## **NCERT-9.4.6**

## EE24BTECH11035 - KOTHAPALLI AKHIL

**Question:** Find the solution of the differential equation:

$$\frac{dy}{dx} = (1+x^2)(1+y^2). (1)$$

**Solution:** Rewriting the equation:

$$\frac{dy}{1+y^2} = (1+x^2)dx. (2)$$

Integrating both sides:

$$\int \frac{dy}{1+y^2} = \int (1+x^2)dx.$$
 (3)

After simplification:

$$\tan^{-1}(y) = x + \frac{x^3}{3} + k. \tag{4}$$

where k is the constant of integration (Here, it is assumed as 0).

## **Numerical Approach:**

I used a for loop for finding the y values as the loop proceeds with iterative formula given below. I took some initial value of x and as loop proceeds I assigned it the value as x + h. where h is the step size, representing the rate of change.

2. Assigned the values of y for different x-values using a for loop.

The iterative formula for updating y-values is:

$$y_n = y_{n-1} + \left(\frac{dy}{dx}\right)h,\tag{5}$$

The iterative formula for updating x-values is:

$$x_n = x_{n-1} + h \tag{6}$$

## **Initial Conditions:**

- x = 0
- y = 0
- h = 0.0002

Using Matplotlib, I plotted the computed points and the graph of the exact solution to verify that they approximately match.

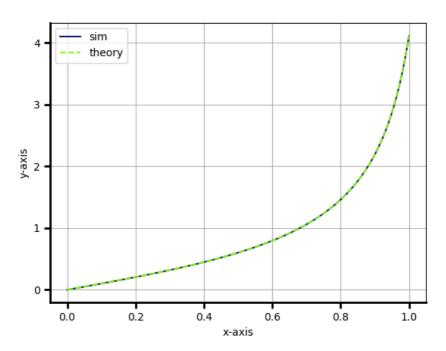


Fig. 0.1: verifying through graph of sim and theory values