightarrow 2^+} f(x) \neq 0$ (B) $\lim_{x \rightarrow 2^-} f(x) \neq 0$
 (C) $\lim_{x \rightarrow 2^+} f(x) \neq \lim_{x \rightarrow 2^-} f(x)$ (D) $f(x)$ is continuous at $x = 2$
- If the function $f(x) = \begin{cases} \frac{k \cos x}{\pi - 2x}, & \text{when } x \neq \frac{\pi}{2} \\ 3, & \text{when } x = \frac{\pi}{2} \end{cases}$ be continuous at $x = \frac{\pi}{2}$, then $k =$
 (A) 3 (B) 6 (C) 12 (D) None of these
- Let $f(x) = \begin{cases} \frac{x^3 + x^2 - 16x + 20}{(x-2)^2}, & \text{if } x \neq 2 \\ k, & \text{if } x = 2 \end{cases}$. If $f(x)$ be continuous for all x , then $k =$
 (A) 7 (B) -7 (C) ± 7 (D) None of these
- The points at which the function $f(x) = \frac{x+1}{x^2+x-12}$ is discontinuous, are
 (A) -3, 4 (B) 3, -4 (C) -1, -3, 4 (D) -1, 3, 4
- The function $f(x) = |x| + \frac{|x|}{x}$ is
 (A) Continuous at the origin
 (B) Discontinuous at the origin because $|x|$ is discontinuous there
 (C) Discontinuous at the origin because $\frac{|x|}{x}$ is discontinuous there
 (D) Discontinuous at the origin because both $|x|$ and $\frac{|x|}{x}$ are discontinuous there
- Which of the following statements is true for graph $f(x) = \log x$
 (A) Graph shows that function is continuous
 (B) Graph shows that function is discontinuous
 (C) Graph finds for negative and positive values of x
 (D) Graph is symmetric along x -axis
- At which points the function $f(x) = \frac{x}{[x]}$, where $[.]$ is greatest integer function, is discontinuous
 (A) Only positive integers
 (B) All positive and negative integers and $(0, 1)$
 (C) All rational numbers
 (D) None of these
- If $f(x) = |x - b|$, then function
 (A) is continuous at $x = 1$ (B) is continuous at $x = b$
 (C) is discontinuous at $x = b$ (D) None of these

11. The value of $f(0)$, so that the function $f(x) = \frac{(27-2x)^{1/3} - 3}{9-3(243+5x)^{1/3}}, (x \neq 0)$ is continuous, is given by
 (A) $2/3$ (B) 6 (C) 2 (D) 4
12. If $f(x) = \frac{x^2 - 10x + 25}{x^2 - 7x + 10}$ for $x \neq 5$ and f is continuous at $x = 5$, then $f(5) =$
 (A) 0 (B) 5 (C) 10 (D) 25
13. In order that the function $f(x) = (x+1)^{\cot x}$ is continuous at $x = 0$, $f(0)$ must be defined as
 (A) $f(0) = \frac{1}{e}$ (B) $f(0) = 0$ (C) $f(0) = e$ (D) None of these
14. The function $f(x) = \sin |x|$ is
 (A) Continuous for all x (B) Continuous only at certain points
 (C) Differentiable at all points (D) None of these
15. If $f(x) = |x|$, then $f(x)$ is
 (A) Continuous for all x (B) Differentiable at $x = 0$
 (C) Neither continuous nor differentiable at $x = 0$
 (D) None of these

1	2	3	4	5
D	C	D	B	A
6	7	8	9	10
B	C	A	B	AB
11	12	13	14	15
C	A	C	A	A

DPP 9 CONTINUITY IN OPEN AND CLOSE INTERVAL

1. If $f(x) = \begin{cases} \sqrt{1+px} - \sqrt{1-px}, & -1 \leq x < 0 \\ \frac{x}{2x+1}, & 0 \leq x \leq 1 \end{cases}$ is continuous in the interval $[-1, 1]$ then p equals -
 (A) -1 (B) 1 (C) 1/2 (D) -1/2
2. If $f(x) = \begin{cases} \frac{x^2}{a}, & 0 \leq x < 1 \\ a, & 1 \leq x < \sqrt{2} \\ \frac{(2b^2-4b)}{x^2}, & \sqrt{2} \leq x < \infty \end{cases}$ is continuous in the interval $[0, \infty)$, then values of a and b are respectively -
 (A) 1, -1 (B) -1, $1 + \sqrt{2}$ (C) -1, 1 (D) None of these
3. Which of the following function is not continuous in the interval $(0, \pi)$.
 (A) $x \sin \frac{1}{x}$ (B) $\begin{cases} 1, & 0 < x \leq \frac{3\pi}{4} \\ 2 \sin\left(\frac{2x}{9}\right), & \frac{3\pi}{4} < x < \pi \end{cases}$ (C) $\tan x$ (D) None of these
4. Graph of a function $f(x)$ is given. Which of the following statements is not correct :

 (A) $f(x)$ is continuous on $(1, 3)$ (B) $f(x)$ is continuous on $(1, 3]$
 (C) $f(x)$ is continuous on $[1, 3]$ (D) none of these
5. If $f(x) = \begin{cases} x^2, & \text{when } x \neq 1 \\ 2, & \text{when } x = 1 \end{cases}$ then
 (A) $\lim_{x \rightarrow 1} f(x) = 2$ (B) $f(x)$ is continuous at $x = 1$
 (C) $f(x)$ is discontinuous at $x = 1$ (D) None of these
6. If $f(x) = \begin{cases} 1+x, & \text{when } x \leq 2 \\ 5-x, & \text{when } x > 2 \end{cases}$, then
 (A) $f(x)$ is continuous at $x = 2$ (B) $f(x)$ is discontinuous at $x = 0$
 (C) $f(x)$ is continuous at $x = 3$ (D) None of these
7. If $f(x) = \begin{cases} 1, & \text{when } 0 < x \leq \frac{3\pi}{4} \\ 2 \sin \frac{2}{9} x, & \text{when } \frac{3\pi}{4} < x < \pi \end{cases}$, then
 (A) $f(x)$ is continuous at $x = 0$ (B) $f(x)$ is continuous at $x = \pi$
 (C) $f(x)$ is continuous at $x = \frac{3\pi}{4}$ (D) $f(x)$ is discontinuous at $x = \frac{3\pi}{4}$
8. If $f(x) = \begin{cases} x \sin x, & \text{when } 0 < x \leq \frac{\pi}{2} \\ \frac{\pi}{2} \sin(\pi + x), & \text{when } \frac{\pi}{2} < x < \pi \end{cases}$, then
 (A) $f(x)$ is discontinuous at $x = \pi/2$ (B) $f(x)$ is continuous at $x = \pi/2$
 (C) $f(x)$ is continuous at $x = 0$ (D) None of these
9. If $f(x) = \begin{cases} \frac{1 - \cos 4x}{x^2}, & \text{when } x < 0 \\ a, & \text{when } x = 0 \\ \frac{\sqrt{x}}{\sqrt{(16 + \sqrt{x})} - 4}, & \text{when } x > 0 \end{cases}$ is continuous at $x = 0$, then the value of 'a' will be
 (A) 8 (B) -8 (C) 4 (D) None of these
10. If $f(x) = \begin{cases} ax^2 - b, & \text{when } 0 \leq x < 1 \\ 2, & \text{when } x = 1 \\ x + 1, & \text{when } 1 < x \leq 2 \end{cases}$ is continuous at $x = 1$, then the most suitable value of a, b are
 (A) $a = 2, b = 0$ (B) $a = 1, b = -1$ (C) $a = 4, b = 2$ (D) All the above
11. If $f(x) = \frac{x - |x|}{x}$, when $x \neq 0$ then

10. (A) $a = 2, b = 0$ (B) $a = 1, b = -1$ (C) $a = 4, b = 2$ (D) All the above

11. If $f(x) = \begin{cases} \frac{x-|x|}{x}, & \text{when } x \neq 0 \\ 2, & \text{when } x = 0 \end{cases}$, then

- (A) $f(x)$ is continuous at $x = 0$ (B) $f(x)$ is discontinuous at $x = 0$
(C) $\lim_{x \rightarrow 0} f(x) = 2$ (D) None of these

12. If the function

$$f(x) = \begin{cases} 1 + \sin \frac{\pi}{2} x & \text{for } -\infty < x \leq 1 \\ ax + b & \text{for } 1 < x < 3 \\ 6 \tan \frac{x\pi}{12} & \text{for } 3 \leq x < 6 \end{cases}$$
 is continuous in the interval $(-\infty, 6)$, then the value of a and b

are respectively -

- (A) 0, 2 (B) 1, 1 (C) 2, 0 (D) 2, 1

13. If $f(x) = \begin{cases} x^2 \sin \frac{1}{x}, & \text{when } x \neq 0 \\ 0, & \text{when } x = 0 \end{cases}$, then

- (A) $f(0^+)$ (B) $f(0^-)$
(C) f is continuous at $x = 0$ (D) None of these

14. The value of k so that the function

$$f(x) = \begin{cases} k(2x - x^2), & \text{when } x < 0 \\ \cos x, & \text{when } x \geq 0 \end{cases}$$
 is continuous at $x = 0$, is

- (A) 1 (B) 2 (C) 4 (D) None of these

15. If $f(x) = \begin{cases} \frac{x}{e^{1/x} + 1}, & \text{when } x \neq 0 \\ 0, & \text{when } x = 0 \end{cases}$, then

- (A) $\lim_{x \rightarrow 0^+} f(x) = 1$ (B) $\lim_{x \rightarrow 0^-} f(x) = 1$
(C) $f(x)$ is continuous at $x = 0$ (D) None of these

1	2	3	4	5
D	C	C	C	C
6	7	8	9	10
AB	C	A	A	D
11	12	13	14	15
B	C	C	D	C

DPP 10 TYPES OF DISCONTINUITY

- The function f is defined in $[-5, 5]$ as $f(x) = x$, if x is rational and $f(x) = -x$, if x is irrational. Then:
 (A) $f(x)$ is continuous at every x , except $x = 0$
 (B) $f(x)$ is discontinuous at every x , except $x = 0$
 (C) $f(x)$ is continuous everywhere
 (D) $f(x)$ is discontinuous everywhere
- If $f(x) = [x]$, where $[x]$ = greatest integer, then at $x = 1$, f is—
 (A) Continuous (B) left continuous (C) right continuous (D) None of these
- If $f(x) = x - [x]$, then f is discontinuous at —
 (A) every natural number (B) every integer
 (C) origin (D) Nowhere
- Function $f(x) = \frac{x^3 - 1}{x^2 - 3x + 2}$ is discontinuous at -
 (A) $x = 1$ (B) $x = 2$ (C) $x = 1, 2$ (D) No where
- For function $f(x) = \begin{cases} \left(1 + \frac{4x}{5}\right)^{1/x}, & x \neq 0 \\ e^{4/5}, & x = 0 \end{cases}$, the correct statement is—
 (A) $f(0^+)$ and $f(0^-)$ do not exist (B) $f(0^+) \neq f(0^-)$
 (C) $f(x)$ continuous at $x = 0$ (D) $\lim_{x \rightarrow 0} f(x) \neq f(0)$
- The function $f(x) = \frac{4 - x^2}{4x - x^3}$ is equal to -
 (A) discontinuous at only one point (B) discontinuous exactly at two points
 (C) discontinuous exactly at three points (D) none of these
- If $f(x) = \frac{1 - \tan x}{4x - \pi}$, $x \neq \frac{\pi}{x}$, $x \in \left[0, \frac{\pi}{2}\right]$, and $f(x)$ is continuous in $\left[0, \frac{\pi}{2}\right]$, then $f(\pi/4)$ is:
 (A) 1 (B) $\frac{1}{2}$ (C) $-\frac{1}{2}$ (D) -1
- If $f(x) = \begin{cases} x^2 - 3, & 2 < x < 3 \\ 2x + 5, & 3 < x < 4 \end{cases}$, the equation whose roots are $\lim_{x \rightarrow 3^+} f(x)$ and $\lim_{x \rightarrow 3^-} f(x)$ is
 (A) $x^2 - 7x + 3 = 0$ (B) $x^2 - 20x + 66 = 0$ (C) $x^2 - 17x + 66 = 0$ (D) $x^2 - 18x + 60 = 0$
- If $f(x) = \begin{cases} x - 1, & x < 0 \\ \frac{1}{4}, & x = 0 \\ x^2, & x > 0 \end{cases}$, then
 (A) $\lim_{x \rightarrow 0^+} f(x) = 1$ (B) $\lim_{x \rightarrow 0^-} f(x) = -1$
 (C) $f(x)$ is continuous at $x = 0$ (D) None of these
- If $f(x) = \begin{cases} \frac{\sin[x]}{[x] + 1}, & \text{for } x > 0 \\ \frac{\cos \frac{\pi}{2}[x]}{[x]}, & \text{for } x < 0 \\ k, & \text{at } x = 0 \end{cases}$, where $[x]$ denotes the greatest integer less than or equal to x , then in order that f be continuous at $x = 0$, the value of k is
 (A) Equal to 0 (B) Equal to 1 (C) Equal to -1 (D) Indeterminate
- The function $f(x) = \begin{cases} x + 2, & 1 \leq x \leq 2 \\ 4, & x = 2 \\ 3x - 2, & x > 2 \end{cases}$ is continuous at
 (A) $x = 2$ only (B) $x \leq 2$ (C) $x \geq 2$ (D) None of these

12. If the function $f(x) = \begin{cases} 5x-4 & , \text{ if } 0 < x \leq 1 \\ 4x^2+3bx & , \text{ if } 1 < x < 2 \end{cases}$ is continuous at every point of its domain, then the value of b is
 (A) -1 (B) 0 (C) 1 (D) None of these
13. The values of A and B such that the function $f(x) = \begin{cases} -2\sin x, & x \leq -\frac{\pi}{2} \\ A\sin x + B, & -\frac{\pi}{2} < x < \frac{\pi}{2} \\ \cos x, & x \geq \frac{\pi}{2} \end{cases}$ is continuous everywhere are
 (A) $A=0, B=1$ (B) $A=1, B=1$ (C) $A=-1, B=1$ (D) $A=-1, B=0$
14. If $f(x) = \frac{x^2-10x+25}{x^2-7x+10}$ for $x \neq 5$ and f is continuous at $x=5$, then $f(5) =$
 (A) 0 (B) 5 (C) 10 (D) 25

1	2	3	4	5
B	C	B	C	C
6	7	8	9	10
C	C	C	B	A
11	12	13	14	
C	A	C	A	

DPP 11 THEOREMS ON CONTINUITY, PROBLEMS ON CONTINUITY

- If function $f(x) = x - |x - x^2|$, $-1 \leq x \leq 1$ then f is-
 (A) continuous at $x = 0$ (B) continuous at $x = 1$
 (C) continuous at $x = -1$ (D) everywhere continuous
- $f(x) = 1 + 2^{1/x}$ is-
 (A) continuous everywhere (B) continuous nowhere
 (C) discontinuous at $x = 0$ (D) None of these
- Let $[.]$ denotes G.I.F. and $f(x) = [x] + [-x]$ and m is any integer, then correct statement is-
 (A) $\lim_{x \rightarrow m} f(x)$ does not exist (B) $f(x)$ is continuous at $x = m$
 (C) $\lim_{x \rightarrow m} f(x)$ exists (D) None of these
- If $f(x) = (\tan x \cot \alpha)^{v(x-\alpha)}$ is continuous at $x = \alpha$, then the value of $f(\alpha)$ is -
 (A) $e^{2 \sin 2\alpha}$ (B) $e^{2 \cos \sec 2\alpha}$ (C) $e^{\cos \sec 2\alpha}$ (D) $e^{\sin 2\alpha}$
- Let $[.]$ denotes G.I.F. for the function $f(x) = \frac{\tan(\pi[x-\pi])}{1+[x]^2}$ the wrong statement is -
 (A) $f(x)$ is discontinuous at $x = 0$ (B) $f(x)$ is continuous for all values of x
 (C) $f(x)$ is continuous at $x = 0$ (D) $f(x)$ is a constant function
- The point of discontinuity of the function $f(x) = \frac{1 - \cos 5x}{1 - \cos 4x}$ is-
 (A) $x = 0$ (B) $x = \pi$ (C) $x = \pi/2$ (D) All the above
- Let $f(x) = \frac{\sqrt{1+\sin x} - \sqrt{1-\sin x}}{x}$. The value which should be assigned to f at $x = 0$ so that it is continuous everywhere is-
 (A) 1 (B) 2 (C) -2 (D) 1/2
- If the function

$$f(x) = \begin{cases} \frac{\sin(k+1)x + \sin x}{x}, & \text{when } x < 0 \\ 1/2, & \text{when } x = 0 \\ \frac{x+1}{2}, & \text{when } x > 0 \end{cases}$$
 is continuous at $x = 0$, then the value of k is-
 (A) 1/2 (B) -1/2 (C) -3/2 (D) 1
- Function $f(x) = \begin{cases} x \tan^{-1}(1/x), & x \neq 0 \\ 0, & x = 0 \end{cases}$ at $x = 0$ is-
 (A) discontinuous (B) continuous (C) differentiable (D) None of these

10. Function $f(x) = \frac{\cos x - \sin x}{\sin 4x}$ is not defined at $x = \frac{\pi}{4}$. The value which should be assigned to f at $x = \frac{\pi}{4}$, so that it is continuous there, is-
- (A) 0 (B) $\frac{1}{2\sqrt{2}}$ (C) $-\frac{1}{\sqrt{2}}$ (D) None
11. If $f(x) = \begin{cases} x \frac{e^{vx} - e^{-vx}}{e^{vx} + e^{-vx}}, & x \neq 0 \\ 0, & x = 0 \end{cases}$, then correct statement is-
- (A) f is continuous at all points except $x = 0$
 (B) f is continuous at every point but not differentiable
 (C) f is differentiable at every point
 (D) f is differentiable only at the origin
12. If $f(x)$ is continuous function and $g(x)$ is discontinuous function, then correct statement is -
- (A) $f(x) + g(x)$ is a continuous function (B) $f(x) - g(x)$ is a continuous function
 (C) $f(x) + g(x)$ is a discontinuous function (D) $f(x) g(x)$ is a continuous function
13. If function is $f(x) = |x| + |x-1| + |x-2|$, then it is -
- (A) discontinuous at $x = 0$ (B) discontinuous at $x = 0, 1$
 (C) discontinuous at $x = 0, 1, 2$ (D) everywhere continuous
14. Function $f(x) = |x-2| - 2|x-4|$ is discontinuous at
- (A) $x = 2, 4$ (B) $x = 2$ (C) Nowhere (D) Except $x = 2, 4$
15. Function $f(x) = |\sin x| + |\cos x| + |x|$ is discontinuous at-
- (A) $x = 0$ (B) $x = \pi/2$ (C) $x = \pi$ (D) No where

1	2	3	4	5
D	C	C	B	A
6	7	8	9	10
D	A	C	B	B
11	12	13	14	15
B	C	D	C	D